

We will analyse the distributions of various extrasolar planets. We will group them into separate clusters, calculate missing information, find the most extreme known planets, and make predictions about the future.

Data has been retrieved from the NASA Exoplanet Archive on the following link: <a href="https://exoplanetarchive.ipac.caltech.edu/cgi-bin/TblView/nph-tblView?app=ExoTbls&config=PS">https://exoplanetarchive.ipac.caltech.edu/cgi-bin/TblView/nph-tblView?app=ExoTbls&config=PS</a>

Firstly, we import the necessary libraries:

import pandas as pd
import numpy as np
import os
import random

import matplotlib.pyplot as plt
from matplotlib.pyplot import figure
import seaborn as sns

from math import pi
import math

from pandas.io.html import read\_html
from urllib.error import HTTPError
import urllib.request

```
from sklearn.cluster import KMeans
from sklearn.cluster import SpectralClustering
sns.set(rc={"figure.figsize":(10, 4)})
pd.set_option('display.max_columns', None)
```

The data has been retrieved and is located on my google disk. Let us download it:

# Loading the Data

```
exoplanets = pd.read_csv('exoplanets.csv', parse_dates=[90])

/usr/local/lib/python3.8/dist-packages/IPython/core/interactiveshell.py:3326: DtypeWa exec(code_obj, self.user_global_ns, self.user_ns)
```

We are dropping all data that does not concern the planet, the star or the system it is orbiting in. Exoplanet research is a relatively new field, and with less than 6000 confirmed exoplanets, there are many inaccuracies and insecurities concerning the general exoplanet population. Nevertheless, the data that is available can paint an interesting picture. We will be removing all upper and lower limits of data as well.

Lets see what data remains within our dataset.

```
exoplanets.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 33829 entries, 0 to 33828
Data columns (total 18 columns):
               Column
                                                                   Non-Null Count Dtype
                                                              -----
              -----

      pl_name
      33829 non-null object

      hostname
      33829 non-null object

      sy_snum
      33829 non-null int64

      sy_pnum
      33829 non-null int64

   1
   2
   3
   4
               discoverymethod 33829 non-null object

      5
      disc_year
      33829 non-null int64

      6
      disc_facility
      33829 non-null object

      7
      pl_orbper
      30957 non-null float64

      8
      pl_orbsmax
      18521 non-null float64

      9
      pl_rade
      23383 non-null float64

      10
      pl_bmasse
      5043 non-null float64

      11
      pl_orbeccen
      16923 non-null float64

      12
      pl_eqt
      15396 non-null float64

      13
      st_spectype
      1976 non-null float64

      14
      st_teff
      31421 non-null float64

      15
      st_rad
      31541 non-null float64

      16
      st_mass
      28555 non-null float64

      17
      sy_dist
      33029 non-null float64

    5
               disc_year 33829 non-null int64
   17 sy_dist
                                                                 33029 non-null float64
dtypes: float64(10), int64(3), object(5)
memory usage: 4.6+ MB
```

Features starting in "pl" relate to the planet, those that start with "st" relate to the star the planet orbits, and "sy" to the exoplanet system.

- pl\_name, pl\_orbper, pl\_orbsmax, pl\_rade, pl\_bmasse, pl\_orbeccen, pl\_eqt are: the name, orbital period, orbital distance, planet's radius, planet's mass, orbital eccentricity, and the equilibrium temperature. These values (except the temperature) are expressed in Earth units.
- hostname the name of the parent star
- sy\_snum, sy\_pnum, sy\_dist are: the number of stars within the system, the number of other known exoplanets in the system, and the system's distance to Earth.
- discoverymethod, disc\_year, disc\_facility are: the method of exoplanet's discovery, the year
  of its discovery, and the science facility that discovered it.
- st\_specttype, st\_teff, st\_rad, st\_mass are: the parent star's spectral type, its temperature, radius, and mass. These values (except the temperature) are expressed in Solar units.

# **Cleaning the Data**

We will be converting data to other types to speed up execution time and reduce the space occupied by the dataset. As well as calculating additional features.

```
# categorical data
exoplanets['discoverymethod'] = exoplanets['discoverymethod'].astype('category')
exoplanets['disc_facility'] = exoplanets['disc_facility'].astype('category')

# numberical data
exoplanets['sy_snum'] = exoplanets['sy_snum'].astype('int8')
exoplanets['sy_pnum'] = exoplanets['sy_pnum'].astype('int8')
exoplanets['disc_year'] = exoplanets['disc_year'].astype('int16')
```

When we take a look at the dateset now:

```
exoplanets.info()
```

The dataset size has been reduced by 1.3 MB. Now, lets take a look at our data:

exoplanets.head()

	pl_name	hostname	sy_snum	sy_pnum	discoverymethod	disc_year	disc_facilit
0	Kepler-10 b	Kepler-10	1	2	Transit	2011	Keple
1	Kepler-102 e	Kepler-102	1	5	Transit	2013	Keple

2	Kepler-1651 b	Kepler-1651	2	1	Transit	2017	Keple
3	Kepler-210	Kepler-210	1	2	Transit	2014	Keple

## And a specific planet:

exoplanets.loc[exoplanets['pl\_name'] == "TRAPPIST-1 b"]

	pl_name	hostname	sy_snum	sy_pnum	discoverymethod	disc_year	disc_fa
114	TRAPPIST-1 b	TRAPPIST-1	1	7	Transit	2016	Obse
115	TRAPPIST-1 b	TRAPPIST-1	1	7	Transit	2016	Obse
3123	TRAPPIST-1 b	TRAPPIST-1	1	7	Transit	2016	Obse
15455	TRAPPIST-1 b	TRAPPIST-1	1	7	Transit	2016	Obse

Here we see that there are multiple entries for each exoplanet. This is because the exoplanet archive keeps track of previous entries. We need a way to reduce the data down into one entry per planet.

The logic behind how we will do this is as follows:

- 1. We will create a separate dataframe, called "temp1" which contains the most recent data for each planet.
- 2. We will create another dataframe, called "temp2" that contains all other entries.
- 3. temp2, with its other entries, will be reduced to one entry per planet, taking the average of each column. In this way, we get the "most agreed upon" value for each data point.
- 4. We will merge the two dataframes, keeping only the "first" data point per each column, for each exoplanet.

In summary, we will take the most recent value provided, if thet value is missing, we will take the average of all older values.

```
temp1 = exoplanets.copy()
temp1.drop_duplicates(subset=["pl_name"], inplace=True, ignore_index=True)
```

Lets check this dataset really does contain only the newest datapoints for each planet.

temp1.loc[temp1['hostname'] == "TRAPPIST-1"]

	pl_name	hostname	sy_snum	sy_pnum	discoverymethod	disc_year	disc_facil:
88	TRAPPIST-1 b	TRAPPIST-1	1	7	Transit	2016	La ६ Observal
89	TRAPPIST-1 c	TRAPPIST-1	1	7	Transit	2016	La ६ Observal
90	TRAPPIST-1 d	TRAPPIST-1	1	7	Transit	2016	La { Observal
91	TRAPPIST-1 e	TRAPPIST-1	1	7	Transit	2017	Mult Observato
92	TRAPPIST-1 f	TRAPPIST-1	1	7	Transit	2017	Mult Observator

Now, we create a dataframe that contains all older datapoints.

```
temp2 = exoplanets.copy()
temp2 = temp2[temp2.duplicated('pl_name') | ~temp2.duplicated('pl_name', keep=False)]
temp2= temp2.groupby('pl_name').mean()
temp2.reset_index(inplace=True)
```

temp2.loc[temp2['pl\_name'] == "TRAPPIST-1 b"]

	pl_name	sy_snum	sy_pnum	disc_year	pl_orbper	pl_orbsmax	pl_rade	pl_bma
4947	TRAPPIST-1	1.0	7.0	2016.0	1.510848	0.011327	1.109	1.080

