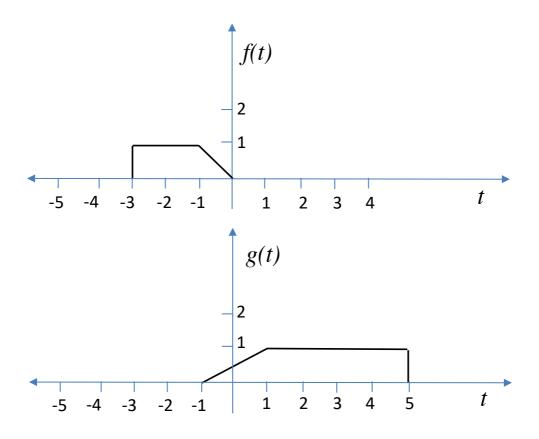
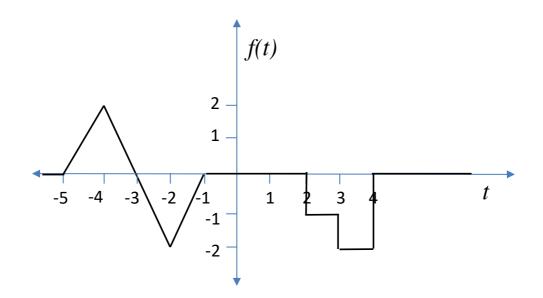
ELEC2040 Signals and systems – Practice for Test 1

Q1 Given f(t), depicted in the first figure below, find a formula for g(t) in terms of f(t), where g(t) is depicted in the second figure below. Show your working.



Q2 For the function f(t) in the following graph:



- (a) Compute the average value of the signal f(t) over the interval [-5,4].
- (b) Compute the average value of the signal f(t) over the interval [-3,3].
- (c) Compute the energy in the signal f(t) over the interval [-5,4].
- (d) Compute the average power of the signal f(t) over the time interval [-5,4].
- (e) Plot f(2t+1)

Q3. Consider the linear system given by the input-output relations:

$$y(t) = 2x(t-3) + 0.5x(t-5)$$

- (a) Write down the impulse response h(t) and draw it
- (b) Write down the output of the system, y(t), when the input signal is $x(t) = \delta(t \tau)$ and draw y(t).
- (c) Is the system time invariant? Explain.

Q4 Evaluate the following integrals:

a)
$$\int_{-\infty}^{\infty} \sin(t) \, \delta(t - \pi / 6) \, dt$$

b)
$$\int_{0}^{\infty} u(t+2) \, \delta(t-1) \, dt$$

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c)
$$\int_{-\infty}^{\infty} (t+1) \left(\delta(t-1) + 2\delta(t-3) \right) dt$$
d)
$$\int_{-\infty}^{\infty} \exp(jt) \, \delta(t-\pi) dt$$

d)
$$\int_{0}^{\infty} \exp(jt) \, \delta(t-\pi) \, dt$$