

## CS558 Introduction to Computer Security

## Chapter 11 Message Authentication and Hash Functions

### Message Authentication and Digital Signature

#### Message authentication

- ❖ Verify that received messages come from the **alleged source**.
- ❖ Verify the **integrity** of a message - data received are exactly as sent by.

### Attacks

- ❖ The following attacks can be identified

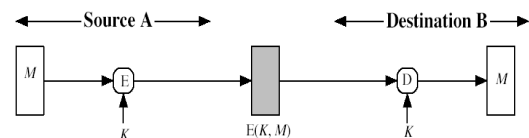
#### Message authentication

- **Masquerade**: insertion of messages into the network from a **fraudulent** source, e.g. fraudulent acknowledgments of message receipt/nonreceipt by someone other than the message recipient
- **Content modification**: changes to the content of a message, e.g. insertion, deletion
- **Sequence modification**: modify a sequence of messages
- **Timing modification**: delay or replay of messages

### Authentication Functions

- ❖ **Authentication functions**: produce an authenticator, a value that can be used to authenticate the message.
  - ❖ **Message encryption**: the ciphertext of the entire message serves as its authenticator
  - ❖ **Message authentication code (MAC)**: a function of the message and a secret key that produces a fixed-length value
  - ❖ **Hash function**: maps a message of any length into a fixed-length hash value

### Message Encryption: Symmetric Encryption



(a) Symmetric encryption: confidentiality and authentication

- ❖ B knows A must have created it
  - ❖ Since only sender and receiver know key used
- ❖ Knows content cannot be altered

## Message Encryption: Symmetric Encryption

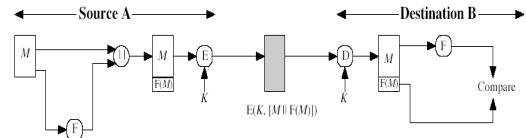
- **Problem:** given a decryption function  $D$  and a secret key  $K$ , the receiver will accept any input  $X$  and produce output  $Y=D(K,X)$ .
- If  $X$  is the ciphertext of a legitimate message  $M$ , then  $Y$  is  $M$ , otherwise, meaningless sequence of bits.

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## Symmetric Encryption: Internal Control

- **Solution:** force the plaintext to have some structure

- E.g. append an **error-detecting code** as a **frame check sequence (FCS)** to each message before encryption.
- **Sender:** prepares a plaintext message  $M$ , provides  $M$  as input to a function  $F$  that produces an FCS, appends FCS to  $M$  and encrypts entire block.
- **Receiver:** decrypts the block, treats the result as a message with an appended FCS, and applies  $F$  to reproduce FCS. If the **calculated FCS = incoming FCS**, then the message is considered authentic.



## Summary: Message Encryption (Symmetric)

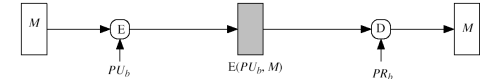
$A \rightarrow B: E(K, M)$

- Provides confidentiality
  - Only A and B share  $K$
- Provides a degree of authentication
  - Could come only from A
  - Has not been altered in transit
  - Requires some formatting/redundancy
- Does not provide signature
  - Receiver could forge message
  - Sender could deny message

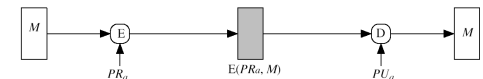
(a) Symmetric encryption

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## Public-key Encryption



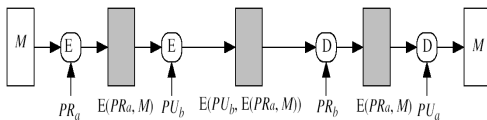
(b) Public-key encryption: confidentiality



(c) Public-key encryption: authentication and signature

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## Public-key Encryption



(d) Public-key encryption: confidentiality, authentication, and signature

- Sender signs message using their **private-key**
- Then encrypts with recipient's **public key**
- Have both **secrecy** and **authentication**
- Again, plaintext needs to have some **internal structure** so that the receiver can distinguish between well-formed plaintext and random bits.