We see in the cell above that this dataframe does indeed contain the average of all older datapoints.

```
temp1 = pd.concat([temp1, temp2], ignore_index=True)
```

temp1.loc[temp1['pl\_name'] == "TRAPPIST-1 b"]

	pl_name	hostname	sy_snum	sy_pnum	discoverymethod	disc_year	disc_fa
88	TRAPPIST-1 b	TRAPPIST-1	1.0	7.0	Transit	2016.0	Obse
10174	TRAPPIST-1	NaN	1 0	7 0	NaNi	2016 D	

Within the temp1 dataframe we now have two rows for each planet. The first contains the

newest data, and the second contains the average of the remaining rows. We will now take the "first" datapoint of each column for each exoplanet.

```
exoplanets = temp1.groupby('pl_name').first()
exoplanets.reset_index(inplace=True)
```

Lets take a look at one of the planets:

exoplanets.loc[exoplanets['pl\_name'] == "TRAPPIST-1 b"]

	pl_name	hostname	sy_snum	sy_pnum	discoverymethod	disc_year	disc_fac
4947	TRAPPIST-1	TRAPPIST-1	1.0	7.0	Transit	2016.0	L: Obser

How many values we are still missing?

exoplanets.isnull().sum(axis = 0)

pl_name	0
hostname	0
sy_snum	0
sy_pnum	0
discoverymethod	0
disc_year	0
<pre>disc_facility</pre>	0
pl_orbper	184
pl_orbsmax	281
pl_rade	1223
pl_bmasse	2831
pl_orbeccen	675
pl_eqt	1354
st_spectype	4684
st_teff	325
st_rad	453
st_mass	27
sy_dist	114
dtype: int64	

Some missing values can be calculated, some can be found on the internet. First, lets handle orbital period and orbital distance.

The orbital distance (pl\_orbsmax) and orbital period (pl\_orbper) are closely related with Kepler's Third Law:

$$P^2 = a^2 * M$$

```
P = Period in years
a = semi major axis (SMA) in AU

M = mass of the star in solar masses

exoplanets[(exoplanets.pl_orbper.notnull() & exoplanets.pl_orbsmax.isnull() & exoplanets.st
```

438

We have 438 planets with either a missing period or distance, and the other parameter available. We can calculate them both using the following functions:

```
def calcSMA(Period, solarMass):
    return round(((Period**2)*solarMass)**(1/3),5)

def calcPeriod(SMA, solarMass):
    return round(((SMA**3)/solarMass)**(0.5),5)
```

We will create temporary dataframes to calcualte the missing values and add them back into our original dataframe.

```
temp1 = exoplanets[(exoplanets.pl_orbper.notnull() & exoplanets.pl_orbsmax.isnull() & exopl
temp1.pl_orbsmax = calcSMA(temp1.pl_orbper/365.25, temp1.st_mass)
exoplanets = pd.concat([exoplanets, temp1], ignore_index=True)
exoplanets.drop_duplicates(subset=["pl_name"], keep='last', inplace=True, ignore_index=True)
temp1 = exoplanets[(exoplanets.pl_orbper.isnull() & exoplanets.pl_orbsmax.notnull() & exopl
temp1.pl_orbper = calcPeriod(temp1.pl_orbsmax, temp1.st_mass)*365.25
exoplanets = pd.concat([exoplanets, temp1], ignore_index=True)
exoplanets.drop_duplicates(subset=["pl_name"], keep='last', inplace=True, ignore_index=True
exoplanets[(exoplanets.pl_orbper.notnull() & exoplanets.pl_orbsmax.isnull() & exoplanets.st
```

We no longer have any planets with either a missing SMA or orbital period. There are systems which are missing their distance to the sun. We can find these distances using web-scraping. We will check the wiki page of each star and retrieve its distance to the sun.

The function for this is defined below:

```
def findDistance(hostname):
```

```
page = 'https://en.wikipedia.org/wiki/NAMESYS'
  page = page.replace("NAMESYS", hostname)
  page = page.replace(" ", "%20")
  try:
   try:
      infoboxes = read_html(page, index_col=0, attrs={"class":"infobox"})
     try:
        distance1 = infoboxes[0].xs(u'Distance').values[0]
        distance2 = ''.join([str(elem) for elem in distance1]).replace(",", ".").replace("
        distance3 = round(float(distance2.lstrip().split(' ')[0])*0.3066,4)
        return distance3
      except KeyError as err:
        #print(f"{err} during the search for {hostname}")
        return None
   except ValueError as err:
      #print(f"{err} during the search for {hostname}")
      return None
 except HTTPError as err:
    if err.code == 404:
      #print(f"Cannot find the wiki page for {hostname}")
      return None
   else:
      raise
temp1 = exoplanets[exoplanets.sy_dist.isnull()].copy()
temp1["sy_dist"] = temp1.hostname.apply(lambda x: findDistance(x))
nFound = temp1[temp1.sy_dist.notnull()].groupby('hostname').first().pl_name.count()
exoplanets = pd.concat([exoplanets, temp1], ignore_index=True)
exoplanets.drop_duplicates(subset=["pl_name"], keep='last', inplace=True, ignore_index=True
print(f"{nFound} previously unknown system distances found")
     11 previously unknown system distances found
Lets try finding the star spectral types as well.
temp1 = exoplanets.groupby("hostname").first()["st_spectype"].isnull().sum()
print(f"{temp1} stars are missing their spectral type.")
     3503 stars are missing their spectral type.
def findStarType(hostname):
  page = 'https://en.wikipedia.org/wiki/NAMESYS'
  page = page.replace("NAMESYS", hostname)
  page = page.replace(" ", "%20")
 try:
```

```
try:
      infoboxes = read html(page, index col=0, attrs={"class":"infobox"})
      try:
        value = infoboxes[0].xs(u'Spectral type').values[0]
        return value
      except KeyError as err:
        #print(f"{err} during the search for {hostname}")
        return None
   except ValueError as err:
      #print(f"{err} during the search for {hostname}")
      return None
  except HTTPError as err:
    if err.code == 404:
      #print(f"Cannot find the wiki page for {hostname}")
   else:
      raise
# scrapedStarTypes = exoplanets[exoplanets.st_spectype.isnull()].copy()
# scrapedStarTypes["st_spectype"] = scrapedStarTypes.hostname.apply(lambda x: findStarType)
# temp2 = scrapedStarTypes[scrapedStarTypes.st_spectype.notnull()].groupby('hostname').firs
# print(f"{temp2} previously unknown star types found")
```

The cell above takes a long time to execute, around 40 minutes. So we will just load its result with the cell below. You can run the cell above if you wish, but you need to skip the one immediately below.

```
urllib.request.urlretrieve("https://drive.google.com/uc?id=1xbGiJaON0zst06uv3_201tyjYosvMWF
scrapedStarTypes = pd.read_csv('scrapedStarTypes.csv', index_col=0)
scrapedStarTypes = scrapedStarTypes.reset_index(level=0)
```

Lets add the found stars into our dataset.

```
exoplanets = pd.concat([exoplanets, scrapedStarTypes], ignore_index=True)
exoplanets.drop_duplicates(subset=["pl_name"], keep='last', inplace=True, ignore_index=True
exoplanets["st_spectype"] = exoplanets.st_spectype.astype(str)
exoplanets["st_spectype"] = exoplanets.st_spectype.apply(lambda x: str(x[:2]))
exoplanets["st_spectype"] = exoplanets.st_spectype.apply(lambda x: None if x == "No" else )
exoplanets.st_spectype = exoplanets.st_spectype.apply(lambda x: None if x=="na" else x)

temp2 = exoplanets.groupby("hostname").first()["st_spectype"].isnull().sum()
```

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```
print(†"{temp2} stars are missing their spectral type. We found {temp1-temp2} missing star 3228 stars are missing their spectral type. We found 275 missing star types
```

An important property of planets is the Equilibrium Temperature. It can be calcualted using the temperature and the radius of the parent star, the distance to the planet, and its albedo. Source:https://www.astro.princeton.edu/~strauss/FRS113/writeup3/

We will be assuming an Albedo value of 0.28.

Lets see how many planets are missing their Equilibrium Temperatures.

