



Boolean network-based analysis of the apoptosis network: Irreversible apoptosis and stable surviving

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ABSTRACT

To understand the design principles of the molecular interaction network associated with the irreversibility of cell apoptosis and the stability of cell surviving, we constructed a Boolean network integrating both the intrinsic and extrinsic pro-apoptotic pathways with pro-survival signal transduction pathways. We performed statistical analyses of the dependences of cell fate on initial states and on input signals. The analyses reproduced the well-known pro- and anti-apoptotic effects of key external signals and network components. We found that the external GF signal by itself did not change the apoptotic ratio from randomly chosen initial states when there is no external TNF signal, but can significantly offset apoptosis induced by the TNF signal. While a complete model produces the expected irreversibility of the apoptosis process, alternative models missing one or more of four selected inter-component connections indicate that the feedback loops directly involving the caspase 3 are essential for maintaining irreversibility of apoptosis. The feedback loops involving P53 showed compensating effects when those involving caspase 3 have been removed. The GF signal significantly increases the stability of the surviving states of the network. The apoptosis network seems to use different modules by design to control the irreversibility of the apoptosis process and the stability of the surviving states. Such a design may accommodate the needed plasticity for the network to adapt to different cellular environments: depending on the strength of external pro-survival signals, apoptosis can be induced either easily or difficultly by pro-apoptotic signal of varying strengths, but proceed with invariable irreversibility.

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1. Introduction

Apoptosis or programmed cell death has been subjected to extensive experimental studies for more than two decades. In the apoptosis process, a range of cellular signals are integrated by a complex molecular network (Falschlehner et al., 2007; Henson and Gibson, 2006). This network as a whole, not the status of individual signaling molecules controls when a cell can (or should) no longer survive and enter programmed death irreversibly (Janes et al., 2005). To understand how the network operates, it is necessary not only to study what are its composing components or what molecular interactions exist between the components, but also to analyze the network as a whole or at the systems level to identify which of its properties are essential for biological functions, and how these properties emerge from the specific way by which the interacting components are organized into an integrated system. In the latter regard, computer models formulating the various molecular components and their interac-

tions can in many aspects complement experimental studies. One main advantage of using computer simulations for systems level analysis is that components or interactions can be systematically varied *in silico*, either individually or jointly, to probe their roles in any general or specific cellular contexts (Stelling, 2004; Wolkenhauer, 2002).

Depending on the states of its components and the signals it receives, the outcome of the apoptosis network can be either surviving or apoptosis. Essential systems level properties of the network should include the robust stability of the surviving state as well as the irreversibility of the survival to apoptotic transition. The former property means that apoptosis can be triggered only by some definite cellular signals, but not by spontaneous fluctuations in the states of individual molecular components. The latter property means that apoptosis, once started, cannot be abolished either by withdrawing of the triggering signals or by spontaneous fluctuations.

How multi-stability and irreversibility generally arise in cellular networks and what their biological implications are have been analyzed theoretically and in some cases demonstrated experimentally (Ferrell, 2002; Ferrell and Xiong, 2001). In these studies, irreversibility and multi-stability have often been

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attributed to nonlinear dynamics associated with feedback loops in the respective networks.

As for the apoptosis network in particular, a number of computer modeling studies based on ordinary differential equations (ODE) have been reported (Bentele et al., 2004; Albeck et al., 2008; Rehm et al., 2006; Bagci et al., 2006; Eissing et al., 2004; Legewie et al., 2006). These ODE models are based on detailed knowledge or assumptions of kinetics parameters associated with all molecular processes considered in the respective models, and provide detailed dynamics of these processes. Thus an advantage of ODE models is that they can not only be used for theoretical analyses (Bagci et al., 2006; Eissing et al., 2004; Legewie et al., 2006), but also be calibrated based on and then tested against quantitative experimental measurements when such measurements are available (Albeck et al., 2008; Rehm et al., 2006). However, most previous ODE models have focused on limited parts of the apoptosis network. To obtain a more complete picture, it is of interest to investigate more extensive networks, especially those involving the interactions of apoptotic pathways with surviving pathways such as the growth factor (GF) pathway. As more molecular components are included, it becomes increasingly challenging to develop mutually compatible ODEs to cover all the different types of molecular processes. Moreover, in the higher-dimensional continuous state space of the ODE framework, it is difficult to formulate and extract systems properties from the complex dynamics. It is also difficult to perform systematic explorations in the model space, kinetic parameter space as well as in the initial condition space.

Boolean network (BN) is an alternative way to model complex cellular networks. A BN is a qualitative mathematical model composed of nodes having discrete states and rules governing the temporal evolution of the states. Since introduced by Kauffman in late 1960s (Kauffman, 1969), BN has been used to model gene regulatory networks and signaling pathways (Huang and Ingber, 2000; Li et al., 2004). Although BN does not model dynamics in terms of continuous variables, it has been argued that BN may provide good approximations to a variety of nonlinear behaviors of biological systems (Amaral et al., 2004). The state space of BN is discrete by definition, and is thus more accessible to statistical analyses. Such analyses readily enable the formulation and extraction of systems level properties for relatively large networks of higher dimensional variable spaces. BN can also afford extensive explorations in the model space and the initial condition space in such systems.

