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S3IT

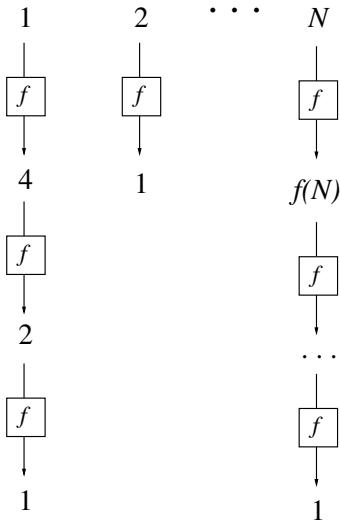
Dynamic and Unbounded Sequences of Tasks

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The $3n+1$ conjecture, a fictitious use case



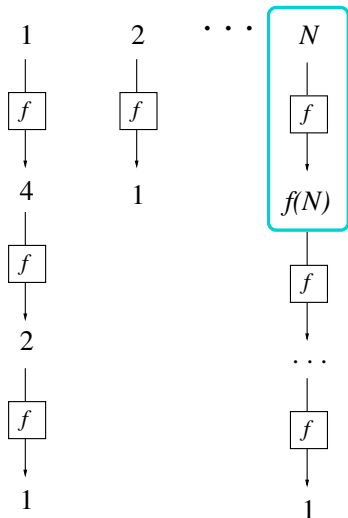
Define a function f , for n positive integer:

- ▶ if n is even, then $f(n) = n/2$,
- ▶ if n is odd, then $f(n) = 3n + 1$,

For every positive integer n , form the sequence $S(n)$: $n \rightarrow f(n) \rightarrow f(f(n)) \rightarrow f(f(f(n))) \rightarrow \dots$

Conjecture: For every positive integer n , the sequence $S(n)$ eventually hits 1.

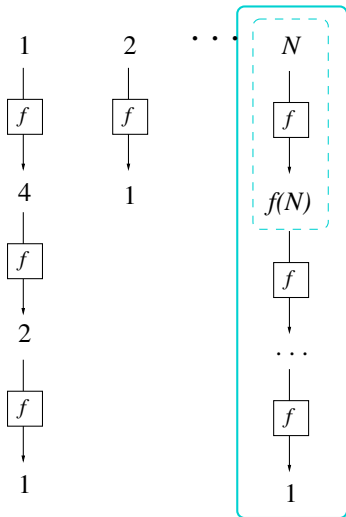
The $3n+1$ conjecture, I



A computational job $F(n, k)$, applies function f to the result of $F(n, k-1)$.

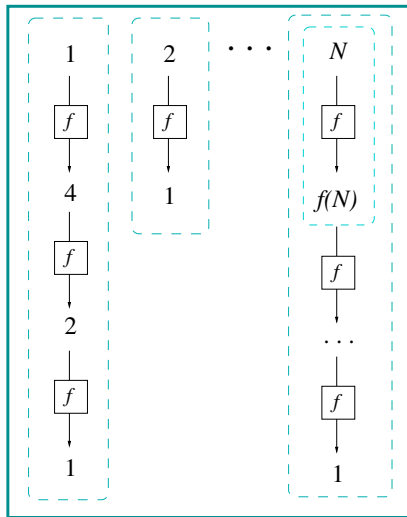
(With $F(n, 0) = n$.)

The $3n+1$ conjecture, II



A sequence $H(n)$ of jobs computes the chain $n \rightarrow f(n) \rightarrow \dots \rightarrow 1$.

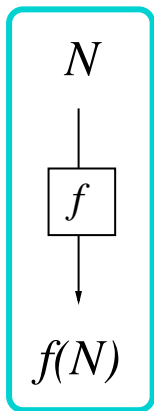
The $3n+1$ conjecture, III



Run one sequence $H(n)$
per each $n = 1, \dots, N$.

They all can run in
parallel.

The $3n+1$ conjecture, IV

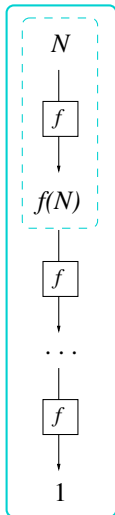


Let's define the simple application that computes f :

```
class HotpoApplication(Application):  
    def __init__(self, n):  
        Application.__init__(  
            self,  
            arguments = ([ '/usr/bin/expr' ] +  
                # run 'expr n / 2' if n even  
                [n, '/', n] if n % 2 == 0  
                # 'expr 1 + 3 * n' if n odd  
                else [1, '+', 3, '*', n]),  
            stdout = "stdout.txt",  
            # ...  
        )
```

