CHAPTER

# A Tour of Computer Systems

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A computer system consists of hardware and systems software that work together to run application programs. Specific implementations of systems change over time, but the underlying concepts do not. All computer systems have similar hardware and software components that perform similar functions. This book is written for programmers who want to get better at their craft by understanding how these components work and how they affect the correctness and performance of their programs.

You are poised for an exciting journey. If you dedicate yourself to learning the concepts in this book, then you will be on your way to becoming a rare "power programmer," enlightened by an understanding of the underlying computer system and its impact on your application programs.

You are going to learn practical skills such as how to avoid strange numerical errors caused by the way that computers represent numbers. You will learn how to optimize your C code by using clever tricks that exploit the designs of modern processors and memory systems. You will learn how the compiler implements procedure calls and how to use this knowledge to avoid the security holes from buffer overflow vulnerabilities that plague network and Internet software. You will learn how to recognize and avoid the nasty errors during linking that confound the average programmer. You will learn how to write your own Unix shell, your own dynamic storage allocation package, and even your own Web server. You will learn the promises and pitfalls of concurrency, a topic of increasing importance as multiple processor cores are integrated onto single chips.

In their classic text on the C programming language [61], Kernighan and Ritchie introduce readers to C using the hello program shown in Figure 1.1. Although hello is a very simple program, every major part of the system must work in concert in order for it to run to completion. In a sense, the goal of this book is to help you understand what happens and why when you run hello on your system.

We begin our study of systems by tracing the lifetime of the hello program, from the time it is created by a programmer, until it runs on a system, prints its simple message, and terminates. As we follow the lifetime of the program, we will briefly introduce the key concepts, terminology, and components that come into play. Later chapters will expand on these ideas.

```
code/intro/hello.c

#include <stdio.h>

int main()

{

printf("hello, world\n");

return 0;

}

code/intro/hello.c
```

Figure 1.1 The hello program. (Source: [60])

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                                                                                    125
                                                                                           10
```

Figure 1.2 The ASCII text representation of hello.c.

#### **1.1** Information Is Bits + Context

Our hello program begins life as a *source program* (or *source file*) that the programmer creates with an editor and saves in a text file called hello.c. The source program is a sequence of bits, each with a value of 0 or 1, organized in 8-bit chunks called *bytes*. Each byte represents some text character in the program.

Most computer systems represent text characters using the ASCII standard that represents each character with a unique byte-size integer value. For example, Figure 1.2 shows the ASCII representation of the hello.c program.

The hello.c program is stored in a file as a sequence of bytes. Each byte has an integer value that corresponds to some character. For example, the first byte has the integer value 35, which corresponds to the character '#'. The second byte has the integer value 105, which corresponds to the character 'i', and so on. Notice that each text line is terminated by the invisible *newline* character '\n', which is represented by the integer value 10. Files such as hello.c that consist exclusively of ASCII characters are known as *text files*. All other files are known as *binary files*.

The representation of hello.c illustrates a fundamental idea: All information in a system—including disk files, programs stored in memory, user data stored in memory, and data transferred across a network—is represented as a bunch of bits. The only thing that distinguishes different data objects is the context in which we view them. For example, in different contexts, the same sequence of bytes might represent an integer, floating-point number, character string, or machine instruction.

As programmers, we need to understand machine representations of numbers because they are not the same as integers and real numbers. They are finite

<sup>1.</sup> Other encoding methods are used to represent text in non-English languages. See the aside on page 86 for a discussion on this.

# **Aside** Origins of the C programming language

C was developed from 1969 to 1973 by Dennis Ritchie of Bell Laboratories. The American National Standards Institute (ANSI) ratified the ANSI C standard in 1989, and this standardization later became the responsibility of the International Standards Organization (ISO). The standards define the C language and a set of library functions known as the *C standard library*. Kernighan and Ritchie describe ANSI C in their classic book, which is known affectionately as "K&R" [61]. In Ritchie's words [92], C is "quirky, flawed, and an enormous success." So why the success?

- C was closely tied with the Unix operating system. C was developed from the beginning as the system programming language for Unix. Most of the Unix kernel (the core part of the operating system), and all of its supporting tools and libraries, were written in C. As Unix became popular in universities in the late 1970s and early 1980s, many people were exposed to C and found that they liked it. Since Unix was written almost entirely in C, it could be easily ported to new machines, which created an even wider audience for both C and Unix.
- C is a small, simple language. The design was controlled by a single person, rather than a committee, and the result was a clean, consistent design with little baggage. The K&R book describes the complete language and standard library, with numerous examples and exercises, in only 261 pages. The simplicity of C made it relatively easy to learn and to port to different computers.
- C was designed for a practical purpose. C was designed to implement the Unix operating system. Later, other people found that they could write the programs they wanted, without the language getting in the way.

C is the language of choice for system-level programming, and there is a huge installed base of application-level programs as well. However, it is not perfect for all programmers and all situations. C pointers are a common source of confusion and programming errors. C also lacks explicit support for useful abstractions such as classes, objects, and exceptions. Newer languages such as C++ and Java address these issues for application-level programs.

approximations that can behave in unexpected ways. This fundamental idea is explored in detail in Chapter 2.

# **1.2** Programs Are Translated by Other Programs into Different Forms

The hello program begins life as a high-level C program because it can be read and understood by human beings in that form. However, in order to run hello.c on the system, the individual C statements must be translated by other programs into a sequence of low-level *machine-language* instructions. These instructions are then packaged in a form called an *executable object program* and stored as a binary disk file. Object programs are also referred to as *executable object files*.

On a Unix system, the translation from source file to object file is performed by a *compiler driver*:

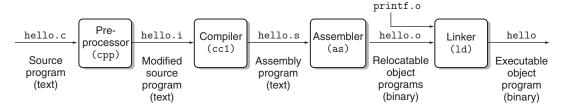


Figure 1.3 The compilation system.

```
linux> gcc -o hello hello.c
```

Here, the GCC compiler driver reads the source file hello.c and translates it into an executable object file hello. The translation is performed in the sequence of four phases shown in Figure 1.3. The programs that perform the four phases (preprocessor, compiler, assembler, and linker) are known collectively as the compilation system.

- Preprocessing phase. The preprocessor (cpp) modifies the original C program according to directives that begin with the '#' character. For example, the #include <stdio.h> command in line 1 of hello.c tells the preprocessor to read the contents of the system header file stdio.h and insert it directly into the program text. The result is another C program, typically with the .i suffix.
