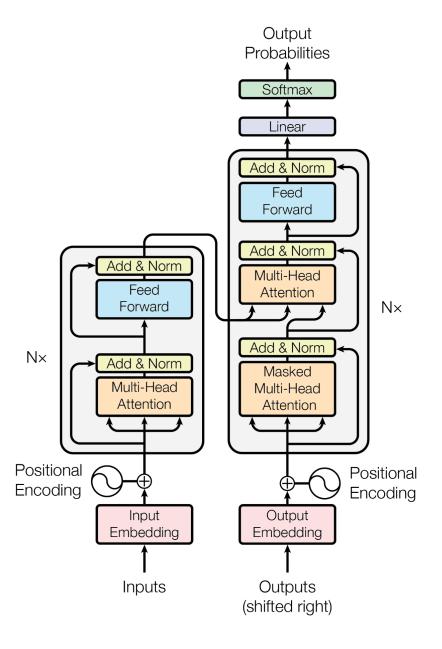
Introduction to Deep Learning Transformers

Shikhar Agnihotri

Liangze Li

11-785, Fall 2023

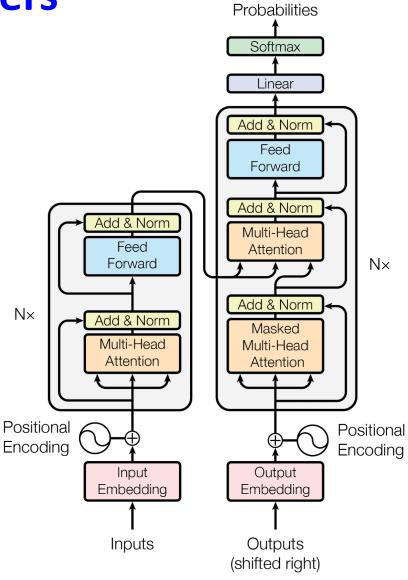
Transformers



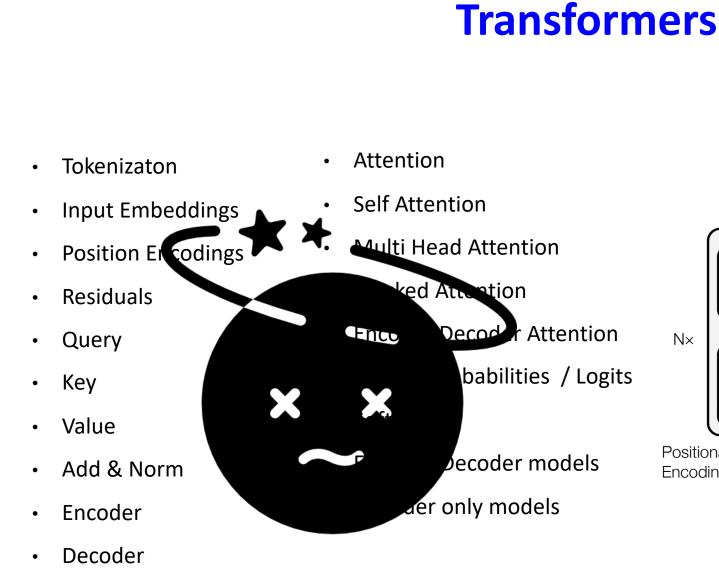
Transformers

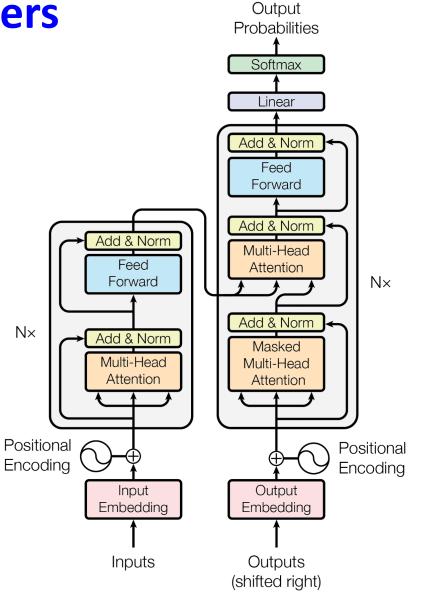
- Tokenizaton
- Input Embeddings
- Position Encodings
- Residuals
- Query
- Key
- Value
- Add & Norm
- Encoder
- Decoder

- Attention
- Self Attention
- Multi Head Attention
- Masked Attention
- Encoder Decoder Attention
- Output Probabilities / Logits
- Softmax
- Encoder-Decoder models
- Decoder only models



Output





Machine Translation

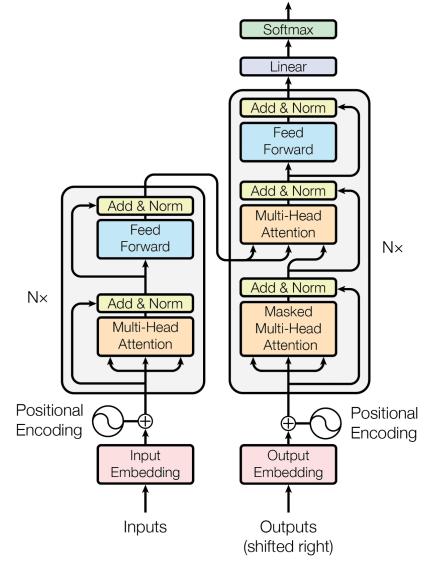
Targets

Ich have einen apfel gegessen



Inputs

I ate an apple



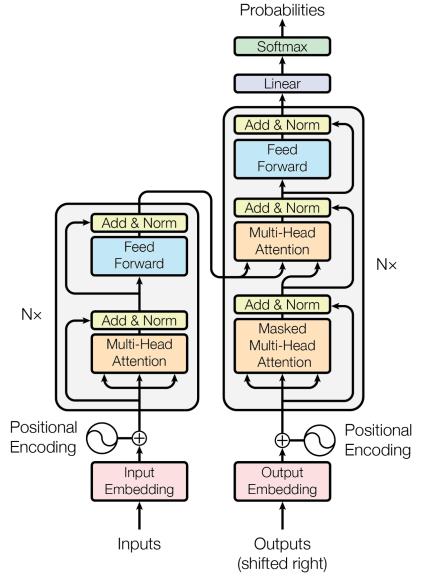
Output Probabilities

Inputs

Processing Inputs

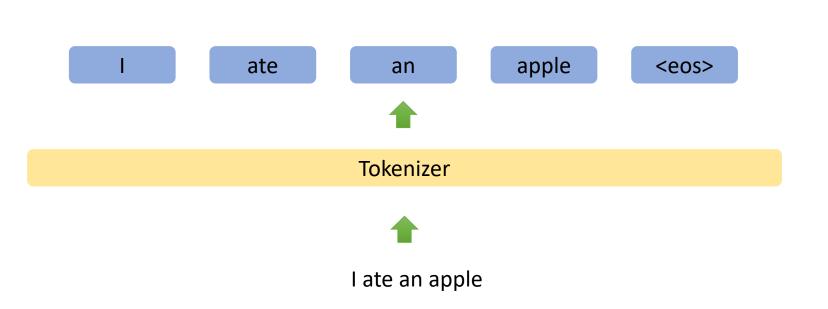
Inputs

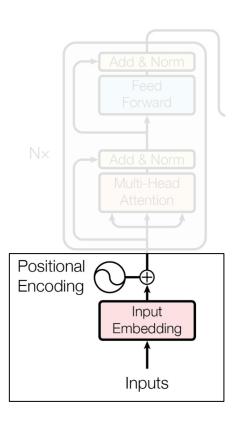
I ate an apple



Output

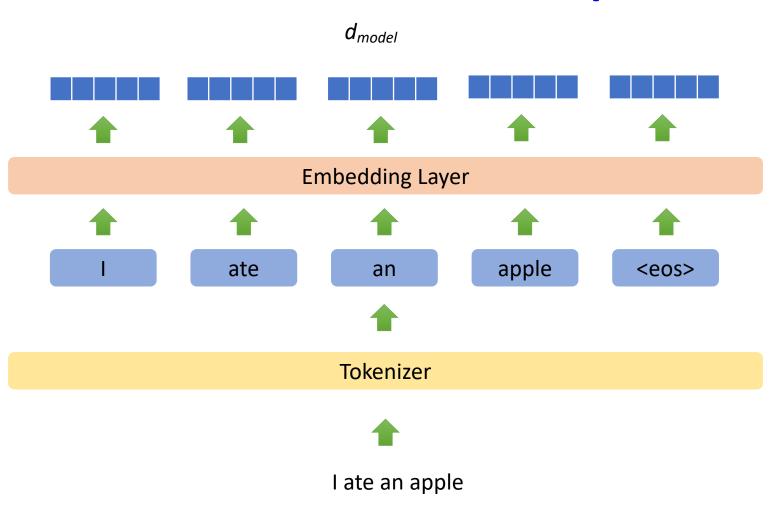
Inputs

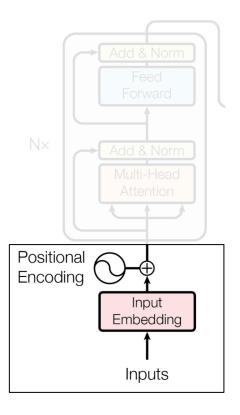




Generate Input Emebeddings

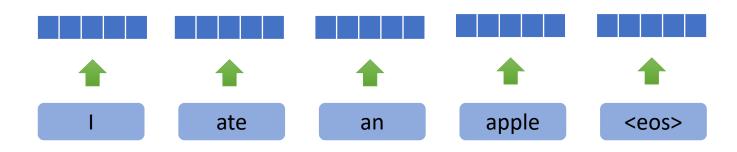
Inputs

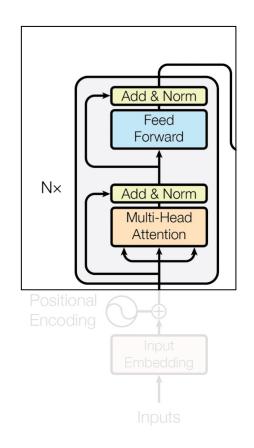


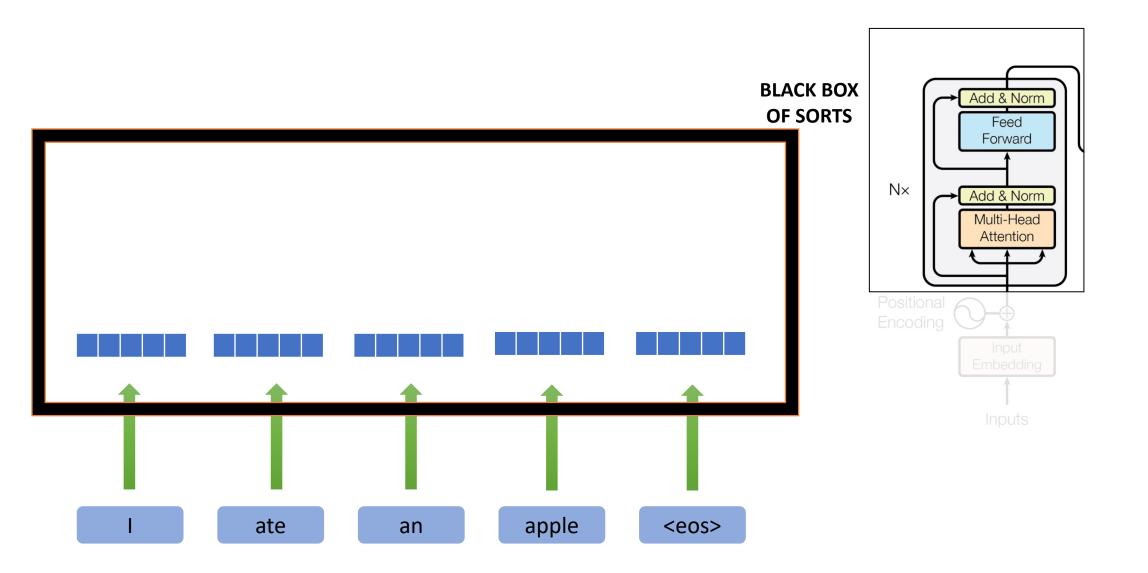


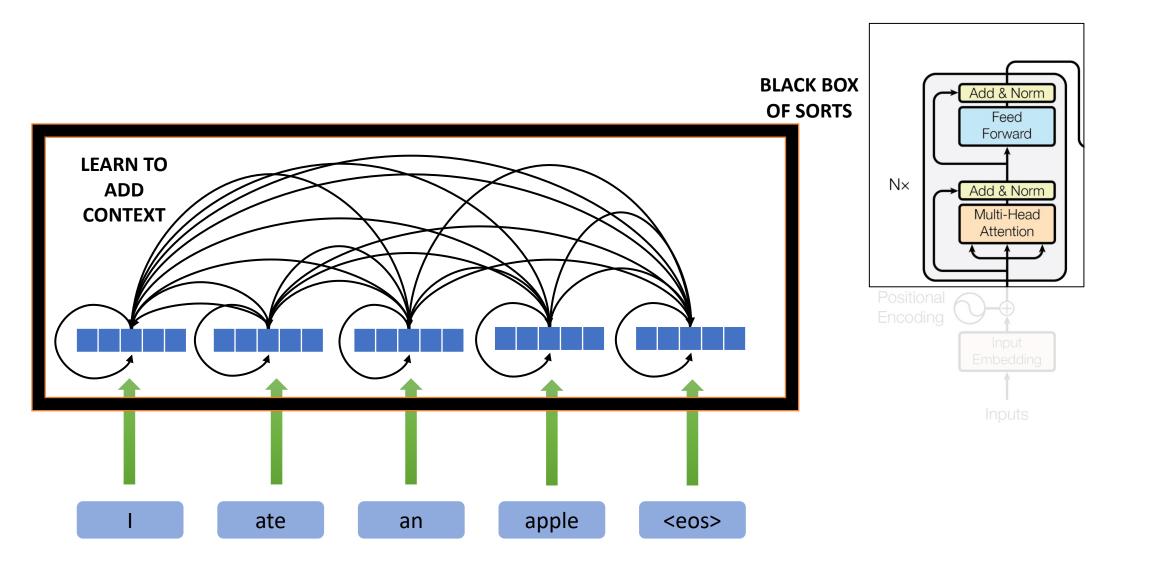
Generate Input Emebeddings

WHERE IS THE CONTEXT?

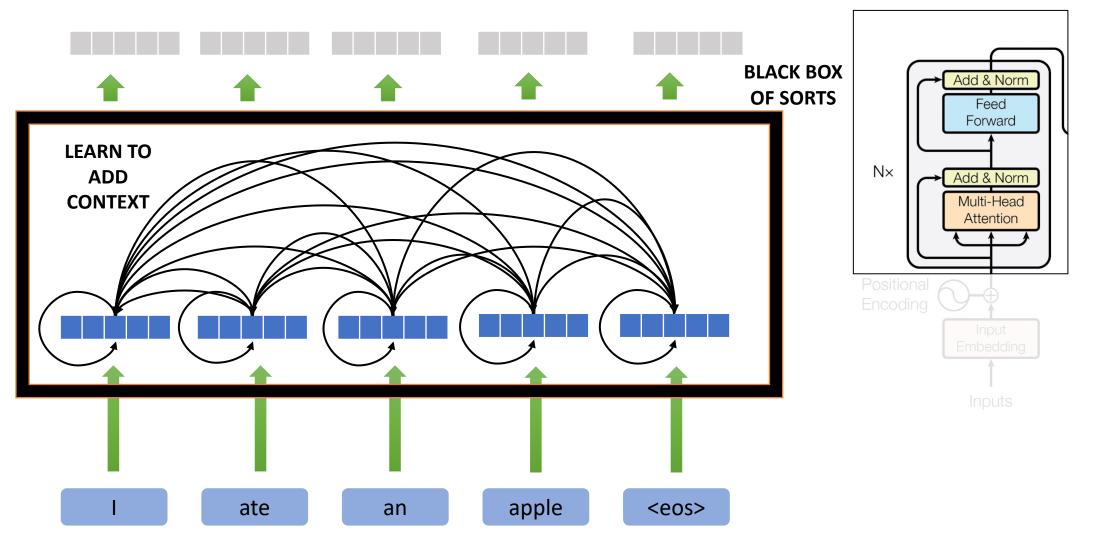






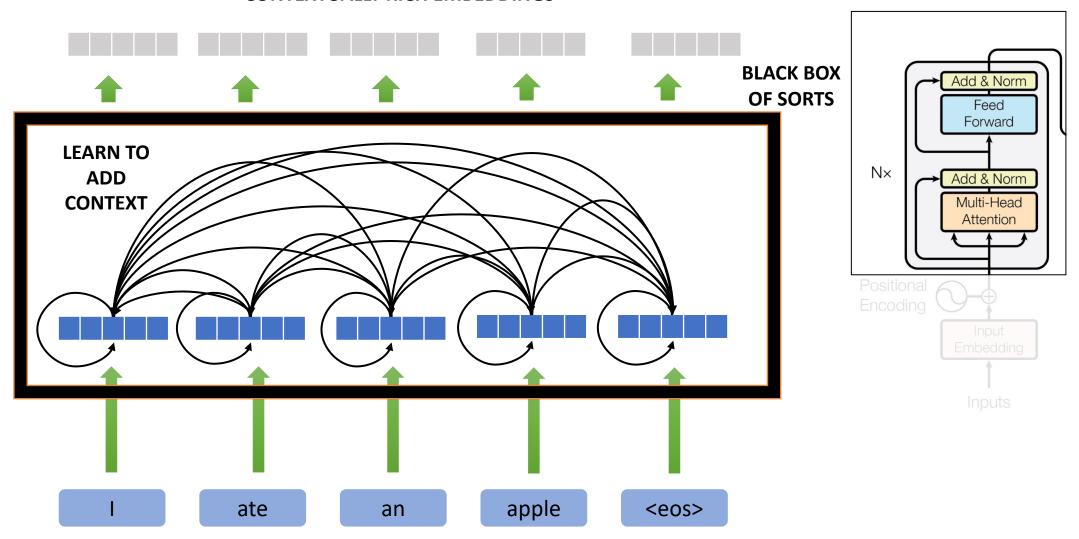


CONTEXTUALLY RICH EMBEDDINGS



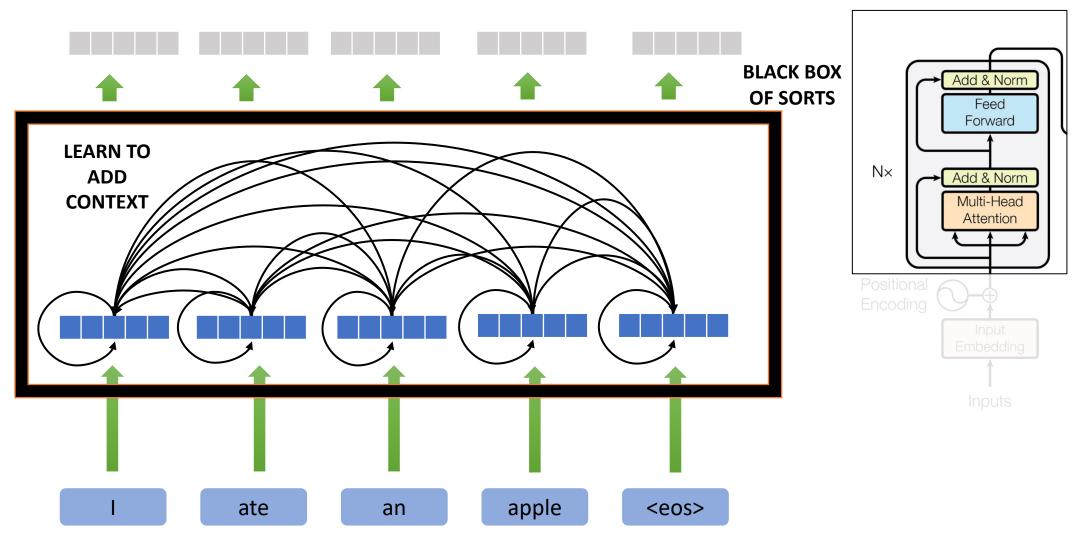
$\alpha_{[ij]}$?