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## Summary: Message Encryption (Public-key)

$A \rightarrow B: E(PU_b, M)$

- Provides confidentiality
  - Only B has  $PR_b$  to decrypt
- Provides no authentication
  - Any party could use  $PU_b$  to encrypt message and claim to be A

(b) Public-key (asymmetric) encryption: confidentiality

$A \rightarrow B: E(PR_a, M)$

- Provides authentication and signature
  - Only A has  $PR_a$  to encrypt
  - Has not been altered in transit
  - Requires some formatting/redundancy
- Any party can use  $PU_a$  to verify signature

(c) Public-key encryption: authentication and signature

$A \rightarrow B: E(PU_b, E(PR_a, M))$

- Provides confidentiality because of  $PU_b$
- Provides authentication and signature because of  $PR_a$

(d) Public-key encryption: confidentiality, authentication, and signature

### Message Authentication Codes

- A MAC function is similar to **encryption**
  - ❖ Difference: MAC alg. **needs not be reversible**, as it must for decryption. In general, MAC function is a **many-to-one** function - many different messages may generate the same MAC value.

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### Message Authentication Code (MAC)

(a) Message authentication

- Use a secret key to generate a small fixed-size block of data  $MAC = C(K, M)$ 
  - ❖  $M$ : input mesg.  $C$ : MAC function.  $K$ : shared secret key
- The message + MAC are transmitted.
- Receiver performs same computation on message and checks it matches the MAC

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### Message Authentication Code (MAC)

(a) Message authentication

- Does this assure that message is **unaltered** and comes from sender?

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  - ❖ Yes

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### Message Authentication Code (MAC)

(a) Message authentication

- Does this assure that message is **unaltered** and comes from sender?
  - ❖ Yes
  - ❖ If an attacker alters the message, then the receiver's calculation of the MAC will differ from the received MAC.
  - ❖ No one else knows the secret key, no one else could prepare a message with a proper MAC.

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### Message Authentication Codes

(a) Message authentication

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### Message Authentication Codes

(a) Message authentication

- Provides **authentication** but not **confidentiality**
  - because the message is transmitted in the clear.

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### Message Authentication Codes

(b) Message authentication and confidentiality; authentication tied to plaintext

(c) Message authentication and confidentiality; authentication tied to ciphertext

- Provides both **authentication** and **confidentiality**
  - Performing encryption after or before the MAC algorithm.

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### Message Authentication Codes

- Symmetric encryption will provide authentication. Why use a MAC?

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### Message Authentication Codes

- Symmetric encryption will provide authentication. Why use a MAC?
  - Sometimes only authentication is needed.
  - One side has a heavy load and cannot afford the time to decrypt all incoming messages - messages are chosen at random for checking
- MAC does **not** provide a **digital signature** because both sender and receiver share the same key.

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### Hash Functions

- Is a variation on the message authentication code
- A hash function accepts a **variable-size** message **M** as input and produces a **fixed-size** output, referred to as a hash code **H(M)**
  - Hash code: **message digest** or **hash value**
- Unlike a MAC, a hash code **does not use a key**, but is a function only of the input message.
- Hash code is used to detect changes to message - a change to **any** bit(s) in the message results in a change to the hash code
- Can use in various ways with message
- Most often to create a digital signature

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### Using Hash Code (1)

(a)

- The message plus concatenated hash code is encrypted using symmetric encryption.
- The message must come from A because only A and B share the secret key.
- The hash code provides the structure required to achieve **authentication**.

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### Using Hash Code (1)

(a)

- The message plus concatenated hash code is encrypted using symmetric encryption.
- The message must come from A because only A and B share the secret key.
- The hash code provides the structure required to achieve **authentication**.
- **Confidential** is also provided because encryption is applied to the entire message.

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### Using Hash Code (2)

(b)

- Only the hash code is encrypted using symmetric encryption
- For applications that do not require confidentiality.

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### Using Hash Code (3)

(c)

- Only the hash code is encrypted using public-key encryption and using sender's private key

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### Using Hash Code (4)

(d)

- If **confidentiality** as well as a **digital signature** is desired, then the message plus the **private-key-encrypted hash code** can be encrypted using a **symmetric secret key**.

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### Using Hash Code (5)

(e)

- It is possible to use a hash function but **no encryption** for message authentication
- Two parties share a **common secret value S**.
- A computes the hash value over the concatenation of **M** and **S**, and appends the resulting hash value to M
- B has S, so can recompute the hash value to verify.
- Because S is not sent, an attacker cannot modify a message or generate a false message.