- Compilation phase. The compiler (cc1) translates the text file hello.i into the text file hello.s, which contains an assembly-language program. This program includes the following definition of function main:

```
main:
1
               $8, %rsp
2
      subq
3
      movl
               $.LCO, %edi
      call
               puts
5
      movl
               $0, %eax
      addq
               $8, %rsp
      ret
```

Each of lines 2–7 in this definition describes one low-level machine-language instruction in a textual form. Assembly language is useful because it provides a common output language for different compilers for different high-level languages. For example, C compilers and Fortran compilers both generate output files in the same assembly language.

• Assembly phase. Next, the assembler (as) translates hello.s into machine-language instructions, packages them in a form known as a relocatable object program, and stores the result in the object file hello.o. This file is a binary file containing 17 bytes to encode the instructions for function main. If we were to view hello.o with a text editor, it would appear to be gibberish.

# **Aside** The GNU project

GCC is one of many useful tools developed by the GNU (short for GNU's Not Unix) project. The GNU project is a tax-exempt charity started by Richard Stallman in 1984, with the ambitious goal of developing a complete Unix-like system whose source code is unencumbered by restrictions on how it can be modified or distributed. The GNU project has developed an environment with all the major components of a Unix operating system, except for the kernel, which was developed separately by the Linux project. The GNU environment includes the EMACS editor, GCC compiler, GDB debugger, assembler, linker, utilities for manipulating binaries, and other components. The GCC compiler has grown to support many different languages, with the ability to generate code for many different machines. Supported languages include C, C++, Fortran, Java, Pascal, Objective-C, and Ada.

The GNU project is a remarkable achievement, and yet it is often overlooked. The modern open-source movement (commonly associated with Linux) owes its intellectual origins to the GNU project's notion of *free software* ("free" as in "free speech," not "free beer"). Further, Linux owes much of its popularity to the GNU tools, which provide the environment for the Linux kernel.

• Linking phase. Notice that our hello program calls the printf function, which is part of the standard C library provided by every C compiler. The printf function resides in a separate precompiled object file called printf.o, which must somehow be merged with our hello.o program. The linker (ld) handles this merging. The result is the hello file, which is an executable object file (or simply executable) that is ready to be loaded into memory and executed by the system.

# 1.3 It Pays to Understand How Compilation Systems Work

For simple programs such as hello.c, we can rely on the compilation system to produce correct and efficient machine code. However, there are some important reasons why programmers need to understand how compilation systems work:

• Optimizing program performance. Modern compilers are sophisticated tools that usually produce good code. As programmers, we do not need to know the inner workings of the compiler in order to write efficient code. However, in order to make good coding decisions in our C programs, we do need a basic understanding of machine-level code and how the compiler translates different C statements into machine code. For example, is a switch statement always more efficient than a sequence of if-else statements? How much overhead is incurred by a function call? Is a while loop more efficient than a for loop? Are pointer references more efficient than array indexes? Why does our loop run so much faster if we sum into a local variable instead of an argument that is passed by reference? How can a function run faster when we simply rearrange the parentheses in an arithmetic expression?

In Chapter 3, we introduce x86-64, the machine language of recent generations of Linux, Macintosh, and Windows computers. We describe how compilers translate different C constructs into this language. In Chapter 5, you will learn how to tune the performance of your C programs by making simple transformations to the C code that help the compiler do its job better. In Chapter 6, you will learn about the hierarchical nature of the memory system, how C compilers store data arrays in memory, and how your C programs can exploit this knowledge to run more efficiently.

- Understanding link-time errors. In our experience, some of the most perplexing programming errors are related to the operation of the linker, especially when you are trying to build large software systems. For example, what does it mean when the linker reports that it cannot resolve a reference? What is the difference between a static variable and a global variable? What happens if you define two global variables in different C files with the same name? What is the difference between a static library and a dynamic library? Why does it matter what order we list libraries on the command line? And scariest of all, why do some linker-related errors not appear until run time? You will learn the answers to these kinds of questions in Chapter 7.
- Avoiding security holes. For many years, buffer overflow vulnerabilities have accounted for many of the security holes in network and Internet servers. These vulnerabilities exist because too few programmers understand the need to carefully restrict the quantity and forms of data they accept from untrusted sources. A first step in learning secure programming is to understand the consequences of the way data and control information are stored on the program stack. We cover the stack discipline and buffer overflow vulnerabilities in Chapter 3 as part of our study of assembly language. We will also learn about methods that can be used by the programmer, compiler, and operating system to reduce the threat of attack.

# **1.4** Processors Read and Interpret Instructions Stored in Memory

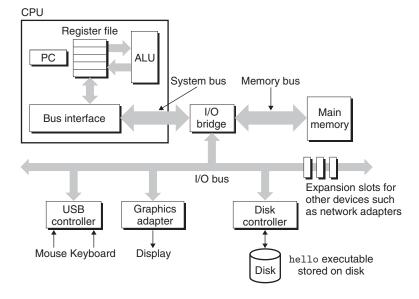
At this point, our hello.c source program has been translated by the compilation system into an executable object file called hello that is stored on disk. To run the executable file on a Unix system, we type its name to an application program known as a *shell*:

linux> ./hello
hello, world
linux>

The shell is a command-line interpreter that prints a prompt, waits for you to type a command line, and then performs the command. If the first word of the command line does not correspond to a built-in shell command, then the shell

Figure 1.4

Hardware organization of a typical system. CPU: central processing unit, ALU: arithmetic/logic unit, PC: program counter, USB: Universal Serial Bus.



assumes that it is the name of an executable file that it should load and run. So in this case, the shell loads and runs the hello program and then waits for it to terminate. The hello program prints its message to the screen and then terminates. The shell then prints a prompt and waits for the next input command line.

# 1.4.1 Hardware Organization of a System

To understand what happens to our hello program when we run it, we need to understand the hardware organization of a typical system, which is shown in Figure 1.4. This particular picture is modeled after the family of recent Intel systems, but all systems have a similar look and feel. Don't worry about the complexity of this figure just now. We will get to its various details in stages throughout the course of the book.

#### **Buses**

Running throughout the system is a collection of electrical conduits called *buses* that carry bytes of information back and forth between the components. Buses are typically designed to transfer fixed-size chunks of bytes known as *words*. The number of bytes in a word (the *word size*) is a fundamental system parameter that varies across systems. Most machines today have word sizes of either 4 bytes (32 bits) or 8 bytes (64 bits). In this book, we do not assume any fixed definition of word size. Instead, we will specify what we mean by a "word" in any context that requires this to be defined.

#### I/O Devices

Input/output (I/O) devices are the system's connection to the external world. Our example system has four I/O devices: a keyboard and mouse for user input, a display for user output, and a disk drive (or simply disk) for long-term storage of data and programs. Initially, the executable hello program resides on the disk.

