

Coffee cup has $m = 350 \text{ g}$ at 93°C , with specific heat $4.2 \text{ J/g}\cdot^\circ\text{C}$
 Person adds 16 g sugar and does 160 J of work stirring the coffee
 Sugar starts at 20°C and has specific heat $1.2 \text{ J/g}\cdot^\circ\text{C}$
 What is final temperature of coffee?

Correct answer $T_f = \frac{W + m_c c_c T_{ci} + m_s c_s T_{si}}{m_c c_c + m_s c_s}$
 $= 92.16^\circ\text{C}$

Analytic: $\Delta E = \Delta E_{\text{thermal coffee}} + \Delta E_{\text{thermal sugar}} = W$

$$m_c c_c (T_f - T_{ci}) + m_s c_s (T_f - T_{si}) = W$$

Distributed
 $m_c c_c$ wrong
 -10%.

$$(m_c c_c T_{ci} - m_c c_c T_f) + m_s c_s T_f - m_s c_s T_{si} = W$$

$$m_c c_c T_{ci} - m_s c_s T_{si} - W = m_c c_c T_f - m_s c_s T_f = (m_c c_c - m_s c_s) T_f$$

$$T_f = \frac{m_c c_c T_{ci} - m_s c_s T_{si} - W}{m_c c_c - m_s c_s}$$

$$= \frac{(350 \cdot 4.2 \cdot 93 - 16 \cdot 1.2 \cdot 20 - 160)}{350 \cdot 4.2 - 16 \cdot 1.2} = 93.86^\circ\text{C}$$

Numeric

$$350 \cdot 4.2 (T_f - 93) + 16 \cdot 1.2 (T_f - 20) = 160$$

$$136710 - 1470 T_f + 19.2 T_f - 960 = 160$$

$$-1450.8 T_f = -135590$$

$$T_f = 93.46$$

-80%.

3 errors: distributed $m_c c_c$ wrong as above

also had a calculator error in second line (boxed)
 no units