CONTEXTUALLY RICH EMBEDDINGS



$\alpha_{[ij]}$? $\Sigma \Pi$?

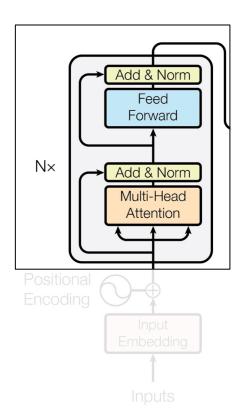
CONTEXTUALLY RICH EMBEDDINGS



$$\alpha_{[ij]}$$
?

From lecture 18:

$$Attention(Q, K, V) = softmax(\frac{QK^T}{\sqrt{d_k}})V$$

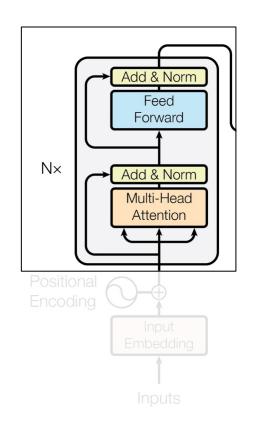


$$\alpha_{[ij]}$$
?

From lecture 18:

Attention
$$(Q, K, V) = \text{softmax}(\frac{QK^T}{\sqrt{d_k}})V$$

- Query
- Key
- Value



Database

```
{"order_100": {"items": "a1", "delivery_date": "a2", ....}},
{"order_101": {"items": "b1", "delivery_date": "b2", ....}},
{"order_102": {"items": "c1", "delivery_date": "c2", ....}},
{"order_103": {"items": "d1", "delivery_date": "d2", ....}},
{"order_104": {"items": "e1", "delivery_date": "e2", ....}},
{"order_105": {"items": "f1", "delivery_date": "f2", ....}},
{"order_106": {"items": "g1", "delivery_date": "g2", ....}},
{"order_107": {"items": "h1", "delivery_date": "h2", ....}},
{"order_108": {"items": "i1", "delivery_date": "i2", ....}},
{"order_109": {"items": "j1", "delivery_date": "j2", ....}},
{"order_109": {"items": "j1", "delivery_date": "j2", ....}},
```

Database

```
{Query: "Order details of order_104"}
OR
{Query: "Order details of order_106"}
```

```
{"order_100": {"items": "a1", "delivery_date": "a2", ....}},
{"order_101": {"items": "b1", "delivery_date": "b2", ....}},
{"order_102": {"items": "c1", "delivery_date": "c2", ....}},
{"order_103": {"items": "d1", "delivery_date": "d2", ....}},
{"order_104": {"items": "e1", "delivery_date": "e2", ....}},
{"order_105": {"items": "f1", "delivery_date": "f2", ....}},
{"order_106": {"items": "g1", "delivery_date": "g2", ....}},
{"order_107": {"items": "h1", "delivery_date": "h2", ....}},
{"order_108": {"items": "i1", "delivery_date": "i2", ....}},
{"order_109": {"items": "j1", "delivery_date": "j2", ....}},
{"order_1109": {"items": "j1", "delivery_date": "j2", ....}},
```

```
{Query: "Order details of order_104"}

OR

{Query: "Order details of order_106"}
```

```
{"order_100": {"items": "a1", "delivery_date": "a2", ....}},
{"order_101": {"items": "b1", "delivery_date": "b2", ....}},
{"order_102": {"items": "c1", "delivery_date": "c2", ....}},
{"order_103": {"items": "d1", "delivery_date": "d2", ....}},
{"order_104": {"items": "e1", "delivery_date": "e2", ....}},
{"order_105": {"items": "f1", "delivery_date": "f2", ....}},
{"order_106": {"items": "g1", "delivery_date": "g2", ....}},
{"order_107": {"items": "h1", "delivery_date": "h2", ....}},
{"order_108": {"items": "i1", "delivery_date": "i2", ....}},
{"order_109": {"items": "j1", "delivery_date": "j2", ....}},
{"order_110": {"items": "j1", "delivery_date": "j2", ....}},
```

```
{Query: "Order details of order_104"}
OR
{Query: "Order details of order 106"}
```

```
{"order_100": {"items": "a1", "delivery_date": "a2", ....}},
{"order_101": {"items": "b1", "delivery_date": "b2", ....}},
{"order_102": {"items": "c1", "delivery_date": "c2", ....}},
{"order_103": {"items": "d1", "delivery_date": "d2", ....}},
{"order_104": {"items": "e1", "delivery_date": "e2", ....}},
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{"order_107": {"items": "h1", "delivery_date": "h2", ....}},
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{"order_109": {"items": "j1", "delivery_date": "j2", ....}},
{"order_109": {"items": "j1", "delivery_date": "j2", ....}},
```

```
{Query: "Order details of order_104"}

OR

{Query: "Order details of order_106"}
```

```
{"order_100": {"items": "a1", "delivery_date": "a2", ....}},
{"order_101": {"items": "b1", "delivery_date": "b2", ....}},
{"order_102": {"items": "c1", "delivery_date": "c2", ....}},
{"order_103": {"items": "d1", "delivery_date": "d2", ....}},
{"order_104": {"items": "e1", "delivery_date": "e2", ....}},
{"order_105": {"items": "f1", "delivery_date": "f2", ....}},
{"order_106": {"items": "g1", "delivery_date": "g2", ....}},
{"order_107": {"items": "h1", "delivery_date": "h2", ....}},
{"order_108": {"items": "i1", "delivery_date": "i2", ....}},
{"order_109": {"items": "j1", "delivery_date": "j2", ....}},
{"order_109": {"items": "j1", "delivery_date": "j2", ....}},
```

Done at the same time!!

{Query: "Order details of order_104"}

OR

{Query: "Order details of order_106"}

```
{"order_100": {"items": "a1", "delivery_date": "a2", ....}},
{"order_101": {"items": "b1", "delivery_date": "b2", ....}},
{"order_102": {"items": "c1", "delivery_date": "c2", ....}},
{"order_103": {"items": "d1", "delivery_date": "d2", ....}},
{"order_104": {"items": "e1", "delivery_date": "e2", ....}},
{"order_105": {"items": "f1", "delivery_date": "f2", ....}},
{"order_106": {"items": "g1", "delivery_date": "g2", ....}},
{"order_107": {"items": "h1", "delivery_date": "h2", ....}},
{"order_108": {"items": "i1", "delivery_date": "i2", ....}},
{"order_109": {"items": "j1", "delivery_date": "j2", ....}},
{"order_109": {"items": "j1", "delivery_date": "j2", ....}},
```

```
{Query: "Order details of order_104"}
OR
{Query: "Order details of order_106"}
```

```
{"order_100": {"items": "a1", "delivery_date": "a2", ....}},
{"order_101": {"items": "b1", "delivery_date": "b2", ....}},
{"order_102": {"items": "c1", "delivery_date": "c2", ....}},
{"order_103": {"items": "d1", "delivery_date": "d2", ....}},
{"order_104": {"items": "e1", "delivery_date": "e2", ....}},
{"order_105": {"items": "f1", "delivery_date": "f2", ....}},
{"order_106": {"items": "g1", "delivery_date": "g2", ....}},
{"order_107": {"items": "h1", "delivery_date": "h2", ....}},
{"order_108": {"items": "i1", "delivery_date": "i2", ....}},
{"order_109": {"items": "j1", "delivery_date": "j2", ....}},
{"order_100": {"items": "k1", "delivery_date": "j2", ....}},
```

Query

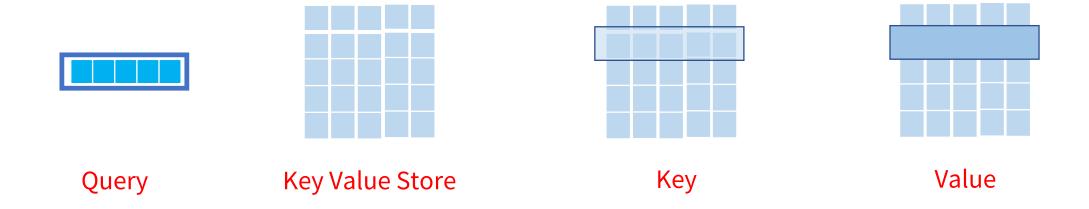
1. Search for info

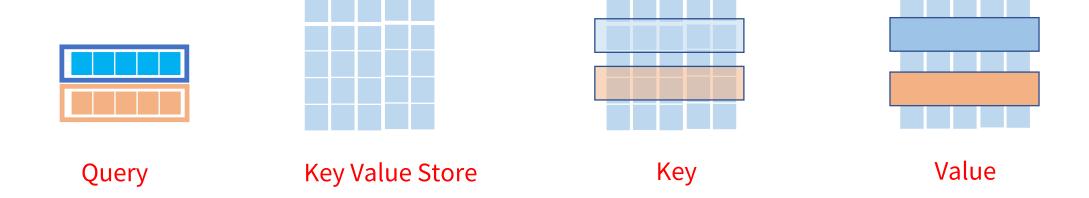
Key

- 1. Interacts directly with Queries
- 2. Distinguishes one object from another
- 3. Identify which object is the most relevant and by how much

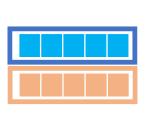
Value

- 1. Actual details of the object
- 2. More fine grained

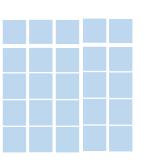




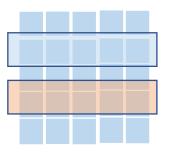
Done at the same time!!



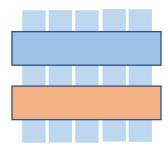




Key Value Store

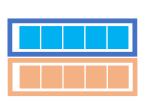


Key



Value

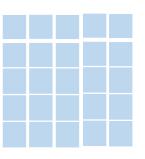
Parallelizable!!!



Query

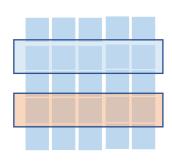
Q



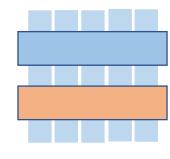


Key Value Store

 QK^T



Key



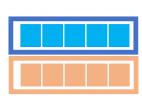
Value

$$softmax(\frac{QK^T}{\sqrt{d}})$$

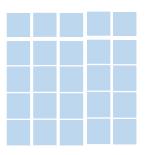
$$softmax(\frac{QK^T}{\sqrt{d}})V$$

Parallelizable!!!

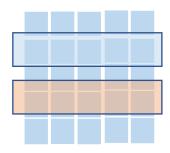
Attention Filter



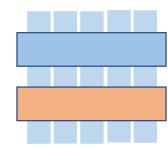
Query



Key Value Store



Key



Value

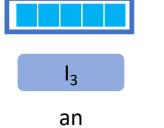
Q

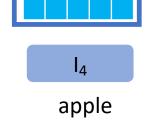
 QK^T

 $softmax(\frac{QK^T}{\sqrt{d}})$

$$softmax(\frac{QK^T}{\sqrt{d}})V$$





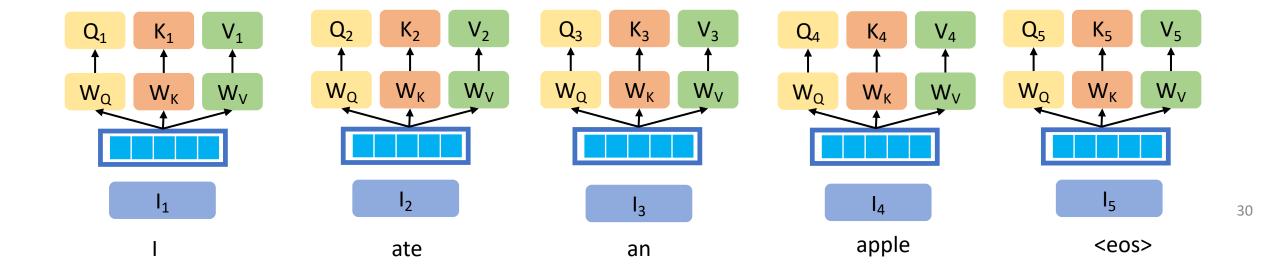




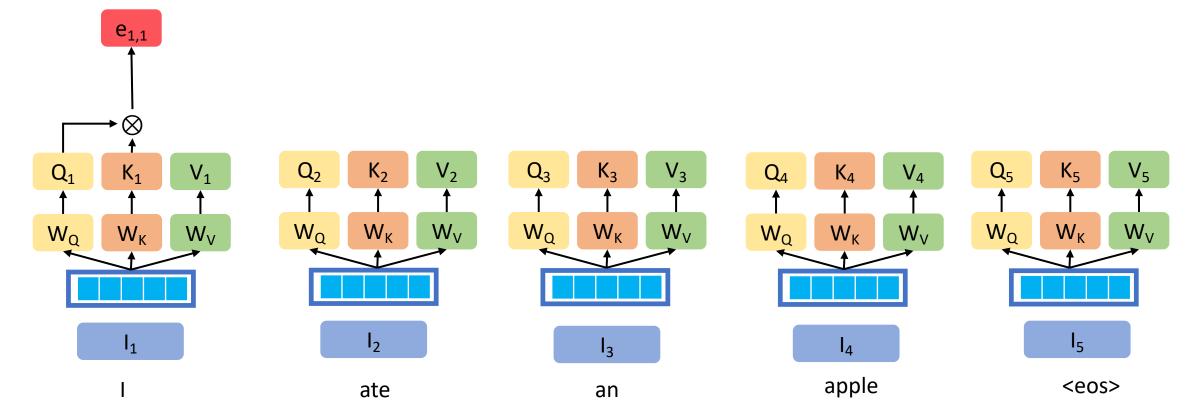
I₅

<eos>

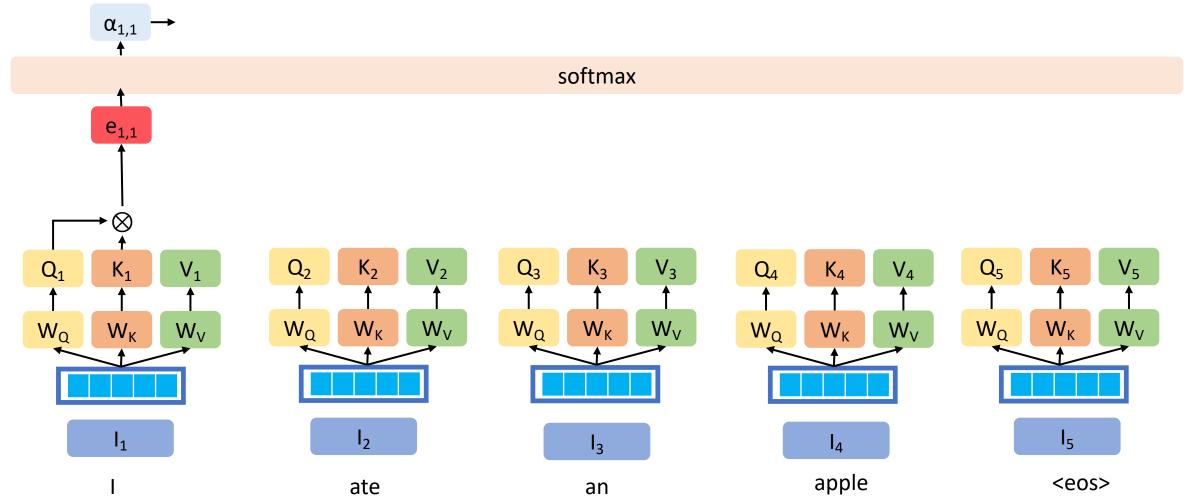
Dimensions across QKV have been dropped for brevity

