Platelet

 $\begin{array}{cc} Team \ Reference \ Material \\ {}_{(unlimited \ version)} \end{array}$



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Chapter 1

Graph Theory

1.1 2-SAT (ct)

```
struct Edge {
       Edge *next;
       int to;
4 } *last[maxn << 1], e[maxn << 2], *ecnt = e;
5 inline void link(int a, int b)
       *++ecnt = (Edge) {last[a], b}; last[a] = ecnt;
  }
  int dfn[maxn], low[maxn], timer, st[maxn], top, id[maxn], colcnt, n;
   bool fail, used[maxn];
   void tarjan(int x, int fa)
11
12
       dfn[x] = low[x] = ++timer; st[++top] = x;
13
       for (R Edge *iter = last[x]; iter; iter = iter -> next)
14
            if (iter -> to != fa)
15
16
                if (!dfn[iter -> to])
17
18
                     tarjan(iter -> to, x);
19
                     cmin(low[x], low[iter -> to]);
20
21
                else if (!id[iter -> to]) cmin(low[x], dfn[iter -> to]);
22
23
       if (dfn[x] == low[x])
25
            ++colcnt; bool flag = 1;
            for (; ;)
27
28
                int now = st[top--];
29
                id[now] = colcnt;
30
                if (now \le 2 * n)
31
32
                     flag \&= !used[id[now <= n ? now + n : now - n]];
33
                    now \mathrel{<=} n \mathrel{?} fail \mathrel{|=} (id[now + n] \mathrel{==} id[now]) : fail \mathrel{|=} (id[now - n] \mathrel{==} id[now]);
34
                if (now == x) break;
            }
37
            used[colcnt] = flag;
38
39
40 }
41 int ans[maxn], tot;
42 int main()
```

1.2. 双连通分量 5

```
43 {
44
            build your graph here.
45
       */
46
       for (R int i = 1; !fail && i <= n; ++i) if (!dfn[i]) tarjan(i, 0);</pre>
47
       if (fail)
48
       {
49
           puts("Impossible");
50
           return 0;
51
       }
52
       for (R int i = 1; i <= n; ++i) if (used[id[i]]) ans[++tot] = i;</pre>
53
       printf("%d\n", tot);
54
       std::sort(ans + 1, ans + tot + 1);
55
       for (R int i = 1; i <= tot; ++i) printf("%d ", ans[i]);
56
       return 0;
57
58
```

1.2 双连通分量

- 1.2.1 点双连通分量
- 1.2.2 边双连通分量
- 1.3 K 短路 (lhy)

```
const int MAXNODE = MAXN + MAXM * 2;
   bool used[MAXN];
   int n, m, cnt, S, T, Kth, N, TT;
   int rt[MAXN], seq[MAXN], adj[MAXN], from[MAXN], dep[MAXN];
   LL dist[MAXN], w[MAXM], ans[MAXK];
   struct GivenEdge{
       int u, v, w;
       GivenEdge() {};
       \label{eq:continuity} \mbox{GivenEdge(int $\_$u, int $\_$v, int $\_$w)} \; : \; \mbox{u($\_$u), $v($\_$v), $w($\_$w)$} \};
   }edge[MAXM];
10
11 struct Edge{
       int v, nxt, w;
12
       Edge() {};
       Edge(int _v, int _nxt, int _w) : v(_v), nxt(_nxt), w(_w) {};
15 }e[MAXM];
   inline void addedge(int u, int v, int w)
16
17
       e[++cnt] = Edge(v, adj[u], w); adj[u] = cnt;
18
19
   void dij(int S)
20
21
       for(int i = 1; i <= N; i++)</pre>
22
23
            dist[i] = INF;
24
            dep[i] = 0x3f3f3f3f;
25
            used[i] = false;
26
            from[i] = 0;
27
       }
28
       static priority_queue<pair<LL, int>, vector<pair<LL, int> >, greater<pair<LL, int> > hp;
29
```

```
while(!hp.empty())hp.pop();
30
       hp.push(make_pair(dist[S] = 0, S));
31
       dep[S] = 1;
32
       while(!hp.empty())
33
34
           pair<LL, int> now = hp.top();
35
           hp.pop();
36
           int u = now.second;
37
           if(used[u])continue;
38
           else used[u] = true;
39
           for(int p = adj[u]; p; p = e[p].nxt)
40
41
                int v = e[p].v;
42
                if(dist[u] + e[p].w < dist[v])</pre>
43
44
                    dist[v] = dist[u] + e[p].w;
45
                    dep[v] = dep[u] + 1;
46
                    from[v] = p;
47
                    hp.push(make_pair(dist[v], v));
48
49
           }
50
       }
51
       for(int i = 1; i <= m; i++)</pre>
                                         w[i] = 0;
52
       for(int i = 1; i <= N; i++)</pre>
53
           if(from[i])w[from[i]] = -1;
54
       for(int i = 1; i <= m; i++)</pre>
55
56
           if(~w[i] && dist[edge[i].u] < INF && dist[edge[i].v] < INF)</pre>
57
58
                w[i] = -dist[edge[i].u] + (dist[edge[i].v] + edge[i].w);
59
           }
60
61
            else
62
            {
                w[i] = -1;
63
           }
64
       }
65
66
  inline bool cmp_dep(int p, int q)
67
68 {
       return dep[p] < dep[q];</pre>
69
71 struct Heap{
       LL key;
72
       int id, lc, rc, dist;
73
       Heap() {};
74
       Heap(LL k, int i, int 1, int r, int d) : key(k), id(i), lc(l), rc(r), dist(d) {};
75
       inline void clear()
76
77
           key = 0;
78
           id = lc = rc = dist = 0;
79
80
  }hp[MAXNODE];
s2 inline int merge_simple(int u, int v)
83
       if(!u)return v;
84
       if(!v)return u;
85
       if(hp[u].key > hp[v].key)
86
```