Each I/O device is connected to the I/O bus by either a *controller* or an *adapter*. The distinction between the two is mainly one of packaging. Controllers are chip sets in the device itself or on the system's main printed circuit board (often called the *motherboard*). An adapter is a card that plugs into a slot on the motherboard. Regardless, the purpose of each is to transfer information back and forth between the I/O bus and an I/O device.

Chapter 6 has more to say about how I/O devices such as disks work. In Chapter 10, you will learn how to use the Unix I/O interface to access devices from your application programs. We focus on the especially interesting class of devices known as networks, but the techniques generalize to other kinds of devices as well.

# Main Memory

The *main memory* is a temporary storage device that holds both a program and the data it manipulates while the processor is executing the program. Physically, main memory consists of a collection of *dynamic random access memory* (DRAM) chips. Logically, memory is organized as a linear array of bytes, each with its own unique address (array index) starting at zero. In general, each of the machine instructions that constitute a program can consist of a variable number of bytes. The sizes of data items that correspond to C program variables vary according to type. For example, on an x86-64 machine running Linux, data of type short require 2 bytes, types int and float 4 bytes, and types long and double 8 bytes.

Chapter 6 has more to say about how memory technologies such as DRAM chips work, and how they are combined to form main memory.

#### **Processor**

The *central processing unit* (CPU), or simply *processor*, is the engine that interprets (or *executes*) instructions stored in main memory. At its core is a word-size storage device (or *register*) called the *program counter* (PC). At any point in time, the PC points at (contains the address of) some machine-language instruction in main memory.<sup>2</sup>

From the time that power is applied to the system until the time that the power is shut off, a processor repeatedly executes the instruction pointed at by the program counter and updates the program counter to point to the next instruction. A processor *appears* to operate according to a very simple instruction execution model, defined by its *instruction set architecture*. In this model, instructions execute

<sup>2.</sup> PC is also a commonly used acronym for "personal computer." However, the distinction between the two should be clear from the context.

in strict sequence, and executing a single instruction involves performing a series of steps. The processor reads the instruction from memory pointed at by the program counter (PC), interprets the bits in the instruction, performs some simple operation dictated by the instruction, and then updates the PC to point to the next instruction, which may or may not be contiguous in memory to the instruction that was just executed.

There are only a few of these simple operations, and they revolve around main memory, the *register file*, and the *arithmetic/logic unit* (ALU). The register file is a small storage device that consists of a collection of word-size registers, each with its own unique name. The ALU computes new data and address values. Here are some examples of the simple operations that the CPU might carry out at the request of an instruction:

- *Load:* Copy a byte or a word from main memory into a register, overwriting the previous contents of the register.
- *Store:* Copy a byte or a word from a register to a location in main memory, overwriting the previous contents of that location.
- *Operate*: Copy the contents of two registers to the ALU, perform an arithmetic operation on the two words, and store the result in a register, overwriting the previous contents of that register.
- *Jump*: Extract a word from the instruction itself and copy that word into the program counter (PC), overwriting the previous value of the PC.

We say that a processor appears to be a simple implementation of its instruction set architecture, but in fact modern processors use far more complex mechanisms to speed up program execution. Thus, we can distinguish the processor's instruction set architecture, describing the effect of each machine-code instruction, from its *microarchitecture*, describing how the processor is actually implemented. When we study machine code in Chapter 3, we will consider the abstraction provided by the machine's instruction set architecture. Chapter 4 has more to say about how processors are actually implemented. Chapter 5 describes a model of how modern processors work that enables predicting and optimizing the performance of machine-language programs.

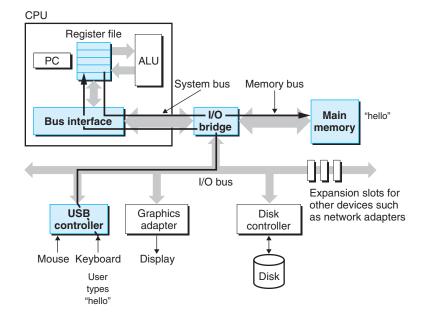
#### 1.4.2 Running the hello Program

Given this simple view of a system's hardware organization and operation, we can begin to understand what happens when we run our example program. We must omit a lot of details here that will be filled in later, but for now we will be content with the big picture.

Initially, the shell program is executing its instructions, waiting for us to type a command. As we type the characters ./hello at the keyboard, the shell program reads each one into a register and then stores it in memory, as shown in Figure 1.5.

When we hit the enter key on the keyboard, the shell knows that we have finished typing the command. The shell then loads the executable hello file by executing a sequence of instructions that copies the code and data in the hello

Figure 1.5
Reading the hello command from the keyboard.



object file from disk to main memory. The data includes the string of characters hello, world\n that will eventually be printed out.

Using a technique known as *direct memory access* (DMA, discussed in Chapter 6), the data travel directly from disk to main memory, without passing through the processor. This step is shown in Figure 1.6.

Once the code and data in the hello object file are loaded into memory, the processor begins executing the machine-language instructions in the hello program's main routine. These instructions copy the bytes in the hello, world\n string from memory to the register file, and from there to the display device, where they are displayed on the screen. This step is shown in Figure 1.7.

## 1.5 Caches Matter

An important lesson from this simple example is that a system spends a lot of time moving information from one place to another. The machine instructions in the hello program are originally stored on disk. When the program is loaded, they are copied to main memory. As the processor runs the program, instructions are copied from main memory into the processor. Similarly, the data string hello,world\n, originally on disk, is copied to main memory and then copied from main memory to the display device. From a programmer's perspective, much of this copying is overhead that slows down the "real work" of the program. Thus, a major goal for system designers is to make these copy operations run as fast as possible.

Because of physical laws, larger storage devices are slower than smaller storage devices. And faster devices are more expensive to build than their slower

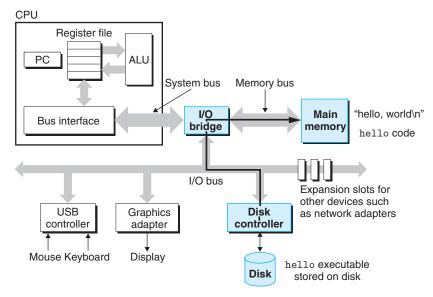


Figure 1.6 Loading the executable from disk into main memory.