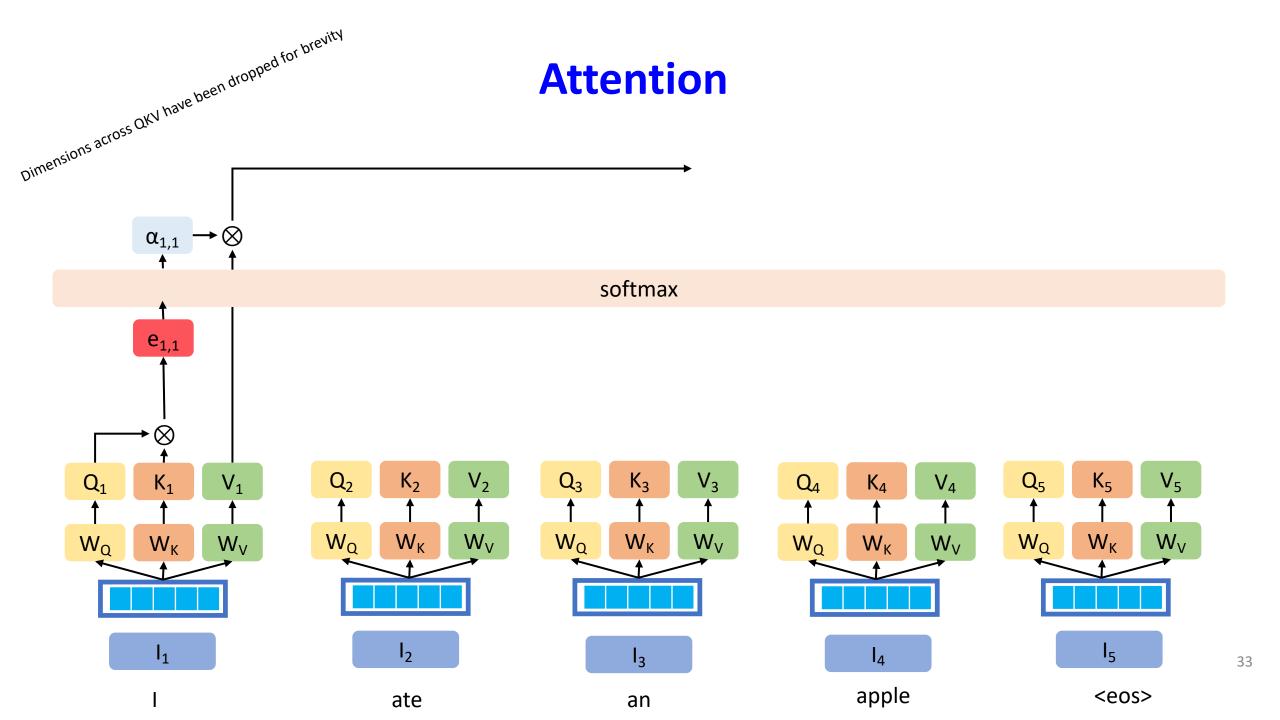


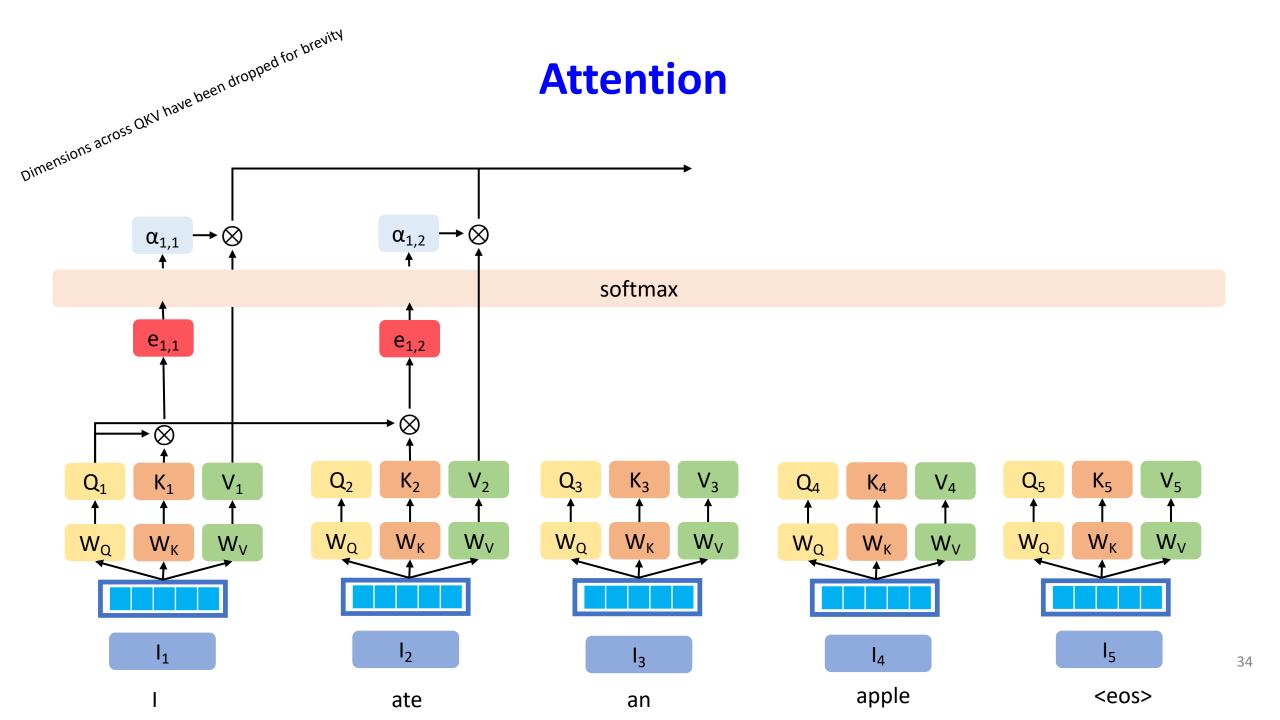
Dimensions across QKV have been dropped for brevity

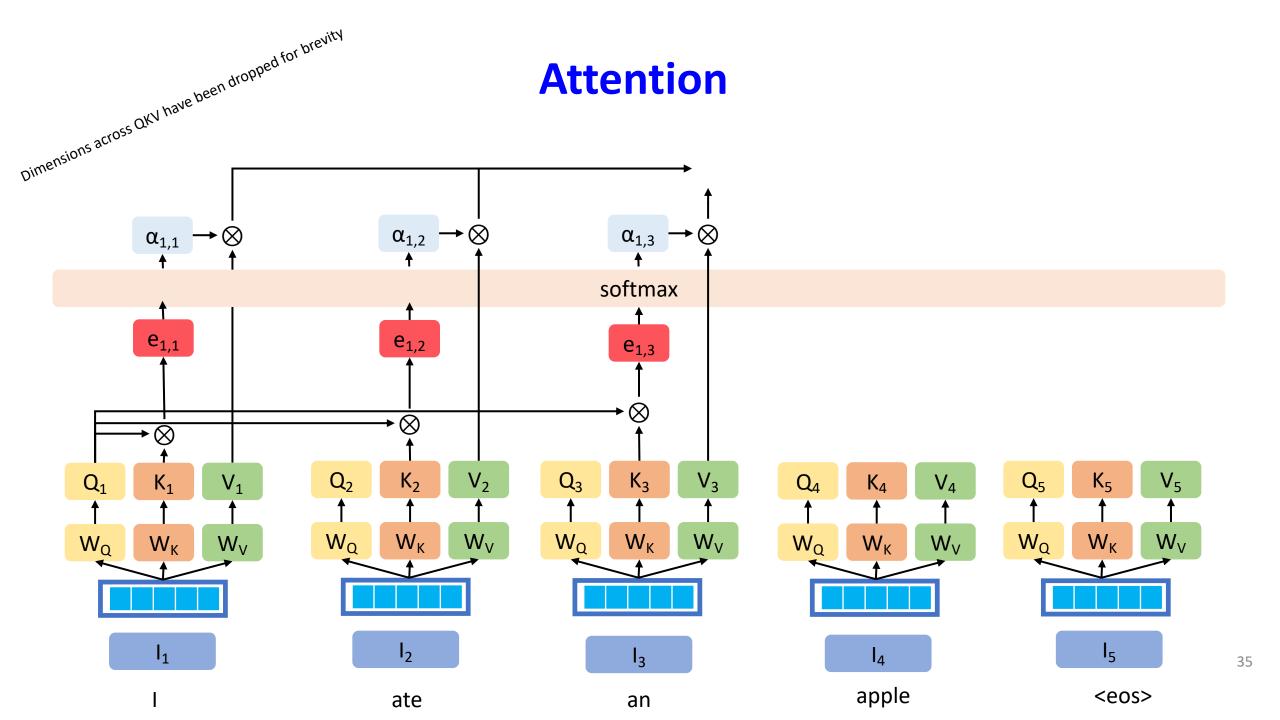


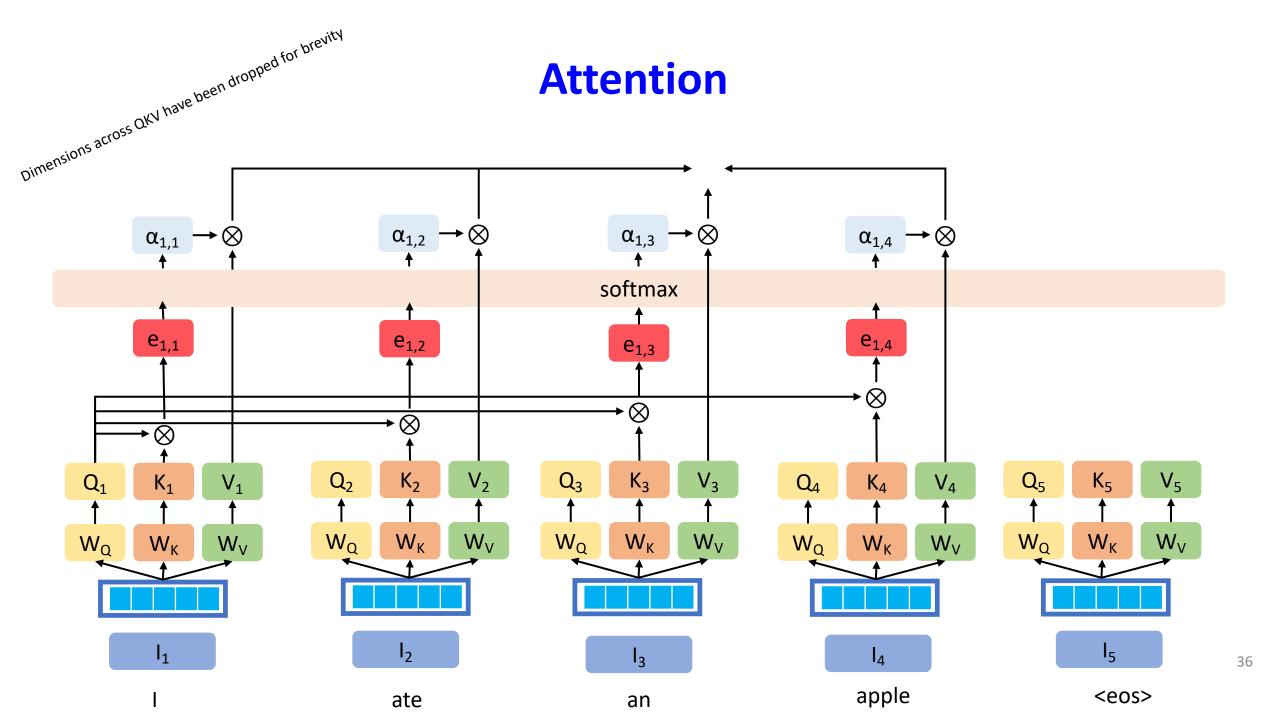
Dimensions across QKV have been dropped for brevity









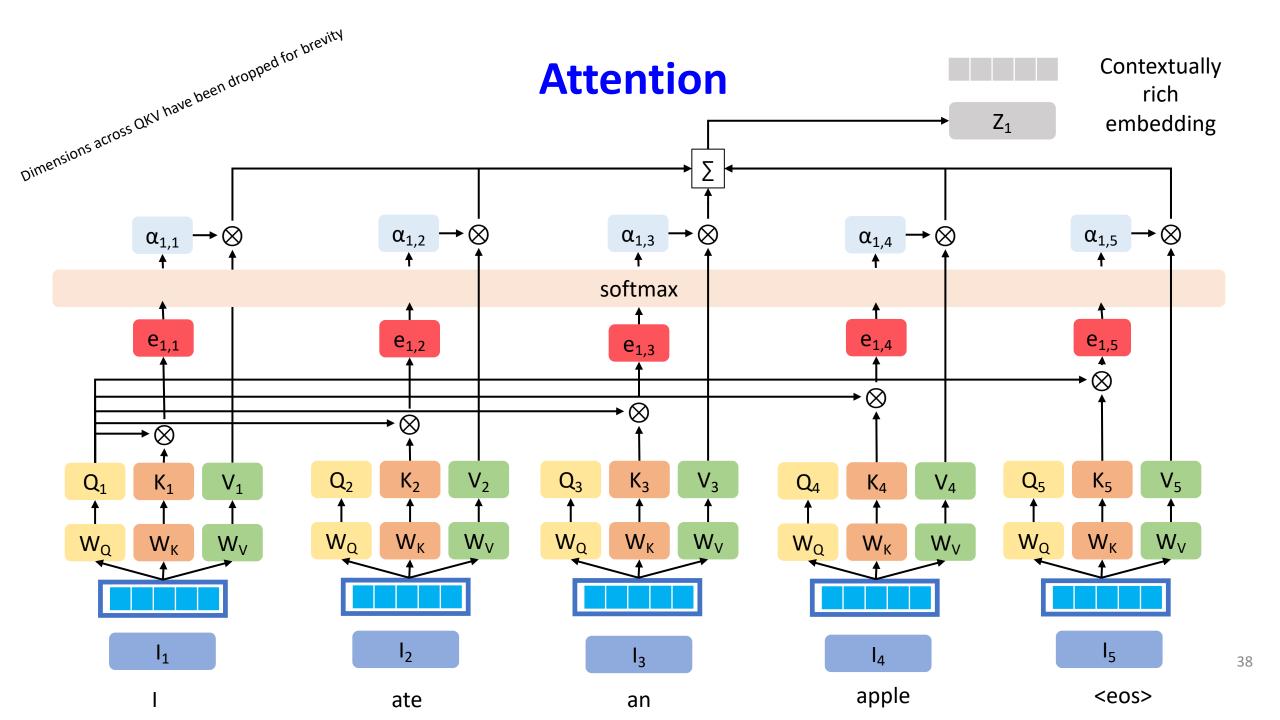


Dimensions across QKV have been dropped for brevity **Attention** $\alpha_{1,3}$ $\alpha_{1,4} \rightarrow \otimes$ $\alpha_{1,2}$ $\alpha_{\text{1,5}}$ softmax e_{1,4} $e_{1,5}$ e_{1,1} e_{1,2} e_{1,3} K_3 K_5 Q_2 K_2 V_2 Q_3 K_4 Q_5 Q_1 K_1 Q_4 W_{Q} W_{K} W_V W_Q W_Q W_V W_{Q} W_{K} W_Q W_{K} W_{K} W_{K} W_V W_V W_V I_1 **I**₂ **I**₅ I_4 I_3 37 apple