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### Requirements for Hash Functions

The purpose of a hash function is to produce a **fingerprint** of a file, message, etc

- A hash function must have the following properties:
  - Can be applied to any sized message **M**
  - Produces fixed-length output **hc**
  - Is easy to compute  $hc = H(M)$  for any message **M**
  - Given **hc** is infeasible to find **x** s.t.  $H(x) = hc$ 
    - **Example in the previous slide:** if not hold, an attacker can easily discover the secret value **s**
  - Given **x** is infeasible to find **y** s.t.  $H(y) = H(x)$
  - It's infeasible to find any **x, y** s.t.  $H(y) = H(x)$

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## Simple Hash Functions

- The input is viewed as a sequence of ***n*-bit blocks**.
- A simple hash function: **XOR** of message blocks

$$C_i = b_{i1} \oplus b_{i2} \oplus \dots \oplus b_{im}$$

- $C_i$ : *i*th bit of the hash code,  $1 \leq i \leq n$
- $m$ : number of *n*-bit blocks in the input
- $B_{ij}$ : *i*th bit in *j*th block

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## Simple Hash Functions

### Not secure

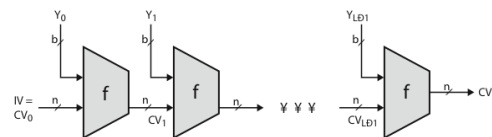
- It is easy to produce a new message that yields the hash code.
- Simply prepare the desired alternate message and then append an *n*-bit block that forces the new message plus block to yield the desired hash code
- Need a stronger cryptographic function (next chapter)

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## Chapter 12 Hash Algorithms

## Hash Algorithm Structure

- The hash function takes an input message and partitions it into ***L* fixed-sized blocks of *b* bits each**.
- The final block also includes **the value of the total length of the input** to the hash function - makes the job of the attacker more difficult

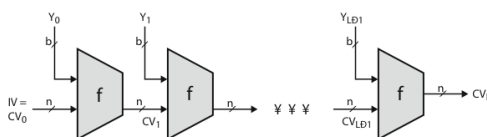


$IV$  = Initial value  
 $CV_i$  = chaining variable  
 $Y_i$  = *i*th input block  
 $f$  = compression algorithm

$L$  = number of input blocks  
 $n$  = length of hash code  
 $b$  = length of input block

## Hash Algorithm Structure

- The algorithm repeatedly uses a compression function ***f*** that takes two inputs
  - An ***n*-bit** output from previous step - chaining variable
  - A ***b*-bit** block
- And produces an ***n*-bit** output.  $b > n \rightarrow$  compression

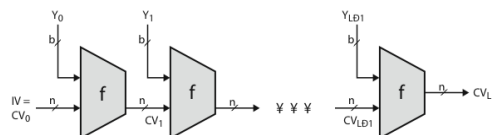


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## Hash Algorithm Structure

- **$CV_0 = IV =$  initial *n*-bit value**
- **$CV_i = f(CV_{i-1}, Y_{i-1}), 1 \leq i \leq L$**
- **$H(M) = CV_L$ , *M* consists of  $Y_0, Y_1, \dots, Y_{L-1}$**



$IV$  = Initial value  
 $CV_i$  = chaining variable  
 $Y_i$  = *i*th input block  
 $f$  = compression algorithm

$L$  = number of input blocks  
 $n$  = length of hash code  
 $b$  = length of input block

## Secure Hash Algorithm (SHA)

- Originally designed by **National Institute of Standards and Technology (NIST)** in 1993
- SHA-1 (160 bits), SHA-256 (256 bits), SHA-512 (512 bits) .....
- We will focus on **SHA-512**: takes as input a message with a maximum length of less than  $2^{128}$  bits and produces as output a **512-bit** message digest.

## SHA-512 Overview

$\oplus$  = word-by-word addition mod  $2^{64}$

- Follows the general structure
- Processing message in 1024-bit blocks

## SHA-512 Overview

$\oplus$  = word-by-word addition mod  $2^{64}$

- Step 1: Append padding bits**
  - The message is padded so that  $\text{length} \bmod 1024 = 896$ . The padding consists of a single 1-bit followed by the necessary number of 0-bits.

## SHA-512 Overview

$\oplus$  = word-by-word addition mod  $2^{64}$

- Step 2: Append length**
  - A block of 128 bits is appended to the message, that contains the length of the original message (does not include the padding)
  - Length of the expanded message:  $N \times 1024$ .