1.3. K 短路 (LHY) 7

```
swap(u, v);
88
        }
89
        hp[u].rc = merge_simple(hp[u].rc, v);
90
        if(hp[hp[u].lc].dist < hp[hp[u].rc].dist)</pre>
91
92
            swap(hp[u].lc, hp[u].rc);
93
94
        hp[u].dist = hp[hp[u].rc].dist + 1;
95
        return u;
96
97
    inline int merge_full(int u, int v)
98
99
        if(!u)return v;
100
        if(!v)return u;
101
        if(hp[u].key > hp[v].key)
102
        {
103
            swap(u, v);
104
        }
105
        int nownode = ++cnt;
106
        hp[nownode] = hp[u];
107
        hp[nownode].rc = merge_full(hp[nownode].rc, v);
108
        if(hp[hp[nownode].lc].dist < hp[hp[nownode].rc].dist)</pre>
109
110
        {
            swap(hp[nownode].lc, hp[nownode].rc);
111
        }
112
        hp[nownode].dist = hp[hp[nownode].rc].dist + 1;
113
        return nownode;
114
115
116
   priority_queue<pair<LL, int>, vector<pair<LL, int> >, greater<pair<LL, int> > Q;
    int main()
117
118
        while(scanf("%d%d", &n, &m) != EOF)
119
120
            scanf("%d%d%d%d", &S, &T, &Kth, &TT);
121
            for(int i = 1; i <= m; i++)</pre>
122
            {
123
                 int u, v, w;
124
                 scanf("%d%d%d", &u, &v, &w);
125
                 edge[i] = \{u, v, w\};
126
            }
127
            N = n;
128
            memset(adj, 0, sizeof(*adj) * (N + 1));
129
            cnt = 0;
130
            for(int i = 1; i <= m; i++)</pre>
131
                 addedge(edge[i].v, edge[i].u, edge[i].w);
132
            dij(T);
133
            if(dist[S] > TT)
134
135
                 puts("Whitesnake!");
136
                 continue;
137
            }
138
            for(int i = 1; i <= N; i++)</pre>
139
                 seq[i] = i;
140
            sort(seq + 1, seq + N + 1, cmp_dep);
141
            cnt = 0;
142
            memset(adj, 0, sizeof(*adj) * (N + 1));
143
            memset(rt, 0, sizeof(*rt) * (N + 1));
144
```

```
for(int i = 1; i <= m; i++)</pre>
145
                 addedge(edge[i].u, edge[i].v, edge[i].w);
146
            rt[T] = cnt = 0;
147
            hp[0].dist = -1;
148
            for(int i = 1; i <= N; i++)</pre>
149
150
                 int u = seq[i], v = edge[from[u]].v;
151
                 rt[u] = 0;
152
                 for(int p = adj[u]; p; p = e[p].nxt)
153
154
                      if(~w[p])
155
156
                          hp[++cnt] = Heap(w[p], p, 0, 0, 0);
157
                          rt[u] = merge_simple(rt[u], cnt);
158
                     }
159
160
                 if(i == 1)continue;
161
                 rt[u] = merge_full(rt[u], rt[v]);
162
163
             while(!Q.empty())Q.pop();
164
             Q.push(make_pair(dist[S], 0));
165
             edge[0].v = S;
166
             for(int kth = 1; kth <= Kth; kth++)</pre>
167
168
                 if(Q.empty())
169
                 {
170
                      ans[kth] = -1;
171
                      continue;
172
173
174
                 pair<LL, int> now = Q.top(); Q.pop();
175
                 ans[kth] = now.first;
176
                 int p = now.second;
                 if(hp[p].lc)
177
                 {
178
                      Q.push(make_pair(+hp[hp[p].lc].key + now.first - hp[p].key, hp[p].lc));
179
                 }
180
                 if(hp[p].rc)
181
                 {
182
                      Q.push(make_pair(+hp[hp[p].rc].key + now.first - hp[p].key, hp[p].rc));
183
                 }
184
                 if(rt[edge[hp[p].id].v])
185
                 {
186
                      Q.push(make_pair(hp[rt[edge[hp[p].id].v]).key + now.first, rt[edge[hp[p].id].v]));
187
                 }
188
            }
189
            if(ans[Kth] == -1 \mid \mid ans[Kth] > TT)
190
             {
191
                 puts("Whitesnake!");
192
             }
193
            else
194
             {
195
                 puts("yareyaredawa");
196
            }
197
        }
198
   }
199
```

1.4. 最大团 9

- 1.4 最大团
- 1.5 一般图最大匹配
- 1.6 带花树
- 1.7 KM 算法
- 1.8 支配树
- 1.8.1 DAG (ct)

```
struct Edge {
       Edge *next;
       int to;
  } ;
5 Edge *last[maxn], e[maxm], *ecnt = e; // original graph
6 Edge *rlast[maxn], re[maxm], *recnt = re; // reversed-edge graph
  Edge *tlast[maxn], te[maxn << 1], *tecnt = te; // dominate tree graph</pre>
   int deg[maxn], q[maxn], fa[maxn][20], all_fa[maxn], fa_cnt, size[maxn], dep[maxn];
   inline void link(int a, int b)
10
   {
       *++ecnt = (Edge) {last[a], b}; last[a] = ecnt; ++deg[b];
11
  }
12
   inline void link_rev(R int a, R int b)
13
   {
14
       *++recnt = (Edge) {rlast[a], b}; rlast[a] = recnt;
15
16
   inline void link_tree(R int a, R int b)
17
18
       *++tecnt = (Edge) {tlast[a], b}; tlast[a] = tecnt;
19
20
   inline int getlca(R int a, R int b)
21
22
       if (dep[a] < dep[b]) std::swap(a, b);</pre>
23
       R int temp = dep[a] - dep[b];
24
       for (R int i; temp; temp -= 1 << i)</pre>
25
           a = fa[a][i = __builtin_ctz(temp)];
26
       for (R int i = 16; ~i; --i)
27
           if (fa[a][i] != fa[b][i])
               a = fa[a][i], b = fa[b][i];
29
       if (a == b) return a;
30
       return fa[a][0];
31
32
   void dfs(R int x)
33
34
       size[x] = 1;
35
       for (R Edge *iter = tlast[x]; iter; iter = iter -> next)
36
           dfs(iter -> to), size[x] += size[iter -> to];
37
38
   int main()
39
40
       q[1] = 0;
41
       R int head = 0, tail = 1;
42
       while (head < tail)
43
44
           R int now = q[++head];
45
           fa_cnt = 0;
46
```

```
for (R Edge *iter = rlast[now]; iter; iter = iter -> next)
47
                all_fa[++fa_cnt] = iter -> to;
           for (; fa_cnt > 1; --fa_cnt)
49
                all_fa[fa_cnt - 1] = getlca(all_fa[fa_cnt], all_fa[fa_cnt - 1]);
50
           fa[now][0] = all_fa[fa_cnt];
51
           dep[now] = dep[all_fa[fa_cnt]] + 1;
52
           if (now) link_tree(fa[now][0], now);
53
           for (R int i = 1; i \le 16; ++i)
54
                fa[now][i] = fa[fa[now][i - 1]][i - 1];
55
           for (R Edge *iter = last[now]; iter; iter = iter -> next)
56
                if (--deg[iter \rightarrow to] == 0) q[++tail] = iter \rightarrow to;
57
       }
58
       dfs(0);
59
       for (R int i = 1; i <= n; ++i) printf("%d\n", size[i] - 1);
60
       return 0;
61
62
```

