

# Parameters Study of Sharing Mechanism on Genetic Algorithm for Multimodal Problem

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**Abstract** Sharing mechanism is widely used in genetic algorithm (GA) to solve multimodal problems. In this paper, the influence of parameters of share function on the search performance of GA is studied. There are three key factors in the share function, which are metric space, distance constant and index constant. First, the metric space is studied based on the performance of GA; second the distance constant is determined based on optimal metric space; finally, according to the metric space and distance constant, the index constant is decided. According to the five criteria of the experiment, the optimal combination of these three parameters are determined to maximize the performance of GAs.

**Keywords** Genetic Algorithm · Niche · Metric Space · Multimodal

## 1 Introduction

Genetic algorithms (GAs) are first introduced in 1975 by Holland[1976Sampson], because of its powerful search ability, which was widely used to solve many search problems. Compared with other random search algorithm, for example, particle swarm optimization, ant colony optimization, and simulated annealing algorithm[2010Zabinsky], GAs are not easily trapped in local optima. Traditional GAs have been to successfully find the optimal value in the domain for unimodal problems, however, sometimes, not only the optimal point but also the secondary important point is needed. Because of its search rule, traditional GAs are failed to maintain the information for a multimodal problem.

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### 1.1 Multimodal Optimization

In order to maintain the diversity of the population for a multimodal problem, it is significant to maximize the number of niche in the population. There are several methods to achieve this target, which are Crowding, Deterministic Crowding and Sharing methods. share Function[1987Goldberg et al. Goldberg, Richardson, et al.]

### 1.2 Genetic Algorithm Procedure

According to Darwin natural evolution theory, the one who fits the environment most well are more possible to survive and reproduction. GA simulates the process of natural evolution which includes selection, crossover and mutation. Because of the powerful search ability of GA, it has been

widely used in many fields for multimodal problems. The procedure diagram of GA as shown in figure 1

### 1.3 Parent Selection

Selection is the most important step of GA algorithm which decides the diversity of the population. To improve the search ability and reduce the search cost, many selection methods [41991Goldberg and Deb] has been invented, the selection schemes can be divided into four classes which are proportionate reproduction, ranking selection, tournament selection and Genitor(or "steady state") selection. In this paper, to maintain a stable subpopulation for multimodal problems, the stochastic remainder algorithm is used for experiment.

### 1.4 Parents Crossover

According to the selected parents, crossover is used to generate the offspring, combining genes from parents to reproduce new members. There are so many research [52010Ahmed, 62009Nebro et al. Nebro, Durillo, Luna, Dorronsoro, and Alba], about the crossover operation in GAs to maximize the diversity of the population. In this paper, one-point crossover strategy is implemented.

### 1.5 Offspring Mutation

Mutation simulates the situation genes on the chromosomes which received from parents randomly changed. The process are used to provide new evolution direction and information for the population, the parameters has during this process has been well researched by Schaffer[71989Schaffer].

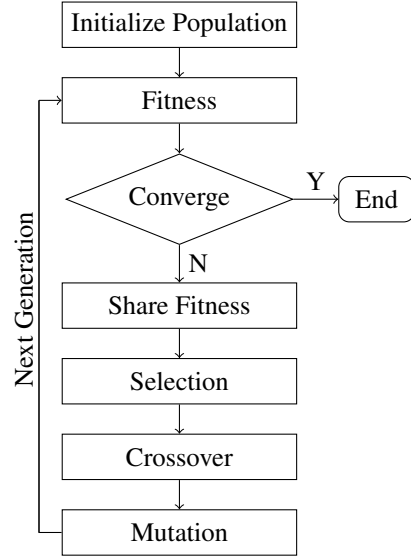


Fig. 1: GA Procedure with Share Function

### 1.6 Sharing

Sharing mechanism is first introduced by Holland [81996Miller and Shaw] to reduce the fitness of similar individual in the population and increase the diversity of the population. For Sharing mechanism, the most important thing is how to identify the number of niches, Miller came up dynamic niche sharing method, and lin developed the method to identify the number of niches in the population. [92002Lin and Wu]

