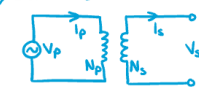


# ① TRANSFORMERS

IDEAL TRANSFORMER

$$\frac{V_p}{V_s} = \frac{N_p}{N_s} = \frac{I_s}{I_p}$$


$$P = IV = I^2 R$$

$$P = \frac{V_m I_m}{2} \cos(\theta_v - \theta_i)$$

POWER DELIVERED TO LOAD  
angle for complex  $V_s, I_s$

$$R'_2 = a^2 R_2$$

$$x'_1 = a^2 x_2$$

EQUIN. CIRCUIT

$$\eta = \frac{P_{OUT}}{P_{IN}} \times 100\%$$

EFFICIENCY

$$\text{rpm} \times \frac{\pi}{30} = \text{rads}^{-1}$$

$$\text{rads}^{-1} \times \frac{30}{\pi} = \text{rpm}$$

KEY

- equations used in the SGTA weekly submission
- other potentially useful equations

# ② DC MOTORS

emf armature

$$V = E_a + I_a R_a$$

DEVELOPED VOLTAGE IN PMDC MOTOR

$$P = \tau \omega$$

MECHANICAL POWER

$$P_d = E_b I_a$$

POWER DEVELOPED

emf rads<sup>-1</sup> rpm

$$\frac{E_a}{E_b} = \frac{\omega_a}{\omega_b} = \frac{N_a}{N_b}$$

$$P_{IN} = V_{IN} I_{IN}$$

DC MOTOR

$$P_{IN} = V_{IN} I_{IN} \cos \phi$$

SINGLE PHASE MOTOR

$$P_{IN} = \sqrt{3} V_{IN} I_{IN} \cos \phi$$

3-PHASE MOTOR

$$F = BIL$$

FORCE IN MOTOR



$$V = K_a \phi \omega + I_a R_a$$

$$K_a = \frac{PZ}{2\pi a}$$

$$\tau = K_a \phi I_a$$

$$\tau \propto \omega_m^k$$

P ⇒ poles  
Z ⇒ conductors

# ③ DC MOTOR SPEED CONTROL

$$E_a I_a = \tau \omega_m$$

DEVELOPED TORQUE

$$E_b = K_b \phi \omega$$

$$\tau = K_t I_a$$

LOAD  
armature torque const.

$$D = \frac{T_1}{T_2} \times 100\%$$

DUTY RATIO

$$\Delta V_s = K_f \omega + I_a R_a$$

$$E_b = K \omega$$

ELEC. MOTOR BACK EMF

$$\tau_m = K I_a$$

ELEC. MOTOR TORQUE

$$V = E_b + R_a I_a + L_a \frac{dI_a}{dt}$$

$$\tau_m = \tau_i + B \omega + J \frac{d\omega}{dt}$$

DIFF. EQUATIONS GOVERNING DC MOTOR

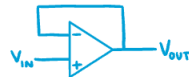
$$\dot{x} = Ax + Bu$$

$$y = Cx + Du$$

STATE-SPACE

u = input  
x = output

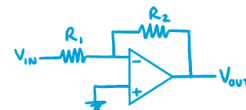
$$V_{OUT} = V_{IN}$$



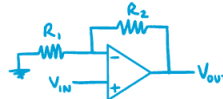
$$V_{OUT} = V_{CC} \sin(V_{IN})$$



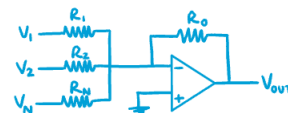
$$V_{OUT} = -\frac{R_2}{R_1} V_{IN}$$



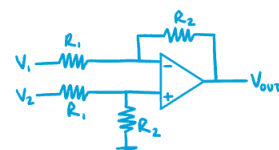
$$V_{OUT} = \left(1 + \frac{R_2}{R_1}\right) V_{IN}$$



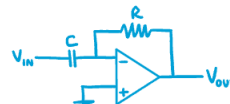
$$V_{OUT} = -\left(V_1 \frac{R_0}{R_1} + V_2 \frac{R_0}{R_2} + \dots + V_N \frac{R_0}{R_N}\right)$$



$$V_{OUT} = \frac{R_2}{R_1} (V_2 - V_1)$$



$$V_{OUT} = -\frac{R}{1/j\omega C} V_{IN}$$



$$V_{OUT} = -\frac{1}{j\omega C R} V_{IN}$$

