

$O(\log n)$

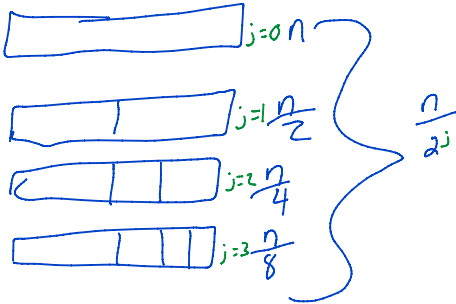
$j = \# \text{ iterations}$

$\frac{n}{2^j} = 1 \log$

$n = 2^j$

$\log n = j \log 2$

$\log n = j$



(array)

$A = [0, 0, 0, 0]$
size = $n \geq 1$

Goal \rightarrow Sum values in array

for loop

add each element \rightarrow total variable

Recursion

def total(A, n) \rightarrow inputs: array & size

if $n == 1$:

return A[n];

base case:

$A = \{1, 2, 3\}$

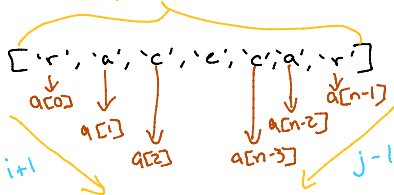
1 element

Recursion \rightarrow else

$A[n] + \text{total}(A, n-1);$

$A = \{1, 2, 3\}$

Reverse array



Swap($a[0], a[n-1]$)
Swap($a[1], a[n-2]$)
Swap($a[2], a[n-3]$)
Swap($a[i+1], a[j-1]$)

Base case

$a = [A]$ \rightarrow array has 1 element

\rightarrow first & last are the same

if base case

return array

def array_reverse(A, begin, end):

if $A[\text{begin}] == A[\text{end}]$:

return A

Recursion \rightarrow else:

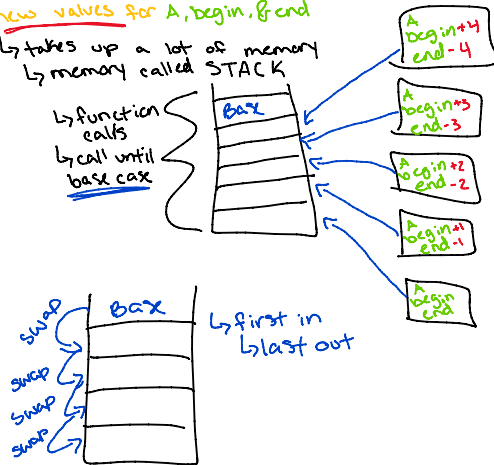
$A[\text{begin}], A[\text{end}] = A[\text{end}], A[\text{begin}]$ \rightarrow don't need return statement

Change boundaries \rightarrow array_reverse(A, begin+1, end-1)

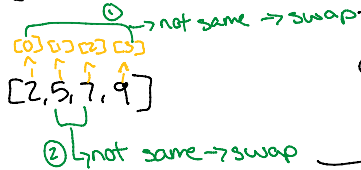
↳ everytime array-reverse is called
 ↳ opens up new scope/environment
 ↳ new values for A, begin, & end

↳ takes up a lot of memory
 ↳ memory called STACK

↳ function calls
 ↳ call until base case



Example: Reverse Order



↳ have to change condition

↳ was: $\text{if } A[\text{begin}] == A[\text{end}]$

↳ changed to:

↳ $\text{if } A[\text{begin}] > A[\text{end}]$

↳ $\text{begin} \leq \text{end}$

↳ don't need return statement

↳ don't need else

↳ swapping → don't need to return