an

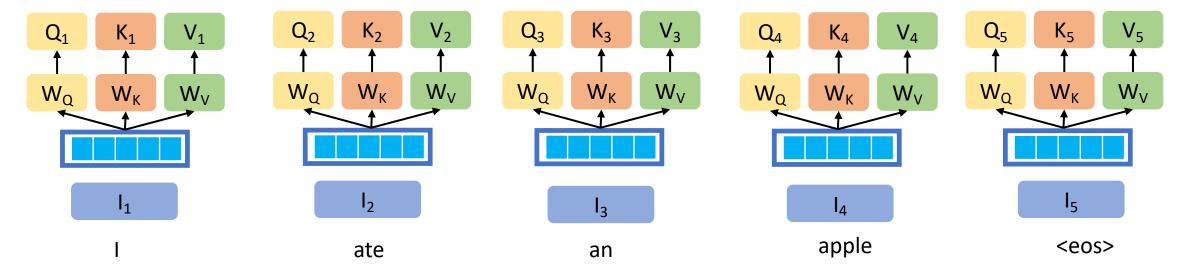
ate

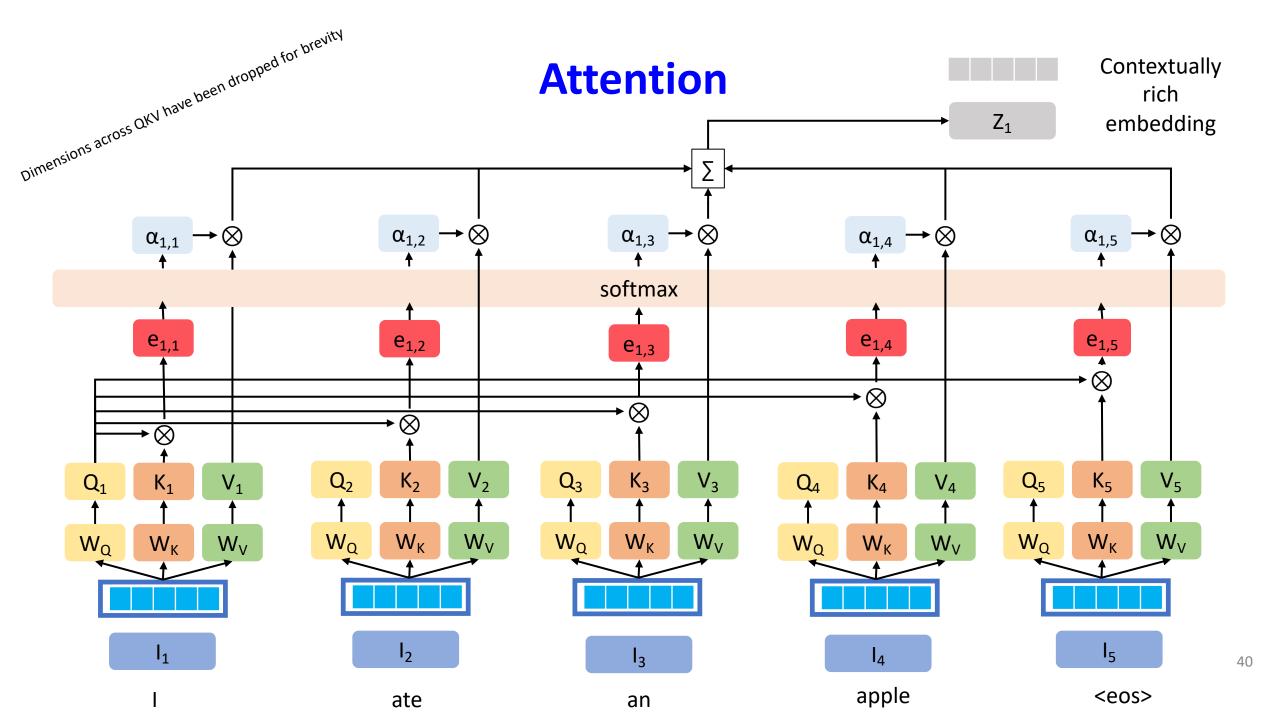
<eos>

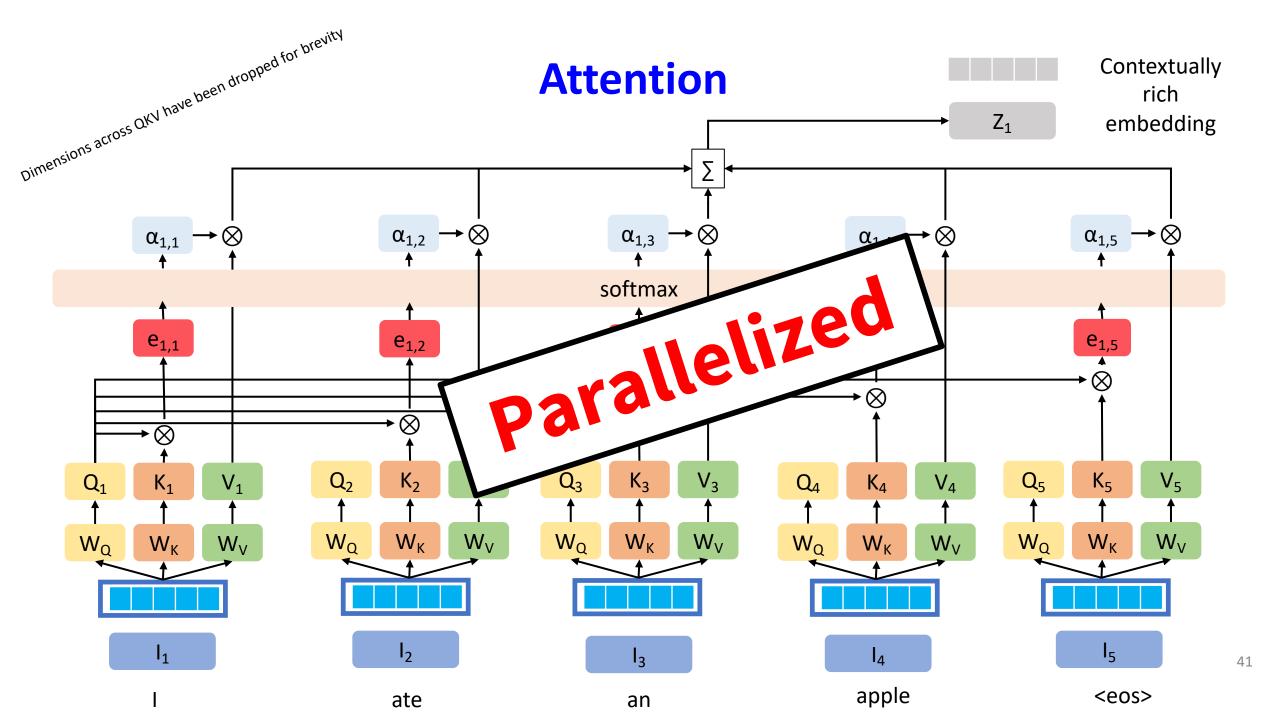


Dimensions across QKV have been dropped for brevity

Attention



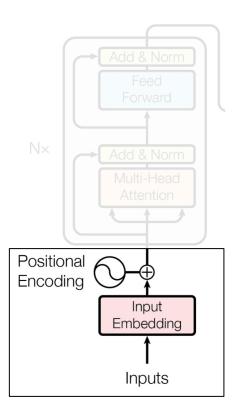




Poll 1 @1296

Which of the following are true about attention? (Select all that apply)

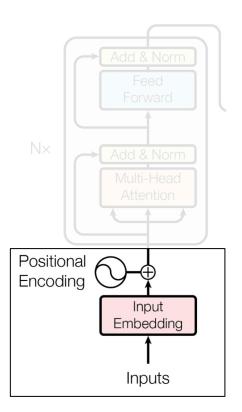
- a. To calculate attention weights for input I_2 , you would use key k_2 , and all queries
- b. To calculate attention weights for input I_2 , you would use query q_2 , and all keys
 - c. We scale the QK^T product to bring attention weights in the range of [0,1]
 - d. We scale the QK^T product to allow for numerical stability

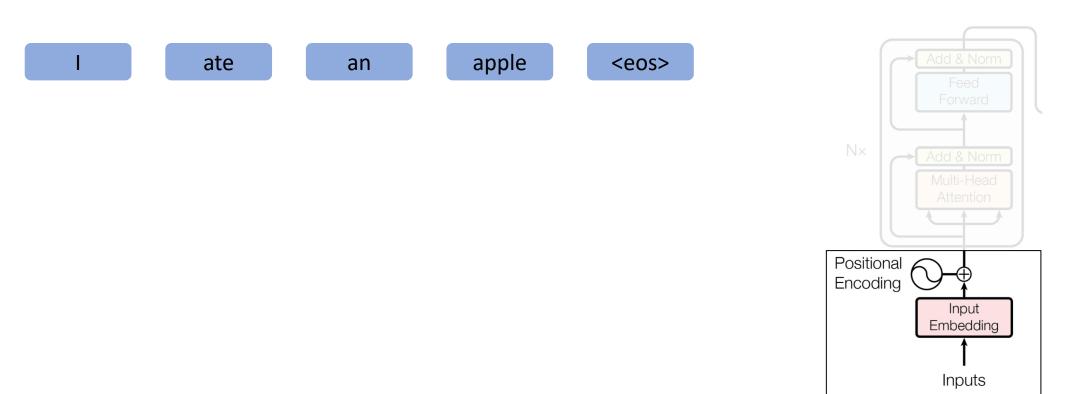


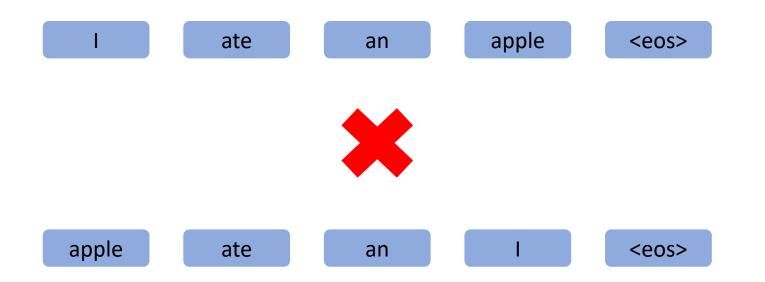
Poll 1 @1296

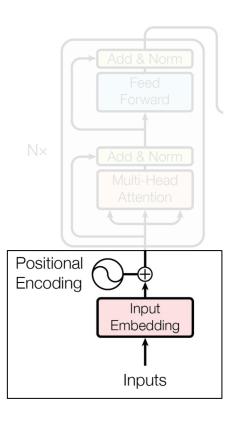
Which of the following are true about attention? (Select all that apply)

- a. To calculate attention weights for input I_2 , you would use key k_2 , and all queries
- b. To calculate attention weights for input I_2 , you would use query q_2 , and all keys
 - c. We scale the QK^T product to bring attention weights in the range of [0,1]
 - d. We scale the QK^T product to allow for numerical stability



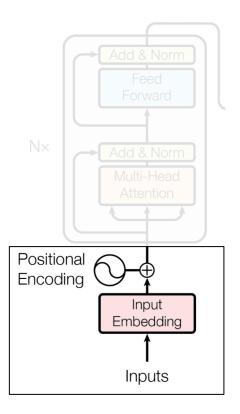






Requirements for Positional Encodings

- Some representation of time ? (like seq2seq ?)
- Should be unique for each position not cyclic



Requirements for Positional Encodings

- Some representation of time ? (like **seq2seq** ?)
- Should be unique for each position not cyclic

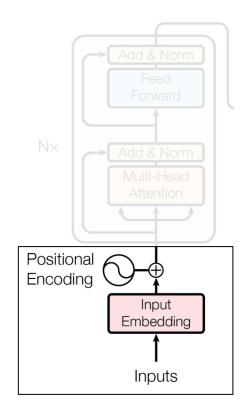
Possible Candidates:

$$P_{t+1} = P_t + \Delta c$$

$$P_{t+1} = e^{P_{t_{\Delta}}C}$$

$$P_{t+1} = e^{P_{t_{\Delta}}c}$$

$$P_{t+1} = P_t^{t_{\Delta}c}$$



Requirements for Positional Encodings

- Some representation of time ? (like seq2seq?)
- Should be unique for each position not cyclic

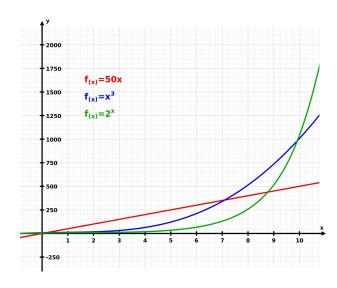
Possible Candidates:

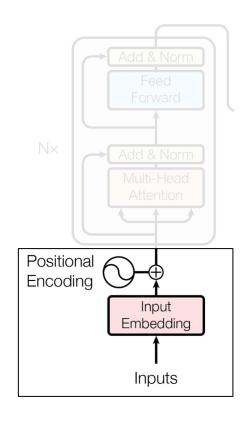
$$P_{t+1} = P_t + \Delta c$$

$$P_{t+1} = e^{P_{t}} \Delta^{\alpha}$$

$$P_{t+1} = e^{P_{t_{\Delta}}c}$$

$$P_{t+1} = P_t^{:t_{\Delta}c}$$





Requirements for Positional Encodings

- Some representation of time ? (like seq2seq?)
- Should be unique for each position not cyclic
- **Bounded**

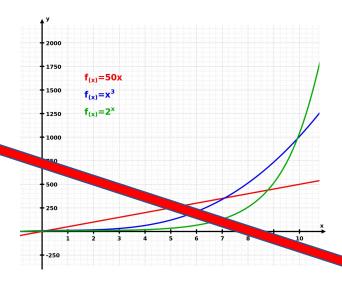
Possible Candidates:

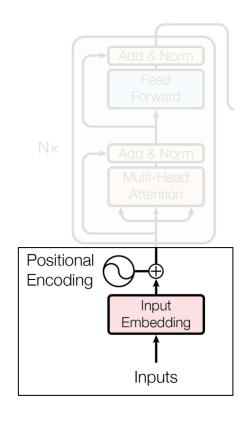
$$P_{t+1} - P_t + \Delta c$$

$$P_{t+1} = e^{P_{t}} \Delta^{C}$$

$$P_{t+1} = e^{P_{t_{\Delta}}c}$$

$$P_{t+1} = P_t^{\cdot t\Delta c}$$



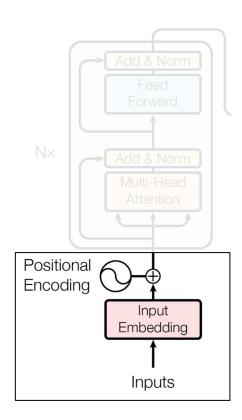


Requirements for Positional Encodings

- Some representation of time ? (like seq2seq ?)
- Should be unique for each position not cyclic
- Bounded

Possible Candidates:

$$P(t + t') = M^{t'} \times P(t)$$



Requirements for Positional Encodings

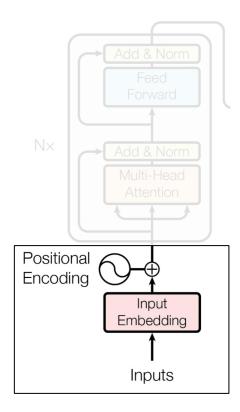
- Some representation of time ? (like seq2seq ?)
- Should be unique for each position not cyclic
- Bounded

Possible Candidates:

$$P(t + t') = M^{t'} \times P(t)$$

M?

- 1. Should be a unitary matrix
- 2. Magnitudes of eigen value should be 1 -> norm preserving



Requirements for Positional Encodings

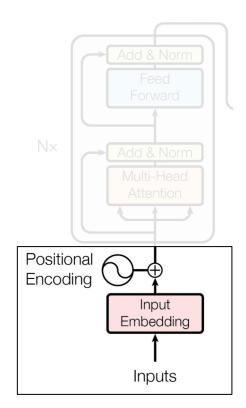
- Some representation of time ? (like seq2seq ?)
- Should be unique for each position not cyclic
- Bounded

Possible Candidates:

$$P(t + t') = M^{t'} \times P(t)$$

M

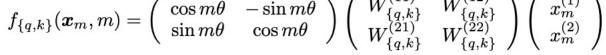
- 1. The matrix can be learnt
- 2. Produces unique rotated embeddings each time



Rotary Positional Embedding

ROFORMER: ENHANCED TRANSFORMER WITH ROTARY Position Embedding

$$f_{\{q,k\}}(\boldsymbol{x}_m,m) = \begin{pmatrix} \cos m\theta & -\sin m\theta \\ \sin m\theta & \cos m\theta \end{pmatrix} \begin{pmatrix} W_{\{q,k\}}^{(11)} & W_{\{q,k\}}^{(12)} \\ W_{\{q,k\}}^{(21)} & W_{\{q,k\}}^{(22)} \end{pmatrix} \begin{pmatrix} x_m^{(1)} \\ x_m^{(2)} \end{pmatrix}$$



MRPC SST-2 STS-B MNLI(m/mm) Model **QNLI** QQP BERTDevlin et al. [2019] 88.9 85.8 71.2 93.5 90.5 84.6/83.4 90.7 RoFormer 89.5 88.0 87.0 86.4 80.2/79.8

Table 2: Comparing RoFormer and BERT by fine tuning on downstream GLEU tasks.

Positional Encoding Input Embeddina Inputs

REF: Rotary Positional Embeddings

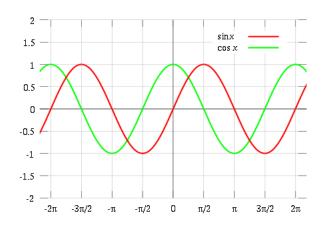
Requirements for Positional Encodings

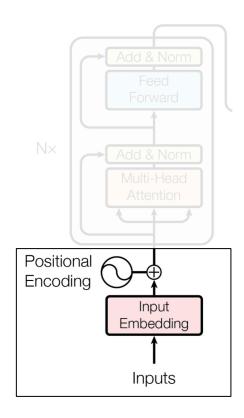
- Some representation of time ? (like seq2seq ?)
- Should be unique for each position not cyclic
- Bounded

Actual Candidates:

sine(**g(t)**)

cosine(g(t))





Requirements for g(t)

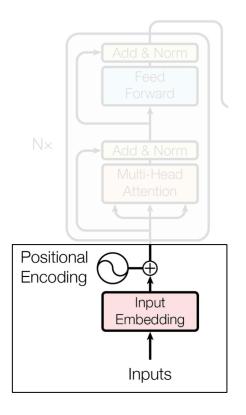
- Must have same dimensions as input embeddings
- Must produce overall unique encodings

pos -> idx of the token in input sentence

-> ith dimension out of d

$$PE_{(pos,2i)} = sin(pos/10000^{2i/d_{model}}) \ PE_{(pos,2i+1)} = cos(pos/10000^{2i/d_{model}})$$

$$PE_{(pos,2i+1)} = cos(pos/10000^{2i/d_{model}})$$



$$PE_{(pos,2i)} = sin(pos/10000^{2i/d_{model}}) \ PE_{(pos,2i+1)} = cos(pos/10000^{2i/d_{model}})$$

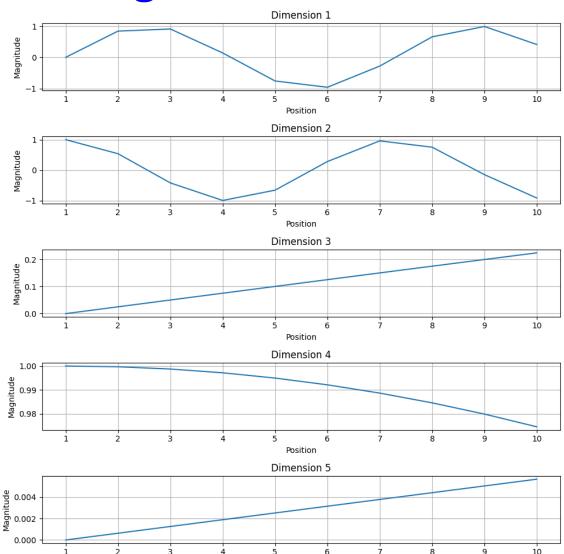
Requirements for g(t)

- Must have same dimensions as input embeddings
- Must produce overall unique encodings

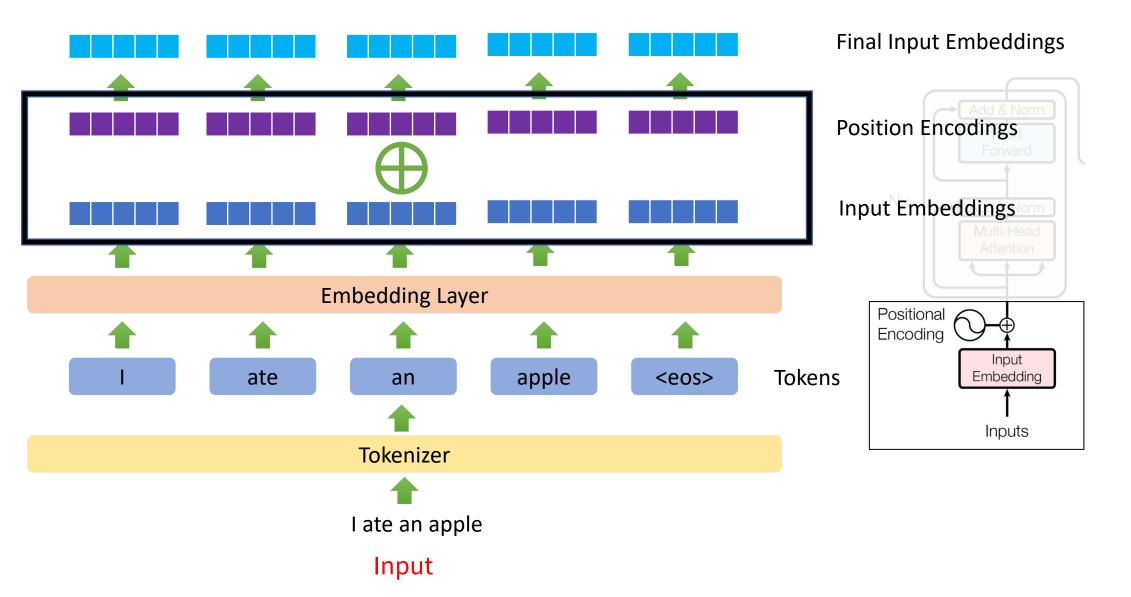
pos -> idx of the token in input sentence

i -> ith dimension out of d

Positional Encoding:



Position

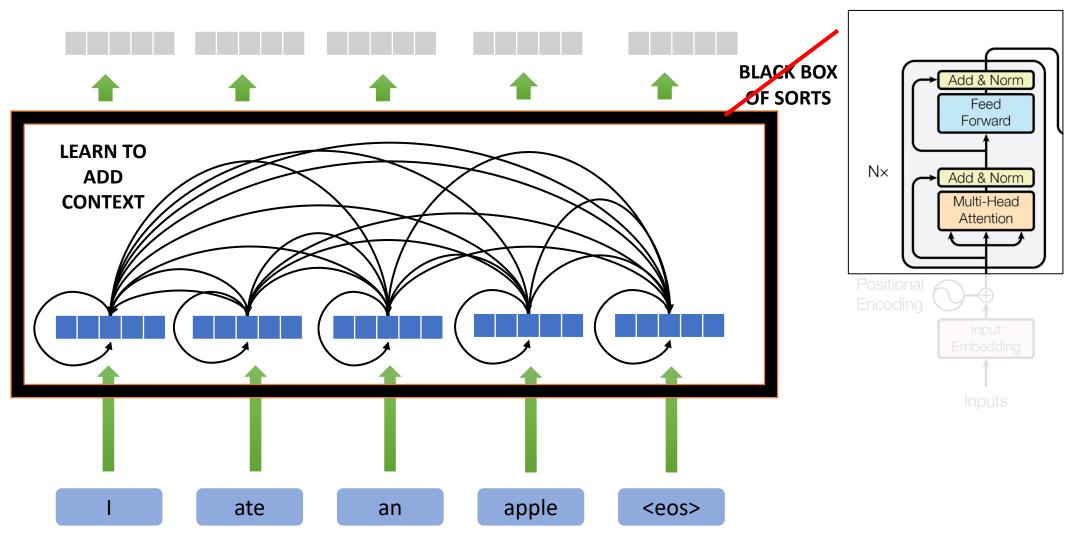


Encoder

 $\alpha_{[ij]}$

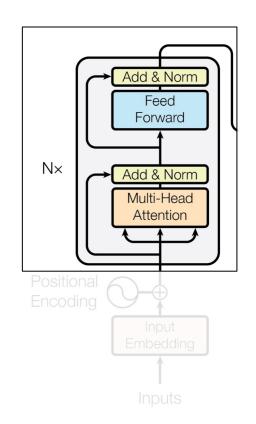
Σ

CONTEXTUALLY RICH EMBEDDINGS

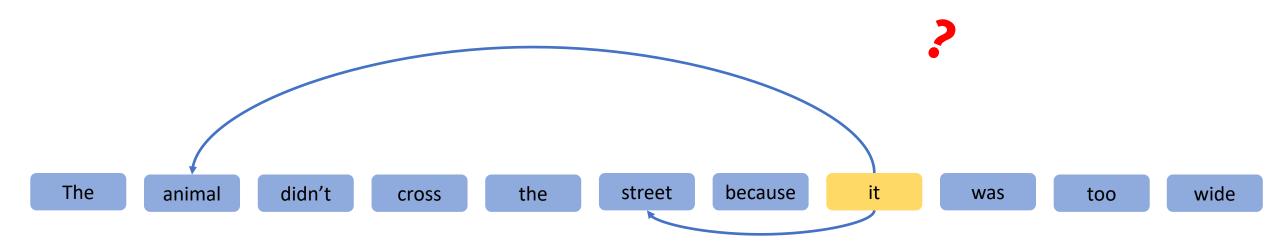


From lecture 18:

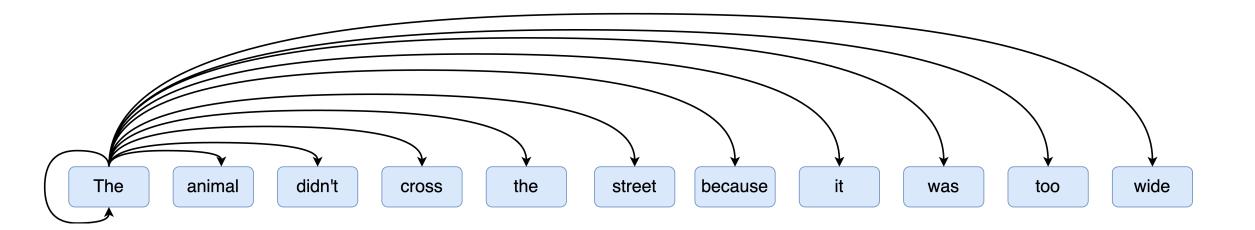
Attention
$$(Q, K, V) = \text{softmax}(\frac{QK^T}{\sqrt{d_k}})V$$

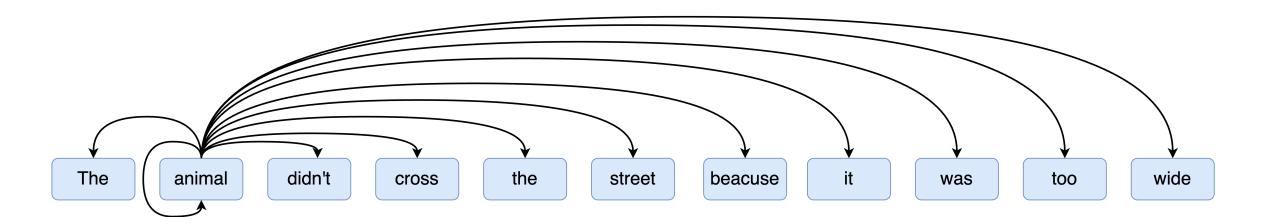


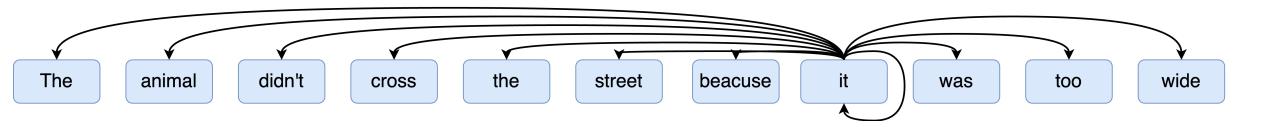
The animal didn't cross the street because it was too wide

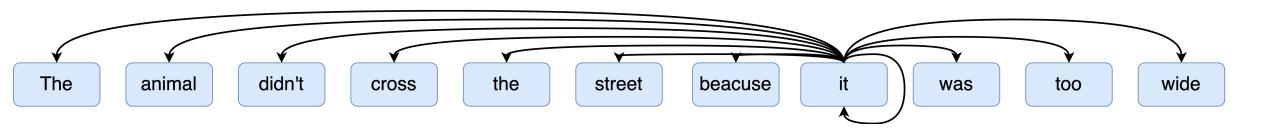


coreference resolution?



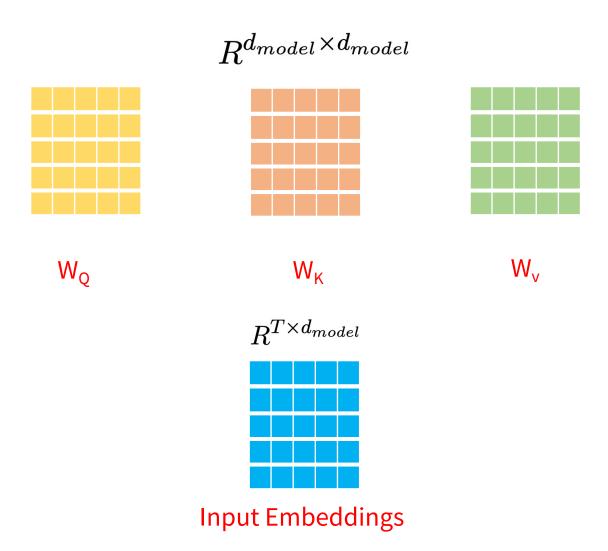


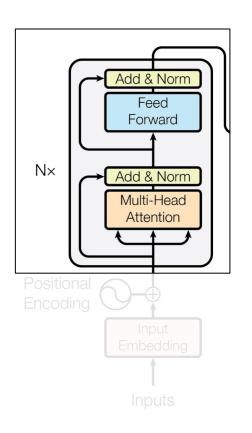


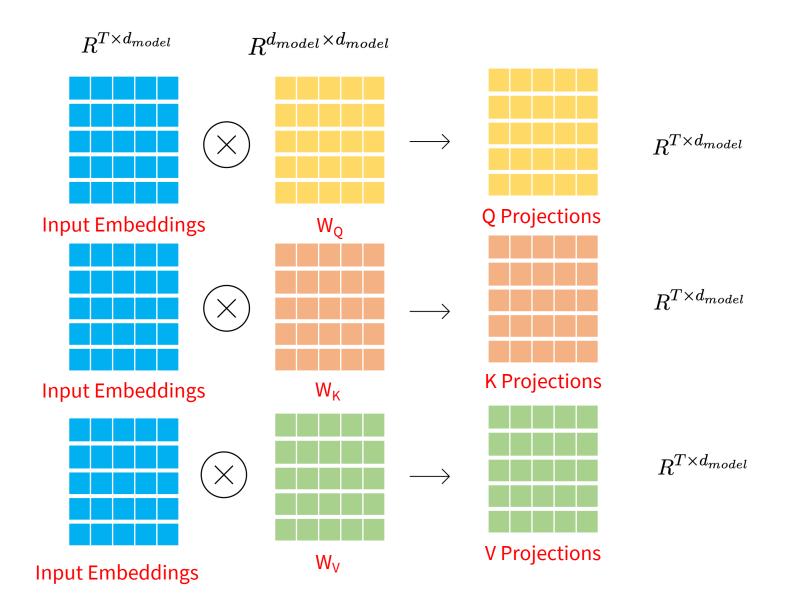


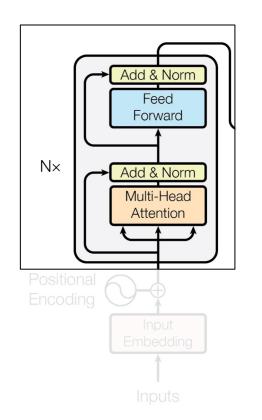
SELF

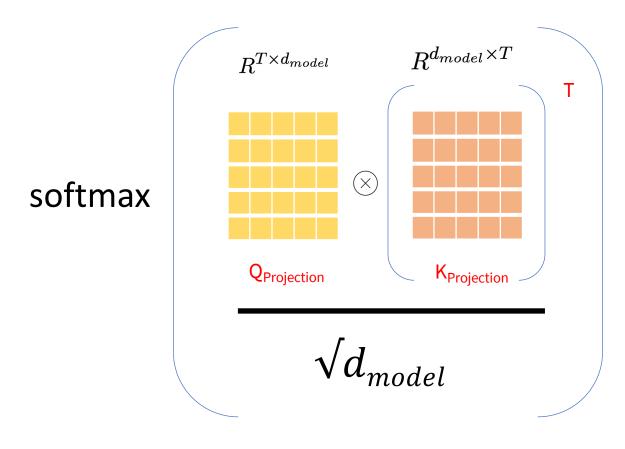
Query Inputs = Key Inputs = Value Inputs

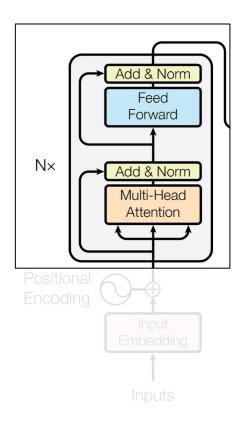


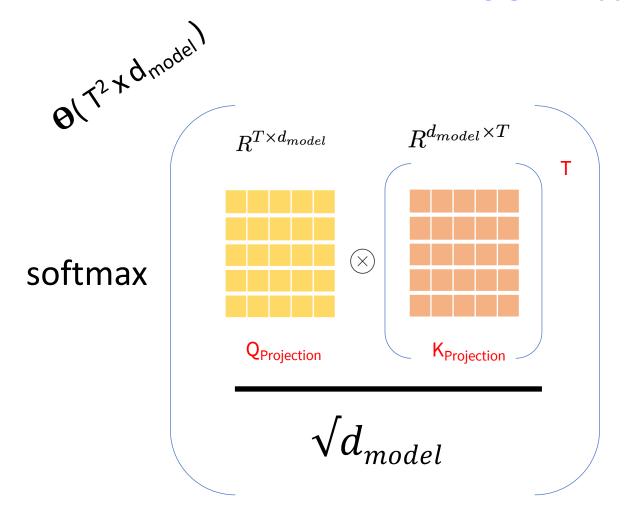


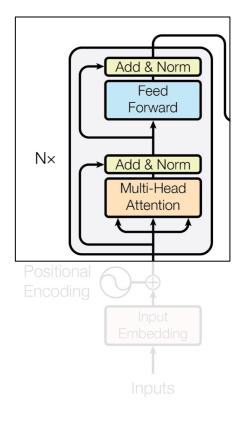


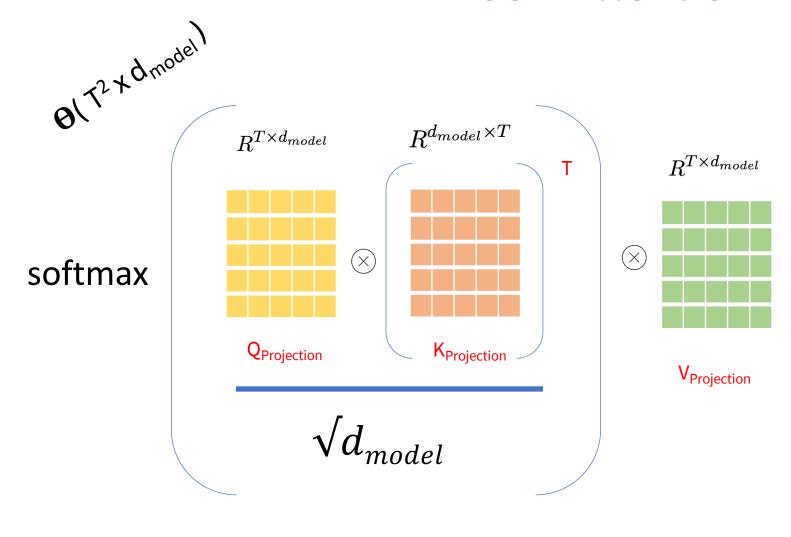


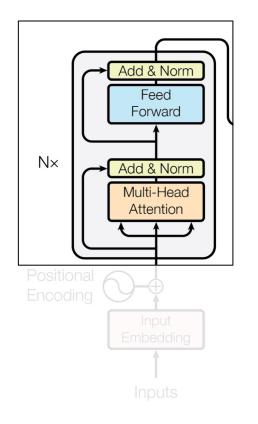


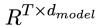


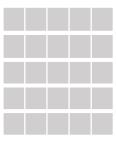




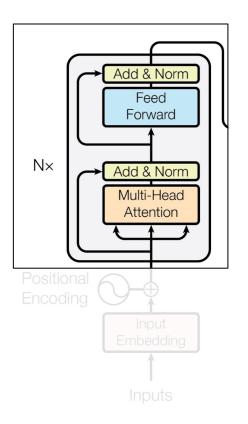


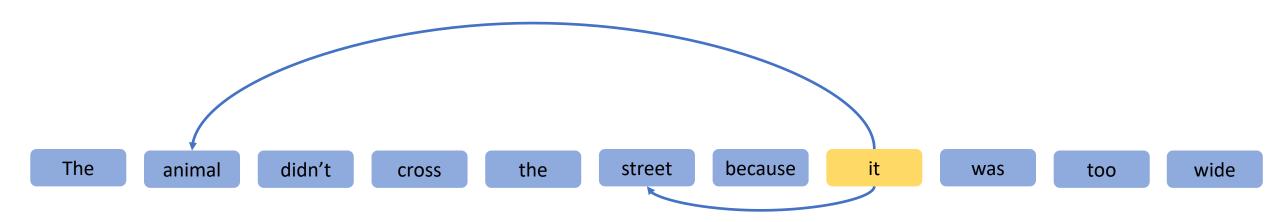






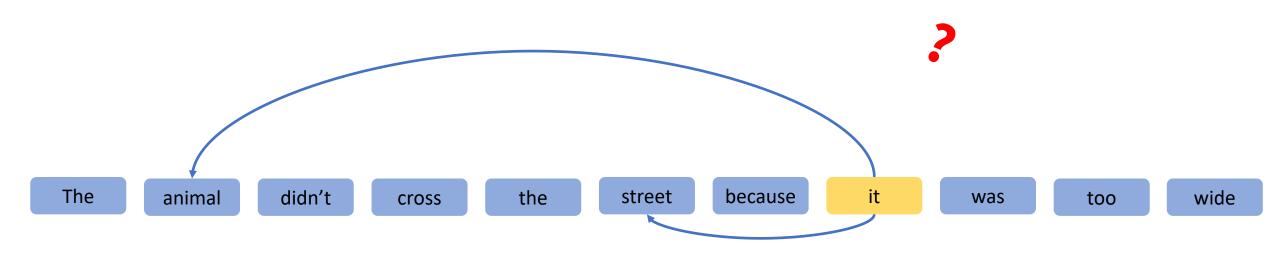
Attention: Z







Self Attention



Sentence boundaries?

coreference resolution



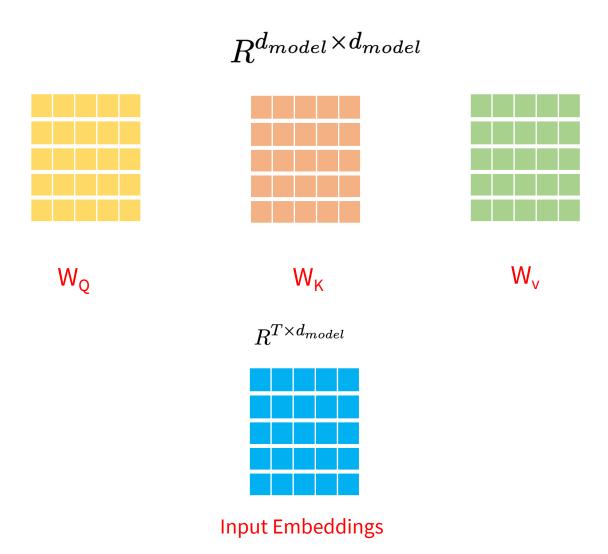
Context?

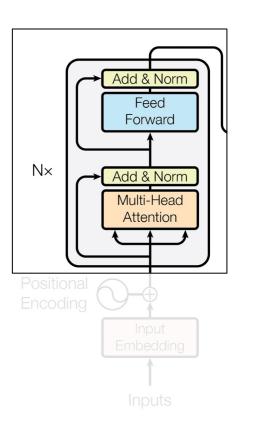
Semantic relationships?

