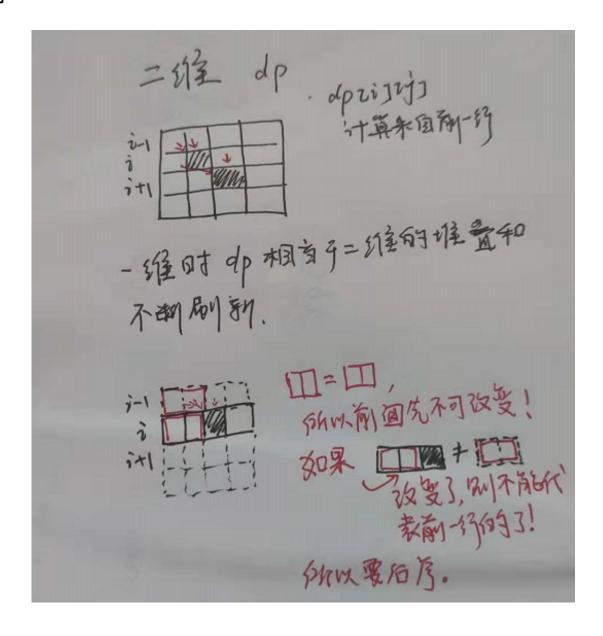
M

In [8]:

```
## 快速排序
 2
    quick_sort = lambda array: array if len(array) <= 1 else quick_sort([item for item in array[</pre>
3
                [array[0]]+quick sort([item for item in array[1:] if item > array[0]])
 4
 5
    # 快速排序 0(logn)
 6
    def quick sort(array):
 7
        if len(array) < 2:
8
            return array
9
        mid = array[len(array)//2]
10
        left, right = [], []
        array. remove (mid)
11
12
        for item in array:
13
            if item \geq = mid:
14
                right.append(item)
15
            else:
16
                left.append(item)
        return quick_sort(left)+[mid]+quick_sort(right)
17
18
    # 冒泡排序0(n^2)
19
20
    def bs(L):
21
        for i in range(len(L)):
22
            for j in range(i, len(L)):
23
                if L[i] > L[j]:
24
                    L[i], L[j] = L[j], L[i]
25
        return L
26
    # 插入排序 0(n<sup>2</sup>)-容易超时
27
28
    def insertionSort(arr):
29
        for i in range(len(arr)):
30
            preIndex = i-1
            current = arr[i] # 跟前面的比较
31
32
            while preIndex >= 0 and arr[preIndex] > current:
33
                arr[preIndex+1] = arr[preIndex]
34
                preIndex-=1
35
            arr[preIndex+1] = current # 此时满足条件
36
        return arr
37
38
    # 归并排序
39
    def sortArray(self, nums):
40
        temp = [0]*len(nums)
41
42
        def mergeSort(1, r):
            if 1 \ge r : return
43
44
            mid = (1+r) // 2
            mergeSort(1, mid)
45
            mergeSort (mid+1, r)
46
            i, j = 1, mid+1
47
            k = 0
48
49
            while i \le mid and j \le r:
50
                if nums[i] < nums[j]:</pre>
51
                    temp[k] = nums[i]
52
                    i += 1
53
                else:
54
                    temp[k] = nums[j]
55
                    j += 1
                k += 1
56
57
            while i <= mid:
```

```
58
                 temp[k] = nums[i]
59
                 i += 1
                 k += 1
60
            while j \le r:
61
62
                 temp[k] = nums[j]
63
                 j += 1
                 k += 1
64
            nums[1:r+1] = temp[:r-1+1]
65
66
        mergeSort(0, 1en(nums)-1)
67
        return nums
```

动态规划



In [2]:

```
## 0-1背包问题, 理论篇
1
2
   ## 二维
3
   W = 4
4
   wt = [2, 1, 3]
   va1 = [4, 2, 3]
5
6
   def knapsack2(W, wt, val):
7
       N = len(wt)
       dp = [[0]*(W+1) for in range(N+1)] # base case 已经初始化,填充多了一行
8
       # dp[i][j] 表示: 从0到i中选择,背包当前容量为j时的价值
9
10
       for i in range (1, N+1):
          for w in range (1, W+1):
11
              if w < wt[i-1]: # wt和val要取i-1才能对应上
12
13
                 dp[i][w] = dp[i-1][w] # 如果到一维情况,那么表示不变<math>dp[w]=dp[w]
14
                 dp[i][w] = max(dp[i-1][w], dp[i-1][w-wt[i-1]]+val[i-1])
15
16
       return dp[N][W]
17
   ## 一维
18
   ## dp 表示二维数组dp的i-1行,一维二维中dp[i]行只用到了dp[i-1]行的东西,所以可复用来更新
19
20
   ## 而必须后序更新是避免重复运用
21
   def knapsack1(W, wt, val):
22
23
       N = len(wt)
       dp = [0]*(W+1) # base case 已经初始化,填充多了一行
24
       # dp[j] 表示: 背包当前容量为j时的价值
25
26
       for i in range(N): # 从0开始
          for w in range (W, wt[i]-1, -1): # W-W-1-...-wt[i]
27
28
                 dp[w] = max(dp[w], dp[w-wt[i]]+val[i]) # 覆盖
29
       return dp[-1]