```
exoplanets[exoplanets.st_teff.notnull() & exoplanets.pl_eqt.isnull() & exoplanets.st_rad.notnull() & exoplanets.st_rad.notnull
```

For these planets we will calculate the Equilibrium Temperature with the following function:

```
def calculateEQTemperature(solarRadi, SMAinAU, T):
    R = solarRadi * 696340
    SMA = SMAinAU * 150000000
    Albedo = 0.28
    return T*((R/(SMA*2))**(0.5))*((1-Albedo)**(1/4))
```

Lets see how well our equation performs on planets for which we know the equilibrium temperature:

```
\label{ligible} eligible = exoplanets[exoplanets.st\_teff.notnull() \& exoplanets.pl\_eqt.notnull() \& exoplaneteligible
```

3841

We will perform the check with 3841 planets. We will create a separate dataframe to perform the calculation. We will calculate a delta temperature - a percentage value that tells us how wrong our calculated value is. We will then see how many planets fall within 10% of the expected value.

```
checkTemp = exoplanets[exoplanets.st_teff.notnull() & exoplanets.pl_eqt.notnull() & exoplar
checkTemp["calculatedTemp"] = calculateEQTemperature(checkTemp.st_rad, checkTemp.pl_orbsma)
checkTemp["deltaTemp"] = checkTemp.pl_eqt/checkTemp.calculatedTemp
within10 = checkTemp[(checkTemp.deltaTemp > 0.9) & (checkTemp.deltaTemp < 1.1)].pl_name.co
within1 = checkTemp[(checkTemp.deltaTemp > 0.99) & (checkTemp.deltaTemp < 1.01)].pl_name.co
print(f"Of {eligible} planets, {within10/eligible:2.1%} fall within 10% of the real value.</pre>
```

```
Of 3841 planets, 79.5% fall within 10% of the real value. 23.5% within 1%
```

These values are acceptable, and we move forward with the calculation. We will calculate the missing values in a separate dataframe, concat it back into exoplanets, and keep the last row which contains the temperature.

```
temp1 = exoplanets[exoplanets.st_teff.notnull() & exoplanets.pl_eqt.isnull() & exoplanets.st
temp1.pl_eqt = calculateEQTemperature(temp1.st_rad, temp1.pl_orbsmax, temp1.st_teff)
exoplanets = pd.concat([exoplanets, temp1], ignore_index=True)
exoplanets.drop_duplicates(subset=["pl_name"], keep='last', inplace=True, ignore_index=True)
```

Lets see how many eligible planets are missing their eq temperature now:

```
exoplanets[exoplanets.st_teff.notnull() & exoplanets.pl_eqt.isnull() & exoplanets.st_rad.notnull() & exoplanets.st_rad.notnull()
```

For the following missing values, we have no way of calculating, or retrieving them from elsewhere on the internet. We can however, calculate new variables that can be useful in our analysis.

```
exoplanets.isnull().sum(axis = 0)
```

pl_name	0
hostname	0
sy_snum	0
sy_pnum	0
discoverymethod	0
disc_year	0
<pre>disc_facility</pre>	0
pl_orbper	11
pl_orbsmax	16
pl_rade	1223
pl_bmasse	2831
pl_orbeccen	675
pl_eqt	449
st_spectype	4266
st_teff	325
st_rad	453
st_mass	27
sy_dist	96
ttv_flag	1509
dtype: int64	

One of these useful variables, is the Earth Similarity Index. A scalar that attempts to reduce the

dimensionality of the differences of planetary characteristic when compared to Earth. In other words, the closer the ESI value is to 1, the closer that planet is to being Earth.

It is explained in the Earth Similarity Index and Habitability Studies of Exoplanets paper.

Earth Similarity Index and Habitability Studies of Exoplanets: <a href="https://arxiv.org/ftp/arxiv/papers/1801/1801.07101.pdf">https://arxiv.org/ftp/arxiv/papers/1801/1801.07101.pdf</a>

One of the variables needed for ESI, is the surface temperature. We can approximate it with the equation given in the paper above:

```
def calculateSurfaceTemp(pl_eqt):
    return 9.65 + 1.096 * pl_eqt

exoplanets["pl_sut"] = calculateSurfaceTemp(exoplanets.pl_eqt)
col = exoplanets.pop("pl_sut")
exoplanets.insert(13, col.name, col)
```

The surface temperatures have been calculated and moved to an appropriate position in the dataframe.

Next, we calculate the density of planets for which we know the mass and radius. All we need is the equation for the volume of the sphere, and the relationship between density, mass and volume:

```
V=rac{4\pi r^3}{3}
```

V - volume

r - radius

$$D = \frac{M}{V}$$

D - density

M - mass

V - volume

```
def calculateDensity(pl_bmasse, pl_rade):
   pl_volume = 4/3*3.14159*(pl_rade**3)
   return pl_bmasse/pl_volume*4.1888

exoplanets["pl_dens"] = calculateDensity(exoplanets.pl_bmasse, exoplanets.pl_rade)
col = exoplanets.pop("pl_dens")
exoplanets.insert(11, col.name, col)
```

An escape velocity of a planet is the minimum speed an object needs to escape the planet's

gravity.

$$V_e = \sqrt{rac{2GM}{r}}$$

 $V_e$  - escape velocity

M - mass

G - gravitational constant ( $6.6743 imes 10^{-11}$ )

```
def calculateEscVelocity(M, R):
    G = 6.67*10**-11
    EscV = (2*G*M/R)**(0.5)
    return EscV*86580.8978

exoplanets["pl_escv"] = calculateEscVelocity(exoplanets.pl_bmasse, exoplanets.pl_rade)
col = exoplanets.pop("pl_escv")
exoplanets.insert(12, col.name, col)
```

We will also add the surface gravity to the equation:

$$g_s=rac{GM}{r^2}$$

 $g_s$  - surface gravity

M - mass

G - gravitational constant ( $6.6743 imes 10^{-11}$ )

```
def calculateSurfaceGavity(pl_rade, pl_bmasse):
   mass = pl_bmasse*5.97*10**24
   radius = pl_rade*6371
   result = (6.674*10**-11*mass)/radius**2
   return result/1000000/9.816
```

