## Lab 2: Resistors and Diodes

ENGR 2420 | Olin College

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## Postlab

1. (a) We derive the equation as follows.

$$-V_{on} + \frac{V_{in}}{U_T} = e^{\frac{V - V_{on}}{U_T}} + \frac{V}{U_T} - V_{on}$$

This can also be simplified to:

$$V_{in} = e^{\frac{V - V_{on}}{U_T}} + V$$

(b) When  $V < V_{on}$  by more than a few  $U_T$ , we can approximate the equation as:

$$V_{in} = V$$

(c) When  $V > V_{on}$  by more than a few  $U_T$ , we can approximate the equation as:

$$V_{in} = e^{\frac{V}{U_T}} + V$$

2. (a)  $V \approx V_1$  if  $V_1 < V_2$  by more than a few  $U_T$  because if term  $e^{\frac{V_1 - V_2}{U_T}}$  will effectively go to zero, allowing the second given equation simplify to  $V = V_1$ .

Additionally,  $V \approx V_2$  if  $V_1 > V_2$  by more than a few  $U_T$  because if  $V_1$  in the term  $e^{\frac{-V_1}{U_T}}$  in the first given equation is big, that whole term will go to zero and the equation will simplify as shown:

$$V = -U_T \log e^{\frac{-V_2}{U_T}} = -U_T \frac{-V_2}{U_T} = V_2$$

(b) We can equate  $V_1$  to  $V_{in}$  and  $V_2$  to  $V_{on}$ , giving us the equation:

$$V = V_{in} - U_T \log(1 + e^{(V_{in} - V_{on})/U_T})$$

This means that the voltage across the transistor is about equal to  $V_{in}$  when it is less than  $V_{on}$ , which matches the behavior of the transistor we measured above.

(c) We can obtain an express for I in terms of  $V_{in}$  as follows:

$$I = \frac{V_{in} - V}{R}$$

$$I \cdot R = V_{in} - V$$

$$I \cdot R = V_{in} - (V_{in} - U_T \log(1 + e^{\frac{V_{in} - V_{on}}{U_T}}))$$

We can further simplify  $\frac{U_T}{R}$  as  $I_{on}$ :

$$I = I_{on} \log(1 + e^{\frac{V_{in} - V_{on}}{U_T}})$$

When  $V_{in} < V_{on}$  by more than a few  $U_T$ , we can approximate the whole term as

When  $V_{in} > V_{on}$  by more than a few  $U_T$ , the 1 term in the log is near meaningless and we can approximate the whole equation as  $I \approx I_{on} \frac{V_{in} - V_{on}}{U_T}$ , which simplifies to  $I \approx \frac{V_{in} - V_{on}}{R}$ 

This fits the behavior observed in our measured data.

(d) We need to find an equation that gives I in terms of  $V_{in}$ . To find the current, we can start with the approximation of the ideal diode equation, given earlier as

$$I = I_s e^{V/U_T}$$

We got V and dealt with  $V_{in}$  in part b, so we can sub in that equation for V as shown.

$$I = I_s e^{V_{in} - U_T \log(1 + e^{(V_{in} - V_{on})/U_T})/U_T}$$

By plotting this, we see that when  $V_{in} < V_{on}$  by more than a few  $U_T$ , the equation follows a logistic curve as we see in our data. Conversely, When  $V_{in} > V_{on}$  by more than a few  $U_T$ , the equation levels off at a value (I'm guessing this should be  $I_{on}$ ?).