In this work, we construct a 40-node Boolean model of the cellular apoptosis network to analyze its systems properties and how they can be linked to specific structural features of the network. Because of the simplicity of BN, we are able to consider a relatively complete set of known molecular processes, including both anti-apoptosis (or pro-survival) and pro-apoptosis pathways, and the integration of intrinsic and extrinsic signals. One major purpose of our study is to understand the emergence of systems properties. These include the stability of the surviving states and the irreversibility of the apoptotic process. Through extensive analyses of the state space, we try to identify key network components that lead to these properties. In silico experiments are performed with a large number of random initial states at different combinations of input cellular signals. Critical pro-survival and pro-apoptotic nodes are identified based on statistical correlations between initial states and final outcomes. Irreversibility of the apoptotic process is characterized using time-dependent input signals. Stability of the surviving states is analyzed based on perturbations in the state space. The roles of specific feedback structures in the network are investigated using simulated knockout experiments.

2. Materials and methods

2.1. Structure of the model

Our BN model (Fig. 1) includes 37 internal nodes representing states of signaling molecules, 2 input nodes representing extracellular signals, and 1 output node corresponding to the DNA damage event. The nodes are interconnected, connections corresponding to a set of rules defining how the states of each node evolve in time depending on the states of other nodes (see below). This model is based on extensive surveys of literature as well as on expert-curated databases, especially the reactome database (<http://www.reactome.org>). Given the complexity of the real networks in cells and our incomplete current knowledge of them, our model is necessarily approximate. The main considerations in choosing nodes and connections are to include as complete as possible known connections that may integrate major extracellular signals determining the survival or apoptosis of cells. Generally accepted major molecular players such as p53 and NFκB are also included. Different molecules may be represented by a single node if they have been reported to play the same or similar roles (e.g., proteins in the same family and of not clearly distinguishable functions, such as the different types of GF signals or different IAPs). More details of the network structure are described below.

2.1.1. Modeling the extrinsic pro-apoptotic signals

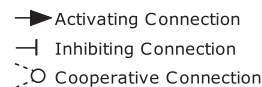
The extrinsic apoptotic pathway involves the activation of the tumor necrosis factor (TNF) family of receptors (TNFRs), represented by TNFR1 and TNFR2 in our model. We use TNF receptor-associated death domain protein (TRADD) to represent the direct downstream targets of TNFR1 (Wang et al., 1999). The major pro-apoptosis effects of these receptors are modeled by the activation of Fas-associated death domain protein (FADD), which in turn leads to the activation of caspase-8 (Morgan et al., 2001). The effects of the extrinsic pro-apoptotic signals on the intrinsic apoptotic pathways are modeled through the activation of receptor-interacting protein (RIP), which then induces p53 activation through a mitogen-activated protein kinase cascade (represented by MEKK-1, JNKK and JNK in the model) (Kelliher et al., 1998; Lin et al., 2000).

2.1.2. Modeling the pro-survival effects of extrinsic TNF signals

The pro-survival effects of these receptors are modeled first as the activation of caspase-8 inhibitory proteins (represented as the cellular form of FLICE-inhibitory protein (cFLIP) in our model) by TNF receptor-associated factors (TRAF), and second as the TNFR-mediated activation of NFκB through the removal of the inhibitor of NFκB protein (IκB) by the activated IκB kinase (IKK) complex. In our model, extrinsic TNF signals have both inhibitory (through TNFR1, RIP and then TRAF2) and activating (through TNFR2 and then TRAF2) effects on NFκB (Kelliher et al., 1998; Lin et al., 2000; Muppidi et al., 2004; Shu et al., 1996; Wu et al., 2005). NFκB exerts negative feedback regulation on its own inducing pathway via activating A20 and IκB (De Valck et al., 1997; Ferran et al., 1998).

2.1.3. Modeling the pro-survival effects of extrinsic growth factor signals

The transduction of extrinsic pro-survival signals is modeled through the growth factor receptors (GFR) and the Akt/PKB protein kinases. Activated GFR activates phosphatidylinositol 3-kinase (PI3K), which produces phosphatidylinositol trisphosphate (PIP3) from PIP2. PIP3 activates Akt (Song et al., 2005). In our model the pro-survival effects of Akt are achieved through its



inhibitory action on the caspase machinery (on caspase 9), on the activation of p53 (on the TNFR mediated MAPK kinase cascade and through murine double minute 2 protein (Mdm2)), as well as on the intrinsic inventory of pro-apoptotic Bcl2-like molecules (on Bcl-2-associated death promoter (BAD)).