   knapsack2(W, wt, val) # 取第一个和第二个
30
```

Out[2]:

6

In []:

```
### 416 等分割子集
1
 2
   def canPartition( nums):
 3
       # 二维
 4
       sumnums = sum(nums)
 5
       if sumnums %2 != 0: return False # 先判断再处理
       n = len(nums)
 6
 7
       sumnums = int(sumnums/2)
8
       dp = [[False]*(sumnums+1) for _ in range(n+1)]
       for i in range(n+1): dp[i][0] = True # 背包装满了
 9
       for i in range(1, n+1):
10
           for j in range(1, sumnums+1):
11
               if j < nums[i-1]:
12
13
                   # 放不下
14
                   dp[i][j] = dp[i-1][j]
15
               else:
16
                   # 放得下,但是放还是不放
                   dp[i][j] = dp[i-1][j] \text{ or } dp[i-1][j-nums[i-1]]
17
       return dp[n][-1]
18
19
20
       #一维
21
22
       sumnums = sum(nums)
23
       n = 1en(nums)
24
       w = sumnums//2
       if sumnums \% 2 != 0:
25
           return False
26
27
       dp = [False] * (w+1)
28
       dp[0] = True
29
       for num in nums:
30
           for i in range (num, w+1) [::-1]:
                                           #不断更新在不同w情况下的dp
               dp[i] = dp[i] \text{ or } dp[i - num]
31
32
       return dp[w] # 定义为是否能放下该重量
33
34
       ## 套模板, 更容易理解
35
       # 背包大小sum//2, 物品的价值=物品的重量
36
       dp = [0]*(w+1)
37
38
       for i in range(n):
           for j in range (w, nums[i]-1, -1):
39
40
               # num[i]会大过背包重量,但是这是不会有任何操作
               dp[j] = max(dp[j], dp[j-nums[i]]+nums[i])
41
42
       return dp[w] == w
43
44
   # 1049 最后一块石头
   def lastStoneWeightII(stones):
45
46
       n = 1en(stones)
       target = sum(stones)//2
47
48
       dp = [0]*(target+1)
       for i in range(n):
49
50
           for j in range(target, stones[i]-1, -1):
51
               dp[j] = max(dp[j], dp[j-stones[i]]+stones[i])
52
       # (sum(stones)-dp[-1])-dp[-1] (一堆〈平均,一堆〉平均,具体为多少未知)
53
       return sum(stpnes)-2*dp[-1]
54
   # 494 目标和 改变数组元素的+-
55
   def findTargetSumWays(nums, target):
56
       # 公式推导可得,不变的排前,变负的排后
57
```

```
58
        # left-right=target, left+right=sum, left=(target+sum)/2
        #回溯, 不去重的组合求和III, 不去重相对于考虑了位置——超时
59
        # 和全排列不同——不要求全部加入(拿捏不准要多少个元素)。
60
        # 和组合求和III(有重复,但不可复用自己(同),但是不考虑顺序)不同,要求考虑位置。
61
        # 动态规划
62
        # 背包容量target, nums[i]即重量和价值,重量和<=target
63
64
        Sum = sum(nums)
        if target > Sum: return 0
65
66
        target, m = (target+Sum)//2, (target+Sum)%2
67
        if m != 0: return 0
        dp = [0]*(target+1)
68
69
        dp[0] = 1
        for i in range(len(nums)):
70
71
            for j in range(target, nums[i]-1,-1):
                dp[j] += dp[j-nums[i]]
72
        return dp[-1]
73
74
    # 474 0和1, 不可复用
75
    def findMaxForm(strs, m, n):
76
77
        # 二维背包问题, n:1行m:0列
        if len(strs) == 0:
78
79
            return 0
        dp = [[0] * (m+1) for _ in range(n+1)]
80
81
        for str in strs:
            # 外物
82
83
            count_0 = str_.count('0')
84
            count 1 = str.count('1')
85
            # for i in range(start, end, 步长)
            # 0-1背包放反序, 内包
86
            for i in range (n, count 1-1, -1):
87
88
                for j in range (m, count 0-1, -1):
                    dp[i][j] = max(dp[i][j], dp[i-count_1][j-count_0]+1)
89
90
        return dp[n][m]
91
92
93
