conundrum /kəˈnʌndrəm/ noun

a confusing problem or question that is very difficult to solve

***The Age: End of a colourful innings*:**

**When named as one of *Wisden*cricketers of the year in 1975, Greig dwelt momentarily on the conundrum of his divided loyalty. ''Just say I feel I have two countries, and regard myself as lucky,'' he said, ''and leave it at that.''**