The intrinsic apoptotic pathways are modeled by including the anti-apoptotic (BclX) and pro-apoptotic (BAD) Bcl2 family of proteins (Shimizu et al., 1999). BAD received activating or pro-apoptotic signals from p53 and inhibitory or pro-survival signals from Akt, and achieves pro-apoptotic effects via inhibitory effects on BclX. BclX prevents the release of apoptotic signals from mitochondrion (mito) which promotes the formation of the apoptosome complex (APC). The latter needs also apoptotic protease activating factor 1 (Apaf1) and activated caspase 9. Pro-apoptotic molecules released by mitochondrion (e.g., Smac) also neutralize the inhibitors of apoptosis (IAP). The node Mito represents the complex but still unclear regulations of the releasing of cytochrome c and Smac by other molecules.

survival signals (via Akt) as well as the intrinsic apoptosis signals, and generates pro-apoptotic output via Bad, Apaf1, and Bid (Haupt et al., 2003; Kim et al., 2005; Yu and Zhang, 2005).

Caspase 3 is the terminal promoter for apoptosis in the model, which not only receives the extrinsic and intrinsic apoptotic input signals via caspase 8 and APC, respectively, but also receives the pro-survival signals from Akt and IAPs. The caspase machinery is modeled as the main activation cascade from caspase 8 to caspase 3, the activation of caspase 7 by caspase 8 or APC which then leads to the activation of caspase 9, the activation of caspase 3 by caspase 9 involving APC, as well as the three positive feed backs from caspase 6 to caspase 3, from caspase 6 to caspase 8 and from caspase 3 to caspase 9 (Mak and Yeh, 2002; Philchenkov, 2004).

Several major connecting points between extrinsic and intrinsic apoptotic pathways before the terminal caspase 3 are built into the model, including Bid that integrates signals from TNF (via caspase 8 and JNK) and p53 (Mak and Yeh, 2002; Yu and Zhang, 2005), and caspase 7 receiving inputs from caspase 8 and APC (Lowe et al., 2004; Philchenkov, 2004). The connections by which extrinsic pro-survival signals disrupt the apoptotic process

include those involving Akt as described above, and the activation of BclX and IAPs by NFkB (Bernal-Mizrachi et al., 2006; Deveraux and Reed, 1999). The GF pathway also receives negative feedback from p53 via PTEN which dephosphorylates PIP3 (Okamura et al., 2006; Yan et al., 2006).

In some of our simulations, alternative models with selected connections knocked out from the complete model shown in Fig. 1 have been employed. The modifications involved in these models will be described in the results section.

2.2. Rules specifying the dynamics

Each node in the model can be in either the ON or the OFF state at a specific time step. Except for the TNF and GF nodes that correspond to external signals, each node receives inputs from one or several nodes (Fig. 1). There are two types of inputs: activating ones and inhibiting ones. The state of node i at the next time step $S_i(t+1)$ depends on its current state $S_i(t)$ as well as the relative magnitudes of the total activating input $A_i(t)$ and the total inhibiting input $H_i(t)$ it receives,

$$S_i(t+1) = \begin{cases} \text{OFF} & \text{if } A_i(t) < H_i(t), \\ \text{ON} & \text{if } A_i(t) > H_i(t), \\ S_i(t) & \text{if } A_i(t) = H_i(t). \end{cases} \quad (1)$$

The value of $A_i(t)$ ($H_i(t)$) is the summations of the contributions of all activating (inhibiting) input connections of node i . The contribution of each connection depends on the current states of the respective upstream nodes, and the dependence specified by one input connection rule. The input connections and the associated rules of each node are listed in supplementary table S1. To make the minimum hypothesis, most of the input rules have the same contribution of 1.0. A few rules are associated with arbitrarily larger values, to reflect the known or assumed dominating influences of the respective input connections (for example, the inhibiting input received by caspases from IAP is associated with a large value).

To mimic the threshold effects of caspase 3 in promoting apoptosis events, the evolution of the node “DNA Damage Event” does not follow Eq. (1) and is not first order in time. This node is always set to the OFF state unless the caspase 3 node has been in the ON state in previous two successive steps: only when both $S_{\text{Cas3}}(t-1) = \text{ON}$ and $S_{\text{Cas3}}(t) = \text{ON}$, $S_{\text{DNA Damage Event}}(t+1) = \text{ON}$, otherwise $S_{\text{DNA Damage Event}}(t+1) = \text{OFF}$.

2.3. Ending criteria and ending states of simulations

Time evolutions of the network are followed by simulations starting from different initial states. Each simulation run ends when either of the following two criteria was met. The first criterion is that the “DNA Damage Event” node has remained in the ON state for a predefined number of successive steps. This criterion as well as the corresponding ending states of the network is denoted as “apoptosis”. The second criterion is that apoptosis has not taken place by the first criterion but a pre-specified maximum number of steps has been reached. The corresponding ending states are denoted as “survival” ones. To determine the parameters (numbers of steps) used in these criteria, we performed simulations with different parameters using a set of 10,000 individual initial states. Results listed in Table S2 show that it is sufficient to test for apoptosis in 20 successive steps and to set the maximum number of steps to 200. Using larger numbers for either criterion does not change the results (Table S2).