    # 完全背包
94
    # 518 零钱兑换II
95
96
    def change (amount, coins):
        # 完全背包
97
98
        dp = [0]*(amount+1)
99
        dp[0] = 1
        for i in range(len(coins)):
100
            for j in range(coins[i], amount+1):
101
                dp[j] += dp[j-coins[i]]
102
        return dp[-1]
103
104
    # 377 组合总和IV
105
106
    def combinationSum4(nums, target):
        dp = [0]*(target+1)
107
108
        dp[0]=1
109
        for i in range(1, target+1): # 背包
110
            for j in range(len(nums)): #物
                if i \ge nums[j]:
111
                   dp[i] += dp[i-nums[i]]
112
113
        return dp[-1]
114
    # 70爬楼梯 排列数
115
    def climbStairs(self, n: int) -> int:
116
        dp = [0]*(n + 1)
117
118
        dp[0] = 1
```

```
119
         m = 2
120
         for j in range (n + 1):
121
             # 遍历背包
122
            for step in range (1, m + 1):
123
                 # 遍历物品
124
                 if j \ge step:
125
                     dp[j] += dp[j - step]
126
         return dp[n]
127
     # 322 零钱兑换I,完全背包,摆列组合都可以
128
129
     def coinChange(coins, amount):
         dp = [amount+1]*(amount+1)
130
         0 = \lceil 0 \rceil db
131
         # for i in range(1, amount+1):
132
133
               for coin in coins:
                  if i < coin: continue
134
135
                   dp[i] = min(dp[i], dp[i-coin]+1) # 记得加一
         # return dp[-1] if dp[-1] \le amount else -1
136
         for coin in coins:
137
138
             for i in range (coin, amount+1):
                 # 少了一行判断
139
140
                 dp[i] = min(dp[i], dp[i-coin]+1) # 记得加一
         return dp[-1] if dp[-1] \le amount else -1
141
142
     # 279 完全平方数
143
144
     def numSquares(n):
         # 完全背包,正序
145
146
         # 最少个数,组合排列都可以
         nums = [i**2 for i in range(1, n + 1) if i**2 <= n] # 构造物
147
         dp = [10**4]*(n+1)
148
149
         dp[0] = 0
         for i in range(len(nums)):
150
151
             for j in range(nums[i], n+1):
                 dp[j] = min(dp[j], dp[j-nums[i]]+1)
152
153
         return dp[-1]
154
     # 单词拆分一
155
     def wordBreak(s, wordDict):
156
157
         n = len(s)
         dp = [False]*(n+1)
158
159
         dp[0] = True
         for i in range(1, n+1):
160
             for word in wordDict:
161
162
                 lenw = len(word)
163
                 if lenw \le i and word == s[i-lenw:i]:
                     dp[i] = dp[i] \text{ or } dp[i-lenw]
164
         return dp[n]
165
166
167
     # 198 打家劫舍 I
168
     def rob(self, nums: List[int]) -> int:
169
         if nums == []:
170
171
            return 0
172
         n = 1en(nums)
173
         dp = [0]*(n+2)
174
         for i in range (2, n+2):
175
             dp[i] = max(dp[i-1], dp[i-2] + nums[i-2])
176
         return dp[-1]
177
178
     # 213 打家劫舍II
179
     def rob(self, nums: List[int]) -> int:
```

```
if nums == []:
180
181
             return 0
         if len(nums) == 1:
182
             return nums[0]
183
         def robsub(nums):
184
             if nums == []:
185
                return 0
186
             n = 1en(nums)
187
188
             dp = [0]*(n+2)
             for i in range (2, n+2):
189
190
                 dp[i] = max(dp[i-1], dp[i-2] + nums[i-2])
191
             return dp[-1]