1.8.2 一般图

1.9 虚树 (ct)

```
struct Edge {
       Edge *next;
       int to;
  } *last[maxn], e[maxn << 1], *ecnt = e;</pre>
5 inline void link(int a, int b)
6
       *++ecnt = (Edge) {last[a], b}; last[a] = ecnt;
       *++ecnt = (Edge) {last[b], a}; last[b] = ecnt;
  int a[maxn], n, dfn[maxn], pos[maxn], timer, inv[maxn], st[maxn];
  int fa[maxn], size[maxn], dep[maxn], son[maxn], top[maxn];
bool vis[maxn];
void dfs1(int x)
14 {
       vis[x] = 1; size[x] = 1; dep[x] = dep[fa[x]] + 1;
15
       for (R Edge *iter = last[x]; iter; iter = iter -> next)
16
           if (!vis[iter -> to])
17
18
               fa[iter -> to] = x;
               dfs1(iter -> to);
20
               size[x] += size[iter -> to];
               size[son[x]] < size[iter -> to] ? son[x] = iter -> to : 0;
22
23
24
  void dfs2(int x)
25
26
       vis[x] = 0; top[x] = x == son[fa[x]] ? top[fa[x]] : x;
27
       dfn[x] = ++timer; pos[timer] = x;
28
       if (son[x]) dfs2(son[x]);
29
       for (R Edge *iter = last[x]; iter; iter = iter -> next)
30
           if (vis[iter -> to]) dfs2(iter -> to);
       inv[x] = timer;
32
34 inline int getlca(int a, int b)
35 {
       while (top[a] != top[b])
36
           dep[top[a]] < dep[top[b]] ? b = fa[top[b]] : a = fa[top[a]];
```

1.9. 虚树 (CT) 11

```
return dep[a] < dep[b] ? a : b;</pre>
38
  }
39
  inline bool cmp(int a, int b)
40
   {
41
       return dfn[a] < dfn[b];</pre>
42
43
   inline bool isson(int a, int b)
44
45
       return dfn[a] <= dfn[b] && dfn[b] <= inv[a];</pre>
46
47
   typedef long long 11;
48
   bool imp[maxn];
49
   struct sEdge {
50
       sEdge *next;
51
       int to, w;
52
  } *slast[maxn], se[maxn << 1], *secnt = se;</pre>
53
  inline void slink(int a, int b, int w)
54
55
       *++secnt = (sEdge) {slast[a], b, w}; slast[a] = secnt;
56
  }
57
   int main()
58
59
       scanf("%d", &n);
60
       for (int i = 1; i < n; ++i)
61
62
       {
           int a, b; scanf("%d%d", &a, &b);
63
           link(a, b);
64
       }
65
       int m; scanf("%d", &m);
66
67
       dfs1(1); dfs2(1);
68
       memset(size, 0, (n + 1) << 2);
       for (; m; --m)
69
70
           int top = 0; scanf("%d", &k);
71
           for (int i = 1; i <= k; ++i) scanf("%d", \&a[i]), vis[a[i]] = imp[a[i]] = 1;
72
           std::sort(a + 1, a + k + 1, cmp);
73
           int p = k;
74
           for (int i = 1; i < k; ++i)
75
           {
76
                int lca = getlca(a[i], a[i + 1]);
77
                if (!vis[lca]) vis[a[++p] = lca] = 1;
78
           }
79
80
           std::sort(a + 1, a + p + 1, cmp);
81
           st[++top] = a[1];
82
           for (int i = 2; i <= p; ++i)
83
           {
                while (!isson(st[top], a[i])) --top;
84
                slink(st[top], a[i], dep[a[i]] - dep[st[top]]);
85
                st[++top] = a[i];
86
           }
87
88
                write your code here.
89
90
           for (int i = 1; i \le p; ++i) vis[a[i]] = imp[a[i]] = 0, slast[a[i]] = 0;
91
92
           secnt = se;
93
       return 0;
94
95
```

1.10 树上点分治 (ct)

```
int root, son[maxn], size[maxn], sum;
  bool vis[maxn];
void dfs_root(int x, int fa)
4 | {
       size[x] = 1; son[x] = 0;
       for (R Edge *iter = last[x]; iter; iter = iter -> next)
           if (iter -> to == fa || vis[iter -> to]) continue;
           dfs_root(iter -> to, x);
           size[x] += size[iter -> to];
10
           cmax(son[x], size[iter -> to]);
11
12
       cmax(son[x], sum - size[x]);
       if (!root || son[x] < son[root]) root = x;</pre>
14
15 }
  void dfs_chain(int x, int fa, int st1, int st2)
16
   {
17
18
          write your code here.
19
20
       for (Edge *iter = last[x]; iter; iter = iter -> next)
21
22
           if (vis[iter -> to] || iter -> to == fa) continue;
23
           dfs_chain(iter -> to, x);
24
25
  | }
26
  void calc(int x)
27
28
       for (Edge *iter = last[x]; iter; iter = iter -> next)
29
30
           if (vis[iter -> to]) continue;
31
           dfs_chain(iter -> to, x);
32
33
               write your code here.
35
36
       }
37 | }
  void work(int x)
38
39
   {
       vis[x] = 1;
40
41
       for (R Edge *iter = last[x]; iter; iter = iter -> next)
42
43
           if (vis[iter -> to]) continue;
44
45
           root = 0;
           sum = size[iter -> to];
46
           dfs_root(iter -> to, 0);
47
           work(root);
48
       }
49
50
51 int main()
52 {
       root = 0; sum = n;
53
       dfs_root(1, 0);
       work(root);
       return 0;
56
57
```