### 1.7 Sharing Issue

The problem within sharing mechanism is how to identify the range of parameters in the formula. Given the number of peaks in population, Deb and Goldberg came up method to set up the appropriate value for  $\sigma_{sh}$ , however, in many problems, the number of peaks is difficult to identify, and more often, the fitness is discrete. So it is important to determine these parameters properly.

$$sh(d_{i,j}) = \begin{cases} 1 - \left(\frac{d_{i,j}}{\sigma_{sh}}\right)^{\alpha_{sh}} & \text{if } d_{i,j} < \sigma_{sh} \\ 0 & \text{otherwise} \end{cases} \quad (1)$$

## 2 Research Method

According to the following share function

$$\begin{aligned} \text{sh}(d) &= 1 - \left( \frac{d}{\sigma_{\text{share}}} \right)^\alpha, \quad d < \sigma_{\text{share}} \\ &= 0, \quad \text{otherwise} \end{aligned}$$

where  $d$  denotes distance between two strings,  $\alpha$  is a constant number,  $\sigma_{\text{share}}$  is also a constant number.

define share fitness  $f'_i$  as the following  
where  $m'_i$  indicates niche count,

$$d_{ij} = d(x_i, x_j) \quad (2)$$

There are three factors which influence the performance of GAs, which are metric space and two constant numbers. Metric space is one of the most important factors which influence the effect of GA. Suppose  $x_i$  and  $x_j$  denotes two different string in the population. Given the metric space  $(M, d)$ , metric function  $d$  is:

$$d : M \times M \rightarrow R$$

This can be divided into the following three steps, the first is the normalization of metric space.

### 1: Metric Normalization

In order to discuss the influence of different parameters, the normalization of metric distance is necessary, suppose  $d_{\max}$  means the longest distance between two strings in the population, So the distance can be normalized by the following formula:

$$d_{\text{norm}} = \frac{d_i}{d_{\max}} \quad (3)$$

After normalization the distance between any two points is:

$$0 \leq d_{ij} \leq 1 \quad (4)$$

### 2: Define Tensor

Define  $D$  and  $D^*$  as the basic metric space and dual metric space, which can be used as the basic building block to define all the metric space, and a tensor with  $r$  basic metric space and  $q$  dual metric space is defined as by the formula:

$$D = |x_i - x_j| \quad (5)$$

$$D^* = \sqrt{|x_i - x_j|} \quad (6)$$

$$t(r, s) := \underbrace{D \otimes \dots \otimes D}_r \times \underbrace{D^* \otimes \dots \otimes D^*}_s \rightarrow R \quad (7)$$

where  $R$  stands for real number.

3: constant  $d_{\text{share}}$  in share formula

Given the best tensor condition, increase the value of  $d_{\text{share}}$  to check the influence of  $d$  on the search ability of GAs. take the step length  $d_{\text{step}} = 0.5$ , after the normalization of metric space, the distance  $d_{\max}$  between two points in  $M$  satisfy  $d_{\max} \leq 1$ . According to the share function theory,  $d_{\text{share}}$  needs great then  $d_{\max}$ . So the range of is  $\{d_{\text{share}} | d > 1\}$

## 3 Experiment and Results

### 3.1 Experiment Method

#### 1. GA

In order to evaluate the impact of the parameters, the mutation process is ignored. The parameters of GA is shown in the table 1

Table 1: GA-parameters

parameter	value
population size	50
encoding method	binary encoding
encoding length	16
selection strategy	roulette wheel
crossover strategy	one-point
mutation strategy	None

The  $i$ th individual in the population converted from binary to decimal by the following formula:

$$x_i = \frac{\sum_{j=1}^{16} 2^{j-1} g_i^j}{2^{15}} \quad (8)$$

#### 2. Evaluation indexes

To evaluate the performance of GA algorithm, four index are come up. The first evaluation criterion is apparent reliability denoted as  $R$ , which is calculate by the following formula

$$R = \frac{n}{N} \quad (9)$$

$n$  stands for the number of GA finds at least one optimal point,  $N$  stands for the number of the run-time of GA.