The $3n+1$ conjecture, V

Now string together applications to compute a single sequence:



```
from gc3libs.workflow \
    import SequentialTaskCollection as Seq

class HotpoSequence(Seq):

    def __init__(self, n):
        # compute first iteration of f
        SequentialTask.__init__(self,
            [ HotpoApplication(n) ])

    def next(self, k):
        last = self.tasks[k].result
        if last == 1:
            return 'TERMINATED'
        else:
            self.tasks.append(HotpoApplication(last))
            return 'RUNNING'
```

The next () method in SequentialTaskCollection

The `next ()` method is called whenever a task in the sequence has turned to `TERMINATED` state.

```
from gc3libs.workflow \
    import SequentialTaskCollection as

class HotpoSequence(Seq):

    # ...

    def next(self, k):
        last = self.tasks[k].result
        if last == 1:
            return 'TERMINATED'
        else:
            self.tasks.append(
                HotpoApplication(last))
            return 'RUNNING'
```


The next () method in SequentialTaskCollection

The second argument to `next ()` is the index (within `self.tasks`) of the task that just finished.

```
from gc3libs.workflow \
    import SequentialTaskCollection as

class HotpoSequence(Seq):

    # ...

    def next(self, k):
        last = self.tasks[k].result
        if last == 1:
            return 'TERMINATED'
        else:
            self.tasks.append(
                HotpoApplication(last))
            return 'RUNNING'
```

The next () method in SequentialTaskCollection

You can access all
attributes of tasks
that are already done.

```
from gc3libs.workflow \
    import SequentialTaskCollection as

class HotpoSequence(Seq):

    # ...

    def next(self, k):
        last = self.tasks[k].result
        if last == 1:
            return 'TERMINATED'
        else:
            self.tasks.append(
                HotpoApplication(last))
            return 'RUNNING'
```

The next () method in SequentialTaskCollection

Returning the state
TERMINATED
interrupts the
sequence: no other
tasks from this
collection will be run.

```
from gc3libs.workflow \
    import SequentialTaskCollection as

class HotpoSequence(Seq):

    # ...

    def next(self, k):
        last = self.tasks[k].result
        if last == 1:
            return 'TERMINATED'
        else:
            self.tasks.append(
                HotpoApplication(last))
            return 'RUNNING'
```

The next () method in SequentialTaskCollection

```
from gc3libs.workflow \
    import SequentialTaskCollection as

class HotpoSequence(Seq):
```

```
# ...
```

It is entirely possible
to modify the
SequentialTaskCollection
and add (or remove)
tasks.

```
def next(self, k):
    last = self.tasks[k].result
    if last == 1:
        return 'TERMINATED'
    else:
        self.tasks.append(
            HotpoApplication(last))
    return 'RUNNING'
```

The next () method in SequentialTaskCollection

Returning state
RUNNING makes the
sequence continue
with task $k+1$

```
from gc3libs.workflow \
    import SequentialTaskCollection as

class HotpoSequence(Seq):

    # ...

    def next(self, k):
        last = self.tasks[k].result
        if last == 1:
            return 'TERMINATED'
        else:
            self.tasks.append(
                HotpoApplication(last))
            return 'RUNNING'
```

The next () method in SequentialTaskCollection

Alternatively, you can **return** a number j less than k , meaning that the sequence will rewind to the j -th task and continue running from there.

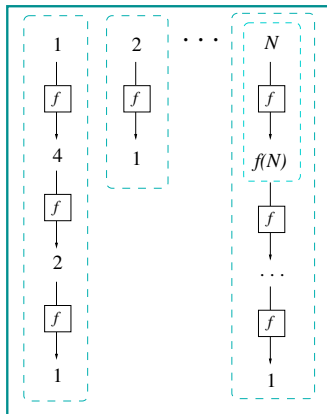
```
from gc3libs.workflow \
    import SequentialTaskCollection as

class HotpoSequence(Seq):

    # ...

    def next(self, k):
        last = self.tasks[k].result
        if last == 1:
            return 'TERMINATED'
        else:
            self.tasks.append(
                HotpoApplication(last))
            return 'RUNNING'
```

The $3n+1$ conjecture, VI



Parallel tasks are independent by definition, so it's even easier to create a collection:

```
tasks = ParallelTaskCollection([  
    HotpoSequence(n)  
    for n in range(1, N)  
])
```

We can run such a collection like any other Task.

Exercise 11.A:

Fill in the missing parts and write a `hotpo.py` session-based script that:

- ▶ takes a single integer parameter N on the command-line:

```
$ python hotpo.py 42
```

- ▶ computes all the “ $3n + 1$ ” sequences of numbers 1 up to N in parallel,
- ▶ prints a final statement that the Collatz conjecture is verified up to N (or —who knows— not?)