         return max( robsub(nums[1:]), robsub(nums[:-1]) )
192
193
     # 337 打家劫舍III
194
     class Solution:
195
196
         # rember
         rob_dict = {}
197
         def rob(self, root: TreeNode) -> int:
198
199
             if not root:
                 # root == None
200
                return 0
201
202
             if root in self.rob_dict.keys():
                 return self.rob_dict[root]
203
204
             if not root. left and not root. right:
                 # 到达这个点在犹豫,没有跳过,那么直接取是最大的
205
206
                 self.rob dict[root] = root.val
207
                 return root.val
             # 如果都不是,那么必然存在左子树或右子树
208
209
             get = root.val
210
             if root.right:
211
                 get += self.rob(root.right.right)+self.rob(root.right.left)
212
             if root.left:
213
                 get += self.rob(root.left.right)+self.rob(root.left.left)
214
             not_get = self.rob(root.left)+self.rob(root.right)
215
             res = max(get, not get)
             self.rob_dict[root] = res
216
217
             return res
```

In [3]:

```
### 多重背包理论篇-->转成0-1背包问题
2
    def multi_pack1(weight, values, nums, bag_weight):
3
        # 将物品展开,将nums消除掉
4
        for i in range(len(nums)):
            while nums[i]:
5
6
                weight.append(weight[i])
7
                value.append(value[i])
8
                nums[i] = 1
9
        dp = [0]*(bag_weight+1)
10
        for i in range(len(weight)):
            for j in range(bag_weight, weight[i]-1,-1):
11
                dp[j] = max(dp[j], dp[j-weight[i]]+value[i])
12
        print(" ".join(map(str, dp)))
13
14
    weight = [1, 3, 4]
15
    values = [15, 20, 30]
16
    nums = [2, 3, 2]
17
18
    bag weight = 10
19
    multi_pack1(weight, values, nums, bag_weight)
```

 $0\ 15\ 30\ 45\ 45\ 50\ 65\ 75\ 75\ 85\ 95$

H

Stock

```
In [ ]:
```

```
1
    # dp[i][j] 表示第i天利润
 2
    #### 121 一次买入,一次卖出,同一天买卖没有收益,k=1
 3
    def maxProfit(self, prices: List[int]) -> int:
 4
 5
       # dp[i][j] i 表示 天数, j 表示 1持有 or 0出售
 6
       n = len(prices)
 7
       dp = [[0]*2 \text{ for i in range(n)}]
       dp[0][0] = 0
 8
 9
       dp[0][1] = -prices[0] # 现金流
10
       for i in range (1, n):
           dp[i][0] = max(dp[i-1][0], dp[i-1][1]+prices[i]) # 手头没有股票: 1. 一直没有 2. 刚卖
11
12
           dp[i][1] = max(dp[i-1][1],-prices[i]) # 手头有股票: 1. 一直有 2. 刚买,前面没有利润
13
       return dp[-1][0]
14
    #### 122 多次买卖 k = +inf
15
    def maxProfit(self, prices: List[int]) -> int:
16
       # 捕获上坡那一段即可, 贪心
17
18
       res = 0
       for i in range(1, len(prices)):
19
20
           res += max(prices[i]-prices[i-1], 0)
21
       return res
22
23
       # 动态规划, 0表示不持有, 1表示持有
24
       n = len(prices)
25
       dp = [[0]*2 \text{ for } \underline{\quad} \text{ in range (n)}]
26
         dp[0][0] = 0
27
       dp[0][1] = -prices[0]
28
       for i in range (1, n):
29
           dp[i][0] = max(dp[i-1][0], dp[i-1][1]+prices[i]) # 不持有(以前没有or刚卖)
30
           dp[i][1] = max(dp[i-1][1], dp[i-1][0]-prices[i]) # 持有(以前有or刚买)
       return dp[-1][0]
31
32
       # dp 加滚动数组
33
34
       n = len(prices)
35
       dp = [[0]*2 for _ in range(2)] # 空间压缩
36
         dp[0][0] = 0
       dp[0][1] = -prices[0]
37
38
       for i in range (1, n):