2.4. Apoptosis ratios

The initial states that end in “apoptosis” are noted as apoptotic initial states. For a given combination of input signals, we compute an apoptosis ratio as the fraction of apoptotic initial states in all randomly selected initial states,

$$\text{Apop\%} = \frac{\text{Number of apoptotic initial states}}{\text{Total number of initial states}} \times 100\%$$

2.5. Initial states

In this work, we aim at obtaining insights into the design principles of the apoptosis network in general. Specific cell types/cellular contexts are not considered. Thus we use unbiased random initial states. Initial states have been sampled at random: each of the 37 internal nodes has an independent probability of 0.5 to be in either the ON state or the OFF state. Simulation results using 10,000, 20,000, 50,000 and 100,000 initial states, respectively, are compared (Table S3), and 10,000 initial states have been found to be sufficient to produce good statistics. We would like to note that in a real experiment, only a small set of initial states would be possible, depending on contexts such as the specific cell type and the particular experimental setup. In most cases detailed knowledge of such dependences are unavailable. Using unbiased random initial states provide a statistical approach towards systems properties of a general apoptosis network in lack of such knowledge.

2.6. Input signal combinations

The temporal evolutions from each of the 10,000 initial states have been monitored with the following combinations of input signals: (1) with no input signals (both TNF and GF in OFF states); (2) with only the TNF signal ON; (3) with only the GF signal ON; and (4) with both the TNF and GF signal ON. Unless specified otherwise (see below), the states of the TNF and GF nodes do not change with time in a simulation.

2.7. Time-dependent or interrupted apoptotic signals

Interruptions of apoptotic signals in a simulation have been employed to investigate the irreversibility of the apoptosis process. Interruption is achieved by setting and maintaining a selected node in its OFF state. Interruptions of the external signal TNF or the internal mitochondria signal are introduced when the node “DNA Damage Event” has been in the ON state for 2 continuous steps, results compared with respective simulations without interruptions. The state of the “DNA Damage Event” node itself is not changed manually but follows the dynamics rules as described earlier.

2.8. Perturbations on the states of the internal nodes

The stability of the surviving ending states with respect to fluctuations in the states of the internal nodes has been investigated. Starting from an ending state, the states of internal nodes are systematically reversed (from ON to OFF or vice versa), either one by one (single-node perturbations) or two at a time (dual-node perturbations), to obtain various perturbed surviving states. Time evolution starting from each of the perturbed states has been followed until one of the previously described ending criterions has again been met.

3. Results and discussions

3.1. Initial states that lead to apoptosis independent of external signals

From the simulations, we found that some of the initial states (lethal initial states) led to “apoptosis” under all the four different input conditions. These states would not be observed in real experiments but provide basis to analyze the roles of individual network components. Table 1 lists the percentages of lethal initial states obtained using the complete model and two alternative models with selected connections removed. These include Model-B in which connection B (see Fig. 1, the positive feedback involving a pro-apoptosis node) has been removed and Model-I in which connection I (see also Fig. 1, the negative feedback involving a pro-survival node) has been deleted. The calculated ratios of lethal initial states do not depend on the set of initial states used, similar ratios of lethal initial states (47–48%) obtained from simulations with different sets of initial states (Table S3).

The state distributions of the internal nodes in the lethal initial states have been computed. Some of them are significantly biased towards either the ON or the OFF state. Table 1 lists those nodes whose probability to be in the ON state ($p(\text{ON})$) in the set of lethal initial states deviates significantly from 0.5 (at confidence levels above 0.995 based on χ^2 tests).

Interestingly, some nodes showed up consistently in the above lists for both the complete model and the two alternative models. Among them, there are those corresponding to well-known pro-apoptotic components such as FADD, Cas8, Ikb, Cas3, BID and mitochondria (Budihardjo et al., 1999; Ko et al., 2005; Li et al., 2005; Narita et al., 1998; Philchenkov, 2004; Sartorius et al., 2001), and those corresponding to anti-apoptotic components including cFLIP, NFkB, BclX and IAP (Bernal-Mizrachi et al., 2006; Deveraux and Reed, 1999; Deveraux et al., 1997; Gross et al., 1999; Shimizu et al., 1999).

The differences between the respective lists produced by the three models can be explained to a large extent by their different topologies. For example, in Model-B, one of the activating input connections into the primary apoptotic effector Cas3 was blocked. To induce apoptosis, compensating inputs from other activators are needed. These could potentially include APC and Cas8. As the assembling of APC is difficult in lack of the TNF signal, Cas8 becomes vital for later Cas3 activation in some lethal initial states.

Thus in lethal initial states associated with Model-B, Cas8 has a significantly large $p(\text{ON})$ (0.65) while the Cas8-inhibitor cFLIP had a significantly small one (0.44). Similarly, in Model-I that misses one of the inhibiting input connections into the primary anti-apoptotic factor IAP, the mitochondria component that is the direct inhibitor of IAP has a significant high $p(\text{ON})$ (0.79).