```
exoplanets["pl_sug"] = calculateSurfaceGavity(exoplanets.pl_rade, exoplanets.pl_bmasse).ast
col = exoplanets.pop("pl_sug")
exoplanets.insert(13, col.name, col)
```

The following equation has been adapted from the ESI calculation provided in the *Earth Similarity Index and Habitability Studies of Exoplanets* document. It consists of three "sub-indexes"; ESII, ESIQ, and ESIt.

$$ESIi = \sqrt{(1 - |rac{R-1}{1+R}|^{0.57})*(1 - |rac{D-1}{1+D}|^{1.07})}$$

ESIi - Earth Similarity Index of the planet's interior

$$ESIg = \sqrt{(1 - |rac{V_e - 1}{1 + V_e}|^{0.7}) * (1 - |rac{g_s - 1}{1 + g_s}|^{1.3})}$$

# ESIg - Earth Similarity Index of the planet's gravity

$$ESIt = (1 - |\frac{T-1}{1+T}|)^{5.58}$$

ESIt - Earth Similarity Index of the planet's temperature

R - planet radius

D - planet density

 $V_e$  - escape velocity

 $g_s$  - surface gravity

T - surface temperature

$$ESI = \sqrt[3]{ESIi * ESIg * ESIt}$$

ESI - Earth Similarity Index

```
def calculateESI(T, EV, G, R, D):
    ESIi = (((1-abs(R-1)/abs(1+R))**0.57)*((1-abs(D-1)/abs(1+D))**1.07))**0.5
    ESIg = (((1-abs(EV-1)/abs(1+EV))**0.7)*((1-abs(G-1)/abs(1+G))**1.3))**0.5
    ESIt = (1-abs(T-288)/abs(288+T))**5.58
    return (ESIi*ESIg*ESIt)**(1/3)
```

exoplanets["ESI"] = calculateESI(exoplanets.pl\_sut, exoplanets.pl\_escv, exoplanets.pl\_sug,
col = exoplanets.pop("ESI")
exoplanets.insert(4, col.name, col)

Lets take a look at our feature-complete dataset:

exoplanets.head()

disc_fac	disc_year	discoverymethod	ESI	sy_pnum	sy_snum	hostname	pl_name	
( Obse	2015.0	Imaging	NaN	1.0	3.0	51 Eri	51 Eri b	0
Obse	1996.0	Radial Velocity	NaN	5.0	2.0	55 Cnc	55 Cnc b	1
McI Obse	2004.0	Radial Velocity	0.060848	5.0	2.0	55 Cnc	55 Cnc e	2
F Obse	2005.0	Imaging	NaN	1.0	1.0	AB Pic	AB Pic b	3
Tra Exc Survoy S	2020.0	Transit	0.211262	2.0	1.0	AU Mic	AU Mic	4

Surv<del>o</del>y S (



# **Solar System Data**

Lets prepare the data for solar system planets too. This will be useful for comparison. The data has been collected from: <a href="https://www.kaggle.com/datasets/jaredsavage/solar-system-major-bodies-data">https://www.kaggle.com/datasets/jaredsavage/solar-system-major-bodies-data</a>

The data has also been manually adapted to earth units.

```
urllib.request.urlretrieve("https://drive.google.com/uc?id=1ix2YDTpHo4Li3mcRg8ZAvlpqWa5ttnc
solData = pd.read_csv('solData.csv')
```

solData["ESI"] = calculateESI(solData.pl\_sut, solData.pl\_escv, solData.pl\_sug, solData.pl\_r

solData

	pl_name	hostname	sy_snum	sy_pnum	eccentricity	pl_dens	pl_sug	pl_escv	
0	Ceres	Sol	1	8	0.07582	0.391940	0.028571	0.045576	C
1	Uranus	Sol	1	8	0.04570	0.230340	0.905102	1.910634	3
2	Pluto	Sol	1	8	0.24880	0.342789	0.063265	0.108132	C
3	Neptune	Sol	1	8	0.01130	0.297084	1.137755	2.105451	3
4	Jupiter	Sol	1	8	0.04890	0.240533	2.529592	5.379803	10
5	Mars	Sol	1	8	0.09350	0.713527	0.378571	0.449508	C
6	Mercury	Sol	1	8	0.20560	0.984674	0.377551	0.379803	C
7	Saturn	Sol	1	8	0.05650	0.124619	1.065306	3.225201	ć
8	Earth	Sol	1	8	0.01670	1.000000	1.000000	1.000000	1
9	Venus	Sol	1	8	0.00670	0.950921	0.905102	0.925827	C
10	Moon	Sol	1	8	0.05490	0.606500	0.165306	0.212690	C

# **Data Visualization and Analysis**

## **The Record Holders**

#### **Highest ESI**

```
print(f"{exoplanets[exoplanets.ESI == exoplanets.ESI.max()].pl_name.to_string(index=False)]
print(f"Its surface temperature is {float(exoplanets[exoplanets.ESI == exoplanets.ESI.max())
print(f"It is located {float(exoplanets[exoplanets.ESI == exoplanets.ESI.max()].sy_dist.to_
```

TRAPPIST-1 e is the planet most similar to Earth. With an Earth Similarity Index of 0 Its surface temperature is 10.5 degrees Celsius, and surface gravity 22.2% lower than It is located 40.7 light-years away from Earh.

#### **First Exoplanets**

```
print(f"{exoplanets[exoplanets.disc_year == exoplanets.disc_year.min()].head(1).pl_name.to_
print(f"They are located {float(exoplanets[exoplanets.disc_year == exoplanets.disc_year.min
```

PSR B1257+12 c and PSR B1257+12 d are the first extra-solar planets discovered in 199 They are located 1956.94 light-years away from Earh.

#### Longest and Shortest Period

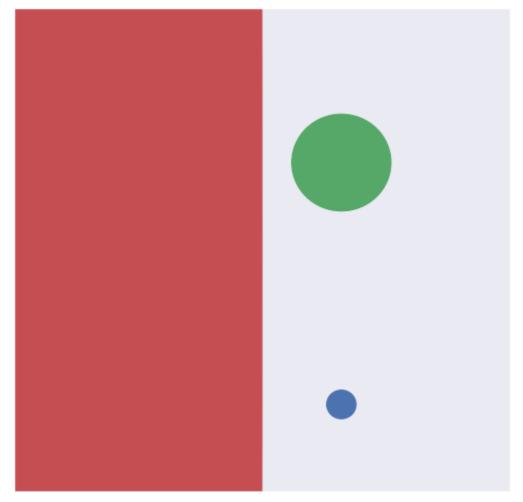
```
exoplanets.replace([np.inf, -np.inf], np.nan, inplace=True)
print(f"{exoplanets[exoplanets.pl_orbper == exoplanets.pl_orbper.max()].pl_name.to_string(i
print(f"Due to Kepler's Third Law, {exoplanets[exoplanets.pl_orbsmax == exoplanets.pl_orbsmax print(f"Its opposite is {exoplanets[exoplanets.pl_orbper == exoplanets.pl_orbper.min()].pl_
```

COCONUTS-2 b is the planet with the longest orbital period. Its year lasts 1100616.01 Due to Kepler's Third Law, COCONUTS-2 b is also the planet that orbits the farthest f Its opposite is PSR J1719-1438 b. Its year lasts just 2.18 hours! And is only 658240

#### **Largest and Smallest**