           dp[i\%2][0] = max(dp[(i-1)\%2][0], dp[(i-1)\%2][1]+prices[i]) # 不持有(以前没有or刚卖)
39
           dp[i%2][1] = max(dp[(i-1)%2][1], dp[(i-1)%2][0]-prices[i]) # 持有(以前有or例买)
40
       return dp[(n-1)\%2][0]
41
42
    #### 123 两次买卖 k=2
43
44
    def maxProfit(self, prices: List[int]) -> int:
       # 5种状态,0 没有操作 1 第一次买入 2 第一次卖出 3 第二次买入 4 第二次卖出
45
       n = 1en(prices)
46
47
       if n == 0: return 0
       dp = [[0]*5 \text{ for i in range}(n)]
48
49
       dp[0][1] = -prices[0]
50
       dp[0][3] = -prices[0] # 在第0天已经做了一次买卖,但是0收益(同一天买卖了)
51
       for i in range (1, n):
           # dp[i][0] = dp[i-1][0] # 没操作
52
           dp[i][1] = max(dp[i-1][0]-prices[i], dp[i-1][1]) # 保持 or 之前没有刚第一次买
53
           dp[i][2] = max(dp[i-1][1]+prices[i], dp[i-1][2]) # 保持 or 之前有刚第一次卖
54
55
           dp[i][3] = max(dp[i-1][2]-prices[i], dp[i-1][3]) # 保持 or 之前没有刚第二次买
           dp[i][4] = max(dp[i-1][3]+prices[i], dp[i-1][4]) # 保持 or 之前有刚第二次卖
56
57
       return dp[-1][4]
```

```
58
   #### 188 k次买卖——思路来源于123 k = any int
59
   def maxProfit(self, k: int, prices: List[int]) -> int:
60
61
       # 观察两次买卖
62
63
       n = 1en(prices)
       if n == 0: return 0
64
       dp = [[0]*(2*k+1) \text{ for i in range(n)}]
65
66
       for j in range (1, 2*k, 2):
           dp[0][j] = -prices[0] # 在第0天已经做了一次买卖,但是0收益(同一天买卖了)
67
       for i in range (1, n):
68
           for j in range (1, 2*k, 2):
69
               dp[i][j] = max(dp[i-1][j-1]-prices[i], dp[i-1][j]) # 保持 or 之前没有刚第一次买
70
               dp[i][j+1] = max(dp[i-1][j]+prices[i], dp[i-1][j+1]) # 保持 or 之前有刚第一次卖
71
               # dp[i][3] = max(dp[i-1][2]-prices[i], dp[i-1][3]) # 保持 or 之前没有刚第二次买
72
73
               # dp[i][4] = max(dp[i-1][3]+prices[i], dp[i-1][4]) # 保持 or 之前有刚第二次卖
74
       return dp[-1][2*k]
75
76
   #### 309 k = +inf and cold -- 把122中的dp[i-1][0]-prices[i]改成dp[i-2][0]-prices[i]即可
77
   def maxProfit(self, prices: List[int]) -> int:
       n = len(prices)
78
       dp = [[0]*2 for _ in range(n)]
79
       dp[0][1] = -prices[0]
80
81
       for i in range (1, n):
           dp[i][0] = max(dp[i-1][0], dp[i-1][1]+prices[i]) # 不持有(以前没有or刚卖)
82
           dp[i][1] = max(dp[i-1][1], dp[i-2][0]-prices[i]) # 持有(以前有or刚买)
83
84
       return dp[-1][0]
85
86
87
   #### 714
   def maxProfit(self, prices: List[int], fee: int) -> int:
88
89
       n = 1en(prices)
       dp = [[0]*2 for _ in range(n)]
90
       dp[0][1] = -prices[0]
91
       for i in range (1, n):
92
           dp[i][0] = max(dp[i-1][0], dp[i-1][1]+prices[i]-fee) # 122中多减去一个手续费
93
           dp[i][1] = max(dp[i-1][1], dp[i-1][0]-prices[i])
94
95
       return dp[-1][0]
```

3/33~

```
In [ ]:
```

```
1
   #### 300 最长递增子序列
 2
   def lengthOfLIS(self, nums: List[int]) -> int:
 3
       n = 1en(nums)
       dp = [1]*n #dp[i] 表示以i结尾的最长子序列长度
 4
       for i in range(1, n):
 5
 6
           for j in range(i):
               if nums[i] > nums[j]: # 符合递增, 找前面比他小的数的dp+1
 7
8
                   dp[i] = max(dp[i], dp[j]+1) # 一直找一直找
       return max(dp)
 9
10
   #### 674 最长递增子串
11
    def findLengthOfLCIS(self, nums: List[int]) -> int:
12
13
       n = 1en(nums)
14
       dp = [1]*n #dp[i] 表示以i结尾的最长子串长度
15
       for i in range (n-1):
           if nums[i+1] > nums[i]:
16
               dp[i+1] = dp[i]+1
17
18
       return max(dp)
19
20
