

a. Here * means AND, and ' means NOT

$$\begin{aligned}
 \text{i. } & (X+Y)*(X+Y') \\
 &= X*X + X*Y' + X*Y + Y*Y1 \\
 &= X + X*X' + X*Y \\
 &= X*(1 + Y + Y') \\
 &= X*1 \\
 &= X
 \end{aligned}$$

ii.

X	Y	Z	X+Y	X'+Z	Y+Z	(X+Y)*(X'+Z)	(X+Y)*(X'+Z)*(Y+Z)
0	0	0	0	1	0	0	0
0	0	1	0	1	1	0	0
0	1	0	1	1	1	1	1
0	1	1	1	1	1	1	1
1	0	0	1	0	0	0	0
1	0	1	1	1	1	1	1
1	1	0	1	0	1	0	0
1	1	1	1	1	1	1	1

By observation of the right-most two columns being the same, the expressions must be equal: $(X+Y)*(X'+Z) = (X+Y)*(X'+Z)*(Y+Z)$

b. Let $I = (A+C'+F'+G)*(A+C'+F+G)*(A+B+C'+D'+G)*(A+C+E+G)*(A'+B+G)*(B+C'+F+G)$

Let $X = A+C'+G$

Therefore $(A+C'+F'+G)*(A+C'+F+G) = (X+F')*(X+F) = X = A+C'+G$

Therefore $I = (A+C'+G)*(A+B+C'+D'+G)*(A+C+E+G)*(A'+B+G)*(B+C'+F+G)$

$= (A+C'+G)*(A'+B+G)*(B+C'+F+G)*(A+B+C'+D'+G)*(A+C+E+G)$

$= (A+C'+G)*(A'+B+G)*(B+C'+G)*(B+C'+F+G)*(A+B+C'+D'+G)*(A+C+E+G)$ by rule ii.

$= (A+C'+G)*(A'+B+G)*(B+C'+G)*(1+F)*(A+B+C'+D'+G)*(A+C+E+G)$

$= (A+C'+G)*(A'+B+G)*(B+C'+G)*(A+B+C'+D'+G)*(A+C+E+G)$

$= (A+C'+G)*(A'+B+G)*(B+C'+G)*(A+B+C'+D'+G)*(A+D'+G)*(A+C+E+G)$ by rule ii.

$= (A+C'+G)*(A'+B+G)*(B+C'+G)*(A+D'+G)*(1+B+C')*(A+C+E+G)$

$= (A+C'+G)*(A'+B+G)*(B+C'+G)*(A+D'+G)*(A+C+E+G)$

$= (A+C'+G)*(A'+B+G)*(A+D'+G)*(A+C+E+G)$ by rule ii.

$= (A+C'+G)*(A'+B+G)*((A+G)+D')*((A+G)+(C+E))$

$= (A+C'+G)*(A'+B+G)*((A+G)*(A+G)+(A+G)*(C+E)+D'*(A+G)+D'*(C+E))$

$= (A+C'+G)*(A'+B+G)*((A+G)*(1+D'+C+E)+D'*(C+E))$

$= (A+C'+G)*(A'+B+G)*(A+G+D'*(C+E))$

$= (A+C'+G)*(A'+B+G)*(A+G+C*D'+E*D')$

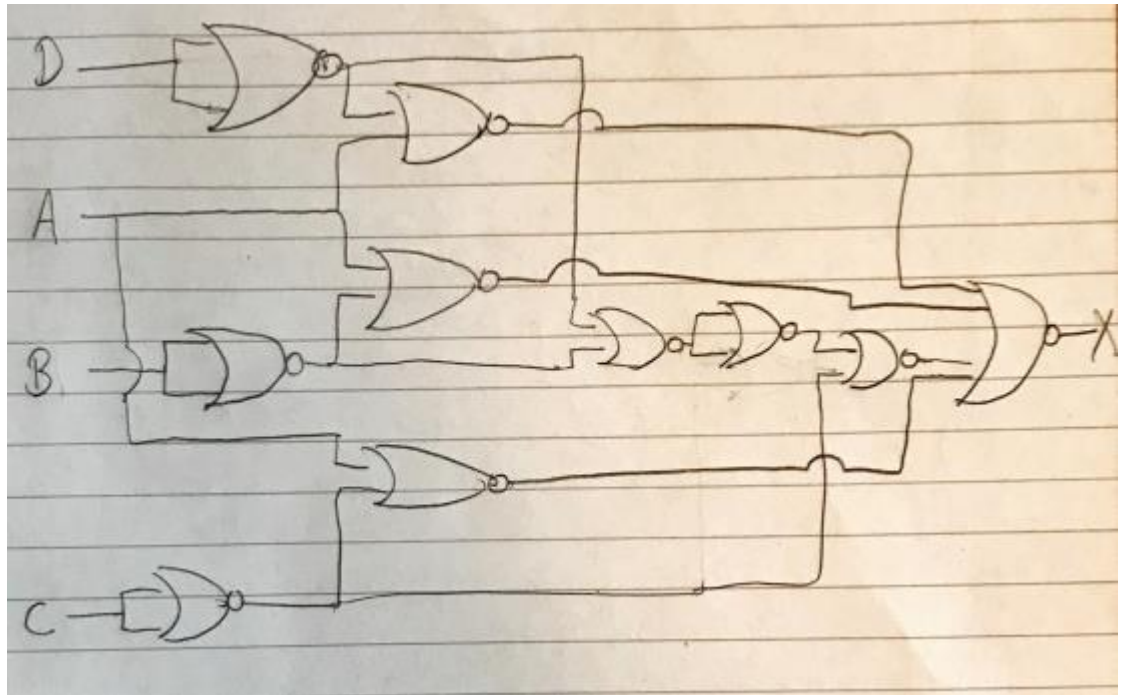
$= (A+C'+G)*(A'+B+G)*(A+E+G)$

c.

i.

CD\AB	00	01	11	10
00	1	0	1	1
01	0	0	1	1
11	0	0	0	1
10	0	0	1	1

$$\begin{aligned}
 V &= ((A'B) + (A'D) + (A'C) + (B'CD))' \\
 &= (A'B)' * (A'D)' * (A'C)' * (B'CD)' \\
 &= (A+B') * (A+D') * (A+C') * (B'+C'+D')
 \end{aligned}$$



ii.