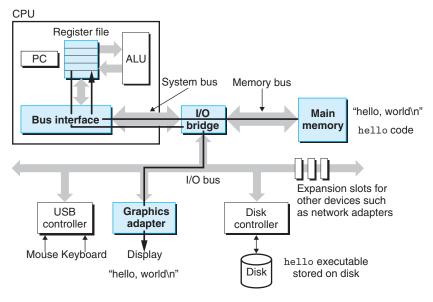
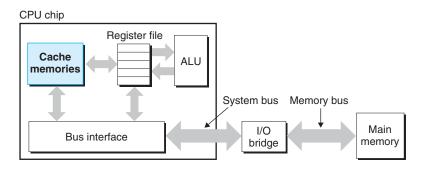


Figure 1.7 Writing the output string from memory to the display.

Figure 1.8 Cache memories.



counterparts. For example, the disk drive on a typical system might be 1,000 times larger than the main memory, but it might take the processor 10,000,000 times longer to read a word from disk than from memory.

Similarly, a typical register file stores only a few hundred bytes of information, as opposed to billions of bytes in the main memory. However, the processor can read data from the register file almost 100 times faster than from memory. Even more troublesome, as semiconductor technology progresses over the years, this *processor–memory gap* continues to increase. It is easier and cheaper to make processors run faster than it is to make main memory run faster.

To deal with the processor-memory gap, system designers include smaller, faster storage devices called cache memories (or simply caches) that serve as temporary staging areas for information that the processor is likely to need in the near future. Figure 1.8 shows the cache memories in a typical system. An L1 cache on the processor chip holds tens of thousands of bytes and can be accessed nearly as fast as the register file. A larger L2 cache with hundreds of thousands to millions of bytes is connected to the processor by a special bus. It might take 5 times longer for the processor to access the L2 cache than the L1 cache, but this is still 5 to 10 times faster than accessing the main memory. The L1 and L2 caches are implemented with a hardware technology known as static random access memory (SRAM). Newer and more powerful systems even have three levels of cache: L1, L2, and L3. The idea behind caching is that a system can get the effect of both a very large memory and a very fast one by exploiting locality, the tendency for programs to access data and code in localized regions. By setting up caches to hold data that are likely to be accessed often, we can perform most memory operations using the fast caches.

One of the most important lessons in this book is that application programmers who are aware of cache memories can exploit them to improve the performance of their programs by an order of magnitude. You will learn more about these important devices and how to exploit them in Chapter 6.

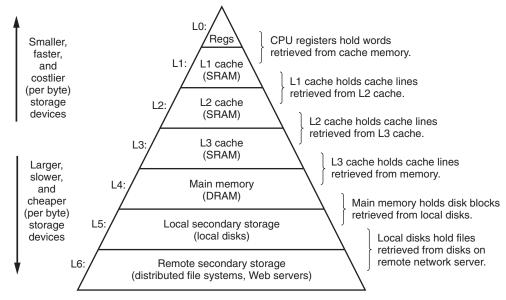


Figure 1.9 An example of a memory hierarchy.

# **1.6** Storage Devices Form a Hierarchy

This notion of inserting a smaller, faster storage device (e.g., cache memory) between the processor and a larger, slower device (e.g., main memory) turns out to be a general idea. In fact, the storage devices in every computer system are organized as a *memory hierarchy* similar to Figure 1.9. As we move from the top of the hierarchy to the bottom, the devices become slower, larger, and less costly per byte. The register file occupies the top level in the hierarchy, which is known as level 0 or L0. We show three levels of caching L1 to L3, occupying memory hierarchy levels 1 to 3. Main memory occupies level 4, and so on.

The main idea of a memory hierarchy is that storage at one level serves as a cache for storage at the next lower level. Thus, the register file is a cache for the L1 cache. Caches L1 and L2 are caches for L2 and L3, respectively. The L3 cache is a cache for the main memory, which is a cache for the disk. On some networked systems with distributed file systems, the local disk serves as a cache for data stored on the disks of other systems.

Just as programmers can exploit knowledge of the different caches to improve performance, programmers can exploit their understanding of the entire memory hierarchy. Chapter 6 will have much more to say about this.

# **1.7** The Operating System Manages the Hardware

Back to our hello example. When the shell loaded and ran the hello program, and when the hello program printed its message, neither program accessed the

Figure 1.10 Layered view of a computer system.

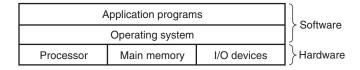
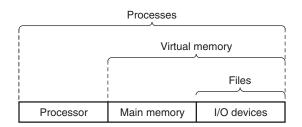


Figure 1.11
Abstractions provided by an operating system.



keyboard, display, disk, or main memory directly. Rather, they relied on the services provided by the *operating system*. We can think of the operating system as a layer of software interposed between the application program and the hardware, as shown in Figure 1.10. All attempts by an application program to manipulate the hardware must go through the operating system.

The operating system has two primary purposes: (1) to protect the hardware from misuse by runaway applications and (2) to provide applications with simple and uniform mechanisms for manipulating complicated and often wildly different low-level hardware devices. The operating system achieves both goals via the fundamental abstractions shown in Figure 1.11: processes, virtual memory, and files. As this figure suggests, files are abstractions for I/O devices, virtual memory is an abstraction for both the main memory and disk I/O devices, and processes are abstractions for the processor, main memory, and I/O devices. We will discuss each in turn.

## 1.7.1 Processes

When a program such as hello runs on a modern system, the operating system provides the illusion that the program is the only one running on the system. The program appears to have exclusive use of both the processor, main memory, and I/O devices. The processor appears to execute the instructions in the program, one after the other, without interruption. And the code and data of the program appear to be the only objects in the system's memory. These illusions are provided by the notion of a process, one of the most important and successful ideas in computer science.

A *process* is the operating system's abstraction for a running program. Multiple processes can run concurrently on the same system, and each process appears to have exclusive use of the hardware. By *concurrently*, we mean that the instructions of one process are interleaved with the instructions of another process. In most systems, there are more processes to run than there are CPUs to run them.

### Aside Unix, Posix, and the Standard Unix Specification

The 1960s was an era of huge, complex operating systems, such as IBM's OS/360 and Honeywell's Multics systems. While OS/360 was one of the most successful software projects in history, Multics dragged on for years and never achieved wide-scale use. Bell Laboratories was an original partner in the Multics project but dropped out in 1969 because of concern over the complexity of the project and the lack of progress. In reaction to their unpleasant Multics experience, a group of Bell Labs researchers—Ken Thompson, Dennis Ritchie, Doug McIlroy, and Joe Ossanna—began work in 1969 on a simpler operating system for a Digital Equipment Corporation PDP-7 computer, written entirely in machine language. Many of the ideas in the new system, such as the hierarchical file system and the notion of a shell as a user-level process, were borrowed from Multics but implemented in a smaller, simpler package. In 1970, Brian Kernighan dubbed the new system "Unix" as a pun on the complexity of "Multics." The kernel was rewritten in C in 1973, and Unix was announced to the outside world in 1974 [93].