It should be noticed that for over 40% of the internal nodes, their state distributions in the lethal or non-lethal initial states do not differ significantly. And for the remaining nodes the deviations of $p(\text{ON})$ from 0.5 in lethal initial states are not large. This suggests that the initial states of internal nodes as individual factors cannot dominate the final outcome of the network, in agreement with a previous data-driven modeling study (Janes et al., 2005).

3.2. The irreversibility of apoptosis and roles of feedback loops

Table 2 presents that in the complete model, Apop% changes between 48% and 97% depending on the external signal combinations. As expected, TNF is strongly apoptosis-promoting. Its effects can be significantly but incompletely offset by the external GF signal. Thus one way to investigate the irreversibility of the apoptosis process is to look at the effects of withdrawing the TNF signal after apoptosis has just started. Besides external signals, internal signals from the mitochondria component can also trigger apoptosis. Thus interrupting of this internal signal has also been considered.

Data in Table 2 suggests that apoptosis in the complete model are irreversible with respect to interruptions of either the external or the internal triggering signal. Previous studies suggested that network irreversibility could be attributed to the presence of positive feedbacks or dual negative feedbacks (Ferrell, 2002; Ferrell and Xiong, 2001). To explore how the feedback connections in our model may affect apoptosis and its irreversibility, we compared the complete model and 15 alternative models that involve deletions of four feedback connections, either separately or in various combinations (Table 2). These include connections B and I described earlier, as well as connections A (“DNA Damage Event” to p53) and II (PTEN to PIP3). Each of connections A and B forms a positive feedback involving pro-apoptosis nodes, while each of connections I and II forms negative feedbacks involving pro-survival nodes. In what follows we will compare the complete and alternative models first in terms of the overall apoptotic ratios

Table 1
Lethal initial states and nodes having significant bias on $p(\text{ON})$.

Model	Apop%		Key nodes of lethal initial states ($p(\text{ON})$)	
	No signal	GF only	Pro-apoptosis	Pro-survival
Original	48%	47%	TNFR1 (0.54), TRADD (0.54), FADD (0.53), Cas8 (0.54), Ikb (0.58), A20 (0.52), Cas3 (0.61), Cas6 (0.58), BID (0.57), p53 (0.52), <u>Mito (0.65)^a</u>	IKK (0.44), NFkB (0.42), BclX (0.41), <u>IAP (0.24)</u>
Knockout B	22%	22%	TNFR1 (0.58), <u>TRADD (0.65)</u> , FADD (0.64), <u>Cas8 (0.65)</u> , Ikb (0.55), APC (0.57), Cas3 (0.70), Cas6 (0.70), BID (0.55), p53 (0.53), <u>Mito (0.66)</u>	cFLIP (0.44), IKK (0.46), NFkB (0.43), BclX (0.44), <u>IAP (0.13)</u>
Knockout I	18%	15%	TRADD (0.54), Cas8 (0.54), Ikb (0.66), A20 (0.58), JNK (0.59), Cas3 (0.58), Cas6 (0.56), BID (0.62), BAD (0.58), <u>p53 (0.56)</u> , <u>Mito (0.79)</u>	RIP (0.46), cFLIP (0.46), TRAF2 (0.43), IKK (0.34), BclX (0.30), <u>IAP (0.18)</u> , PIP2 (0.46), <u>PIP3 (0.36)</u> , AKT (0.43), Mdm2 (0.42)

^a Nodes with underline had larger than 0.6 or smaller than 0.4 $p(\text{ON})$.

Table 2

Apoptosis ratios (%) obtained in normal, TNF signal-interrupted and mitochondrial signal-interrupted simulations.

Model	Apop% (Ori/iTNF/iMitochondria)			
	No signal ^a	GF only	TNF only	Double signals
Original	48/-/48 ^b	47/-/47	97/97/97	64/64/64
A ^c	48/-/48	47/-/47	97/97/97	62/62/62
B	22/-/22	22/-/22	97/97/97	58/58/58
I	18/-/8	15/-/0	97/80/68	54/29/0
II	47/-/47	47/-/47	97/97/97	60/60/60
AB	22/-/22	22/-/22	97/97/97	55/55/55
AI	15/-/8	0/-/0	97/75/68	0/0/0
AIi	47/-/47	47/-/47	97/97/97	59/59/59
BI	8/-/2	7/-/0	97/83/77	49/24/0
BII	22/-/22	22/-/22	97/97/97	53/53/53
I II	17/-/7	13/-/0	97/78/64	15/15/0
ABI	6/-/3	0/-/0	97/81/77	0/0/0
ABII	22/-/22	22/-/22	97/97/97	51/51/51
AI II	13/-/7	0/-/0	97/71/64	0/0/0
BI II	7/-/2	7/-/0	97/81/74	12/12/0
ALL	5/-/2	0/-/0	97/78/74	0/0/0

^a Different input signal conditions are considered.

