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Program Structures & Algorithms
Fall2021
Assignment No.5

Task

Please see the presentation on *Assignment on Parallel Sorting* under the *Exams. etc.* module.

Your task is to implement a parallel sorting algorithm such that each partition of the array is sorted in parallel. You will consider two different schemes for deciding whether to sort in parallel.

1. A cutoff (defaults to, say, 1000) which you will update according to the first argument in the command line when running. It's your job to experiment and come up with a good value for this cutoff. If there are fewer elements to sort than the cutoff, then you should use the system sort instead.
2. Recursion depth or the number of available threads. Using this determination, you might decide on an ideal number (t) of separate threads (stick to powers of 2) and arrange for that number of partitions to be parallelized (by preventing recursion after the depth of $\lg t$ is reached).
3. An appropriate combination of these.

There is a *Main* class and the *ParSort* class in the *sort.par* package of the INFO6205 repository. The *Main* class can be used as is but the *ParSort* class needs to be implemented where you see "TODO..." [it turns out that these TODOs are already implemented].

Unless you have a good reason not to, you should just go along with the Java8-style future implementations provided for you in the class repository.

You must prepare a report that shows the results of your experiments and draws a conclusion (or more) about the efficacy of this method of parallelizing sort. Your experiments should

involve sorting arrays of sufficient size for the parallel sort to make a difference. You should run with many different array sizes (they must be sufficiently large to make parallel sorting worthwhile, obviously) and different cutoff schemes.

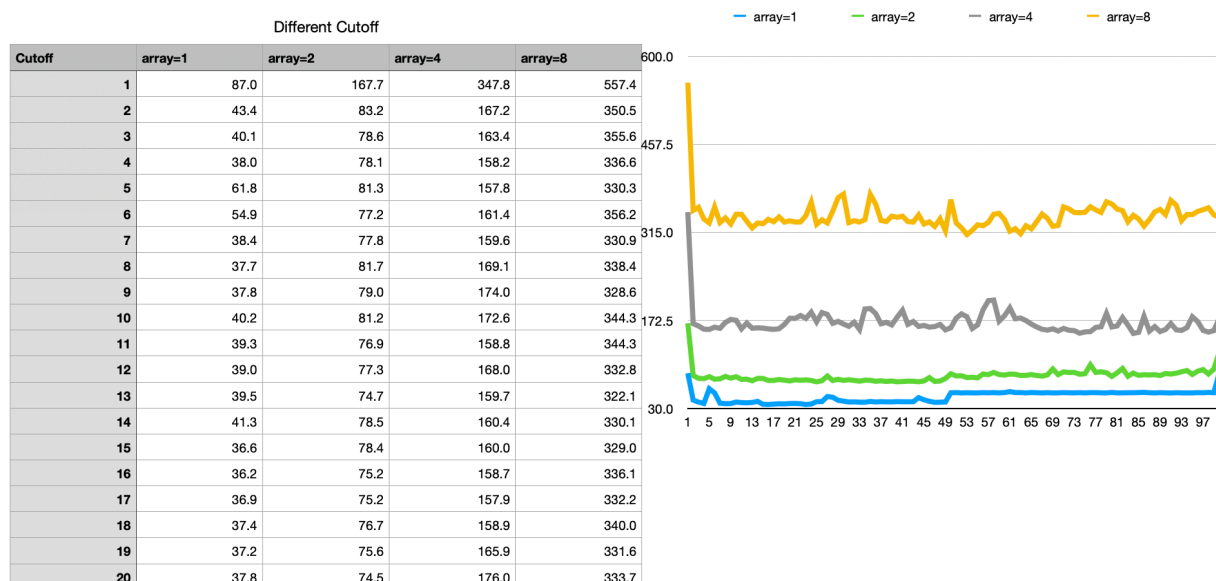
For varying the number of threads available, you might want to consult the following resources:

- <https://www.callicoder.com/java-8-completablefuture-tutorial/#a-note-about-executor-and-thread-pool> (Links to an external site.)
- <https://stackoverflow.com/questions/36569775/how-to-set-forkjoinpool-with-the-desired-number-of-worker-threads-in-completable> (Links to an external site.)

Good luck and enjoy.