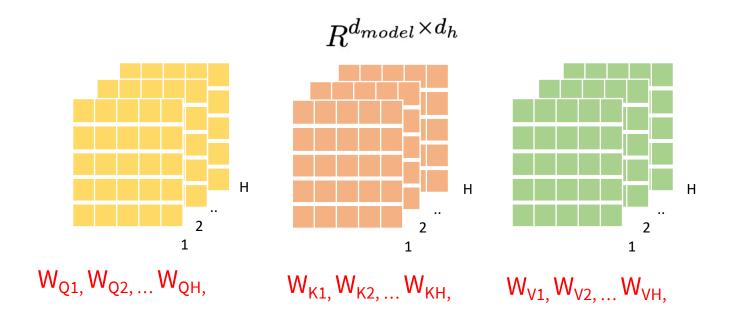
Part of Speech?

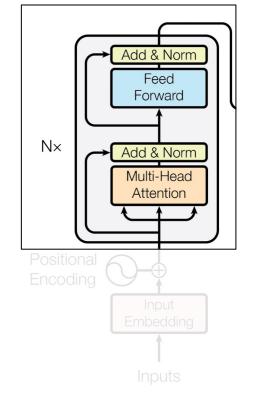
Comparisons?

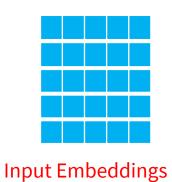
Self Attention



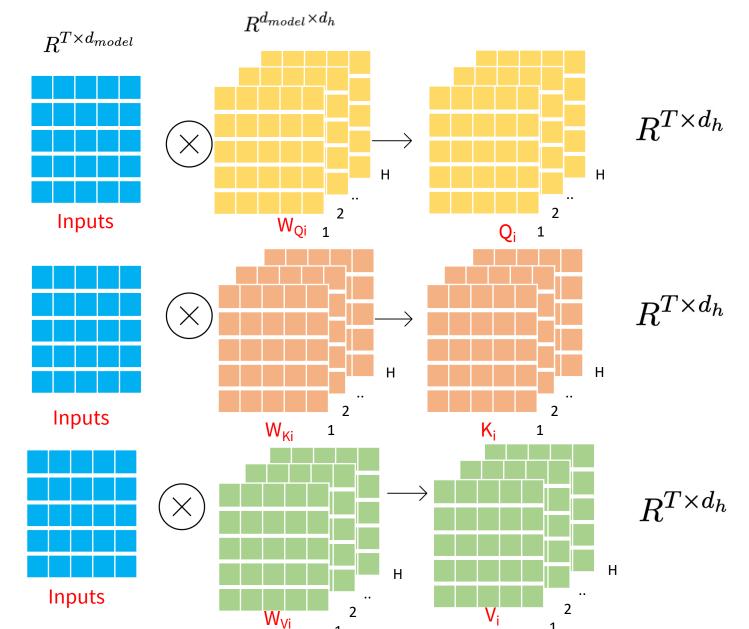


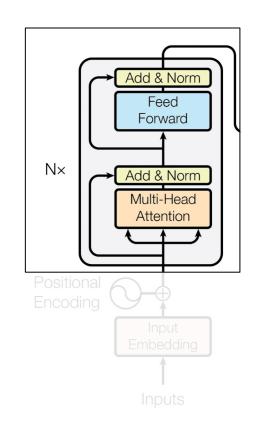


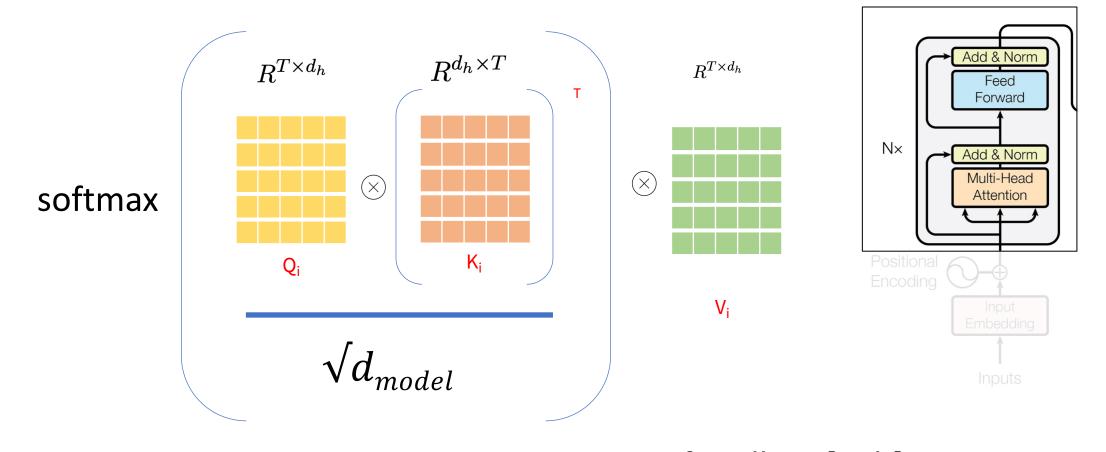




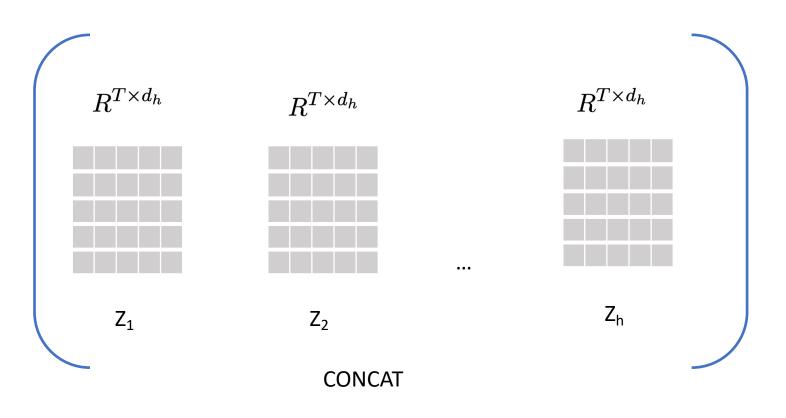
$$d_h = \frac{d_{model}}{h}$$

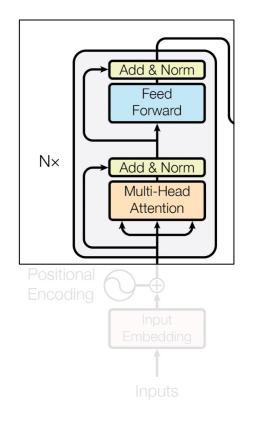






for all $i \in [1, h]$

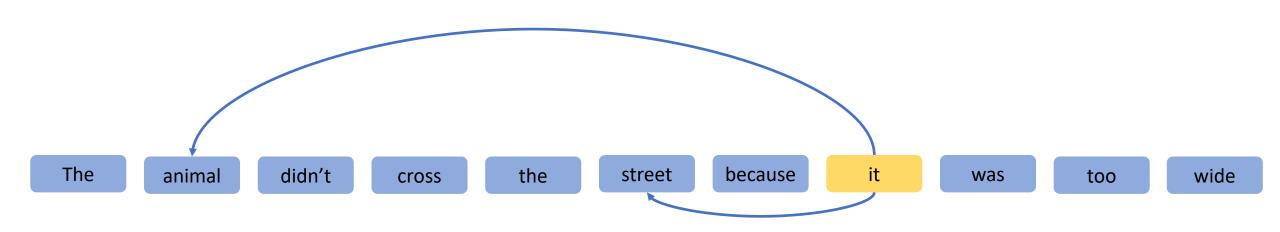


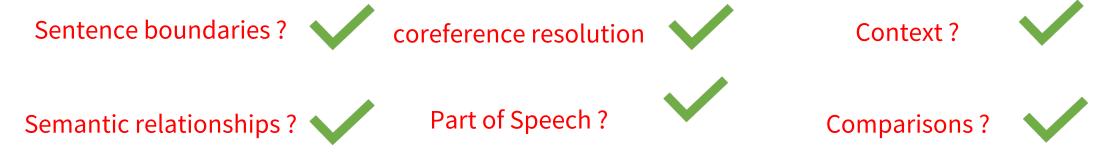


Multi Head Attention : Z

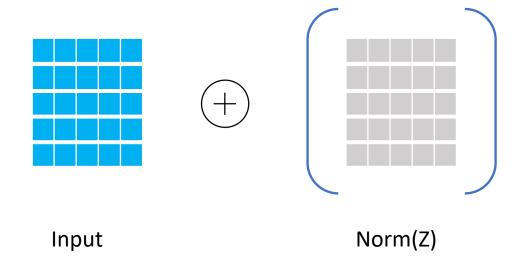
$$d_h = \frac{d_{model}}{h}$$

$$R^{T \times d_{model}}$$





Add & Norm

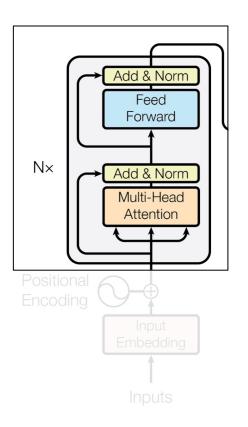


Normalization(Z)

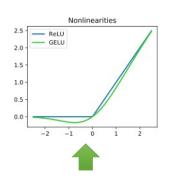
- Mean 0, Std dev 1
- Stabilizes training
- Regularization effect

Add -> Residuals

- Avoid vanishing gradients
- Train deeper networks

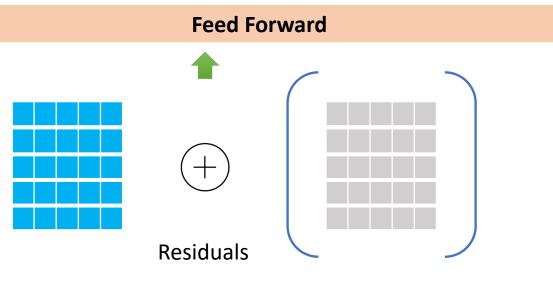


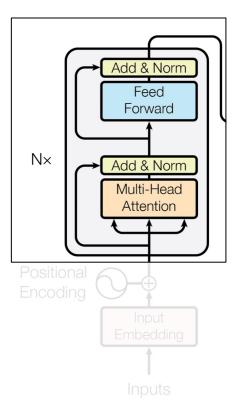
Feed Forward



Feed Forward

- Non Linearity
- Complex Relationships
- Learn from each other



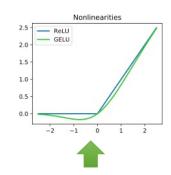


Input

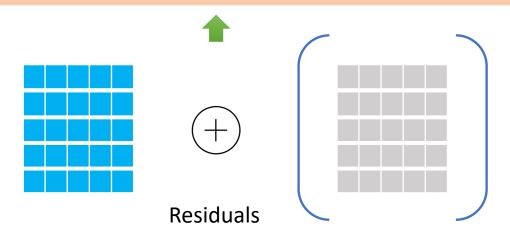
Norm(Z)

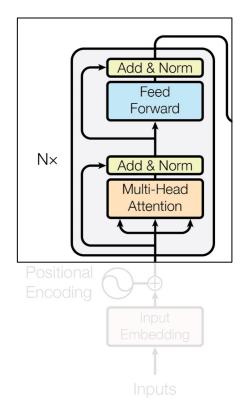
Add & Norm

Add & Norm



Feed Forward



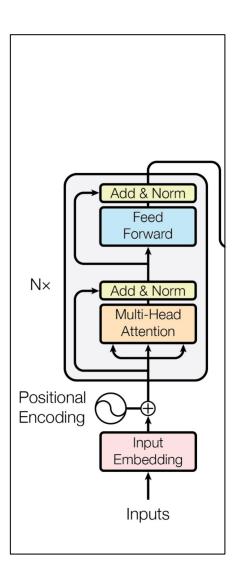


Input Norm(Z)

Encoders

Encoder

ENCODER



Encoders

Encoder

ENCODER

•

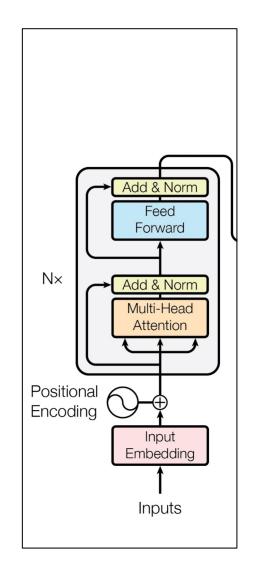
•

ENCODER

ENCODER

Input to Encoder_{i+1}

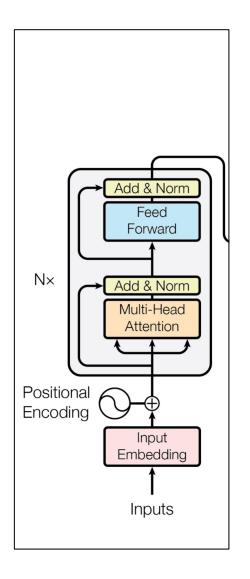
Output from Encoder_i



Transformers

- ✓ Tokenizaton
- ✓ Input Embeddings
- **✓ Position Encodings**
- ✓ Residuals
- ✓ Query
- ✓ Key
- ✓ Value
- ✓ Add & Norm
- ✓ Encoder
- Decoder

- ✓ Attention
- ✓ Self Attention
- ✓ Multi Head Attention
- Masked Attention
- Encoder Decoder Attention
- Output Probabilities / Logits
- Softmax
- Encoder-Decoder models
- Decoder only models