   #### 718 最长重复子串
21
   def findLength(self, nums1: List[int], nums2: List[int]) -> int:
22
       # 子串
       n = 1en(nums1)
23
24
       m = 1en(nums2)
25
       res = 0
26
       dp = [[0]*(m+1) for in range(n+1)] # 以i-1为结尾的nums1,以j-1为结尾的nums2的最长重复子
27
       for i in range (1, n+1):
28
           for j in range(1, m+1):
29
               if nums1[i-1] == nums2[j-1]: # 错位对齐
                   dp[i][j] = dp[i-1][j-1]+1 # 不相等即为0
30
               res = max(res, dp[i][j])
31
32
       return res
33
   #### 1143 最长公共子序列
34
35
   def longestCommonSubsequence(self, text1: str, text2: str) -> int:
36
       m = 1en(text1)
37
       n = 1en(text2)
38
       if n == 0 or m == 0:
           {\tt return}\ 0
39
40
       dp = [[0]*(n+1) for _ in range(m+1)] # 定义二维dp table # 以i-1为结尾的text1,以j-1为结
       for i in range(1, m+1): # i, j对应谁要对应上
41
           for j in range(1, n+1):
42
               if text1[i-1] == text2[j-1]:
43
                   dp[i][j] = dp[i-1][j-1]+1
44
45
               else:
46
                   dp[i][j] = max(dp[i-1][j], dp[i][j-1])
47
       return dp[-1][-1]
48
49
50
   ### 53 最大子序号, 贪心的另一种解法
51
   def maxSubArray(self, nums: List[int]) -> int:
52
       n = 1en(nums)
53
       dp = [0]*n
       dp[0] = nums[0]
54
55
       for i in range (1, n):
           dp[i] = max(dp[i-1]+nums[i], nums[i])
56
       return max(dp)
57
```

```
58
     ### 392 判断子序列,有顺序,不能用hashmap表
59
60
     def isSubsequence(self, s: str, t: str) -> bool:
61
         # 双指针
62
         p1, p2 = 0, 0
         while p1 < len(s) and p2 < len(t):
63
64
             if s[p1] == t[p2]:
65
                 p1 += 1
             p2 += 1
66
67
         if pl == len(s): return True # pl 最终会跳到len(s)
68
         return False
69
         # 动态规划解法
70
71
         n = len(s)
72
         m = len(t)
         dp = \lceil \lceil 0 \rceil * (m+1) \text{ for in range} (n+1) \rceil
73
74
         for i in range(1, n+1):
75
             for j in range (1, m+1):
                 if s[i-1] == t[j-1]:
76
77
                     dp[i][j] = dp[i-1][j-1]+1
78
                 else:
79
                     dp[i][j] = dp[i][j-1]
         return dp[-1][-1] == n
80
81
82
     ### 115 不同的序列
83
84
     def numDistinct(self, s: str, t: str) -> int:
85
         # t 是字典
         n = len(s)
86
         m = len(t)
87
88
         dp = [[0]*(m+1) \text{ for in } range(n+1)]
         for i in range (n+1):
89
90
             dp[i][0] = 1
         for j in range(1, m+1):
91
             dp[0][j] = 0
92
         for i in range (1, n+1):
93
94
             for j in range (1, m+1):
                 if s[i-1] == t[j-1]:
95
96
                     # 删除这一个可能存在匹配个数,不加入
97
                     dp[i][j] = dp[i-1][j-1] + dp[i-1][j]
98
                 else:
                     # 不加入这一个
99
                     dp[i][j] = dp[i-1][j]
100
101
         return dp[-1][-1]
102
     #### 583 两个字符串的删除
103
     def minDistance(self, word1: str, word2: str) -> int:
104
         n = 1en(word1)
105
106
         m = 1en(word2)
         dp = [[0]*(m+1) for _ in range(n+1)]
107
108
         for i in range (n+1):
109
             dp[i][0] = i
110
         for j in range (1, m+1):
             dp[0][j] = j
111
         for i in range (1, n+1):
112
113
             for j in range (1, m+1):