Experiments

1. A cutoff



(Figure 1.different cutoff value with different array length)

Figure 1 is the experimental data of cutoff. The base of cutoff is 10,000. From the statistical data chart, we can see that as the cuffoff increases to about 40,000, the time spent to sort arrays of different lengths decreases significantly, but then with the cutoff. Increasing, the time consumed for sorting random arrays of the same length has not changed significantly, and it is basically a horizontal line. Therefore, when the number of threads is fixed, the recommended cutoff value is 40,000.

2. available threads

Table 1

| Threadnum | array=1 | array=2 | array=4 | array=8 |
|-----------|---------|---------|---------|---------|
| 1 | 32 | 36 | 98 | 236 |
| 2 | 57 | 39 | 54 | 104 |
| 4 | 52 | 78 | 54 | 116 |
| 8 | 72 | 89 | 61 | 112 |
| 16 | 75 | 106 | 56 | 111 |
| 32 | 98 | 36 | 33 | 107 |
| 64 | 79 | 23 | 38 | 84 |
| 128 | 74 | 34 | 41 | 85 |
| 256 | 83 | 23 | 50 | 92 |
| 512 | 91 | 21 | 46 | 87 |

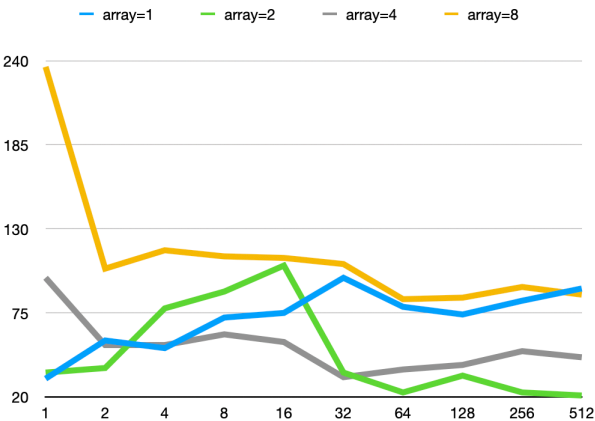
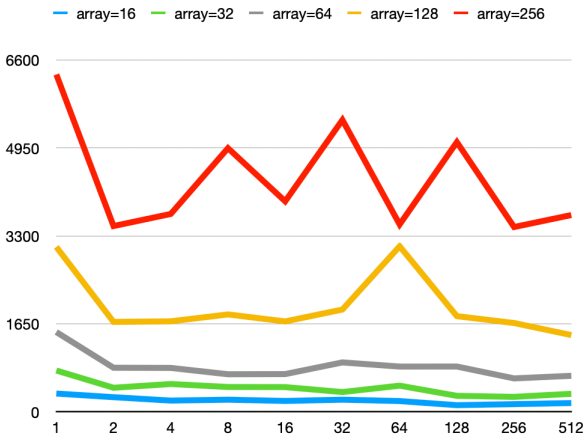


Table 1-1

| Threadnum | array=16 | array=32 | array=64 | array=128 | array=256 |
|-----------|----------|----------|----------|-----------|-----------|
| 1 | 344 | 776 | 1498 | 3094 | 6329 |
| 2 | 276 | 453 | 828 | 1688 | 3486 |
| 4 | 212 | 523 | 825 | 1699 | 3713 |
| 8 | 229 | 467 | 706 | 1828 | 4947 |
| 16 | 205 | 465 | 709 | 1697 | 3950 |
| 32 | 229 | 372 | 928 | 1920 | 5476 |
| 64 | 203 | 492 | 850 | 3106 | 3516 |
| 128 | 126 | 301 | 851 | 1796 | 5060 |
| 256 | 145 | 282 | 628 | 1667 | 3468 |
| 512 | 166 | 339 | 677 | 1441 | 3692 |



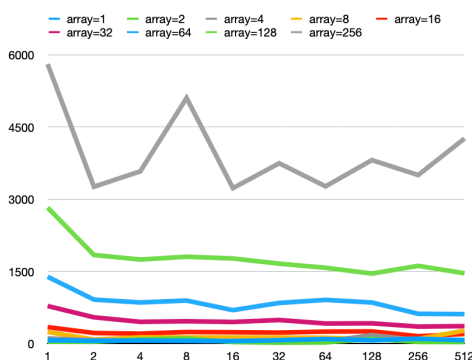
(Figure 2.different thread numbers value with different array length)