Machine Translation

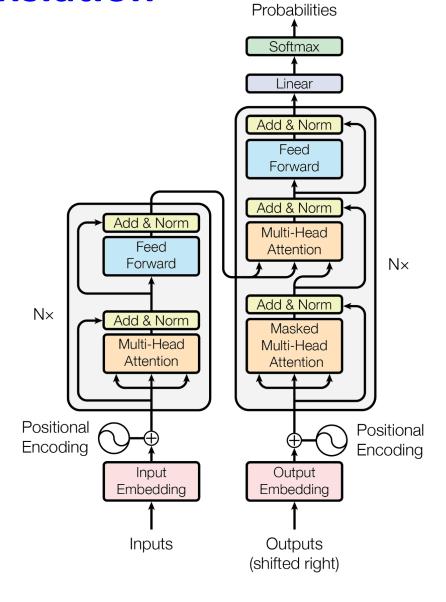
Targets

Ich have einen apfel gegessen



Inputs

I ate an apple

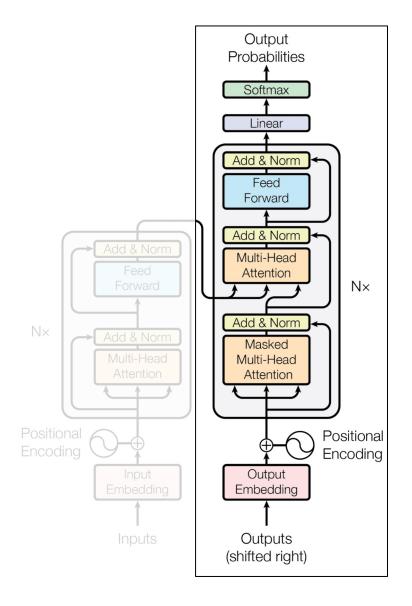


Output

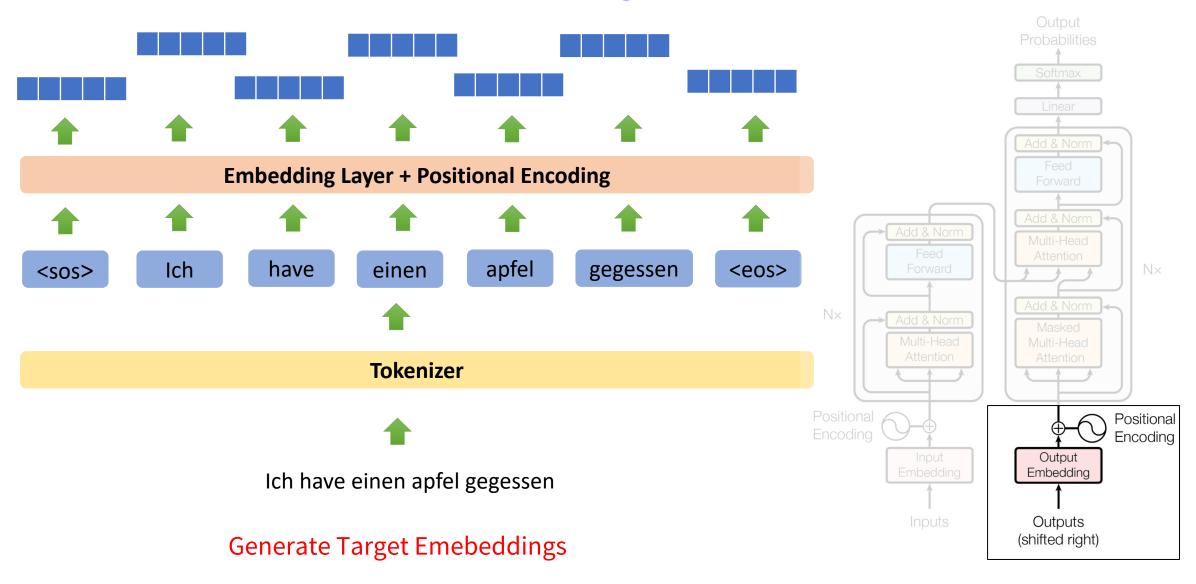
Targets

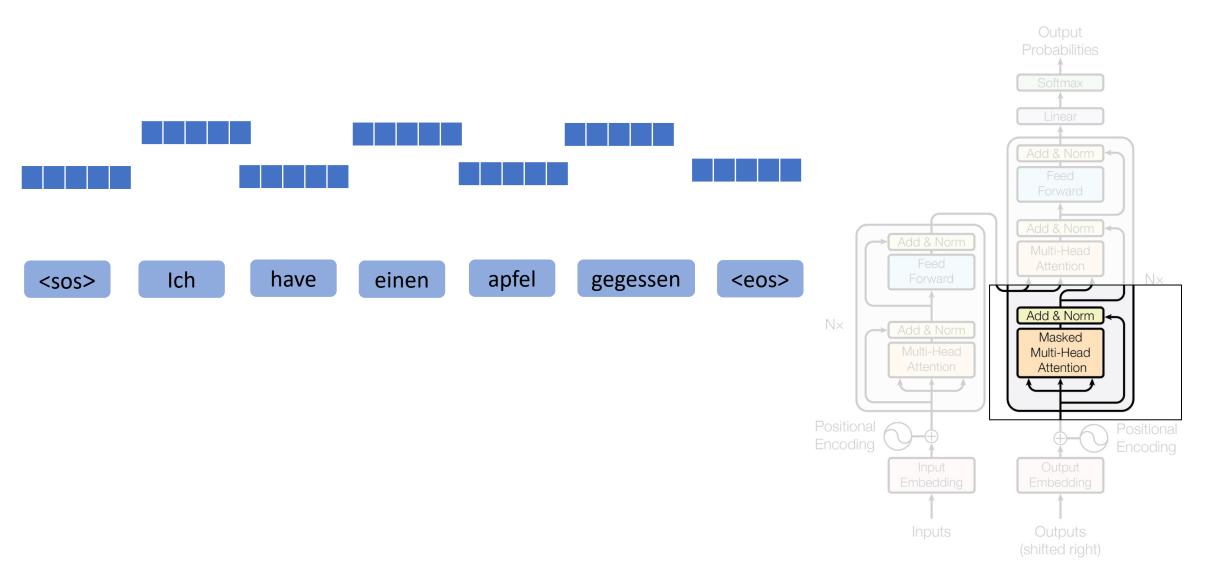
Targets

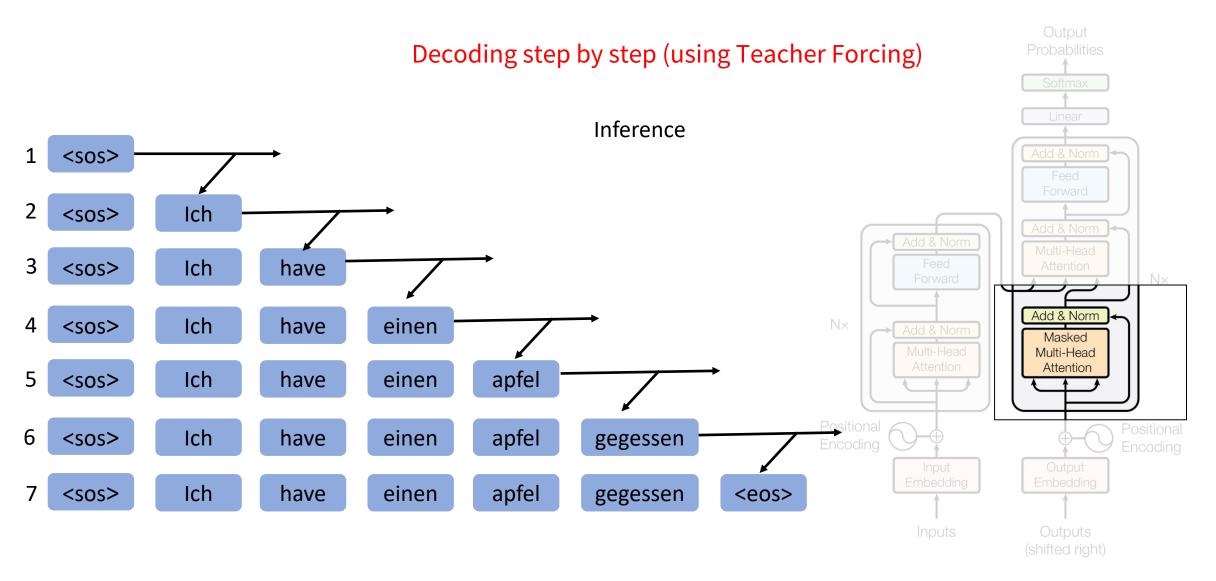
Ich have einen apfel gegessen

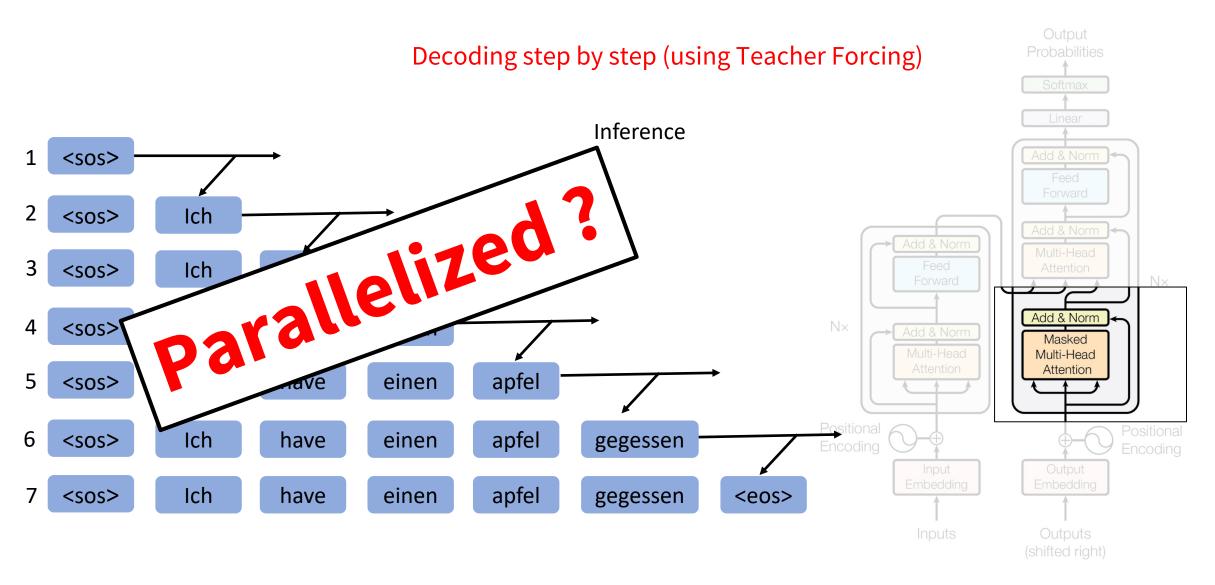


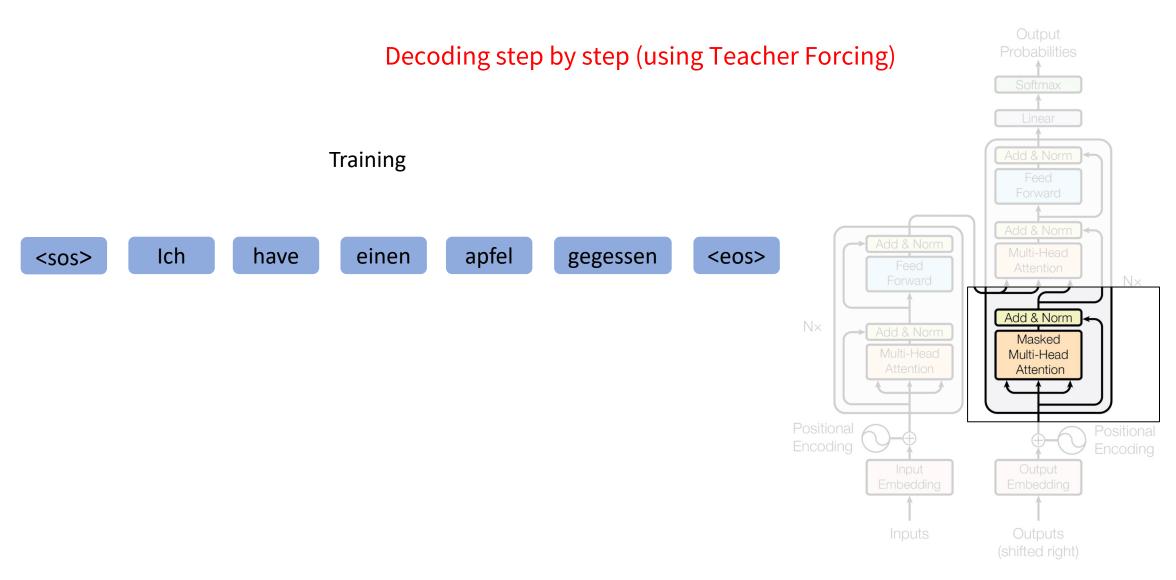
Targets

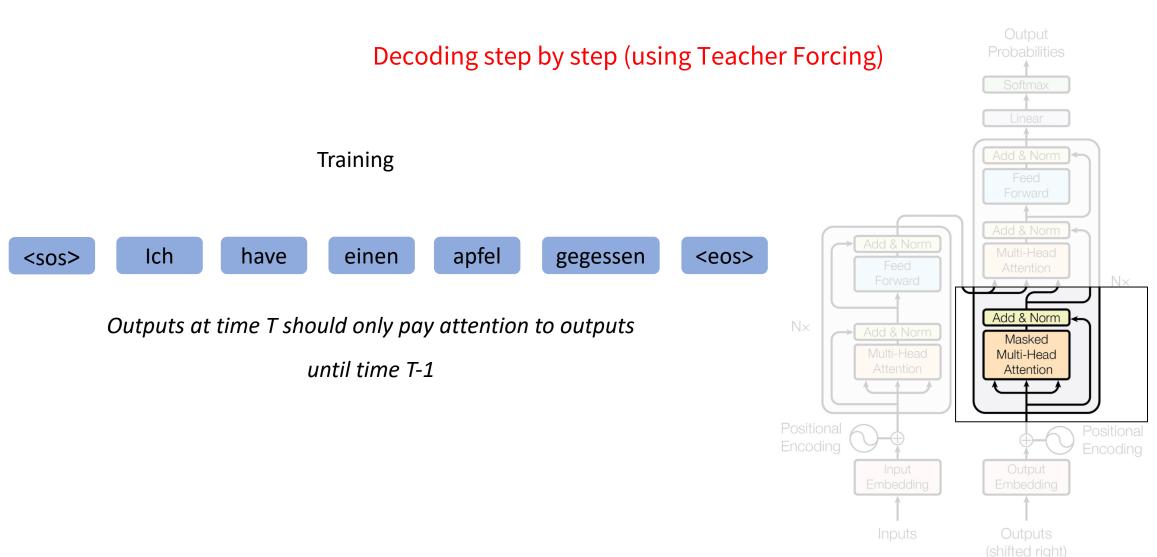


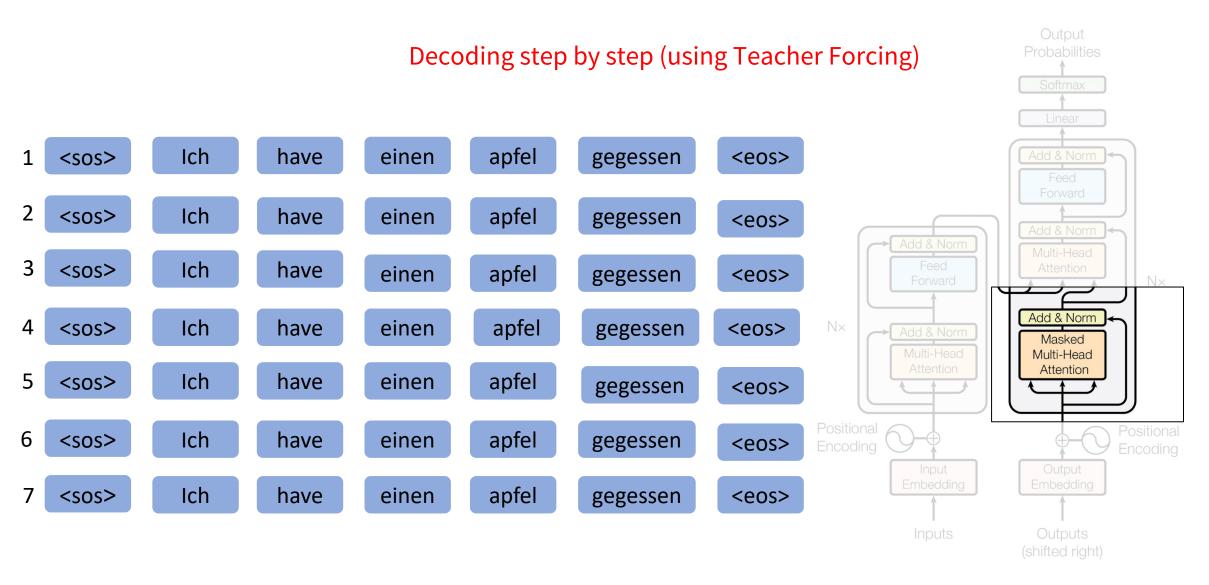


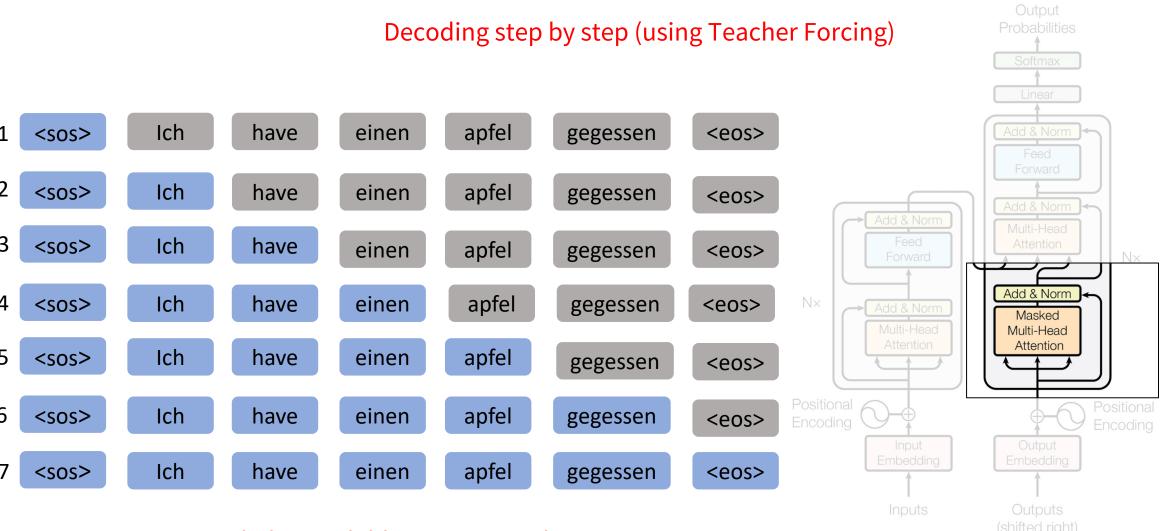




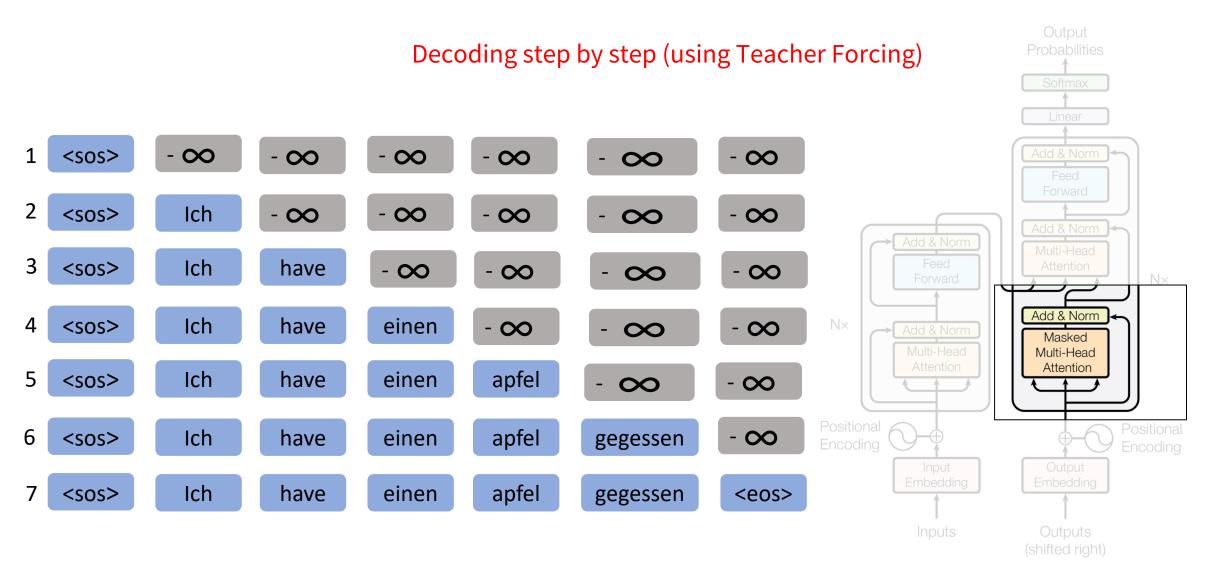


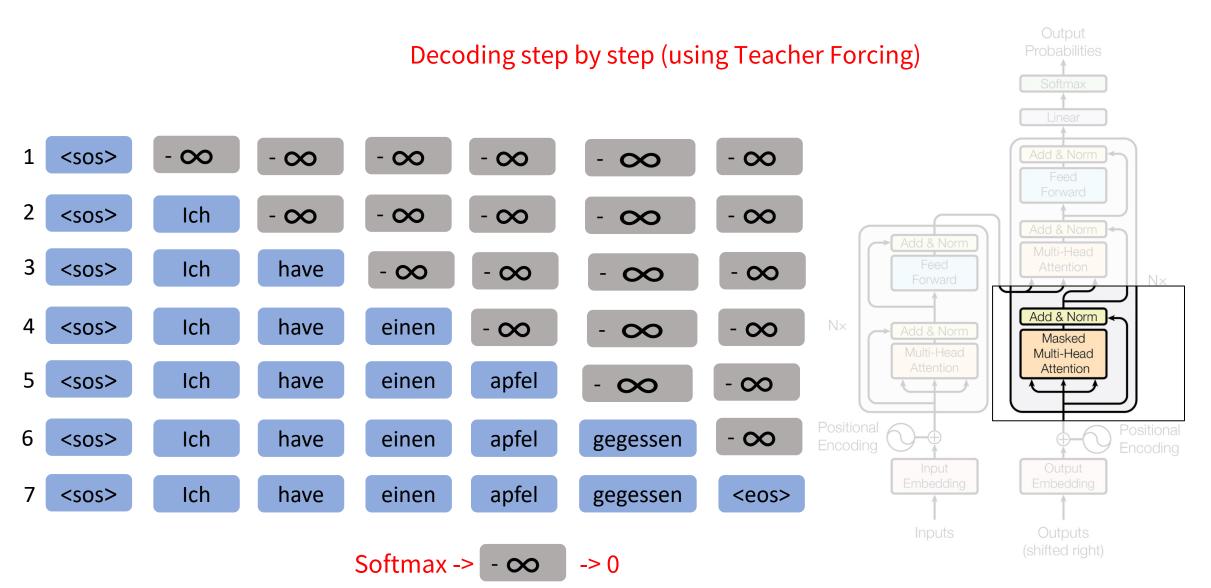


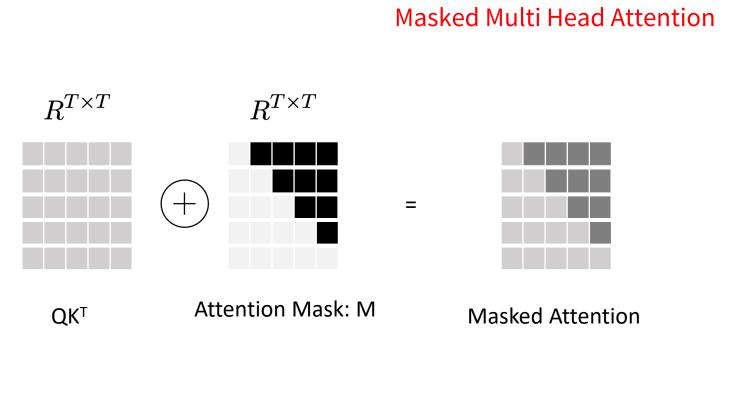


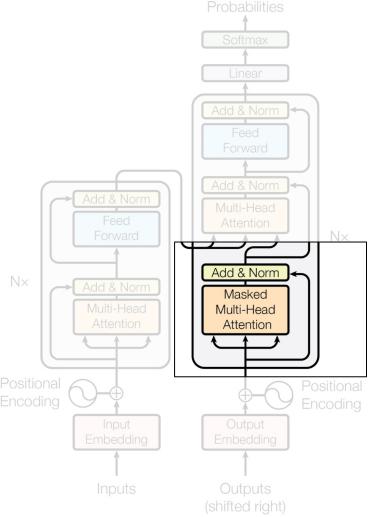


Mask the available attention values?