^b The first number corresponds to apoptosis ratio in normal, the second in TNF signal-interrupted and the third in mitochondrial signal-interrupted simulations.

^c 16 alternative models designed by knocking out different combinations of connections A, B, I and II labeled in Fig. 1 were considered. The letters in this column means the feedbacks that the model lost.

without signal interruptions, and then in terms of the irreversibility with respect to signal interruptions.

3.2.1. Overall apoptotic ratios

Effects of knockouts on the overall apoptotic ratio have been observed for three combinations of input signals (No signal, GF only and Double signals, respectively. See Table 2). The various knockouts have little effect on Apop% (97%) with the TNF signal ON and the GF signal OFF.

Deletions of different connections have significantly different effects on the overall apoptotic ratio. Removing one or both of the connections B (Cas6→Cas3, activating) and I (Cas3+Cas6→IAP, inhibiting) induces noticeable decreases in Apop% (from 47–48% to 15–22% without TNF signal and from 64% to 54–58% with double signals). Removing one or both of the connections A (DNA Damage Event→p53, activating) and II (PTEN→PIP3, inhibiting) has little or minor effects as long as connection I has not been removed. However, after connection I has been deleted, further deletion of either connection A or II significantly reduces Apop% (to 0–17%) at the presence of the GF signal (the only GF and double signal cases in Table 2). These results imply that the feedbacks involving connections B and I play more essential roles in promoting apoptosis than feedbacks involving connections A and II. On the other hand, at the presence of external anti-apoptotic signals such as GF, the presence of feedbacks involving A or II can partly compensate for the loss of the feedback involving I.

In our model, connections B and I are involved in positive feedbacks containing caspase 3. They are shown to play essential roles in maintaining a high Apop% without TNF. Connections A and II are related to p53. It has been suggested that positive feedbacks involving caspase 3 are responsible for the fast switching behavior of caspase 3 in apoptosis (Choi et al., 2007). Overexpression of IAPs may disrupt apoptosis (Conte et al., 2001). The small effect of deleting connection II alone is consistent with the experimental results that the inhibition of PTEN was not required for survival of some cells (Kandasamy and Srivastava, 2002; Nielsen-Preiss et al., 2003).

3.2.2. Irreversibility of apoptosis

Interestingly, among the various alternative models, only those involving the knockout of connection I showed noticeable degradations in the irreversibility of the apoptosis process (Table 2). This is true for both the TNF-interrupting and mitochondria interrupting simulations. The importance of connection I in apoptosis irreversibility agree with the ODE-based study of Legwie and Bluthgen (Legewie et al., 2006), which suggested that irreversibility of the caspase cascade might rely on significant competitive binding of activated caspases with XIAP.

Table 2 also shows that the effects of knocking out connection I are noticeably stronger when the mitochondria signal is interrupted than when the TNF signal is withdrawn. For example, in Model-I in which only connection I is missing, none of the apoptosis runs are irreversible with respect to the interruption of the mitochondria signal (interrupted Apop% = 0), but part of the runs are still irreversible with respect to the withdrawing of the TNF signal (interrupted Apop% = 29%). This result suggests that in certain cellular contexts, the apoptosis process may be associated with different degrees of irreversibility with respect to the withdrawing of extra-cellular or intra-cellular triggering signals. The disappearing of intrinsic pro-apoptotic signals may more likely lead to the abolishment of apoptosis.

Besides connection I, connection A also plays a role in irreversibility. Although knocking out connection A alone do not have much effects, alternative models missing both I and A showed significant loss of irreversibility with respect to the withdrawing of the external TNF signal as compared with those only missing connection I.

3.3. Surviving ending states and their stability

For simulations that did not end in apoptosis, the final states belong to a small set of steady surviving states. There are in total 40 such states associated with different combinations of input signals. Different surviving ending states are outcomes of varying numbers of initial states. We define the number of initial states leading to a particular ending state as the accessibility of the ending state. For a given combination of input signals, a relative accessibility for a particular ending state is defined as the fraction of initial states leading to it among all initial states that end in survival. Table 3 lists all the surviving ending states, the respective signal combinations, and the absolute and relative accessibilities.

Each of the surviving ending states has been subjected to single-node perturbations (37 perturbations for each ending state) as well as dual-node perturbations (666 perturbations in total for each ending state). Simulations starting from these perturbed states ended either in a surviving state or in apoptosis. We note the latter as survival to apoptosis (S→A) transitions. For each surviving ending state, Table 3 lists all the single-node perturbations that lead to S→A transition as well as the number of dual-node perturbations leading to the same transition. To facilitate our discussions, we group the 40 surviving ending states into four categories based on the respective number of dual-node perturbations that lead to apoptosis: “very stable” for 0, “stable” for 1–10, “unstable” for 11–100, and “very unstable” for >100. Fig. 2 represents the final states of individual nodes in each surviving ending state, ending states belonging to different categories of stability depicted with different symbols.

