Multivariate Interpolation

**Abstract**

Demonstrate multivariate interpolation using the Vandermonde matrix method. We will be designing an algorithm that creates a polynomial interpolation given some sample data. This algorithm will be analyzed to determine where it is most useful. Specifically, we will be looking at different types of functions and sample sizes.

**Introduction**

Interpolation is a method used to approximate a function by using a sample data set. Multivariate interpolation involves interpolating a function of more than one variable. In many scientific applications there will be functions of multiple parameters required for computation. Some examples of these functions are the weather (variables: temperature, wind speed, humidity), people (variables: height, weight, hair color), and gas mileage (variables: speed, tire pressure, wind speed). Therefore, having a way to interpolate samples of these studies allows researchers to predict future outcomes like forecasting the weather or calculating the cost of gas for a road trip.

There are many methods used to do multidimensional interpolation which each have their own strengths and weaknesses. The purpose of this paper is to examine a specific algorithm used for multivariate interpolation and report on its performance and where it can be improved. Three-dimensional graphs will be used to visually display the resulting interpolated polynomials. This along with error analysis will be our means of judging the success of our interpolated polynomial.

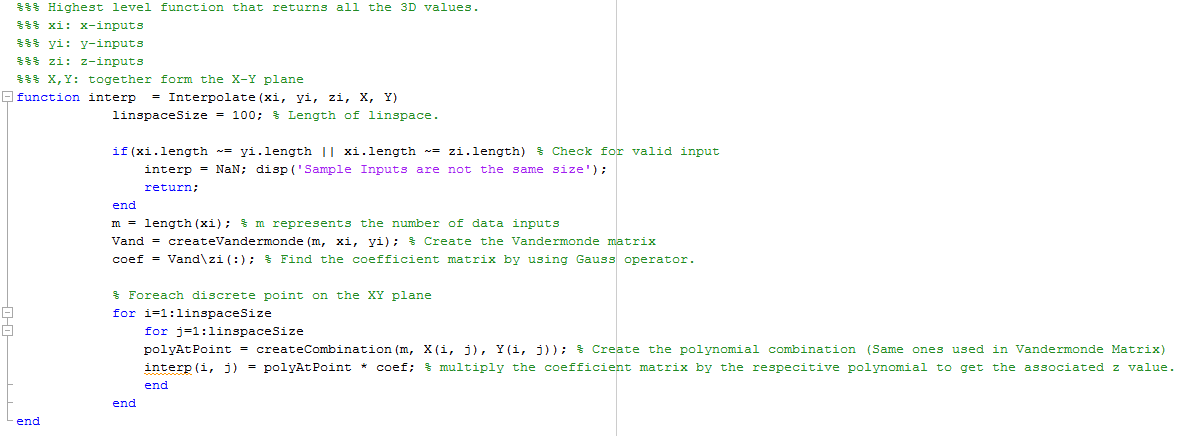
**Related Works**

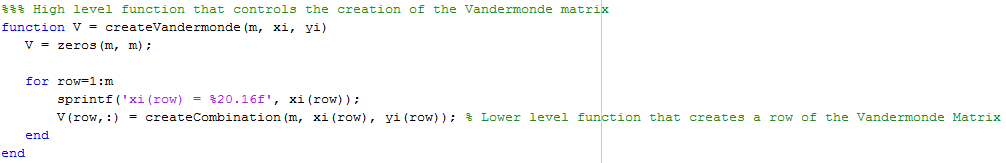
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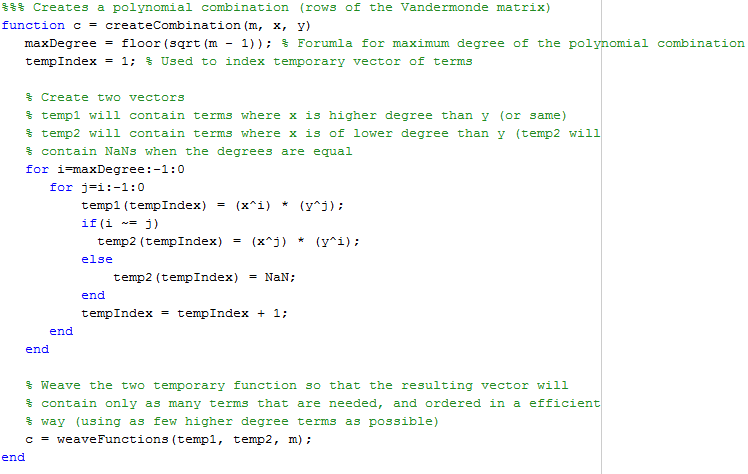
**Algorithm**

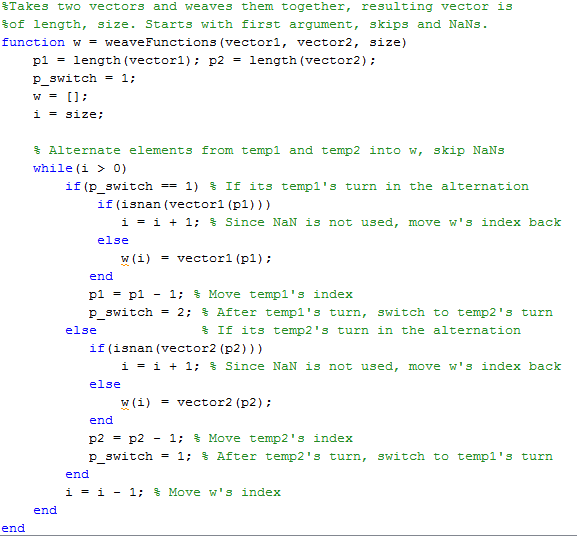
The Vandermonde matrix method involves creating an *n x n* matrix where each row is a linear combination of monomials which span a set of basis functions. The coefficients are determined by using the equation V\*c = z, where V is the Vandermonde matrix, c are the coefficients, and z is the solution vector given in the data set. The algorithm must be able to create this matrix given a set of data points, determine the degree of the polynomial, create the basis function, and fill in the matrix row by row using the same index of x and y values for each row. Then the algorithm solves the system using the equation above for the coefficients and creates a general polynomial which can be used to interpolate any set of data points.

**Algorithm Code**

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**Results**

So far we have created the algorithm which successfully creates the Vandermonde matrix and solves for the coefficients, but we are having issues with the polynomial created. We debugging the algorithm by plotting the polynomial in the 3-D plane and outputting sample values to compare with the expected results. The code has been included with this report.

**Conclusion**

(to be written)