1.11. 树上倍增 (CT) 13

1.11 树上倍增 (ct)

```
int fa[maxn][17], mn[maxn][17], dep[maxn];
  bool vis[maxn];
3 void dfs(int x)
       vis[x] = 1;
       for (int i = 1; i <= 16; ++i)
            if (dep[x] < (1 << i)) break;</pre>
           fa[x][i] = fa[fa[x][i - 1]][i - 1];
9
           mn[x][i] = dmin(mn[x][i - 1], mn[fa[x][i - 1]][i - 1]);
10
11
       for (Edge *iter = last[x]; iter; iter = iter -> next)
12
           if (!vis[iter -> to])
13
14
15
                fa[iter \rightarrow to][0] = x;
16
                mn[iter -> to][0] = iter -> w;
                dep[iter \rightarrow to] = dep[x] + 1;
17
                dfs(iter -> to);
18
           }
19
20
  inline int getlca(int x, int y)
21
22
       if (dep[x] < dep[y]) std::swap(x, y);</pre>
23
       int t = dep[x] - dep[y];
24
       for (int i = 0; i <= 16 && t; ++i)
25
            if ((1 << i) & t)
                x = fa[x][i], t ^= 1 << i;
27
       for (int i = 16; i >= 0; --i)
29
           if (fa[x][i] != fa[y][i])
30
                x = fa[x][i];
31
                y = fa[y][i];
32
33
       if (x == y) return x;
34
       return fa[x][0];
35
36
   inline int getans(int x, int f)
37
38
       int ans = inf, t = dep[x] - dep[f];
39
       for (int i = 0; i \le 16 \&\& t; ++i)
40
           if (t & (1 << i))
41
42
                cmin(ans, mn[x][i]);
43
                x = fa[x][i];
44
                t ^= 1 << i;
45
           }
46
       return ans;
```

1.12 Prufer 编码

1.13 Link-Cut Tree (ct)

```
struct Node *null;
struct Node {
    Node *ch[2], *fa, *pos;
```

```
int val, mn, l, len; bool rev;
        // min_val in chain
        inline bool type()
6
7
        {
            return fa -> ch[1] == this;
8
        }
9
        inline bool check()
10
11
12
            return fa -> ch[type()] == this;
        }
13
        inline void pushup()
14
15
            pos = this; mn = val;
16
            ch[0] \rightarrow mn < mn ? mn = ch[0] \rightarrow mn, pos = ch[0] \rightarrow pos : 0;
17
            ch[1] \rightarrow mn < mn ? mn = ch[1] \rightarrow mn, pos = ch[1] \rightarrow pos : 0;
18
            len = ch[0] -> len + ch[1] -> len + 1;
19
20
        inline void pushdown()
21
22
        {
            if (rev)
23
            {
                 ch[0] -> rev ^= 1;
25
                 ch[1] -> rev ^= 1;
26
                 std::swap(ch[0], ch[1]);
27
                 rev ^= 1;
28
29
        }
30
        inline void pushdownall()
31
32
33
            if (check()) fa -> pushdownall();
34
            pushdown();
35
        inline void rotate()
36
37
            bool d = type(); Node *f = fa, *gf = f -> fa;
38
            (fa = gf, f \rightarrow check()) ? fa \rightarrow ch[f \rightarrow type()] = this : 0;
39
            (f \rightarrow ch[d] = ch[!d]) != null ? ch[!d] \rightarrow fa = f : 0;
40
            (ch[!d] = f) -> fa = this;
41
            f -> pushup();
42
        }
43
        inline void splay(bool need = 1)
44
45
46
            if (need) pushdownall();
            for (; check(); rotate())
47
                 if (fa -> check())
48
                      (type() == fa \rightarrow type() ? fa : this) \rightarrow rotate();
49
            pushup();
50
51
        inline Node *access()
52
53
            Node *i = this, *j = null;
54
            for (; i != null; i = (j = i) -> fa)
55
56
                 i -> splay();
57
                 i \rightarrow ch[1] = j;
58
                 i -> pushup();
59
60
            return j;
61
62
        inline void make_root()
63
```

1.14. 仙人掌 15

```
access();
65
           splay();
66
           rev ^= 1;
67
       }
68
       inline void link(Node *that)
69
70
           make_root();
71
           fa = that;
72
           splay(0);
73
74
       inline void cut(Node *that)
75
76
           make_root();
77
           that -> access();
78
           that -> splay(0);
79
           that -> ch[0] = fa = null;
80
           that -> pushup();
81
82
   } mem[maxn];
83
   inline Node *query(Node *a, Node *b)
84
85
       a -> make_root(); b -> access(); b -> splay(0);
       return b -> pos;
87
   inline int dist(Node *a, Node *b)
89
90
       a -> make_root(); b -> access(); b -> splay(0);
91
       return b -> len;
92
93
```

1.14 仙人掌

1.15 弦图

1.16 最小割

1.17 最大流 (ct)

```
struct Edge {
       Edge *next, *rev;
       int to, cap;
  } *last[maxn], *cur[maxn], e[maxm], *ecnt = e;
  inline void link(R int a, R int b, R int w)
6
       *++ecnt = (Edge) {last[a], ecnt + 1, b, w}; last[a] = ecnt;
       *++ecnt = (Edge) {last[b], ecnt - 1, a, 0}; last[b] = ecnt;
9
   int ans, s, t, q[maxn], dep[maxn];
10
   inline bool bfs()
11
12
       memset(dep, -1, (t + 1) << 2);
13
       dep[q[1] = t] = 0; int head = 0, tail = 1;
14
       while (head < tail)
15
16
           int now = q[++head];
17
           for (Edge *iter = last[now]; iter; iter = iter -> next)
18
               if (dep[iter -> to] == -1 && iter -> rev -> cap)
19
```

```
dep[q[++tail] = iter \rightarrow to] = dep[now] + 1;
20
21
       return dep[s] != -1;
22
23
24 int dfs(int x, int f)
25
   {
       if (x == t) return f;
26
       int used = 0;
27
       for (Edge* &iter = cur[x]; iter; iter = iter -> next)
28
            if (iter \rightarrow cap && dep[iter \rightarrow to] + 1 == dep[x])
29
30
                int v = dfs(iter -> to, dmin(f - used, iter -> cap));
31
                iter -> cap -= v;
32
                iter -> rev -> cap += v;
33
                used += v;
34
                if (used == f) return f;
35
36
37
       return used;
38
  inline void dinic()
39
40
       while (bfs())
41
42
            memcpy(cur, last, sizeof cur);
43
            ans += dfs(s, inf);
44
45
46
```