## SHA-512 Processing of a Single 1024-Bit Block

- Step 3: Initialize hash buffer**
  - A 512-bit buffer is used to hold intermediate and final results of the hash function. The buffer can be represented as eight 64-bit registers (a,b,c,d,e,f,g,h)

## SHA-512 Processing of a Single 1024-Bit Block

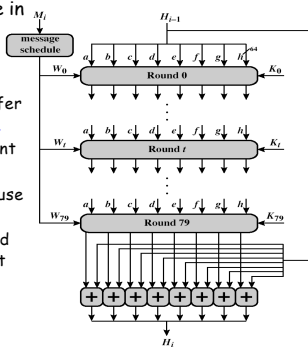
- Step 3: Initialize hash buffer**
  - The 8 registers are initialized to the following 64-bit integers (hexadecimal values):

a = 6A09E667F3BCC908  
 b = BB67AE8584CAA73B  
 c = 3C6EF372FE94F82B  
 d = A54FF53A5F1D36F1  
 e = 510E527FADE682D1  
 f = 9B05688C2B3E6C1F  
 g = 1F83D9ABFB41BD6B  
 h = 5BE0CD19137E2179

## SHA-512 Processing of a Single 1024-Bit Block

- Step 4: Process message in 1024-bit (128-word) blocks

- Consists of 80 rounds
- Updating a 512-bit buffer
- Using a 64-bit value  $W_i$  derived from the current message block  $M_i$
- Each round also makes use of a constant  $K_i$
- The output of the Round 79 is added to the input to the first round to produce  $H_i$ .



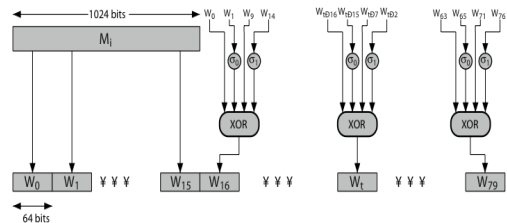
## Creation of 80-Word Input Sequence

$$\sigma_0(x) = \text{ROTR}^1(x) \oplus \text{ROTR}^8(x) \oplus \text{SHR}^7(x)$$

$$\sigma_1(x) = \text{ROTR}^{19}(x) \oplus \text{ROTR}^{61}(x) \oplus \text{SHR}^6(x)$$

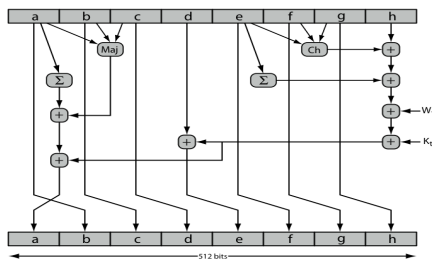
$\text{ROTR}^n(x)$  = circular right shift of the 64-bit argument  $x$  by  $n$  bits

$\text{SHR}^n(x)$  = left shift of the 64-bit argument  $x$  by  $n$  bits with padding by zeros on the right



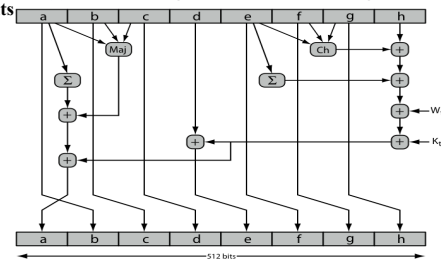
## SHA-512 Round Function

- $T1 = h + \text{Ch}(e,f,g) + \Sigma e + Wi + Ki$ ,  $T2 = \Sigma a + \text{Maj}(a,b,c)$
- $a = T1 + T2$ ,  $b = a$ ,  $c = b$ ,  $d = c$ ,  $e = d + T1$ ,  $f = e$ ,  $g = f$ ,  $h = g$
- $\text{Maj}(a,b,c) = (a \text{ AND } b) \oplus (a \text{ AND } c) \oplus (b \text{ AND } c)$
- $\text{ch}(e,f,g) = \text{if } e \text{ then } f \text{ else } g$



## SHA-512 Round Function

- $T1 = h + \text{Ch}(e,f,g) + \Sigma e + Wi + Ki$ ,  $T2 = \Sigma a + \text{Maj}(a,b,c)$
- $a = T1 + T2$ ,  $b = a$ ,  $c = b$ ,  $d = c$ ,  $e = d + T1$ ,  $f = e$ ,  $g = f$ ,  $h = g$
- $\Sigma e = \text{ROTR}^{14}(e) \oplus \text{ROTR}^{18}(e) \oplus \text{ROTR}^{41}(e)$
- $\text{ROTR}^n(x)$  = circular right shift of the 64-bit argument  $x$  by  $n$  bits



## Midterm Exam

- Date: March 15th (Thursday)
- Time: 4:25pm - 5:50pm
- Place: LH-009
- Close book, close notes

## Final Exam

- Date: May 11th (Friday)
- Time: 10:25am - 12:25
- Place: FA-258
- Close book, close notes