```
print(f"{exoplanets[exoplanets.pl_rade == exoplanets.pl_rade.max()].pl_name.to_string(index)
print(f"{exoplanets[exoplanets.pl_rade == exoplanets.pl_rade.min()].pl_name.to_string(index)
print(f"{exoplanets[exoplanets.pl_rade == exoplanets.pl_rade.max()].pl_name.to_string(index)
plt.figure(figsize=(8, 8), dpi=80)
circle1 = plt.Circle((-449.5, 0.5), 450, color='r')
circle2 = plt.Circle((0.66, 0.68), 0.1, color='g')
circle3 = plt.Circle((0.66, 0.18), 0.1*exoplanets.pl_rade.min(), color='b')
plt.gca().add_patch(circle1).axes.get_xaxis().set_visible(False)
plt.gca().add_patch(circle2).axes.get_yaxis().set_visible(False)
plt.gca().add_patch(circle3);
```

HD 100546 b is the largest known exoplanet. It has a radius 77 times bigger than Eart Kepler-37 b is the smallest. It has a radius 29.6% that of Earth's. That is smaller t HD 100546 b (red), Earth (green), and Kepler-37 b (blue):



#### Most and Least Massive, & Escape Velocity

print(f"{exoplanets[exoplanets.pl\_bmasse == exoplanets.pl\_bmasse.max()].pl\_name.to\_string()
print(f"It also has the highest escape velocity, at {exoplanets.pl\_escv.max()\*11.2:.5} km/s

print(f"{exoplanets[exoplanets.pl\_bmasse == exoplanets.pl\_bmasse.min()].pl\_name.to\_string()
print(f"It however, does not have the lowest escape velocity. That title goes to {exoplanet

PH2 b is the most massive known exoplanet. It is 25426.4 times heavier than Earth. It also has the highest escape velocity, at 583.15 km/s, 52.07 times larger than Eart PSR B1257+12 b is the least massive exoplanet. It is 2.0% the mass of the Earth. It however, does not have the lowest escape velocity. That title goes to Kepler-444 e

#### **Most Eccentric Orbit**

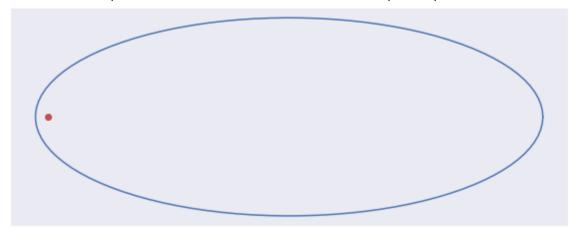
print(f"{exoplanets[exoplanets.pl\_orbeccen == exoplanets.pl\_orbeccen.max()].pl\_name.to\_stri
print(f"It goes from {(exoplanets.pl\_orbeccen.max()+1)\*float(exoplanets[exoplanets.pl\_orbec

```
print(f"The red dot represents the star while the blue elipse represents the orbit of {exo;
        #x-position of the center
         #y-position of the center
v = 0.5
        #radius on the x-axis
a=2
            #radius on the y-axis
b=0.1561
t = np.linspace(0, 2*pi, 100)
plt.plot( u+a*np.cos(t) , v+b*np.sin(t) )
plt.plot(-0.90035,0.5, "ro")
plt.grid(color='lightgray',linestyle='--')
ax = plt.gca()
ax.axes.xaxis.set_ticklabels([])
ax.axes.yaxis.set_ticklabels([])
ax.grid(False)
plt.show()
```

HD 20782 b has the highest eccentricity at 0.95.

It goes from 2.6616 AU at its farthest, to 0.068 AU at the closest.

The red dot represents the star while the blue elipse represents the orbit of HD 2078



#### Hottest

```
print(f"{exoplanets[exoplanets.pl_eqt == exoplanets.pl_eqt.max()].pl_name.to_string(index=F)
print(f"That is {int(exoplanets.pl_eqt.max()) - 5778} degrees hotter than the surface of or
```

KOI-55 b has the highest equilibrium temperature at 7105K, or 6832 degrees celsius. That is 1327 degrees hotter than the surface of our Sun!

#### **Highest surface gravity**

#### Most and least dense

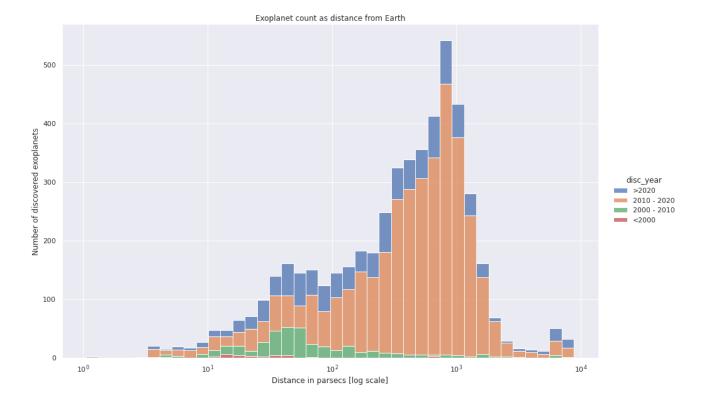
```
print(f"{exoplanets[exoplanets.pl_dens == exoplanets.pl_dens.max()].pl_name.to_string(inde)
print(f"{exoplanets[exoplanets.pl_dens == exoplanets.pl_dens.min()].pl_name.to_string(inde)
```

KOI-4777.01 is the densest known exoplanet. It is 747 times denser than Earth. Kepler-444 e is the least dense exoplanet. It is 0.00699% Earth's density.

## **Count Plots**

Lets plot the exoplanet systems according to their distance and discovery year. Note that one parces equals 3.26156 light-years.

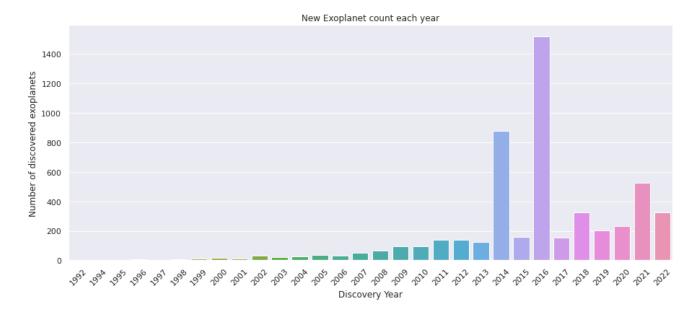
temp1 = exoplanets.sort\_values(by=["disc\_year"], ascending=False).copy()
temp1.disc\_year = temp1.disc\_year.apply(lambda x: "<2000" if (x<2000) else ("2000 - 2010" :
ax = sns.displot(temp1, x="sy\_dist", log\_scale=True, height=8.3, aspect=13/8.3, hue="disc\_year")
ax.set(xlabel='Distance in parsecs [log scale]', ylabel='Number of discovered exoplanets',
plt.show()</pre>



## The count plot per year:

```
temp1 = exoplanets.sort_values(by=["disc_year"], ascending=True).copy()
fig, ax = plt.subplots()
plt.gcf().set_size_inches((15, 6))

ax = sns.countplot(x=temp1.disc_year.astype("int16"))
ax.set(xlabel='Discovery Year', ylabel='Number of discovered exoplanets', title="New Exopl;
plt.xticks(rotation=45)
plt.show()
```



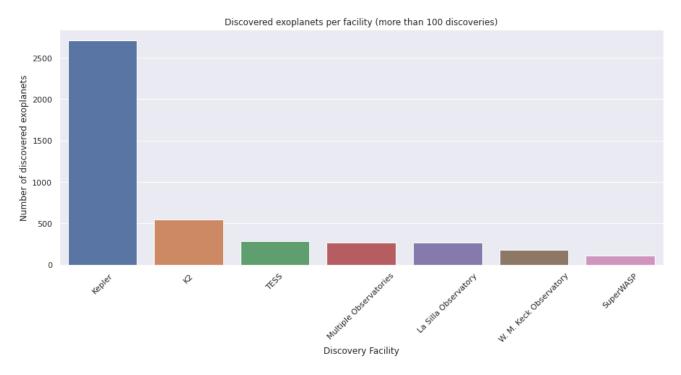
Why do we see a large jump in newly discovered exoplanets in 2014 and 2016? Because the Kepler space telescope responsible for the vast majority of exoplanet discoveries, released its data in those two years. We also see another uptick in 2018, when Kepler released its final data before being deactivated.

Let's take a look at the count plot of discovery facilities;

