

c) ~~$\left(\begin{pmatrix} 3 \\ 2 \\ 1 \end{pmatrix} \cdot \frac{1}{\sqrt{5}} \begin{pmatrix} -1 \\ 2 \\ 0 \end{pmatrix} = 0 \right)$ where~~

Let \vec{r} = the position vector of the point in the plane closest to the origin

$\therefore \vec{r} = \lambda \hat{n}$ where λ = the perpendicular distance to the plane from the origin

$$(\vec{r} - \vec{a}) \cdot \hat{n} = 0$$

for some point with position vector \vec{a} on the plane

$$\therefore \vec{r} \cdot \hat{n} - \vec{a} \cdot \hat{n} = 0$$

$$\therefore \lambda \hat{n} \cdot \hat{n} - \vec{a} \cdot \hat{n} = 0$$

$$\therefore \lambda = \vec{a} \cdot \hat{n}$$

\forall points on the plane with position vector \vec{a}

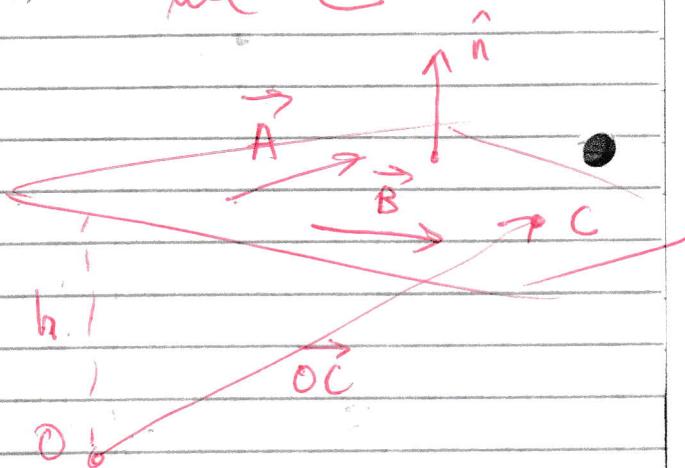
wlog. take $\vec{a} = \begin{pmatrix} 3 \\ 2 \\ 1 \end{pmatrix}$

use C

$$\therefore \lambda = \begin{pmatrix} 3 \\ 2 \\ 1 \end{pmatrix} \cdot \frac{1}{\sqrt{5}} \begin{pmatrix} -1 \\ 2 \\ 0 \end{pmatrix}$$

$$= \frac{1}{\sqrt{5}} (-3 + 4 + 0)$$

$$= \frac{1}{\sqrt{5}}$$



$$h = \vec{OC} \cdot \hat{n}$$

$$\hat{n} = \frac{\vec{A} \times \vec{B}}{\|\vec{A} \times \vec{B}\|}$$