

$$\therefore I + iJ = \frac{1}{a+bi} (e^{(a+bi)x} - 1)$$

$$= \frac{(a-bi)}{a^2+b^2} (e^{ax} (\cos(bx) + i \sin(bx)) - 1)$$

$$= \frac{(a-bi)(e^{ax} \cos(bx) + i e^{ax} \sin(bx) - 1)}{a^2+b^2}$$

$$= \frac{ae^{ax} \cos(bx) + aie^{ax} \sin(bx) - a - bi e^{ax} \cos(bx) + be^{ax} \sin(bx) + bi}{a^2+b^2}$$

$$= \frac{e^{ax} (b \sin(bx) + a \cos(bx)) + a}{a^2+b^2} + i \frac{e^{ax} (a \sin(bx) - b \cos(bx)) + b}{a^2+b^2}$$

$$\therefore I = \frac{e^{ax} (b \sin(bx) + a \cos(bx)) + a}{a^2+b^2}$$

$$J = \frac{e^{ax} (a \sin(bx) - b \cos(bx)) + b}{a^2+b^2}$$

$$15a. \text{ Let } I_n = \int_0^1 (1-x^{n-1})^n dx$$

By integration by parts on I_n :

$$\begin{array}{|l} \text{①} \\ + \quad (1-x^{n-1})^n \\ - \quad -n(n-1)x^{n-2} (1-x^{n-1})^{n-1} \end{array} \quad \begin{array}{|l} I \\ 1 \\ x \end{array}$$

$$I_n = \left[x(1-x^{n-1})^n \right]_0^1 + n(n-1) \int_0^1 x^{n-1} (1-x^{n-1})^{n-1} dx$$

$$= n(n-1) \int_0^1 x^{n-1} (1-x^{n-1})^{n-1} dx$$

$$= n(1-n) \int_0^1 -x^{n-1} (1-x^{n-1})^{n-1} dx$$

$$= n(1-n) \int_0^1 ((1-x^{n-1})(1-x^{n-1})^{n-1} - (1-x^{n-1})^{n-1}) dx$$