114
                 if word1[i-1] == word2[j-1]:
                     dp[i][j] = dp[i-1][j-1]
115
116
                     dp[i][j] = min(dp[i-1][j]+1, dp[i][j-1]+1, dp[i-1][j-1]+2) # 下标-1 为删除操作
117
         return dp[-1][-1]
118
```

```
119
120
     #### 72 编辑距离
121
     def minDistance(self, word1: str, word2: str) -> int:
122
         n = len(word1)
123
         m = 1en(word2)
         dp = [[0]*(m+1) for _ in range(n+1)]
124
125
         for i in range (n+1):
             dp[i][0] = i
126
         for j in range(m+1):
127
             dp[0][j] = j
128
         for i in range(1, n+1):
129
130
             for j in range (1, m+1):
                 if word1[i-1] == word2[j-1]: # word和dp错位一格
131
                     dp[i][j] = dp[i-1][j-1]
132
133
                 else:
                     dp[i][j] = min(dp[i-1][j]+1, dp[i][j-1]+1, dp[i-1][j-1]+1)
134
135
         return dp[-1][-1]
136
     #### 647 回文子串
137
138
     def countSubstrings(self, s: str) -> int:
139
         result = 0
         n = 1en(s)
140
         dp = [[False]*n for _ in range(n)]
141
142
         for i in range (n-1, -1, -1):
143
             for j in range(i, n):
144
                 if s[i] == s[j]:
145
                     if j-i \le 1:
                         dp[i][j] = True
146
147
                         result += 1
                     elif dp[i+1][j-1]:
148
149
                         dp[i][j] = True
150
                         result += 1
151
         return result
152
     #### 516 最长回文子串
153
     def longestPalindromeSubseq(self, s: str) -> int:
154
155
         n = 1en(s)
         dp = [[0]*n for in range(n)]
156
157
         for i in range(n):
             dp[i][i] = 1
158
159
         for i in range (n-1, -1, -1):
160
             for j in range (i+1, n):
                 if s[i] == s[j]:
161
                     dp[i][j] = dp[i+1][j-1]+2
162
163
                 else:
                     dp[i][j] = max(dp[i+1][j], dp[i][j-1])
164
         return dp[0][-1]
165
166
167
     #### 高楼扔鸡蛋
168
169
     def superEggDrop(self, k: int, n: int) -> int:
170
         # 单纯备忘录超出时间限制
171
         memo = \{\}
172
         def dp(k, n):
173
             if k == 1: return n
             if n == 0: return 0
174
175
             if (k, n) in memo. keys():
                 return memo[(k,n)]
176
             res = float('inf')
177
             \# for i in range (1, n+1):
178
                   # 这种属于线性搜索, 让i 从0 开始到n
179
```

```
180
                    res = \min(\text{res}, \max(\text{dp}(k, n-i), \text{dp}(k-1, i-1))+1) # res = \min(\text{res}, \max(\overline{P}, \overline{P})+1)
              # 替换为二分搜索, 就是将i->(0, n) 变成->(mid)
181
              1o = 1; hi = n
182
              while lo <= hi:
183
                  # 通过循环不断的改变mid
184
                  mid = 1o+(hi-1o)//2
185
                  broken = dp(k-1, mid-1)
186
                  not_broken = dp(k, n-mid)
187
188
                  if broken > not_broken:
                      hi = mid -1 # mid相当于i
189
190
                      res = min(res, broken+1)
191
192
                      lo = mid + 1 # mid相当于i
193
                      res = min(res, not_broken+1)
194
              memo[(k, n)] = res
195
              return res
196
         return dp(k, n)
197
198
         # 换定义