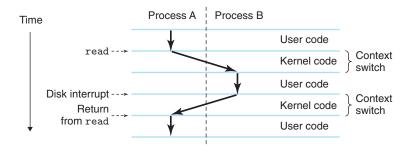
Because Bell Labs made the source code available to schools with generous terms, Unix developed a large following at universities. The most influential work was done at the University of California at Berkeley in the late 1970s and early 1980s, with Berkeley researchers adding virtual memory and the Internet protocols in a series of releases called Unix 4.xBSD (Berkeley Software Distribution). Concurrently, Bell Labs was releasing their own versions, which became known as System V Unix. Versions from other vendors, such as the Sun Microsystems Solaris system, were derived from these original BSD and System V versions.

Trouble arose in the mid 1980s as Unix vendors tried to differentiate themselves by adding new and often incompatible features. To combat this trend, IEEE (Institute for Electrical and Electronics Engineers) sponsored an effort to standardize Unix, later dubbed "Posix" by Richard Stallman. The result was a family of standards, known as the Posix standards, that cover such issues as the C language interface for Unix system calls, shell programs and utilities, threads, and network programming. More recently, a separate standardization effort, known as the "Standard Unix Specification," has joined forces with Posix to create a single, unified standard for Unix systems. As a result of these standardization efforts, the differences between Unix versions have largely disappeared.

Traditional systems could only execute one program at a time, while newer *multi-core* processors can execute several programs simultaneously. In either case, a single CPU can appear to execute multiple processes concurrently by having the processor switch among them. The operating system performs this interleaving with a mechanism known as *context switching*. To simplify the rest of this discussion, we consider only a *uniprocessor system* containing a single CPU. We will return to the discussion of *multiprocessor* systems in Section 1.9.2.

The operating system keeps track of all the state information that the process needs in order to run. This state, which is known as the *context*, includes information such as the current values of the PC, the register file, and the contents of main memory. At any point in time, a uniprocessor system can only execute the code for a single process. When the operating system decides to transfer control from the current process to some new process, it performs a *context switch* by saving the context of the current process, restoring the context of the new process, and

Figure 1.12 Process context switching.



then passing control to the new process. The new process picks up exactly where it left off. Figure 1.12 shows the basic idea for our example hello scenario.

There are two concurrent processes in our example scenario: the shell process and the hello process. Initially, the shell process is running alone, waiting for input on the command line. When we ask it to run the hello program, the shell carries out our request by invoking a special function known as a *system call* that passes control to the operating system. The operating system saves the shell's context, creates a new hello process and its context, and then passes control to the new hello process. After hello terminates, the operating system restores the context of the shell process and passes control back to it, where it waits for the next command-line input.

As Figure 1.12 indicates, the transition from one process to another is managed by the operating system *kernel*. The kernel is the portion of the operating system code that is always resident in memory. When an application program requires some action by the operating system, such as to read or write a file, it executes a special *system call* instruction, transferring control to the kernel. The kernel then performs the requested operation and returns back to the application program. Note that the kernel is not a separate process. Instead, it is a collection of code and data structures that the system uses to manage all the processes.

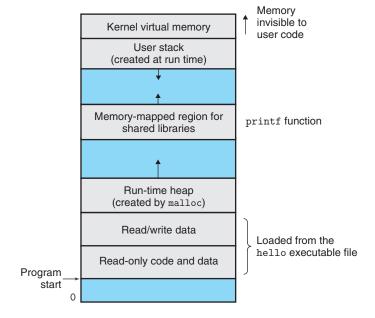
Implementing the process abstraction requires close cooperation between both the low-level hardware and the operating system software. We will explore how this works, and how applications can create and control their own processes, in Chapter 8.

#### 1.7.2 Threads

Although we normally think of a process as having a single control flow, in modern systems a process can actually consist of multiple execution units, called *threads*, each running in the context of the process and sharing the same code and global data. Threads are an increasingly important programming model because of the requirement for concurrency in network servers, because it is easier to share data between multiple threads than between multiple processes, and because threads are typically more efficient than processes. Multi-threading is also one way to make programs run faster when multiple processors are available, as we will discuss in

Figure 1.13
Process virtual address
space. (The regions are not

drawn to scale.)



Section 1.9.2. You will learn the basic concepts of concurrency, including how to write threaded programs, in Chapter 12.

#### 1.7.3 Virtual Memory

Virtual memory is an abstraction that provides each process with the illusion that it has exclusive use of the main memory. Each process has the same uniform view of memory, which is known as its virtual address space. The virtual address space for Linux processes is shown in Figure 1.13. (Other Unix systems use a similar layout.) In Linux, the topmost region of the address space is reserved for code and data in the operating system that is common to all processes. The lower region of the address space holds the code and data defined by the user's process. Note that addresses in the figure increase from the bottom to the top.

The virtual address space seen by each process consists of a number of well-defined areas, each with a specific purpose. You will learn more about these areas later in the book, but it will be helpful to look briefly at each, starting with the lowest addresses and working our way up:

- Program code and data. Code begins at the same fixed address for all processes, followed by data locations that correspond to global C variables. The code and data areas are initialized directly from the contents of an executable object file—in our case, the hello executable. You will learn more about this part of the address space when we study linking and loading in Chapter 7.
- *Heap*. The code and data areas are followed immediately by the run-time *heap*. Unlike the code and data areas, which are fixed in size once the process begins

running, the heap expands and contracts dynamically at run time as a result of calls to C standard library routines such as malloc and free. We will study heaps in detail when we learn about managing virtual memory in Chapter 9.

- Shared libraries. Near the middle of the address space is an area that holds the code and data for *shared libraries* such as the C standard library and the math library. The notion of a shared library is a powerful but somewhat difficult concept. You will learn how they work when we study dynamic linking in Chapter 7.
- Stack. At the top of the user's virtual address space is the *user stack* that the compiler uses to implement function calls. Like the heap, the user stack expands and contracts dynamically during the execution of the program. In particular, each time we call a function, the stack grows. Each time we return from a function, it contracts. You will learn how the compiler uses the stack in Chapter 3.
- *Kernel virtual memory*. The top region of the address space is reserved for the kernel. Application programs are not allowed to read or write the contents of this area or to directly call functions defined in the kernel code. Instead, they must invoke the kernel to perform these operations.

For virtual memory to work, a sophisticated interaction is required between the hardware and the operating system software, including a hardware translation of every address generated by the processor. The basic idea is to store the contents of a process's virtual memory on disk and then use the main memory as a cache for the disk. Chapter 9 explains how this works and why it is so important to the operation of modern systems.