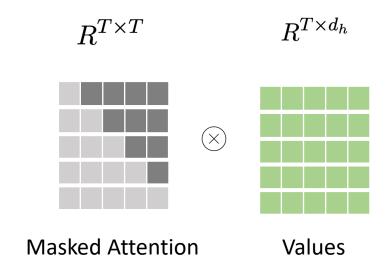


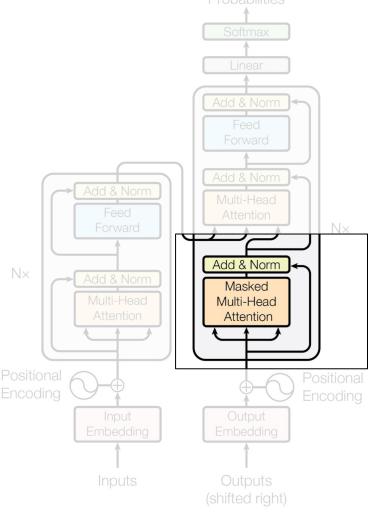




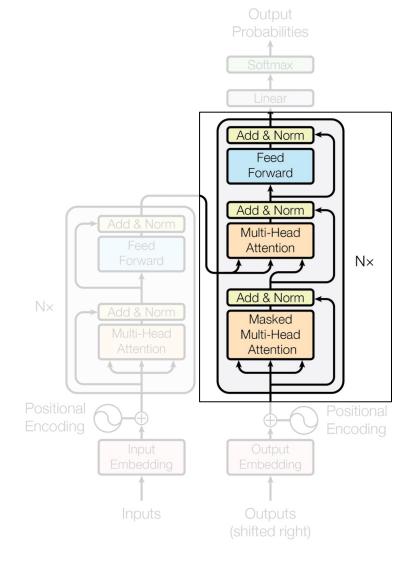




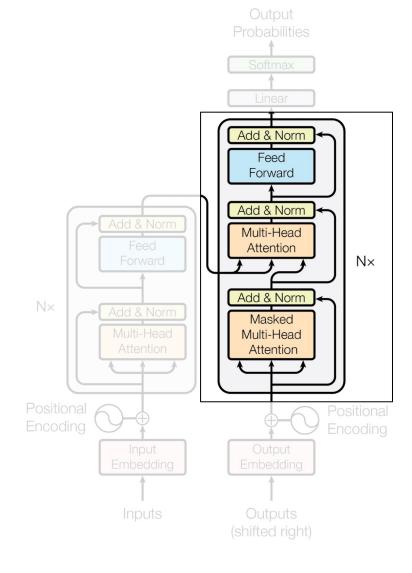




Encoder Decoder Attention ? Add & Norm



Encoder Decoder Attention?

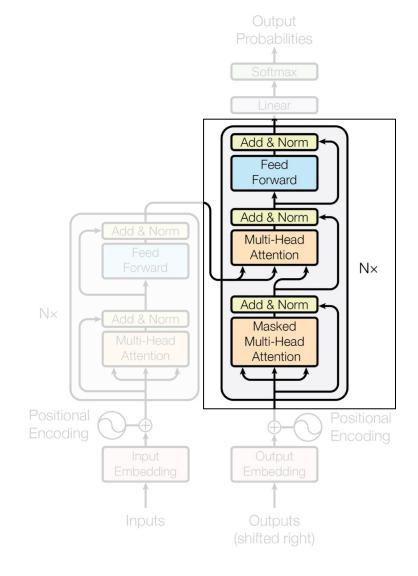


Encoder Self Attention

- 1. Queries from Encoder Inputs
- 2. Keys from Encoder Inputs
- 3. Values from Encoder Inputs

Decoder Masked Self Attention

- 1. Queries from Decoder Inputs
- 2. Keys from Decoder Inputs
- 3. Values from Decoder Inputs



Attention

{Key, Value store}

```
{Query: "Order details of order_104"}
```

{Query: "Order details of order_106"}

```
{"order_100": {"items":"a1", "delivery_date":"a2", ...}},
{"order_101": {"items":"b1", "delivery_date":"b2", ...}},
{"order_102": {"items":"c1", "delivery_date":"c2", ...}},
{"order_103": {"items":"d1", "delivery_date":"d2", ...}},
{"order_104": {"items":"e1", "delivery_date":"e2", ...}},
{"order_105": {"items":"f1", "delivery_date":"f2", ...}},
{"order_106": {"items":"g1", "delivery_date":"g2", ...}},
{"order_107": {"items":"h1", "delivery_date":"h2", ...}},
{"order_108": {"items":"i1", "delivery_date":"i2", ...}},
{"order_109": {"items":"j1", "delivery_date":"j2", ...}},
{"order_110": {"items":"k1", "delivery_date":"k2", ...}}
```

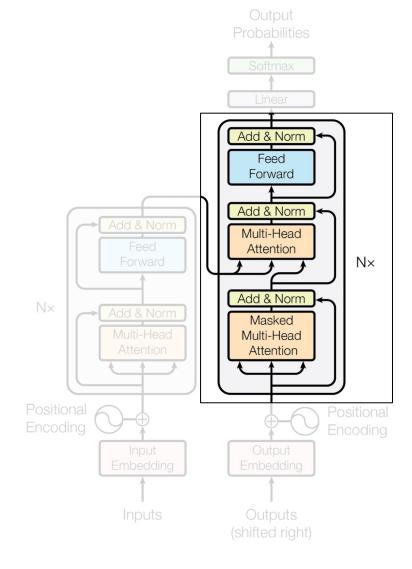
Encoder

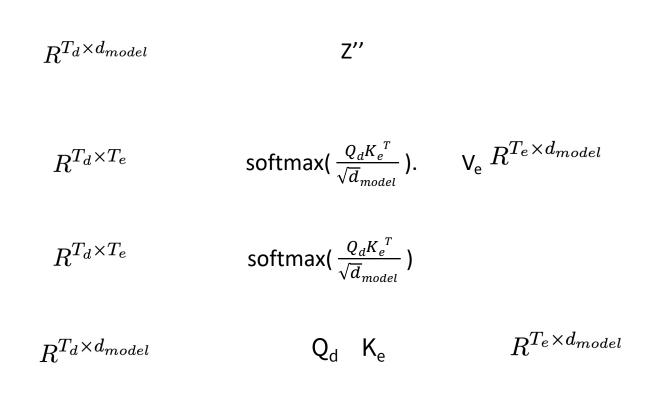
Decoder

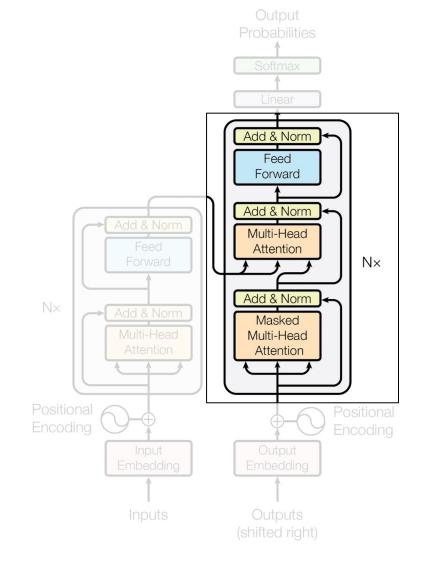
Keys from **Encoder Outputs**Values from **Encoder Outputs**

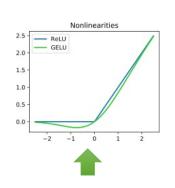
Queries from **Decoder Inputs**

NOTE: Every decoder block receives the same FINAL encoder output

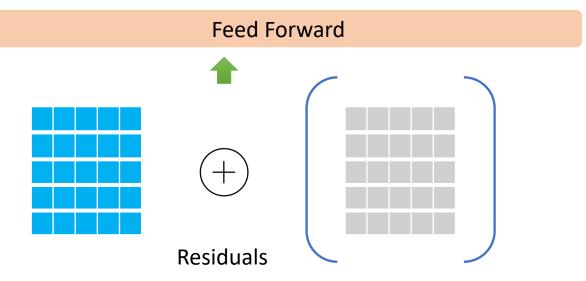


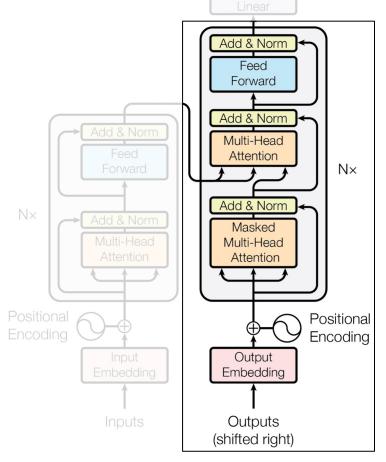






- Non Linearity
- Complex Relationships
- Learn from each other



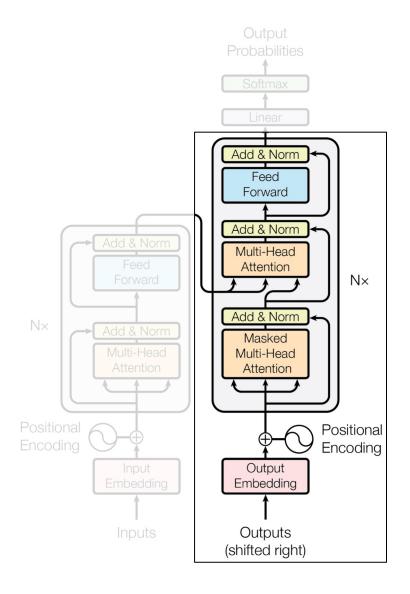


Add n Norm Decoder Self Attn

Norm(Z'')

Decoder

DECODER



Decoder

DECODER

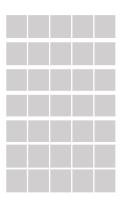
•

•

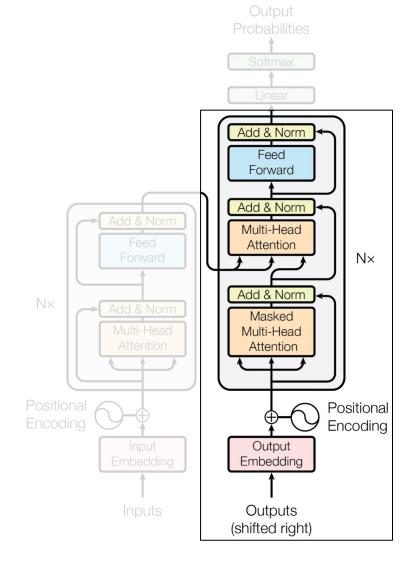
DECODER

DECODER

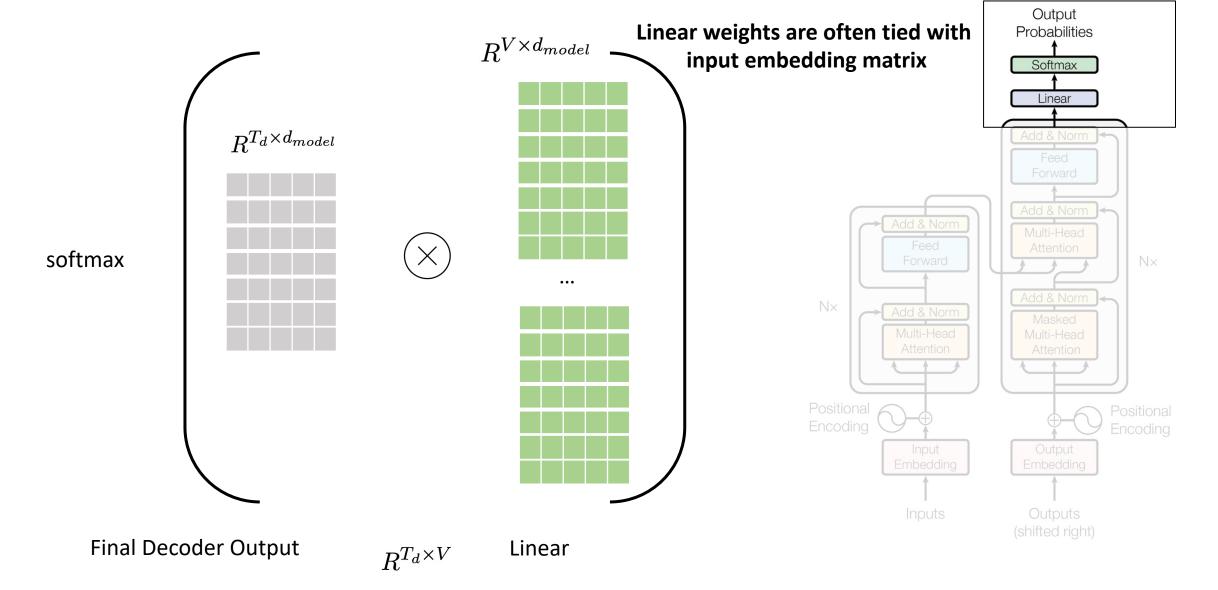
 $R^{T_d \times d_{model}}$



Decoder output

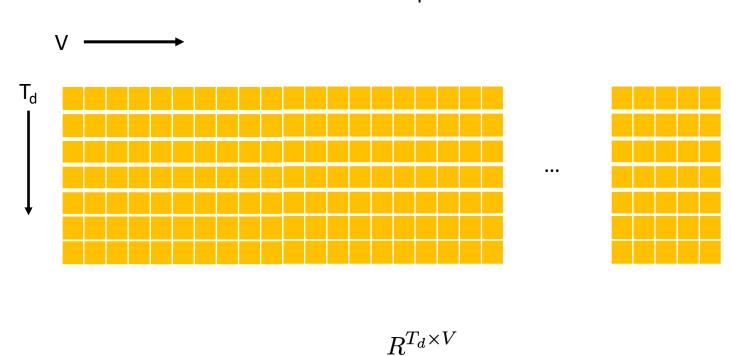


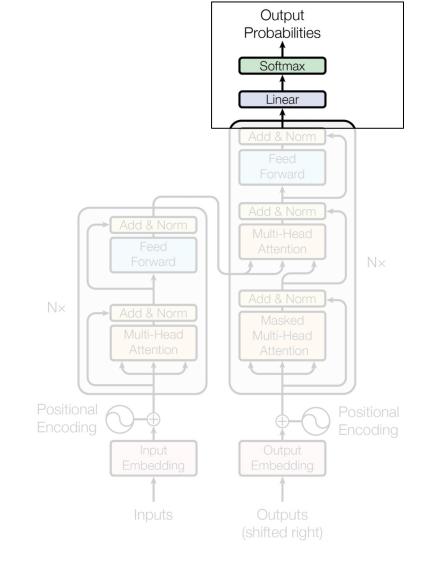
Linear



Softmax

Output Probabilities





Poll 2 (@1297)

Which of the following are true about transformers?

- a. Transformers can always be run in parallel
- b. Transformer decoders can only be parallelized during training
- c. Positional encodings help parallelize the transformer encoder
- d. Queries, keys, and values are obtained by splitting the input into 3 equal segments
- e. Multiheaded attention helps transformers find different kinds of relations between the tokens
- f. During decoding, decoder outputs function as queries and keys while the values come from the encoder

Poll 2 (@1126)

Which of the following are true about transformers?

- a. Transformers can always be run in parallel
- b. Transformer decoders can only be parallelized during training
- c. Positional encodings help parallelize the transformer encoder
- d. Queries, keys, and values are obtained by splitting the input into 3 equal segments
- e. Multiheaded attention helps transformers find different kinds of relations between the tokens
- f. During decoding, decoder outputs function as queries and keys while the values come from the encoder

Transformers

Targets

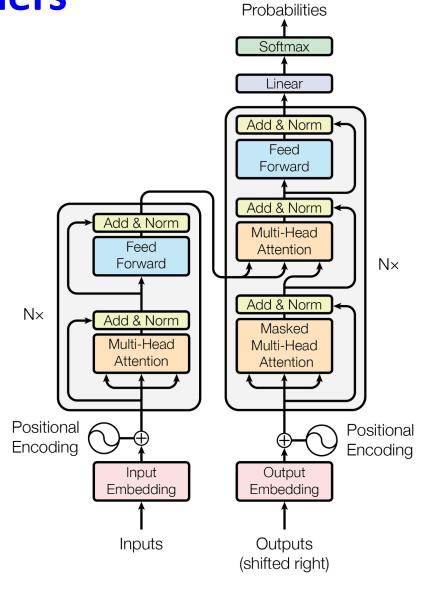
Ich have einen apfel gegessen



Inputs

I ate an apple

Machine Translation



Output

Transformers

- ✓ Tokenizaton
- ✓ Input Embeddings
- **✓ Position Encodings**
- ✓ Residuals
- ✓ Query
- ✓ Key
- ✓ Value
- ✓ Add & Norm
- ✓ Encoder
- ✓ Decoder

- ✓ Attention
- ✓ Self Attention
- ✓ Multi Head Attention
- ✓ Masked Attention
- ✓ Encoder Decoder Attention
- ✓ Output Probabilities / Logits
- ✓ Softmax
- Encoder-Decoder models
- Decoder only models