1.18 费用流 (ct)

```
struct Edge {
       Edge *next, *rev;
       int from, to, cap, cost;
  } *last[maxn], *prev[maxn], e[maxm], *ecnt = e;
5 inline void link(int a, int b, int w, int c)
6
       *++ecnt = (Edge) {last[a], ecnt + 1, a, b, w, c}; last[a] = ecnt;
       *++ecnt = (Edge) {last[b], ecnt - 1, b, a, 0, -c}; last[b] = ecnt;
int s, t, q[maxn << 2], dis[maxn];</pre>
11 ll ans;
bool inq[maxn];
13 #define inf Ox7fffffff
inline bool spfa()
15 {
       for (int i = 1; i <= t; ++i) dis[i] = inf;</pre>
16
       int head = 0, tail = 1; dis[q[1] = s] = 0;
17
       while (head < tail)</pre>
18
19
           int now = q[++head]; inq[now] = 0;
20
           for (Edge *iter = last[now]; iter; iter = iter -> next)
21
               if (iter -> cap && dis[iter -> to] > dis[now] + iter -> cost)
               {
23
                    dis[iter -> to] = dis[now] + iter -> cost;
24
                    prev[iter -> to] = iter;
25
                    !inq[iter \rightarrow to] ? inq[q[++tail] = iter \rightarrow to] = 1 : 0;
26
27
28
       return dis[t] != inf;
29
```

```
30 }
  inline void mcmf()
31
32
       int x = inf:
33
       for (Edge *iter = prev[t]; iter; iter = prev[iter -> from]) cmin(x, iter -> cap);
34
       for (Edge *iter = prev[t]; iter; iter = prev[iter -> from])
35
36
           iter -> cap -= x;
37
           iter -> rev -> cap += x;
38
           ans += 111 * x * iter -> cost;
39
       }
40
41
```

1.19 有上下界的网络流 (Durandal)

B(u,v) 表示边 (u,v) 流量的下界,C(u,v) 表示边 (u,v) 流量的上界,设 F(u,v) 表示边 (u,v) 的实际流量设 G(u,v) = F(u,v) - B(u,v),则 $0 \le G(u,v) \le C(u,v) - B(u,v)$

• 无源汇的上下界可行流

建立超级源点 S^* 和超级汇点 T^* ,对于原图每一条边 (u,v) 在新网络中连如下三条边: $S^* \to v$,容量为 B(u,v); $u \to T^*$,容量为 B(u,v); $u \to v$,容量为 C(u,v) - B(u,v)。最后求新网络的最大流,判断从 超级源点 S^* 出发的边是否都满流即可,边 (u,v) 的最终解中的实际流量为 G(u,v) + B(u,v)。

- 有源汇的上下界可行流 从汇点 T 到源点 S 连一条上界为 ∞ ,下界为 0 的边。按照无源汇的上下界可行流一样做即可,流量即为 $T\to S$ 边上的流量。
- 有源汇的上下界最大流
 - 在有源汇的上下界可行流中,从汇点 T 到源点 S 的边改为连一条上界为 ∞,下界为 x 的边。x 满足二分性质,找到最大的 x 使得新网络存在有源汇的上下界可行流即为原图的最大流。
 - 从汇点 T 到源点 S 连一条上界为 ∞ ,下界为 0 的边,变成无源汇的网络。按照无源汇的上下界可行流的方法,建立超级源点 S^* 与超级汇点 T^* ,求一遍 S^* → T^* 的最大流,再将从汇点 T 到源点 S 的这条边拆掉,求一次 S → T 的最大流即可。
- 有源汇的上下界最小流
 - 在有源汇的上下界可行流中,从汇点 T 到源点 S 的边改为连一条上界为 x,下界为 0 的边。x 满足二分性质,找到最小的 x 使得新网络存在有源汇的上下界可行流即为原图的最大流。
 - 按照无源汇的上下界可行流的方法,建立超级源点 S^* 与超级汇点 T^* ,求一遍 $S^* \to T^*$ 的最大流,但是注意不加上汇点 T 到源点 S 的这条边,即不使之改为无源汇的网络去求解。求完后,再加上那条汇点 T 到源点 S 的边,上界为 ∞ 的边。因为这条边的下界为 0,所以 S^* , T^* 无影响,再求一次 $S^* \to T^*$ 的最大流。若超级源点 S^* 出发的边全部满流,则 $T \to S$ 边上的流量即为原图的最小流,否则无解。

1.20 zkw 费用流

1.21 差分约束

Chapter 2

Math

2.1 int64 相乘取模 (Durandal)

```
int64_t mul(int64_t x, int64_t y, int64_t p) {
   int64_t t = (x * y - (int64_t) ((long double) x / p * y + 1e-3) * p) % p;
   return t < 0 ? t + p : t;
}</pre>
```

2.2 扩展欧几里得 (gy)

```
// return gcd(a, b)
   // ax+by=gcd(a,b)
  int extend_gcd(int a, int b, int &x, int &y) {
       if (b == 0) {
           x = 1, y = 0;
           return a;
       int res = extend_gcd(b, a % b, x, y);
      int t = y;
       y = x - a / b * y;
10
       x = t;
11
       return res;
12
13
14 // return minimal positive integer x so that ax+by=c
15 // or -1 if such x does not exist
int solve_equ(int a, int b, int c) {
       int x, y, d;
       d = extend_gcd(a, b, x, y);
       if (c % d)
19
           return -1;
20
       int t = c / d;
21
       x *= t;
22
       y *= t;
23
       int k = b / d;
24
       x = (x \% k + k) \% k;
25
       return x;
27
28 // return minimal positive integer x so that ax==b \pmod{p}
^{29} // or -1 if such x does not exist
30 int solve(int a, int b, int p) {
      a = (a \% p + p) \% p;
       b = (b \% p + p) \% p;
```

```
return solve_equ(a, p, b);

yellow return solve_equ(a, p, b);

yellow return solve_equ(a, p, b);
```

2.3 中国剩余定理 (Durandal)

返回是否可行,余数和模数结果为 r_1 , m_1

```
bool CRT(int &r1, int &m1, int r2, int m2) {
    int x, y, g = extend_gcd(m1, m2, x, y);
    if ((r2 - r1) % g != 0) return false;
    x = 111 * (r2 - r1) * x % m2;
    if (x < 0) x += m2;
    x /= g;
    r1 += m1 * x;
    m1 *= m2 / g;
    return true;
}</pre>
```

2.4 线性同余不等式 (Durandal)

必须满足 $0 \le d < m$, $0 \le l \le r < m$, 返回 $\min\{x \ge 0 \mid l \le x \cdot d \mod m \le r\}$, 无解返回 -1

```
int64_t calc(int64_t d, int64_t m, int64_t l, int64_t r) {
   if (1 == 0) return 0;
   if (d == 0) return -1;
   if (d * 2 > m) return calc(m - d, m, m - r, m - l);
   if ((1 - 1) / d < r / d) return (1 - 1) / d + 1;
   int64_t k = calc((-m % d + d) % d, d, l % d, r % d);
   if (k == -1) return -1;
   return (k * m + l - 1) / d + 1;
}</pre>
```