         dp = [[0]*(n+1) for _ in range(k+1)]
199
200
         m = 0
201
         while dp[k][m] < n:
             m += 1
202
203
             for i in range (1, k+1):
                  dp[i][m] = dp[i][m-1] + dp[i-1][m-1] + 1
204
205
         {\tt return}\ {\tt m}
```



In []:

```
1
    #### 739 每日温度
 2
    def dailyTemperatures(self, temperatures: List[int]) -> List[int]:
 3
        #单调栈
 4
        n = len(temperatures)
 5
        res = [0]*n # 存放结果
 6
        stack = [] # 存放索引而并非元素值stack
 7
        for i in range (n-1, -1, -1):
 8
            while s and temperatures[stack[-1]] <= temperatures[i]:
 9
                stack.pop()
10
            res[i] = 0 if not stack else stack[-1]-i
            stack.append(i)
11
12
        return res
13
14
    #### 下一个更大的数
    def nextGreaterElements(self, nums: List[int]) -> List[int]:
15
16
        n = 1en(nums)
        res = [0]*n
17
        stack = []
18
19
        for i in range (n-1, -1, -1):
20
            while stack and stack[-1] \le nums[i]:
21
                stack. pop()
22
            res[i] = -1 if not stack else stack[-1]
23
            stack.append(nums[i])
24
        return res
25
    #### 503 循环数组,下一个更大的元素
26
27
    def nextGreaterElements(self, nums: List[int]) -> List[int]:
28
        n = 1en(nums)
29
        res = [0]*n
30
        stack = []
        for i in range (2*n-1, -1, -1):
31
32
            while stack and stack[-1] \le nums[i\%n]:
                stack.pop()
33
            res[i\%n] = -1 \text{ if not stack else stack}[-1]
34
35
            stack.append(nums[i%n])
36
        return res
37
38
    #### 42 接雨水
39
    def trap(self, height: List[int]) -> int:
40
        # 暴力求解 (319/320) 0(N<sup>2</sup>)
41
42
        n = 1en(height)
43
        res = 0
44
        for i in range (1, n-1):
            leftmax, rightmax = 0, 0
45
            for j in range(i, n):
46
47
                rightmax = max(rightmax, height[j])
            for j in range (i, -1, -1):
48
49
                leftmax = max(leftmax, height[j])
50
            res += min(leftmax, rightmax)-height[i]
51
        return res
52
        #暴力+备忘录(dp全部算完)0(N)
53
54
        n = len(height)
        if n == 0: return 0
55
        res = 0
56
57
        leftmax = [0]*n
```

```
58
        rightmax = [0]*n
        leftmax[0] = height[0]
59
        rightmax[-1] = height[-1]
60
        for i in range (1, n):
61
            leftmax[i] = max(height[i], leftmax[i-1])
62
63
        for i in range (n-2, -1, -1):
            rightmax[i] = max(height[i], rightmax[i+1])
64
        for i in range(1, n-1):
65
66
            res += min(leftmax[i], rightmax[i])-height[i]
67
        return res
68
        # 双指针
69
70
        if not height: return 0
71
        n = 1en(height)
72
        left, right = 0, n-1
73
        res = 0
74
        leftmax, rightmax = height[0], height[-1]
75
        while left <= right:
76
            leftmax = max(leftmax, height[left])
77
            rightmax = max(rightmax, height[right])
            if leftmax < rightmax:</pre>
78
79
                # 管小不管大,可能存在更大但不在乎
                res += leftmax - height[left]
80
81
                left += 1
82
            else:
83
                res += rightmax - height[right]
84
                right -= 1
85
        return res
```