Figure 2 shows the fixed cutoff value, cutoff=40000, and the base of the array length is 250,000. The table data is the sorting time required for different numbers of threads to sort arrays of the same length. It can be seen that when the length of the array is large, as the number of threads increases, the required time decreases sharply, but when the number of threads exceeds a certain value, Performance declines, and the time required for sorting may increase. I guess the reason is that in addition to multi-threading will increase the creation overhead, there is also the overhead of switching context. The optimal value of the number of threads is not easy to determine. When the array length is small (length<250,000), the advantage of multithreading is not obvious. When the array length is large (length>=2,000,000), the number of threads is 4, 8, 16 may be the best choice.

3.An appropriate combination

cutoff=10,000

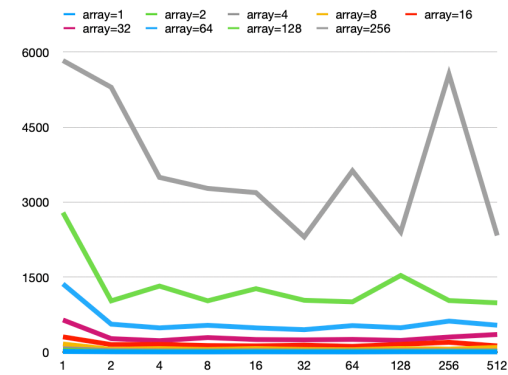
| Threadnum | array=1 | array=2 | array=4 | array=8 | array=16 | array=32 | array=64 | array=128 | array=256 |
|-----------|---------|---------|---------|---------|----------|----------|----------|-----------|-----------|
| 1 | 70 | 39 | 108 | 243 | 343 | 782 | 1390 | 2827 | 5810 |
| 2 | 59 | 37 | 68 | 85 | 221 | 547 | 915 | 1843 | 3262 |
| 4 | 64 | 89 | 73 | 130 | 207 | 453 | 856 | 1748 | 3581 |
| 8 | 58 | 108 | 68 | 129 | 242 | 465 | 895 | 1806 | 5106 |
| 16 | 54 | 33 | 42 | 128 | 237 | 450 | 696 | 1770 | 3232 |
| 32 | 72 | 20 | 56 | 125 | 229 | 491 | 846 | 1662 | 3749 |
| 64 | 96 | 26 | 46 | 122 | 250 | 418 | 909 | 1577 | 3269 |
| 128 | 69 | 98 | 176 | 93 | 255 | 422 | 855 | 1456 | 3815 |
| 256 | 102 | 35 | 71 | 96 | 154 | 354 | 620 | 1617 | 3504 |
| 512 | 72 | 33 | 57 | 271 | 201 | 364 | 613 | 1463 | 4263 |



(Figure 3.cutoff=10,000 and different thread numbers value with different array length)

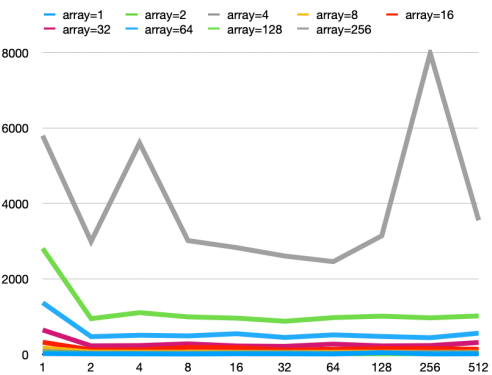
cutoff=20,000

| Threadnum | array=1 | array=2 | array=4 | array=8 | array=16 | array=32 | array=64 | array=128 | array=256 |
|-----------|---------|---------|---------|---------|----------|----------|----------|-----------|-----------|
| 1 | 15 | 36 | 70 | 165 | 307 | 645 | 1365 | 2790 | 5828 |
| 2 | 9 | 15 | 32 | 59 | 153 | 272 | 561 | 1027 | 5294 |
| 4 | 7 | 13 | 27 | 73 | 158 | 231 | 487 | 1322 | 3494 |
| 8 | 6 | 13 | 26 | 54 | 134 | 293 | 538 | 1028 | 3273 |
| 16 | 8 | 14 | 30 | 73 | 127 | 254 | 487 | 1270 | 3189 |
| 32 | 7 | 13 | 25 | 55 | 141 | 247 | 451 | 1038 | 2304 |
| 64 | 6 | 13 | 27 | 50 | 118 | 257 | 532 | 1007 | 3625 |
| 128 | 9 | 14 | 30 | 76 | 159 | 236 | 489 | 1534 | 2403 |
| 256 | 8 | 15 | 29 | 62 | 199 | 304 | 622 | 1033 | 5554 |
| 512 | 7 | 13 | 28 | 96 | 127 | 355 | 540 | 987 | 2333 |