The second criterion is the normalized cost of GA, denoted as  $C_n$ , which is calculated by the following equation:

$$C_n = N_g P / R \quad (10)$$

where  $P$  is population size.

The third criterion is population richness, denoted as  $P_r$ , which is calculated by the following formula:

$$P_r = N / P$$

Population richness is used to denote how many optimal points these GA maintains.

The fourth criterion is the number of best output, denoted by  $O_n$ .

The last criterion is the number of niche, denoted by  $N_n$ , the number of niche can be used to represents the ability of the GA to maintain sub-population.

### 3.2 Result

Example 1:

$$f_1(x) = \sin^6(5.1\pi x + .5) \quad (11)$$

The experiment result in the table 2, with  $d_{share}$  equals 2 and the value of  $\sigma$  is 1.

Table 2: Tensor Parameter

tensor	$R$	$C$	$O_n$	$P_r$	$N_n$
$t(1,0)$	0.99	2020	5.1	11.84	5.12
$t(0,1)$	0.97	2051	3.83	7.32	4.0
$t(1,1)$	0.82	2439	1.9	3.9	2.46
$t(0,2)$	0.86	2339	1.94	3.77	2.34
$t(1,2)$	0.94	2127	2.06	3.58	2.34
$t(2,2)$	0.82	2439	1.84	3.24	2.30
$t(0,3)$	0.89	2234	1.89	3.46	2.25
$t(1,3)$	0.89	2272	1.72	3.38	2.22
$t(2,3)$	0.90	2222	1.86	3.40	2.20
$t(3,3)$	0.94	2127	1.96	3.24	2.10

According to the table 2, with the sum of  $r + s$  increases, the population richness  $P_r$ , The number of best output  $O_n$  and the number of niches  $N_n$  decrease, and when  $r = 1$  and  $q = 0$ , apparent reliability  $R$  obtain the maximaize value, GA obtains the best result. as shown in Fig. 2

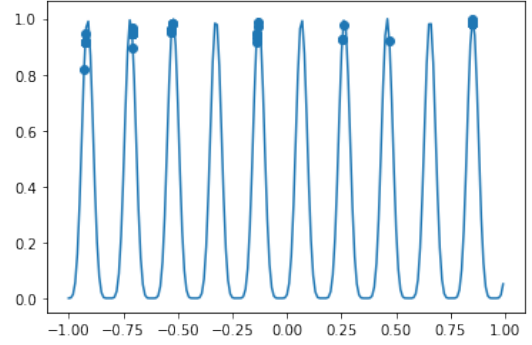


Fig. 2: Result 1

2. constant influence under tensor  $t(1,0)$

Because  $t(1,0)$  obtain the best search result,

Table 3:  $d_{share}$  parameter

$d_{share}$	$R$	$C$	$O_n$	$P_r$	$N_n$
1.1	0.98	2040	4.08	12.24	5.42
1.6	0.98	2040	5.10	13.36	5.52
2.1	0.98	2040	5.18	12.06	5.12
2.6	1.0	2000	5.16	10.2	4.66
3.1	0.98	2040	4.70	9.32	4.44
3.6	0.96	2083	4.5	8.22	4.12
4.1	0.98	2040	4.86	8.44	4.18

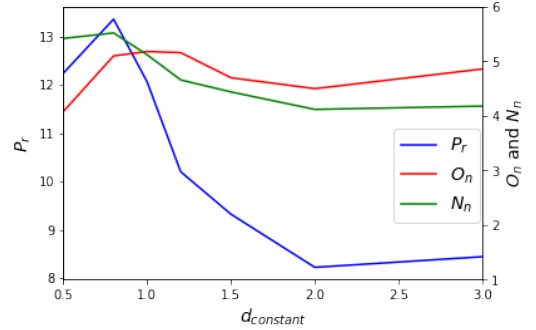


Fig. 3: metric denominator

According to Tab 3, we can see that when  $d_{share} = 1.6$ , the performance of GA is best; Combined with Fig.3, when