2.5 组合数

2.6 高斯消元

2.7 Miller Rabin & Pollard Rho (gy)

```
st In Java, use BigInteger.isProbablePrime(int certainty) to replace miller_rabin(BigInteger
    \rightarrow number)
    * Test Set / First Wrong Answer
   * 2 / 2,047
    * 2, 3 / 1,373,653
    * 31, 73 / 9,080,191
    * 2, 3, 5 / 25,326,001
    * 2, 3, 5, 7 / 3,215,031,751 (> Int.MAX_VALUE)
   * 2, 7, 61 / 4,759,123,141
   * 2, 13, 23, 1662803 / 1,122,004,669,633
10
   * 2, 3, 5, 7, 11 / 2,152,302,898,747
11
   * 2, 3, 5, 7, 11, 13 / 3,474,749,660,383
12
   * 2, 3, 5, 7, 11, 13, 17 / 341,550,071,728,321
13
   * 2, 3, 5, 7, 11, 13, 17, 19, 23 / 3,825,123,056,546,413,051
14
   * 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37 / 318,665,857,834,031,151,167,461 (> Long.MAX_VALUE)
15
   * 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41 / 3,317,044,064,679,887,385,961,981
```

20 CHAPTER 2. MATH

```
17 */
  const int test_case_size = 12;
19 const int test_cases[test_case_size] = {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37};
   int64_t multiply_mod(int64_t x, int64_t y, int64_t p) {
20
       int64_t t = (x * y - (int64_t) ((long double) x / p * y + 1e-3) * p) % p;
21
       return t < 0? t + p: t;
22
23
   int64_t add_mod(int64_t x, int64_t y, int64_t p) {
       return (Oull + x + y) % p;
25
26
  int64_t power_mod(int64_t x, int64_t exp, int64_t p) {
27
       int64_t ans = 1;
28
       while (exp) {
29
           if (exp & 1)
30
               ans = multiply_mod(ans, x, p);
31
           x = multiply_mod(x, x, p);
32
           exp >>= 1;
33
       }
35
       return ans;
  | ጉ
36
   bool miller_rabin_check(int64_t prime, int64_t base) {
37
       int64_t number = prime - 1;
38
       for (; ~number & 1; number >>= 1)
39
           continue;
40
       int64_t result = power_mod(base, number, prime);
41
42
       for (; number != prime - 1 && result != 1 && result != prime - 1; number <<= 1)
43
           result = multiply_mod(result, result, prime);
44
       return result == prime - 1 || (number & 1) == 1;
  }
45
46 bool miller_rabin(int64_t number) {
       if (number < 2)
47
           return false;
48
       if (number < 4)
49
          return true;
50
       if (~number & 1)
52
       for (int i = 0; i < test_case_size && test_cases[i] < number; i++)</pre>
           if (!miller_rabin_check(number, test_cases[i]))
55
               return false;
56
       return true;
  ĺ٦
57
   int64_t gcd(int64_t x, int64_t y) {
58
       return y == 0 ? x : gcd(y, x % y);
59
60
   int64_t pollard_rho_test(int64_t number, int64_t seed) {
61
       int64_t x = rand() \% (number - 1) + 1, y = x;
62
       int head = 1, tail = 2;
63
       while (true) {
64
           x = multiply_mod(x, x, number);
65
           x = add_mod(x, seed, number);
66
           if (x == y)
67
               return number;
68
           int64_t answer = gcd(std::abs(x - y), number);
69
           if (answer > 1 && answer < number)</pre>
```

```
71
               return answer;
           if (++head == tail) {
72
73
               y = x;
               tail <<= 1;
74
           }
75
       }
76
77
   void factorize(int64_t number, std::vector<int64_t> &divisor) {
78
       if (number > 1) {
79
           if (miller_rabin(number)) {
80
               divisor.push_back(number);
81
           } else {
82
               int64_t factor = number;
83
               while (factor >= number)
84
                    factor = pollard_rho_test(number, rand() % (number - 1) + 1);
85
               factorize(number / factor, divisor);
86
               factorize(factor, divisor);
87
           }
88
       }
89
```

- 2.8 $O(m^2 \log n)$ 线性递推
- 2.9 Polynomial
- 2.9.1 FFT
- 2.9.2 NTT & 多项式求逆
- 2.10 拉格朗日插值
- 2.11 杜教筛
- 2.12 BSGS (ct,gy)
- 2.12.1 BSGS

p 是素数,返回 $\min\{x \ge 0 \mid y^x \equiv z \mod p\}$

```
const int mod = 19260817;
  struct Hash
2
   {
3
       Hash *next;
       int key, val;
  } *last[mod], mem[100000], *tot = mem;
   inline void insert(R int x, R int v)
       *++tot = (Hash) {last[x \% mod], x, v}; last[x \% mod] = tot;
9
10
   inline int query(R int x)
11
12
       for (R Hash *iter = last[x % mod]; iter; iter = iter -> next)
13
           if (iter -> key == x) return iter -> val;
14
       return -1;
15
  }
16
17 inline void del(R int x)
```

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```
last[x \% mod] = 0;
20 }
21 int main()
22
  {
       for (; T; --T)
23
24
           R int y, z, p; scanf("%d%d%d", &y, &z, &p);
25
           R int m = (int) sqrt(p * 1.0);
26
27
           y %= p; z %= p;
           if (!y && !z) {puts("0"); continue;}
28
           if (!y) {puts("Orz, I cannot find x!"); continue;}
29
           R int pw = 1;
30
           for (R int i = 0; i < m; ++i, pw = 111 * pw * y % p) insert(111 * z * pw % p, i);
31
           R int ans = -1;
32
           for (R int i = 1, t, pw2 = pw; i \leq p / m + 1; ++i, pw2 = 111 * pw2 * pw % p)
33
               if ((t = query(pw2)) != -1) {ans = i * m - t; break;}
34
           if (ans == -1) puts("Orz, I cannot find x!");
35
           else printf("%d\n", ans );
36
           tot = mem; pw = 1;
           for (R int i = 0; i < m; ++i, pw = 111 * pw * y % p) del(111 * z * pw % p);
39
       return 0;
40
41
```

2.12.2 扩展 BSGS

必须满足 $0 \le a < p$, $0 \le b < p$, 返回 $\min\{x \ge 0 \mid a^x \equiv b \mod p\}$