3.3.1. The effects of the external GF signal on stability of the surviving ending states

Table 3 suggests that although the GF signal does not significantly increase the overall survival ratio when there is no TNF signal (Table 2), the presence of the GF signal can greatly

3.3.3. Nodes playing some controlling roles in the stability of the surviving ending states at different input combinations

Fig. 2 suggests that there are some important correlations between the stability of the surviving ending states and the state of individual nodes in those states.

Without any external signals, there are three surviving ending states, one with IAP ON and the other two with IAP OFF (Fig. 2a). The state with IAP ON is stable upon single-node perturbation and is associated with only 14 dual-node perturbations that lead to $S \rightarrow A$ transitions. The other two states are much less stable upon either type of perturbations. In contrast to IAP, the activation of mitochondria exhibits strong destabilizing effects. Of the three surviving ending states, the one with Mito activated is the most unstable one (Table 3).

With only the TNF signal ON, the only 4 surviving states are all very unstable. The IAP node is OFF and the mitochondria node is ON in all of them (Fig. 2b). These states are “survival” only because Cas8 was inhibited by cFLIP before the activation of the downstream pro-apoptotic pathways.

With only the GF signal ON, all 11 surviving states belong to either the “stable” or “very stable” category. Comparisons of the states of individual nodes imply the importance of NFκB: the states with NFκB ON and IκB OFF are more stable (Fig. 2c).

With both TNF and GF signals ON, NFκB and Cas8 exhibited dominant effects. States with NFκB ON and Cas8 OFF all belong to

the “very stable” category, while states with NFκB OFF and Cas8 ON all belong to either the “unstable” or “very unstable” categories (Fig. 2d). It is interesting to note that IAP is always in the activated state in these surviving ending states, but states with activated IAP can still be unstable.

The above results may be correlated with reported levels of expression of IAP, NFκB and caspase-8 in tumor cells. Such cells may be associated with high stability of the surviving states. IAP was reported to have a high level of expression in different cells (Endo et al., 2004; Hofmann et al., 2002; Nemoto et al., 2004). However, from its expression level alone one could not individually predict the effects of chemotherapy in non-small-cell lung cancer (NSCLC) (Ferreira et al., 2001). NFκB has different levels of expression in NSCLC cells and the apoptotic rate was lower in cells with higher NFκB expressions (Zhang et al., 2006). Caspase-8 was up-regulated in NSCLC cells in the pro-caspase form. The apoptotic rate was significantly higher in the cells with a stronger immunostaining pattern of caspase-8 (Tormanen-Napankangas et al., 2001).

4. Conclusions

In summary, we have analyzed the apoptosis network using a Boolean model. Based on simulations started from randomly