#### 1.7.4 Files

A *file* is a sequence of bytes, nothing more and nothing less. Every I/O device, including disks, keyboards, displays, and even networks, is modeled as a file. All input and output in the system is performed by reading and writing files, using a small set of system calls known as *Unix I/O*.

This simple and elegant notion of a file is nonetheless very powerful because it provides applications with a uniform view of all the varied I/O devices that might be contained in the system. For example, application programmers who manipulate the contents of a disk file are blissfully unaware of the specific disk technology. Further, the same program will run on different systems that use different disk technologies. You will learn about Unix I/O in Chapter 10.

# **1.8** Systems Communicate with Other Systems Using Networks

Up to this point in our tour of systems, we have treated a system as an isolated collection of hardware and software. In practice, modern systems are often linked to other systems by networks. From the point of view of an individual system, the

# **Aside** The Linux project

In August 1991, a Finnish graduate student named Linus Torvalds modestly announced a new Unix-like operating system kernel:

From: torvalds@klaava.Helsinki.FI (Linus Benedict Torvalds)

Newsgroups: comp.os.minix

Subject: What would you like to see most in minix? Summary: small poll for my new operating system

Date: 25 Aug 91 20:57:08 GMT

Hello everybody out there using minix -

I'm doing a (free) operating system (just a hobby, won't be big and professional like gnu) for 386(486) AT clones. This has been brewing since April, and is starting to get ready. I'd like any feedback on things people like/dislike in minix, as my OS resembles it somewhat (same physical layout of the file-system (due to practical reasons) among other things).

I've currently ported bash(1.08) and gcc(1.40), and things seem to work. This implies that I'll get something practical within a few months, and I'd like to know what features most people would want. Any suggestions are welcome, but I won't promise I'll implement them :-)

Linus (torvalds@kruuna.helsinki.fi)

As Torvalds indicates, his starting point for creating Linux was Minix, an operating system developed by Andrew S. Tanenbaum for educational purposes [113].

The rest, as they say, is history. Linux has evolved into a technical and cultural phenomenon. By combining forces with the GNU project, the Linux project has developed a complete, Posix-compliant version of the Unix operating system, including the kernel and all of the supporting infrastructure. Linux is available on a wide array of computers, from handheld devices to mainframe computers. A group at IBM has even ported Linux to a wristwatch!

network can be viewed as just another I/O device, as shown in Figure 1.14. When the system copies a sequence of bytes from main memory to the network adapter, the data flow across the network to another machine, instead of, say, to a local disk drive. Similarly, the system can read data sent from other machines and copy these data to its main memory.

With the advent of global networks such as the Internet, copying information from one machine to another has become one of the most important uses of computer systems. For example, applications such as email, instant messaging, the World Wide Web, FTP, and telnet are all based on the ability to copy information over a network.

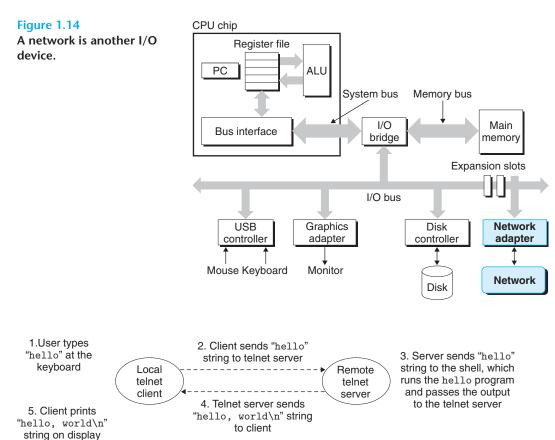


Figure 1.15 Using telnet to run hello remotely over a network.

Returning to our hello example, we could use the familiar telnet application to run hello on a remote machine. Suppose we use a telnet *client* running on our local machine to connect to a telnet *server* on a remote machine. After we log in to the remote machine and run a shell, the remote shell is waiting to receive an input command. From this point, running the hello program remotely involves the five basic steps shown in Figure 1.15.

After we type in the hello string to the telnet client and hit the enter key, the client sends the string to the telnet server. After the telnet server receives the string from the network, it passes it along to the remote shell program. Next, the remote shell runs the hello program and passes the output line back to the telnet server. Finally, the telnet server forwards the output string across the network to the telnet client, which prints the output string on our local terminal.

This type of exchange between clients and servers is typical of all network applications. In Chapter 11 you will learn how to build network applications and apply this knowledge to build a simple Web server.

# 1.9 Important Themes

This concludes our initial whirlwind tour of systems. An important idea to take away from this discussion is that a system is more than just hardware. It is a collection of intertwined hardware and systems software that must cooperate in order to achieve the ultimate goal of running application programs. The rest of this book will fill in some details about the hardware and the software, and it will show how, by knowing these details, you can write programs that are faster, more reliable, and more secure.

To close out this chapter, we highlight several important concepts that cut across all aspects of computer systems. We will discuss the importance of these concepts at multiple places within the book.

#### 1.9.1 Amdahl's Law

Gene Amdahl, one of the early pioneers in computing, made a simple but insightful observation about the effectiveness of improving the performance of one part of a system. This observation has come to be known as Amdahl's law. The main idea is that when we speed up one part of a system, the effect on the overall system performance depends on both how significant this part was and how much it sped up. Consider a system in which executing some application requires time  $T_{\rm old}$ . Suppose some part of the system requires a fraction  $\alpha$  of this time, and that we improve its performance by a factor of k. That is, the component originally required time  $\alpha T_{\rm old}$ , and it now requires time  $(\alpha T_{\rm old})/k$ . The overall execution time would thus be

$$T_{\text{new}} = (1 - \alpha)T_{\text{old}} + (\alpha T_{\text{old}})/k$$
$$= T_{\text{old}}[(1 - \alpha) + \alpha/k]$$

From this, we can compute the speedup  $S = T_{\text{old}}/T_{\text{new}}$  as

$$S = \frac{1}{(1 - \alpha) + \alpha/k} \tag{1.1}$$

As an example, consider the case where a part of the system that initially consumed 60% of the time ( $\alpha=0.6$ ) is sped up by a factor of 3 (k=3). Then we get a speedup of  $1/[0.4+0.6/3]=1.67\times$ . Even though we made a substantial improvement to a major part of the system, our net speedup was significantly less than the speedup for the one part. This is the major insight of Amdahl's law—to significantly speed up the entire system, we must improve the speed of a very large fraction of the overall system.

### Practice Problem 1.1 (solution page 64)

Suppose you work as a truck driver, and you have been hired to carry a load of potatoes from Boise, Idaho, to Minneapolis, Minnesota, a total distance of 2,500 kilometers. You estimate you can average 100 km/hr driving within the speed limits, requiring a total of 25 hours for the trip.