```
i int64_t ex_bsgs(int64_t a, int64_t b, int64_t p) {
       if (b == 1)
2
           return 0;
3
       int64_t t, d = 1, k = 0;
       while ((t = std::__gcd(a, p)) != 1) {
           if (b \% t) return -1;
           k++, b /= t, p /= t, d = d * (a / t) % p;
           if (b == d) return k;
       }
9
10
       map.clear();
       int64_t m = std::ceil(std::sqrt((long double) p));
11
       int64_t a_m = pow_mod(a, m, p);
12
       int64_t mul = b;
13
       for (int j = 1; j \le m; j++) {
14
           (mul *= a) %= p;
15
           map[mul] = j;
16
17
       for (int i = 1; i <= m; i++) {
18
           (d *= a_m) \%= p;
19
           if (map.count(d))
20
               return i * m - map[d] + k;
^{21}
       }
22
       return -1;
23
  ١}
24
25 | int main() {
       int64_t a, b, p;
26
       while (scanf("%lld%lld", &a, &b, &p) != EOF)
           printf("%lld\n", ex_bsgs(a, b, p));
       return 0;
29
30
```

2.13 直线下整点个数 (gy)

必须满足 $a\geq 0,\,b\geq 0,\,m>0,\,$ 返回 $\sum\limits_{i=0}^{n-1}\frac{a+bi}{m}$

```
int64_t count(int64_t n, int64_t a, int64_t b, int64_t m) {
   if (b == 0)
      return n * (a / m);
   if (a >= m)
      return n * (a / m) + count(n, a % m, b, m);
   if (b >= m)
      return (n - 1) * n / 2 * (b / m) + count(n, a, b % m, m);
   return count((a + b * n) / m, (a + b * n) % m, m, b);
}
```

2.14 单纯形

2.15 辛普森积分

Chapter 3

Geometry

3.1 点、直线、圆 (gy)

```
using number = long double;
const number eps = 1e-8;
3 number _sqrt(number x) {
      return std::sqrt(std::max(x, (number) 0));
5 }
  number _asin(number x) {
      x = std::min(x, (number) 1), x = std::max(x, (number) -1);
      return std::asin(x);
9
  number _acos(number x) {
10
       x = std::min(x, (number) 1), x = std::max(x, (number) -1);
11
       return std::acos(x);
12
13
14 int sgn(number x) {
       return (x > eps) - (x < -eps);
15
16
  int cmp(number x, number y) {
17
       return sgn(x - y);
18
19
  struct point {
20
      number x, y;
       point() {}
       point(number x, number y) : x(x), y(y) {}
       number len2() const {
24
          return x * x + y * y;
25
26
       number len() const {
27
           return _sqrt(len2());
28
29
       point unit() const {
30
           return point(x / len(), y / len());
       point rotate90() const {
33
           return point(-y, x);
34
35
       friend point operator+(const point &a, const point &b) {
36
           return point(a.x + b.x, a.y + b.y);
```

3.1. 点、直线、圆 (GY)

```
38
       friend point operator-(const point &a, const point &b) {
39
           return point(a.x - b.x, a.y - b.y);
40
41
       friend point operator*(const point &a, number b) {
42
           return point(a.x * b, a.y * b);
43
44
       friend point operator/(const point &a, number b) {
45
           return point(a.x / b, a.y / b);
46
47
       friend number dot(const point &a, const point &b) {
48
49
           return a.x * b.x + a.y * b.y;
50
       friend number det(const point &a, const point &b) {
51
           return a.x * b.y - a.y * b.x;
52
53
       friend number operator == (const point &a, const point &b) {
54
           return cmp(a.x, b.x) == 0 && cmp(a.y, b.y) == 0;
55
56
   };
57
   number dis2(const point &a, const point &b) {
       return (a - b).len2();
59
60
   number dis(const point \&a, const point \&b) {
61
       return (a - b).len();
62
   }
63
   struct line {
64
       point a, b;
65
66
       line() {}
67
       line(point a, point b) : a(a), b(b) {}
       point value() const {
           return b - a;
69
70
  };
71
   bool point_on_line(const point &p, const line &l) {
72
       return sgn(det(p - 1.a, p - 1.b)) == 0;
73
  }
74
   // including endpoint
75
  bool point_on_ray(const point &p, const line &l) {
77
       return sgn(det(p - 1.a, p - 1.b)) == 0 &&
78
           sgn(dot(p - 1.a, 1.b - 1.a)) >= 0;
79
   // including endpoints
80
   bool point_on_seg(const point &p, const line &1) {
81
       return sgn(det(p - 1.a, p - 1.b)) == 0 &&
82
           sgn(dot(p - 1.a, 1.b - 1.a)) >= 0 &&
83
           sgn(dot(p - 1.b, 1.a - 1.b)) >= 0;
84
85
   bool seg_has_intersection(const line &a, const line &b) {
86
       if (point_on_seg(a.a, b) || point_on_seg(a.b, b) ||
87
               point_on_seg(b.a, a) || point_on_seg(b.b, a))
88
           return /* including endpoints */ true;
89
       return sgn(det(a.a - b.a, b.b - b.a)) * sgn(det(a.b - b.a, b.b - b.a)) < 0
90
           && sgn(det(b.a - a.a, a.b - a.a)) * sgn(det(b.b - a.a, a.b - a.a)) < 0;
91
92
   point intersect(const line &a, const line &b) {
93
       number s1 = det(a.b - a.a, b.a - a.a);
94
       number s2 = det(a.b - a.a, b.b - a.a);
```