cutoff=40,000

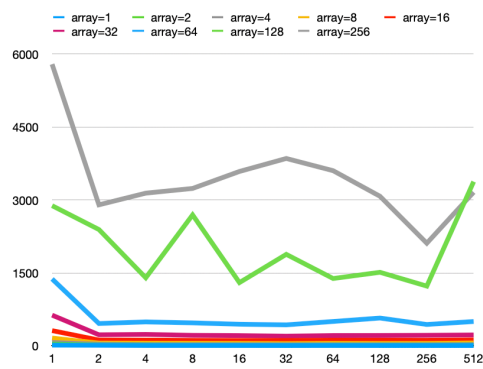
| Threadnum | array=1 | array=2 | array=4 | array=8 | array=16 | array=32 | array=64 | array=128 | array=256 |
|-----------|---------|---------|---------|---------|----------|----------|----------|-----------|-----------|
| 1 | 16 | 38 | 72 | 164 | 318 | 644 | 1366 | 2805 | 5797 |
| 2 | 9 | 15 | 28 | 55 | 114 | 222 | 466 | 943 | 2991 |
| 4 | 8 | 14 | 26 | 53 | 117 | 230 | 503 | 1103 | 5604 |
| 8 | 5 | 12 | 25 | 50 | 180 | 275 | 486 | 990 | 3013 |
| 16 | 11 | 22 | 33 | 49 | 174 | 219 | 543 | 957 | 2828 |
| 32 | 10 | 20 | 39 | 47 | 111 | 209 | 444 | 875 | 2604 |
| 64 | 6 | 13 | 25 | 50 | 129 | 268 | 513 | 971 | 2456 |
| 128 | 43 | 13 | 26 | 53 | 152 | 220 | 471 | 1009 | 3141 |
| 256 | 6 | 13 | 43 | 50 | 149 | 230 | 438 | 965 | 7986 |
| 512 | 11 | 20 | 41 | 52 | 130 | 311 | 557 | 1015 | 3553 |



(Figure 5.cutoff=40,000 and different thread numbers value with different array length)

cutoff=80,000

| Threadnum | array=1 | array=2 | array=4 | array=8 | array=16 | array=32 | array=64 | array=128 | array=256 |
|-----------|---------|---------|---------|---------|----------|----------|----------|-----------|-----------|
| 1 | 15 | 36 | 68 | 160 | 313 | 631 | 1375 | 2882 | 5790 |
| 2 | 11 | 18 | 33 | 56 | 119 | 227 | 459 | 2391 | 2899 |
| 4 | 7 | 15 | 27 | 54 | 117 | 235 | 492 | 1399 | 3139 |
| 8 | 7 | 12 | 25 | 53 | 112 | 216 | 472 | 2692 | 3236 |
| 16 | 7 | 11 | 24 | 51 | 110 | 211 | 444 | 1300 | 3585 |
| 32 | 6 | 10 | 23 | 46 | 112 | 199 | 431 | 1881 | 3852 |
| 64 | 7 | 12 | 24 | 52 | 115 | 212 | 501 | 1384 | 3601 |
| 128 | 6 | 12 | 24 | 49 | 115 | 213 | 571 | 1512 | 3075 |
| 256 | 6 | 12 | 24 | 50 | 114 | 217 | 439 | 1228 | 2110 |
| 512 | 6 | 13 | 28 | 59 | 122 | 224 | 500 | 3376 | 3158 |



(Figure 6.cutoff=80,000 and different thread numbers value with different array length)

From Figure 3, Figure 4, Figure 5, Figure 6, we observe the experimental data of different cutoffs and thread numbers, we can find that when the array length is small (length<2,000,000), cutoff=4000, ThreadNumber=8, which is the optimal combination , When the length of the array is large (length>=2,000,000), cutoff=4000, ThreadNumber=16, it is the optimal combination.