### **Aside** Expressing relative performance

The best way to express a performance improvement is as a ratio of the form  $T_{\rm old}/T_{\rm new}$ , where  $T_{\rm old}$  is the time required for the original version and  $T_{\rm new}$  is the time required by the modified version. This will be a number greater than 1.0 if any real improvement occurred. We use the suffix 'x' to indicate such a ratio, where the factor "2.2×" is expressed verbally as "2.2 times."

The more traditional way of expressing relative change as a percentage works well when the change is small, but its definition is ambiguous. Should it be  $100 \cdot (T_{\rm old} - T_{\rm new})/T_{\rm new}$ , or possibly  $100 \cdot (T_{\rm old} - T_{\rm new})/T_{\rm old}$ , or something else? In addition, it is less instructive for large changes. Saying that "performance improved by 120%" is more difficult to comprehend than simply saying that the performance improved by  $2.2 \times$ .

- A. You hear on the news that Montana has just abolished its speed limit, which constitutes 1,500 km of the trip. Your truck can travel at 150 km/hr. What will be your speedup for the trip?
- B. You can buy a new turbocharger for your truck at www.fasttrucks.com. They stock a variety of models, but the faster you want to go, the more it will cost. How fast must you travel through Montana to get an overall speedup for your trip of 1.67×?

# Practice Problem 1.2 (solution page 64)

A car manufacturing company has promised their customers that the next release of a new engine will show a  $4\times$  performance improvement. You have been assigned the task of delivering on that promise. You have determined that only 90% of the engine can be improved. How much (i.e., what value of k) would you need to improve this part to meet the overall performance target of the engine?

One interesting special case of Amdahl's law is to consider the effect of setting k to  $\infty$ . That is, we are able to take some part of the system and speed it up to the point at which it takes a negligible amount of time. We then get

$$S_{\infty} = \frac{1}{(1 - \alpha)} \tag{1.2}$$

So, for example, if we can speed up 60% of the system to the point where it requires close to no time, our net speedup will still only be  $1/0.4 = 2.5 \times$ .

Amdahl's law describes a general principle for improving any process. In addition to its application to speeding up computer systems, it can guide a company trying to reduce the cost of manufacturing razor blades, or a student trying to improve his or her grade point average. Perhaps it is most meaningful in the world

of computers, where we routinely improve performance by factors of 2 or more. Such high factors can only be achieved by optimizing large parts of a system.

## 1.9.2 Concurrency and Parallelism

Throughout the history of digital computers, two demands have been constant forces in driving improvements: we want them to do more, and we want them to run faster. Both of these factors improve when the processor does more things at once. We use the term *concurrency* to refer to the general concept of a system with multiple, simultaneous activities, and the term *parallelism* to refer to the use of concurrency to make a system run faster. Parallelism can be exploited at multiple levels of abstraction in a computer system. We highlight three levels here, working from the highest to the lowest level in the system hierarchy.

### **Thread-Level Concurrency**

Building on the process abstraction, we are able to devise systems where multiple programs execute at the same time, leading to *concurrency*. With threads, we can even have multiple control flows executing within a single process. Support for concurrent execution has been found in computer systems since the advent of time-sharing in the early 1960s. Traditionally, this concurrent execution was only *simulated*, by having a single computer rapidly switch among its executing processes, much as a juggler keeps multiple balls flying through the air. This form of concurrency allows multiple users to interact with a system at the same time, such as when many people want to get pages from a single Web server. It also allows a single user to engage in multiple tasks concurrently, such as having a Web browser in one window, a word processor in another, and streaming music playing at the same time. Until recently, most actual computing was done by a single processor, even if that processor had to switch among multiple tasks. This configuration is known as a *uniprocessor system*.

When we construct a system consisting of multiple processors all under the control of a single operating system kernel, we have a *multiprocessor system*. Such systems have been available for large-scale computing since the 1980s, but they have more recently become commonplace with the advent of *multi-core* processors and *hyperthreading*. Figure 1.16 shows a taxonomy of these different processor types.

Multi-core processors have several CPUs (referred to as "cores") integrated onto a single integrated-circuit chip. Figure 1.17 illustrates the organization of a

Figure 1.16
Categorizing different processor configurations.
Multiprocessors are becoming prevalent with the advent of multicore processors and hyperthreading.

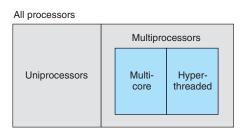
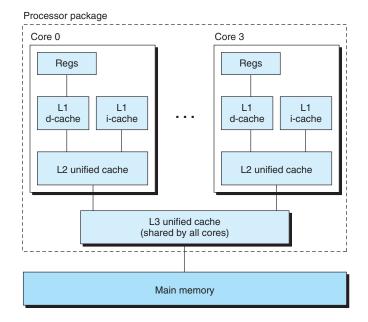


Figure 1.17
Multi-core processor
organization. Four
processor cores are
integrated onto a single
chip.



typical multi-core processor, where the chip has four CPU cores, each with its own L1 and L2 caches, and with each L1 cache split into two parts—one to hold recently fetched instructions and one to hold data. The cores share higher levels of cache as well as the interface to main memory. Industry experts predict that they will be able to have dozens, and ultimately hundreds, of cores on a single chip.

Hyperthreading, sometimes called *simultaneous multi-threading*, is a technique that allows a single CPU to execute multiple flows of control. It involves having multiple copies of some of the CPU hardware, such as program counters and register files, while having only single copies of other parts of the hardware, such as the units that perform floating-point arithmetic. Whereas a conventional processor requires around 20,000 clock cycles to shift between different threads, a hyperthreaded processor decides which of its threads to execute on a cycle-by-cycle basis. It enables the CPU to take better advantage of its processing resources. For example, if one thread must wait for some data to be loaded into a cache, the CPU can proceed with the execution of a different thread. As an example, the Intel Core i7 processor can have each core executing two threads, and so a four-core system can actually execute eight threads in parallel.

The use of multiprocessing can improve system performance in two ways. First, it reduces the need to simulate concurrency when performing multiple tasks. As mentioned, even a personal computer being used by a single person is expected to perform many activities concurrently. Second, it can run a single application program faster, but only if that program is expressed in terms of multiple threads that can effectively execute in parallel. Thus, although the principles of concurrency have been formulated and studied for over 50 years, the advent of multi-core and hyperthreaded systems has greatly increased the desire to find ways to write application programs that can exploit the thread-level parallelism available with

the hardware. Chapter 12 will look much more deeply into concurrency and its use to provide a sharing of processing resources and to enable more parallelism in program execution.