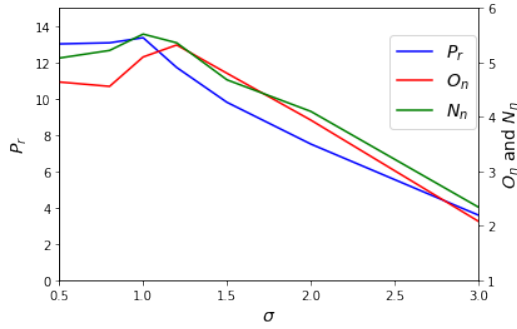
$$1.1 \leq d_{share} \leq 2.1$$

The GA performed the best.

3. power index influence

Table 4:  $\sigma$  parameter

$\sigma$	$R$	$C$	$O_n$	$P_r$	$N_n$
0.5	0.98	2040	4.64	13.02	5.08
0.8	0.92	2173	4.56	13.08	5.22
1.0	0.98	2040	5.10	13.36	5.52
1.2	0.98	2040	5.32	11.72	5.36
1.5	0.96	2083	4.80	9.80	4.68
2.0	0.96	2083	3.94	7.50	4.10
3.0	0.96	2083	2.08	3.58	2.34

Fig. 4:  $\sigma$  parameter

Example 2:

$$f_1(x) = \cos^6(5.1\pi x + .5)$$

Table 5: Metric Space Example

Metric	$R$	$C$	$O_n$	$P_r$	$N_n$
$t(1,0)$	1.00	2000	4.98	11.6	4.94
$t(0,1)$	0.96	2083	3.74	7.82	4.40
$t(1,1)$	0.94	2127	1.76	4.56	2.86
$t(0,2)$	0.88	2272	1.72	3.60	2.30
$t(1,2)$	0.92	2173	1.6	3.74	2.36
$t(2,2)$	0.94	2127	1.82	3.62	2.22
$t(0,3)$	0.86	2325	1.76	3.52	2.22
$t(1,3)$	0.92	2173	1.68	3.54	2.26
$t(2,3)$	0.94	2127	1.86	3.54	2.20
$t(3,3)$	0.94	2127	2.00	3.32	2.18

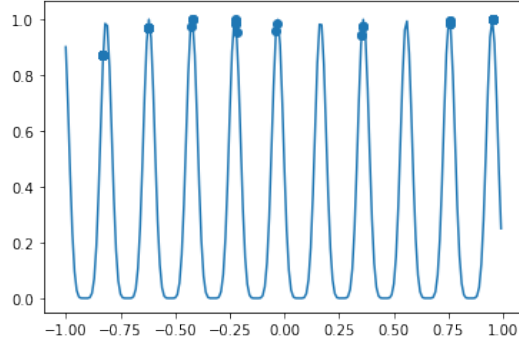


Fig. 5: Result 2

Table 6: Metric Space

$l_{step}$	$R$	$C$	$O_n$	$P_r$	$N_n$
1.1	0.98	2040	4.08	12.24	5.42
1.6	0.98	2040	5.10	13.36	5.52
2.1	0.98	2040	5.18	12.06	5.12
2.6	1.0	2000	5.16	10.2	4.66
3.1	0.98	2040	4.70	9.32	4.44
3.6	0.96	2083	4.5	8.22	4.12
4.1	0.98	2040	4.86	8.44	4.18

Four evaluation criteria are used. The first is normalized cost per genetic search,

$$C_n$$

cost is determined by the following formula.

#### 4 Conclusion

In this paper, three variables of sharing function tensor,  $d_{share}$ ,  $\sigma$  was analysed. The experiment result is measured by five indexes, normalized search cost, population richness, the number of niche number, the number of optima.

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