```
temp1.Sorr_values(uy=[ p1_name ], ascending=raise, inplace=inde)
temp1.disc_facility = temp1.disc_facility.apply(lambda x: ("TESS") if x== "Transiting Exop!
temp1 = temp1[temp1['p1_name'] > 100]

fig, ax = plt.subplots()
plt.gcf().set_size_inches((15, 6))

ax = sns.barplot(data=temp1, x="disc_facility", y="p1_name")
ax.set(xlabel='Discovery Facility', ylabel='Number of discovered exoplanets', title="Discovery plt.xticks(rotation=45);
```



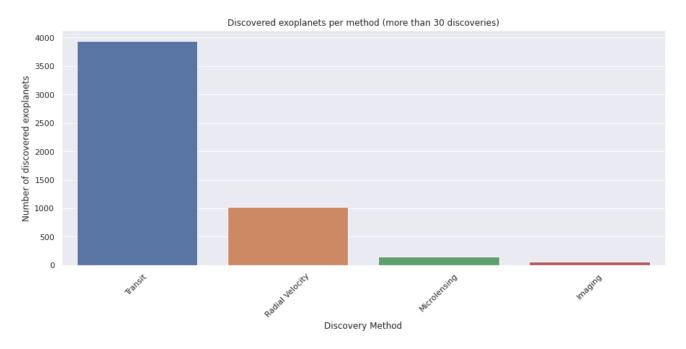
#### And the count plot of discovery methods;

```
temp1 = exoplanets.groupby("discoverymethod").pl_name.count()
temp1 = temp1.reset_index()
temp1.sort_values(by=["pl_name"], ascending=False, inplace=True)
temp1 = temp1[temp1['pl_name'] > 30]

fig, ax = plt.subplots()
plt.gcf().set_size_inches((15, 6))

ax = sns.barplot(data=temp1, x="discoverymethod", y="pl_name")
ax.set(xlabel='Discovery Method', ylabel='Number of discovered exoplanets', title="Discoverymethod")
```

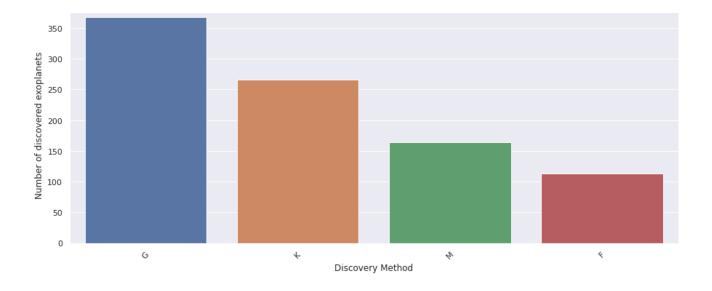
#### plt.xticks(rotation=45);



Transit timing is the most common method of discovering exoplanets. It consists of staring at a star for long periods of time, and watching for periodic dips in the star's brightness caused by a transiting exoplanet. This introduces a strong discovery bias towards small stars (whose light can more easily be blocked), larger planets (that block more of their stats light), and shorter period planets (because they transit more often).

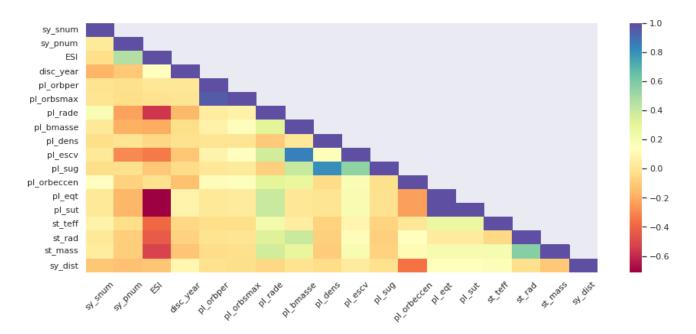
```
temp1 = exoplanets.copy()
temp1.st_spectype = temp1.st_spectype.str[:1]
temp1 = temp1.groupby("st_spectype").pl_name.count()
temp1 = temp1.reset_index()
temp1.sort_values(by=["pl_name"], ascending=False, inplace=True)
temp1 = temp1[temp1['pl_name'] > 30]
fig, ax = plt.subplots()
plt.gcf().set_size_inches((15, 6))
ax = sns.barplot(data=temp1, x="st_spectype", y="pl_name")
ax.set(xlabel='Discovery Method', ylabel='Number of discovered exoplanets', title="Discover plt.xticks(rotation=45);
```

Discovered exoplanets per method (more than 30 discoveries), and for which we know the star type



## **Data correlation**

temp1 = exoplanets.corr(method='pearson').where(np.tril(np.ones(exoplanets.corr(method='pearson'), ax = plt.subplots(figsize=(15,6))
hmap=sns.heatmap(temp1,cmap="Spectral")
ax.set\_xticklabels(ax.get\_xticklabels(), rotation=45);



We see several features which are highly correlated. Such as equilibrium temperature (pl\_eqt) and surface temperature (pl\_sut) which makes a lot of sense, as we used a linear equation to connect the two. Planetary density (pl\_dens) and planetary escape velocity (pl\_escv) are similarly connected - as the density determines the velocity.

Observation 1: An interesting observation concerns the Earth similarity index (ESI) and the number of other planets found in the planetary system (sy\_pnum). This suggests that more habitable planets, or those that are more earth-like, have a higher chance of forming with other planetary companions. This meshes well with the numerous theories that the large gas giants such as Jupiter and Saturn, played key roles in shepherding the formation of the Earth. And other exoplanets might do the same for their system's most habitable planets.

Observation 2: Another point to consider is the negative correlation between the distance to the exoplanet (sy\_dist) and its orbital eccentricity (pl\_orbeccen). We see this as the main discovery technique with which we can discover the eccentricity, is the radial velocity method. Where we measure the small changes in the motion of the parent star. These miniscule changes become much harder to detect with distance, and this is an example of selection bias. It is not that planets become less eccentric with distance from the earth, but our telescopes are not sensitive enough to probe those distant worlds in such a way as to reveal the most eccentric ones.

## Clustering

Exoplanets can be best clustered using density and radius. We will be using Spectral Clustering, and focusing on planets with a density less than 2 times the Earth's, and a radius less than 16 times the Earth's.

First, we will take a look at all the exoplanets in this range, by plotting them onto a scatter plot. We will also load in the planets of our Solar System as a comparison.

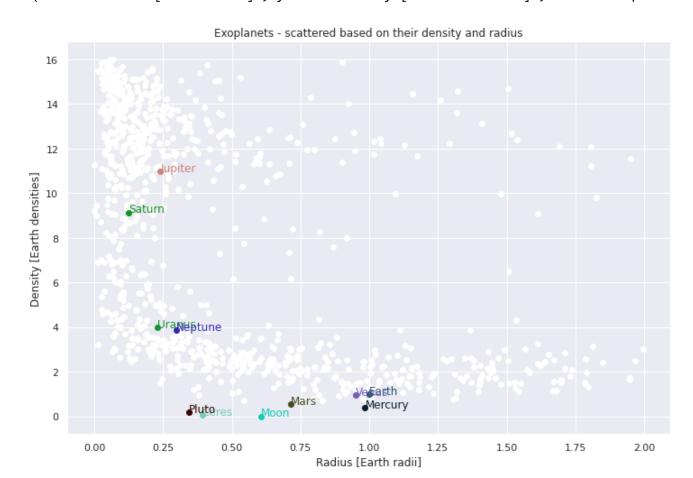
```
temp1 = pd.DataFrame()
temp1["pl_dens"]=exoplanets[(exoplanets.pl_dens < 100000)].pl_dens
temp1["pl_rade"]=exoplanets[(exoplanets.pl_dens < 100000)].pl_rade

fig, ax = plt.subplots()
plt.gcf().set_size_inches((12, 8))

upperDenslimit = 2
upperRadelimit = 16</pre>
```

```
ax.scatter(temp1[(temp1.pl_dens<upperDenslimit) & (temp1.pl_rade<upperRadelimit)].pl_dens,