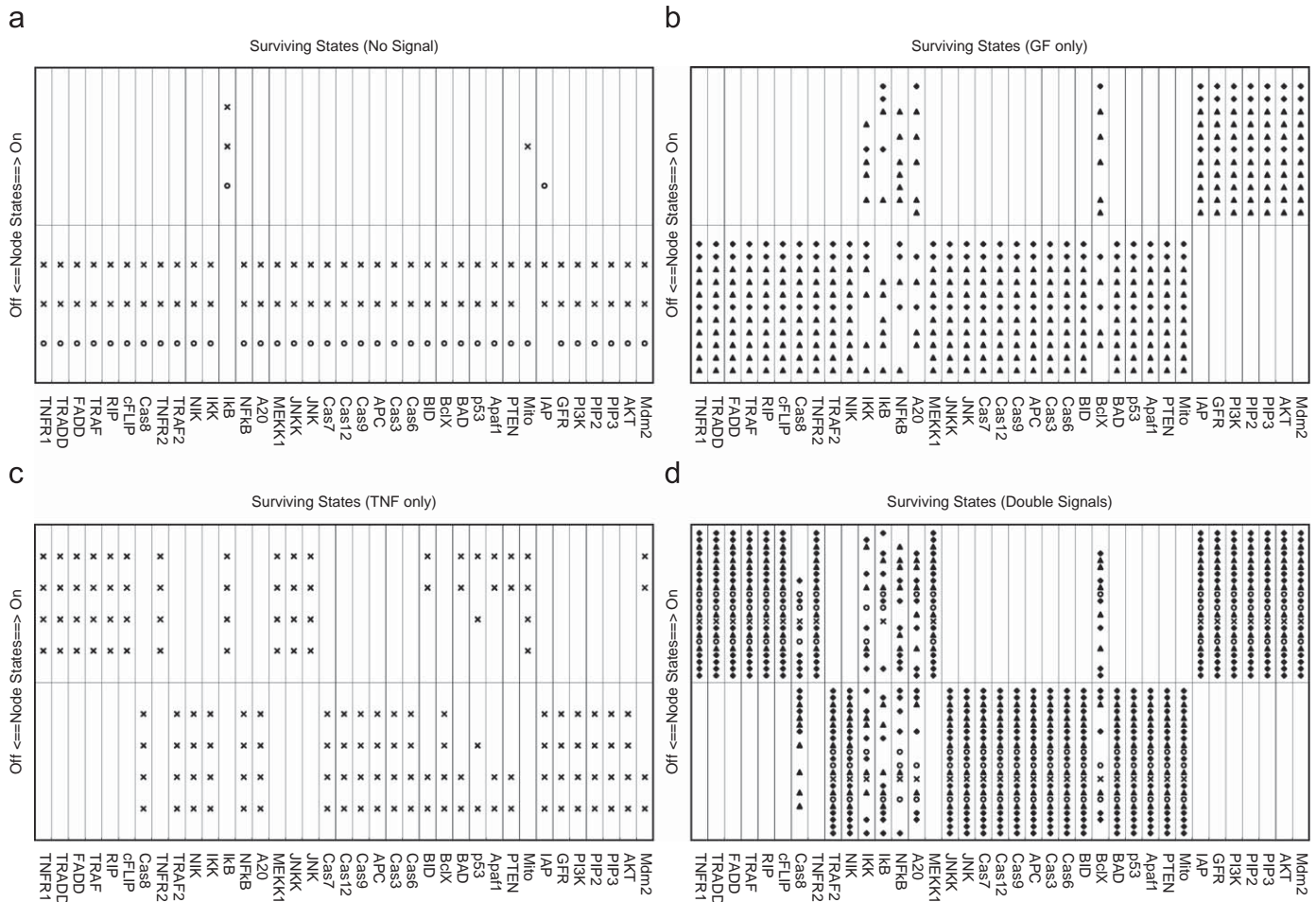


Fig. 2. States of individual nodes in and the stability category of different surviving states. Each node corresponds to one column. Each surviving state corresponds to two lines of symbols, one above zero and another below zero. A symbol in a column and a line above (below) zero indicates that the corresponding node in a particular survival state is in the ON (OFF) state. The shapes of the symbols represent stability categories of surviving states: solid triangles for “very stable”, solid diamonds for “stable”, circles for “unstable” and crosses for “very unstable”. Steady surviving states under different input signal conditions are shown: (a) no signal; (b) TNF only; (c) GF only; and (d) GF and TNF.

sampled initial states, the model is able to reproduce well-known pro-apoptotic and pro-survival molecular components (nodes). The effects of the initial states of some but not all of these nodes depend on the presence/missing of certain key feedback loops. The model suggested that although irreversibility of the apoptosis process indeed depends on the presence of feedback loops in the network structure, not all the four feedback loops investigated in this work contributed similarly. Two of the investigated feedbacks directly involving Cas3 are essential in promoting apoptosis as well as in maintaining its irreversibility. The other two feedbacks related to p53 showed compensating effects only when the former two are missing. Moreover, disruptions in the intrinsic pro-apoptotic signal are more likely to induce abolishment of apoptosis than the withdrawing of the extra-cellular signal. These were found to be consistent with previous experimental or in silico results (Conte et al., 2001; Legewie et al., 2006). We found that the external GF signal was of key importance for the stability of the surviving states of the network. The states of a few key nodes in surviving states are also strongly correlated to the stability of the respective network state.

The above results suggested some general design principles of the apoptosis network. The irreversibility of the apoptosis process and the stability of the surviving states might, at first sight, be mutually exclusive. The apoptosis network seems to have achieved both in the same network framework by using different components to control the two properties. The irreversibility of apoptosis mostly and redundantly relies on down-stream positive feedback loops, while the stability of the surviving states depends more on the presence of external pro-survival signals. Such a design may provide some plasticity for cell apoptosis to adapt to different biological contexts. The strength of the external pro-survival signal may control how easy or difficult it can be to trigger apoptosis, but once the cell enters apoptosis, the process cannot be reversed.

Our model necessarily involves large simplifications: components are represented only as nodes with two possible states; dynamics are governed by simple rules replacing complex molecular processes. However, using such a simplified model allowed us to model a more complete network than using ODE models involving detailed dynamics. The network model has included known molecular pathways integrating external and intrinsic apoptotic and surviving signals. Given the simplifications and the lack of detailed knowledge about the status of various cellular components under many experimental circumstances, we did not try to approximate experimental results obtained in a particular cellular context. Instead, we performed simulations starting from randomly initial states with unbiased distributions, and extracted and analyzed systems properties based on statistics. It is important to note that many of the computer generated initial states cannot be realized in real experiments (e.g., the cell cannot survive), but they do contain valuable information for the characterization and understanding of the design principles of the network.

Compared with ODE models, Boolean networks are certainly limited in approximating experimental results and in making context-specific quantitative predictions of cellular dynamics. Our work suggested that BN models, however, might allow for easier integration of various experimental information and more systematic explorations in both the model space and state space, and provide results that are readily subjected to a variety of statistical analyses. As interest in systems level properties and how such properties emerge from the integration of various network components increases, we expect that BN models like those presented here will complement other types of in silico approaches as well as experimental ones in studies of complex cellular networks.

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Appendix A. Supplementary material

Supplementary data associated with this article can be found in the online version at doi:10.1016/j.jtbi.2009.04.024.

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