

Gauss' law

1

(a) $E = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2}$ $Q = +92e$ (92 protons)

(b) use the above

(c) No charge enclosed.

2

(a) $\vec{E} \cdot \hat{n}_2$ (parallel) $\vec{E} \cdot \hat{n}_1$ (anti-parallel)

(b) $\vec{E} \cdot \hat{n}_1 = E n_1 \cos \theta$

3

$$\phi_E = \oint \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0}$$

4

→ use Gauss law

5

6

Flux, $\phi = \vec{E} \cdot \vec{A}$

$$|A| = (0.22)(0.28) \text{ m}^2$$

$$= EA \cos \theta$$

$$|E| = 28 \times 10^3 \text{ N/C}$$

$$\underline{\theta = 0^\circ}, \quad \underline{\theta = 30^\circ}, \quad \underline{\theta = 90^\circ}$$

7

$$\underline{|A| = 4 \text{ m}^2}$$

$$\phi = EA$$

8

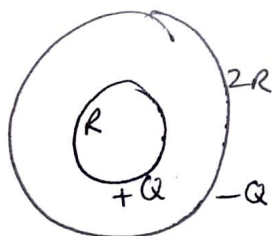
9

please ~~try~~ try yourself.

10

$$E = \frac{2\sigma}{\epsilon_0}$$

11

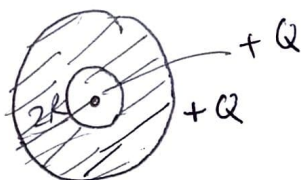


(i) $\phi_E = \oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enclosed}}}{\epsilon_0}$

$$\phi_E = \frac{+Q}{\epsilon_0} [R < r < 2R]$$

(ii) $\phi_E = 0 \quad [r < R]$

12



Since conducting, all the charges are at the outer surface, thus, $+Q + Q \rightarrow 2Q$

13

$$Q(r) = \int_0^r \rho dv = \frac{4}{3} \pi r^3 \rho$$

Ratio, $\frac{Q(r)}{Q} = \left(\frac{r}{R}\right)^3$ total charge, $Q = \left[\frac{4}{3} \pi R^3\right] \rho$

for, $r = \frac{R}{2}$ charge ratio $\approx \frac{1}{8}$

14

$\rho(r) = ar$

thus, $Q(r) = \int_0^R \rho(r) dv$
 $= \int_0^R ar 4\pi r^2 dr$

$Q = \frac{4}{3} \pi a R^4$

15

surface charge density, ~~$\sigma = \epsilon_0 E$~~

(a)

$$\sigma = \epsilon_0 E$$

$$E = -150 \text{ N/C}$$

$$= -1.33 \text{ nC/m}^2$$

(b)

$$R_E = 6.38 \times 10^6 \text{ m}$$

$$\text{Then total charge, } Q = 4\pi R_E^2 \sigma$$

$$= 4\pi R_E^2 (\epsilon_0 E)$$

$$= -680 \text{ KC.}$$