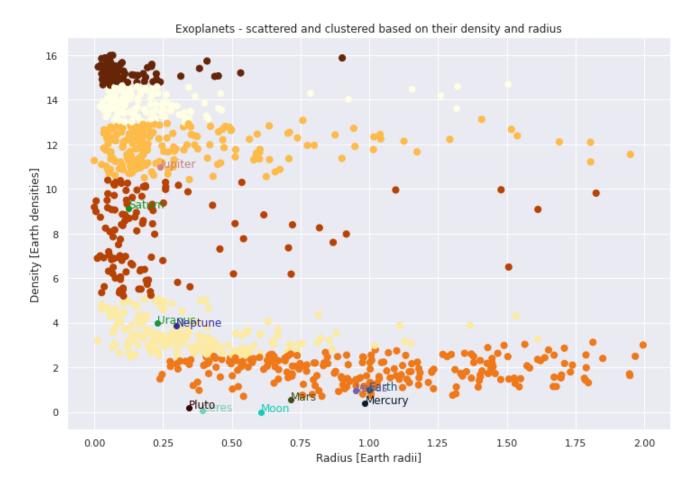
color = ["#"+''.join([random.choice('0123456789ABCDEF') for j in range(6)]) for i in range(for ind in solData.index:
    ax.scatter(solData['pl_dens'][ind],solData['pl_rade'][ind],c=color[ind])
    ax.annotate(solData['pl_name'][ind], (solData['pl_dens'][ind],solData['pl_rade'][ind]), (ax.set(xlabel='Radius [Earth radii]', ylabel='Density [Earth densities]', title="Exoplanets")</pre>
```



Now we will cluster these datapoints into 6 clusters.

```
labels = model.fit_predict(temp2)
ax.scatter(temp2.pl_dens, temp2.pl_rade, c=labels, s=50, cmap='YlOrBr');
for ind in solData.index:
   ax.scatter(solData['pl_dens'][ind],solData['pl_rade'][ind],c=color[ind])
   ax.annotate(solData['pl_name'][ind], (solData['pl_dens'][ind],solData['pl_rade'][ind]), (solData['pl_dens'][ind],solData['pl_rade'][ind]), (solData['pl_dens'][ind],solData['pl_rade'][ind]), (solData['pl_dens'][ind],solData['pl_rade'][ind]), (solData['pl_dens'][ind],solData['pl_rade'][ind]), (solData['pl_dens'][ind],solData['pl_rade'][ind]), (solData['pl_dens'][ind],solData['pl_rade'][ind])
```

ax.set(xlabel='Radius [Earth radii]', ylabel='Density [Earth densities]', title="Exoplanets



We clearly see the separation between the planet types within our own solar system.

- 1. Earth, Venus, Mars and Mercury are all in the "lowest" cluster. This can be though of as the Terrestrial Cluster.
- 2. Uranus and Neptune are in their own Ice Giant Cluster.
- 3. As a Gas Giant with an extremely low density (lower than water's), Saturn belongs in the third cluster, the Puff Planet Cluster.
- 4. Jupiter is the largest Gas Giant, and belongs in his own cluster, the true Gas Giant Cluster.
- 5. & 6. The clusters above the Gas Giant, contains planets whose masses put Jupiter's to shame. We have no planets in this range within our own planetary system.

## Classification

We will manually set ranges and classes for variables such as mass, temperature and density, as proposed in this paper:

## https://bit.ly/3jSfJ6M

I have used a modified system for classification, taking into account the "unknown densities" - densities many hundreds of times above Earth's.

```
def classify(value, array):
    i = 0

if value:
    while (value > array[1][i]) & (i <= len(array[1])):
        i = i + 1
    planetClass = array[0][i]
else:
    planetClass = "?"

return planetClass</pre>
```

Each planet is classified based on the modified values presented in the paper.

```
exoplanets["massClass"] = exoplanets.apply(lambda x: classify(x.pl_bmasse, [["?", "M", "E",
exoplanets["tempClass"] = exoplanets.apply(lambda x: classify(x.pl_eqt, [["?", "F", "A", "Vexoplanets["planetClass"] = exoplanets.apply(lambda x: classify(x.pl_dens, [["?", "p", "g", "g"))
```

Lets take a look at the count plots for Mass, Temperature, and Density:

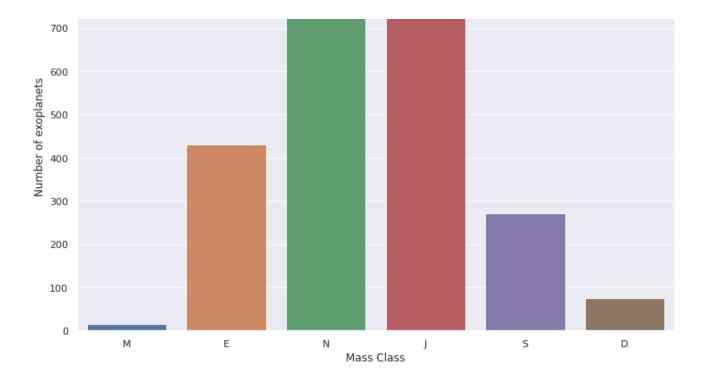
```
fig, ax = plt.subplots()
plt.gcf().set_size_inches((12, 8))

temp1 = exoplanets[exoplanets.massClass != "?"].copy()

ax = sns.countplot(x="massClass", data=temp1, order=["M", "E", "N", "J", "S", "D"])
ax.set(xlabel='Mass Class', ylabel='Number of exoplanets', title="Count of known exoplanets")
```

Count of known exoplanets in each mass class

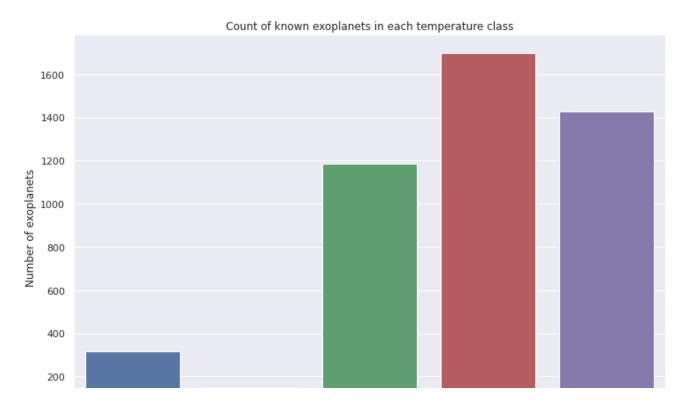
800

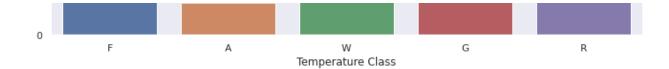