#### Instruction-Level Parallelism

At a much lower level of abstraction, modern processors can execute multiple instructions at one time, a property known as *instruction-level parallelism*. For example, early microprocessors, such as the 1978-vintage Intel 8086, required multiple (typically 3–10) clock cycles to execute a single instruction. More recent processors can sustain execution rates of 2–4 instructions per clock cycle. Any given instruction requires much longer from start to finish, perhaps 20 cycles or more, but the processor uses a number of clever tricks to process as many as 100 instructions at a time. In Chapter 4, we will explore the use of *pipelining*, where the actions required to execute an instruction are partitioned into different steps and the processor hardware is organized as a series of stages, each performing one of these steps. The stages can operate in parallel, working on different parts of different instructions. We will see that a fairly simple hardware design can sustain an execution rate close to 1 instruction per clock cycle.

Processors that can sustain execution rates faster than 1 instruction per cycle are known as *superscalar* processors. Most modern processors support superscalar operation. In Chapter 5, we will describe a high-level model of such processors. We will see that application programmers can use this model to understand the performance of their programs. They can then write programs such that the generated code achieves higher degrees of instruction-level parallelism and therefore runs faster.

# Single-Instruction, Multiple-Data (SIMD) Parallelism

At the lowest level, many modern processors have special hardware that allows a single instruction to cause multiple operations to be performed in parallel, a mode known as *single-instruction*, *multiple-data* (SIMD) parallelism. For example, recent generations of Intel and AMD processors have instructions that can add 8 pairs of single-precision floating-point numbers (C data type float) in parallel.

These SIMD instructions are provided mostly to speed up applications that process image, sound, and video data. Although some compilers attempt to automatically extract SIMD parallelism from C programs, a more reliable method is to write programs using special *vector* data types supported in compilers such as GCC. We describe this style of programming in Web Aside OPT:SIMD, as a supplement to the more general presentation on program optimization found in Chapter 5.

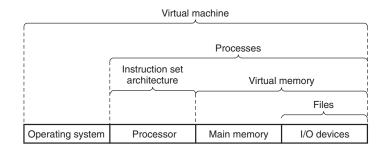
#### 1.9.3 The Importance of Abstractions in Computer Systems

The use of *abstractions* is one of the most important concepts in computer science. For example, one aspect of good programming practice is to formulate a simple application program interface (API) for a set of functions that allow programmers to use the code without having to delve into its inner workings. Different program-

Some abstractions provided by a computer system. A major theme

Figure 1.18

system. A major theme in computer systems is to provide abstract representations at different levels to hide the complexity of the actual implementations.



ming languages provide different forms and levels of support for abstraction, such as Java class declarations and C function prototypes.

We have already been introduced to several of the abstractions seen in computer systems, as indicated in Figure 1.18. On the processor side, the *instruction set architecture* provides an abstraction of the actual processor hardware. With this abstraction, a machine-code program behaves as if it were executed on a processor that performs just one instruction at a time. The underlying hardware is far more elaborate, executing multiple instructions in parallel, but always in a way that is consistent with the simple, sequential model. By keeping the same execution model, different processor implementations can execute the same machine code while offering a range of cost and performance.

On the operating system side, we have introduced three abstractions: *files* as an abstraction of I/O devices, *virtual memory* as an abstraction of program memory, and *processes* as an abstraction of a running program. To these abstractions we add a new one: the *virtual machine*, providing an abstraction of the entire computer, including the operating system, the processor, and the programs. The idea of a virtual machine was introduced by IBM in the 1960s, but it has become more prominent recently as a way to manage computers that must be able to run programs designed for multiple operating systems (such as Microsoft Windows, Mac OS X, and Linux) or different versions of the same operating system.

We will return to these abstractions in subsequent sections of the book.

# 1.10 Summary

A computer system consists of hardware and systems software that cooperate to run application programs. Information inside the computer is represented as groups of bits that are interpreted in different ways, depending on the context. Programs are translated by other programs into different forms, beginning as ASCII text and then translated by compilers and linkers into binary executable files.

Processors read and interpret binary instructions that are stored in main memory. Since computers spend most of their time copying data between memory, I/O devices, and the CPU registers, the storage devices in a system are arranged in a hierarchy, with the CPU registers at the top, followed by multiple levels of hardware cache memories, DRAM main memory, and disk storage. Storage devices that are higher in the hierarchy are faster and more costly per bit than those lower in the

hierarchy. Storage devices that are higher in the hierarchy serve as caches for devices that are lower in the hierarchy. Programmers can optimize the performance of their C programs by understanding and exploiting the memory hierarchy.

The operating system kernel serves as an intermediary between the application and the hardware. It provides three fundamental abstractions: (1) Files are abstractions for I/O devices. (2) Virtual memory is an abstraction for both main memory and disks. (3) Processes are abstractions for the processor, main memory, and I/O devices.

Finally, networks provide ways for computer systems to communicate with one another. From the viewpoint of a particular system, the network is just another I/O device.

# **Bibliographic Notes**

Ritchie has written interesting firsthand accounts of the early days of C and Unix [91, 92]. Ritchie and Thompson presented the first published account of Unix [93]. Silberschatz, Galvin, and Gagne [102] provide a comprehensive history of the different flavors of Unix. The GNU (www.gnu.org) and Linux (www.linux.org) Web pages have loads of current and historical information. The Posix standards are available online at (www.unix.org).

#### **Solutions to Practice Problems**

### Solution to Problem 1.1 (page 58)

This problem illustrates that Amdahl's law applies to more than just computer systems.

- A. In terms of Equation 1.1, we have  $\alpha = 0.6$  and k = 1.5. More directly, traveling the 1,500 kilometers through Montana will require 10 hours, and the rest of the trip also requires 10 hours. This will give a speedup of  $25/(10+10) = 1.25 \times$ .
- B. In terms of Equation 1.1, we have  $\alpha = 0.6$ , and we require S = 1.67, from which we can solve for k. More directly, to speed up the trip by  $1.67 \times$ , we must decrease the overall time to 15 hours. The parts outside of Montana will still require 10 hours, so we must drive through Montana in 5 hours. This requires traveling at 300 km/hr, which is pretty fast for a truck!

#### Solution to Problem 1.2 (page 59)

Amdahl's law is best understood by working through some examples. This one requires you to look at Equation 1.1 from an unusual perspective. This problem is a simple application of the equation. You are given S = 4 and  $\alpha = 0.9$ , and you must then solve for k:

$$4 = 1/(1 - 0.9) + 0.9/k$$
$$0.4 + 3.6/k = 1.0$$
$$k = 6.0$$