```
fig, ax = plt.subplots()
plt.gcf().set_size_inches((12, 8))

temp1 = exoplanets[exoplanets.tempClass != "?"].copy()

ax = sns.countplot(x="tempClass", data=temp1, order=["F", "A", "W", "G", "R"])
ax.set(xlabel='Temperature Class', ylabel='Number of exoplanets', title="Count of known exc
```

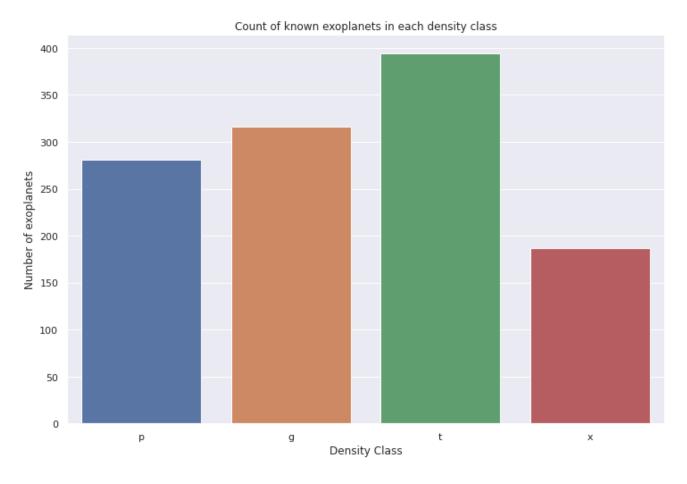




```
fig, ax = plt.subplots()
plt.gcf().set_size_inches((12, 8))

temp1 = exoplanets[exoplanets.planetClass != "?"].copy()

ax = sns.countplot(x="planetClass", data=temp1, order=["p", "g", "t", "x"])
ax.set(xlabel='Density Class', ylabel='Number of exoplanets', title="Count of known exoplanets")
```



Are there any exoplanets with the same classification as Earth? We are looking for a planet with a class of "EAt".

exoplanets[(exoplanets.massClass == "E") & (exoplanets.tempClass == "A") & (exoplanets.plar

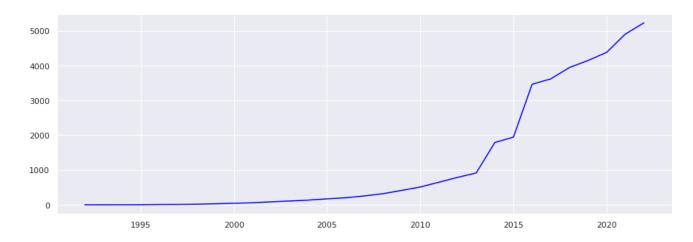
	pl_name	hostname	sy_snum	sy_pnum	ESI	discoverymethod	disc_year
398	K2-18 b	K2-18	1.0	2.0	0.806230	Transit	2015.0
438	K2-3 d	K2-3	1.0	3.0	0.812223	Transit	2015.0
612	L 98-59 d	L 98-59	1.0	4.0	0.705965	Transit	2019.0
4313	TRAPPIST-1 e	TRAPPIST-1	1.0	7.0	0.941255	Transit	2017.0
++							



All these worlds have ESI higher than any other object in the solar system besides Earth.

# Predicting the next milestones in exoplanet discoveries

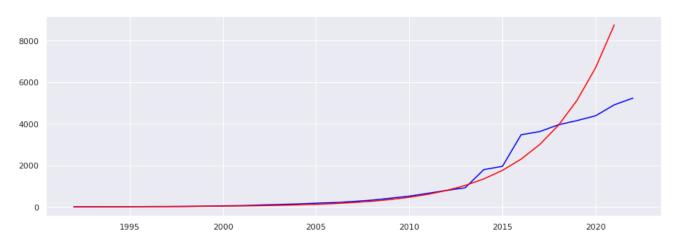
```
temp2 = exoplanets.groupby("disc_year").pl_name.count()
temp1 = temp2.cumsum()
plt.figure(figsize=(15,5))
plt.plot(temp1, c="blue")
plt.show()
```



import numpy as np
from sklearn.linear\_model import LinearRegression

```
temp2 = temp1
temp2 = temp2.to_frame()
temp2.rename(columns={'pl_name': 'y'}, inplace=True)
temp2["log_y"] = np.log(temp2.y)
temp2["year"] = temp2.index - 1991
# Create a numpy array of data:
x = temp2.year.to_numpy().reshape((-1, 1))
y = temp2.log_y.to_numpy()
# Create an instance of a linear regression model and fit it to the data with the fit() fur
model = LinearRegression().fit(x, y)
# The following section will get results by interpreting the created instance:
# Obtain the coefficient of determination by calling the model with the score() function, 1
r_sq = model.score(x, y)
print('coefficient of determination:', r_sq)
# Print the Intercept:
print('intercept:', model.intercept_)
# Print the Slope:
print('slope:', model.coef_)
# Predict a Response and print it:
y_pred = model.predict(x)
print('Predicted response:', y_pred, sep='\n')
     coefficient of determination: 0.9748802613653331
     intercept: 1.0392566604749103
     slope: [0.2679142]
     Predicted response:
     [1.30717086 1.84299927 2.11091347 2.37882768 2.64674188 2.91465609
      3.18257029 3.45048449 3.7183987 3.9863129 4.2542271 4.52214131
      4.79005551 5.05796971 5.32588392 5.59379812 5.86171232 6.12962653
      6.39754073 6.66545493 6.93336914 7.20128334 7.46919754 7.73711175
      8.00502595 8.27294016 8.54085436 8.80876856 9.07668277 9.34459697]
x = np.arange(1,100).reshape(-1,1)
y_pred = model.predict(x)
temp1=pd.DataFrame(x+1991, y_pred)
temp1 = temp1.reset_index()
temp1 = temp1.rename(columns={"index": "count"})
temp1["exo_count"] = temp1["count"].apply(lambda x: math.exp(x))
temp1.pop("count")
temp1 = temp1.rename(columns={0: "year"})
temp1 = temp1.set_index('year')
plt.figure(figsize=(15,5))
plt.plot(exoplanets.groupby("disc_year").pl_name.count().cumsum(), c ="blue")
plt.plot(temp1[:30], c ="red")
```

#### plt.show()



```
print("The model predicts:")
target = 10000
print(f"We will reach {target} known exoplanets by the end of {temp1['exo_count'].gt(target)
target = 100000
print(f"We will reach {target} known exoplanets by the end of {temp1['exo count'].gt(target)
target = 1000000
print(f"We will reach {target} known exoplanets by the end of {temp1['exo_count'].gt(target)
target = 10000000
print(f"We will reach {target} known exoplanets by the end of {temp1['exo_count'].gt(target)
target = 100000000
print(f"We will reach {target} known exoplanets by the end of {temp1['exo count'].gt(target
target = 1000000000
print(f"We will reach {target} known exoplanets by the end of {temp1['exo count'].gt(target)
     The model predicts:
     We will reach 10000 known exoplanets by the end of 2022.
     We will reach 100000 known exoplanets by the end of 2031.
     We will reach 1000000 known exoplanets by the end of 2039.
     We will reach 10000000 known exoplanets by the end of 2048.
     We will reach 100000000 known exoplanets by the end of 2056.
     We will reach 1000000000 known exoplanets by the end of 2065.
```

Even though our predictions for the year 2022 are already wrong, the model confirms the findings of René Heller and László L. Kiss in their paper "Exoplanet Vision 2050" where they predict 100 000 000 known exoplanets by that year. Our model predicts the 100 000 000th planet will be discovered sometime in the latter half of 2056

Exoplanet Vision 2050: https://arxiv.org/pdf/1911.12114.pdf

# When will humanity discover every single planet in our Galaxy?

Predictions for the exact number of planets within the Milky Way range from 100 to 200 billion. And if current trends continue:

print(f"Humanity will discover all of the Milky Way's planets sometime between {temp1['exo\_ Humanity will discover all of the Milky Way's planets sometime between 2082 and 2085

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