```
return (b.a * s2 - b.b * s1) / (s2 - s1);
   }
97
   point projection(const point &p, const line &1) {
        return l.a + (l.b - l.a) * dot(p - l.a, l.b - l.a) / (l.b - l.a).len2();
99
100
   number dis(const point &p, const line &l) {
101
        return std::abs(dot(p - 1.a, 1.b - 1.a)) / (1.b - 1.a).len();
102
103
   point symmetry_point(const point &a, const point &o) {
104
        return o + o - a;
105
106
   point reflection(const point &p, const line &l) {
107
        return symmetry_point(p, projection(p, 1));
108
   }
109
   struct circle {
110
       point o;
111
        number r;
112
        circle() {}
113
        circle(point o, number r) : o(o), r(r) {}
114
115 };
    bool intersect(const line &1, const circle &a, point &p1, point &p2) {
        number x = dot(1.a - a.o, 1.b - 1.a);
117
        number y = (1.b - 1.a).len2();
118
        number d = x * x - y * ((1.a - a.o).len2() - a.r * a.r);
119
        if (sgn(d) < 0) return false;</pre>
120
        point p = 1.a - (1.b - 1.a) * (x / y), delta = (1.b - 1.a) * (_sqrt(d) / y);
121
        p1 = p + delta, p2 = p - delta;
122
        return true;
125
    bool intersect(const circle &a, const circle &b, point &p1, point &p2) {
        if (a.o == b.o \&\& cmp(a.r, b.r) == 0)
           return /* value for coincident circles */ false;
127
        number s1 = (b.o - a.o).len();
128
        if (cmp(s1, a.r + b.r) > 0 \mid \mid cmp(s1, std::abs(a.r - b.r)) < 0)
129
            return false;
130
        number s2 = (a.r * a.r - b.r * b.r) / s1;
131
        number aa = (s1 + s2) / 2, bb = (s1 - s2) / 2;
132
        point p = (b.o - a.o) * (aa / (aa + bb)) + a.o;
133
        point delta = (b.o - a.o).unit().rotate90() * _sqrt(a.r * a.r - aa * aa);
134
        p1 = p + delta, p2 = p - delta;
135
        return true;
136
137
    bool tangent(const point &p0, const circle &c, point &p1, point &p2) {
138
        number x = (p0 - c.o).len2();
139
        number d = x - c.r * c.r;
140
        if (sgn(d) < 0) return false;</pre>
141
        if (sgn(d) == 0)
142
            return /* value for point_on_line */ false;
143
        point p = (p0 - c.o) * (c.r * c.r / x);
144
145
        point delta = ((p0 - c.o) * (-c.r * \_sqrt(d) / x)).rotate90();
        p1 = c.o + p + delta;
146
        p2 = c.o + p - delta;
147
        return true;
148
149
   bool ex_tangent(const circle &a, const circle &b, line &l1, line &l2) {
150
        if (cmp(std::abs(a.r - b.r), (b.o - a.o).len()) == 0) {
151
            point p1, p2;
152
            intersect(a, b, p1, p2);
153
            11 = 12 = line(p1, p1 + (a.o - p1).rotate90());
154
```

3.1. 点、直线、圆 (GY) 27

```
return true;
155
        } else if (cmp(a.r, b.r) == 0) {
156
            point dir = b.o - a.o;
157
            dir = (dir * (a.r / dir.len())).rotate90();
158
            11 = line(a.o + dir, b.o + dir);
159
            12 = line(a.o - dir, b.o - dir);
160
            return true;
161
        } else {
162
            point p = (b.o * a.r - a.o * b.r) / (a.r - b.r);
163
            point p1, p2, q1, q2;
164
            if (tangent(p, a, p1, p2) && tangent(p, b, q1, q2)) {
165
                11 = line(p1, q1);
166
                12 = line(p2, q2);
167
                return true;
168
            } else {
169
                return false;
170
            }
171
        }
172
173
   bool in_tangent(const circle &a, const circle &b, line &l1, line &l2) {
174
        if (cmp(a.r + b.r, (b.o - a.o).len()) == 0) {
175
176
            point p1, p2;
            intersect(a, b, p1, p2);
177
            11 = 12 = line(p1, p1 + (a.o - p1).rotate90());
178
            return true;
179
        } else {
180
            point p = (b.o * a.r + a.o * b.r) / (a.r + b.r);
181
            point p1, p2, q1, q2;
182
            if (tangent(p, a, p1, p2) && tangent(p, b, q1, q2)) {
183
                11 = line(p1, q1);
184
                12 = line(p2, q2);
185
186
                return true;
            } else {
187
                return false;
188
            }
189
        }
190
191 }
```

- 3.2 点到凸包切线
- 3.3 直线凸包交点
- 3.4 凸包游戏
- 3.5 半平面交
- 3.6 旋转卡壳
- 3.7 判断圆是否有交
- 3.8 最小圆覆盖
- 3.9 最小球覆盖
- 3.10 $O(n^2 \log n)$ 圆交面积和重心
- 3.11 圆与多边形交
- 3.12 $O(n \log n)$ 凸多边形内的最大圆
- 3.13 三维凸包
- 3.14 三维绕轴旋转

Chapter 4

String

- 4.1 KMP
- 4.2 AC 自动机
- 4.3 后缀数组
- 4.4 后缀自动机
- 4.5 Manacher
- 4.6 回文自动机
- 4.7 最小表示法

Chapter 5

Data Structure

5.1 莫队 (ct)

```
int size;
   struct Query {
       int 1, r, id;
       inline bool operator < (const Queuy &that) const {return 1 / size != that.1 / size ? 1 < that.1
        \hookrightarrow: ((1 / size) & 1 ? r < that.r : r > that.r);}
5 | } q[maxn];
6 int main()
7 | {
       size = (int) sqrt(n * 1.0);
       std::sort(q + 1, q + m + 1);
       int 1 = 1, r = 0;
10
       for (int i = 1; i <= m; ++i)
           for (; r < q[i].r; ) add(++r);
14
           for (; r > q[i].r; ) del(r--);
           for (; 1 < q[i].1; ) del(1++);
15
           for (; 1 > q[i].1; ) add(--1);
16
17
               write your code here.
18
19
20
       return 0;
21
```

5.2 ST 表 (ct)

```
int a[maxn], f[20][maxn], n;
int Log[maxn];

void build()
{
    for (int i = 1; i <= n; ++i) f[0][i] = a[i];

    int lim = Log[n];
    for (int j = 1; j <= lim; ++j)
    {
        int *fj = f[j], *fj1 = f[j - 1];
        for (int i = 1; i <= n - (1 << j) + 1; ++i)
        fj[i] = dmax(fj1[i], fj1[i + (1 << (j - 1))]);
}
</pre>
```

5.3. 可并堆 (CT) 31

```
14 int Query(int 1, int r)
15 {
       int k = Log[r - 1 + 1];
16
       return dmax(f[k][1], f[k][r - (1 << k) + 1]);
17
   }
18
   int main()
19
   {
20
       scanf("%d", &n);
21
       Log[0] = -1;
22
       for (int i = 1; i <= n; ++i)
23
24
           scanf("%d", &a[i]);
25
           Log[i] = Log[i >> 1] + 1;
26
       }
27
       build();
28
       int q;
29
       scanf("%d", &q);
30
       for (; q; --q)
31
32
           int 1, r; scanf("%d%d", &1, &r);
33
           printf("%d\n", Query(1, r));
34
35
36
```

5.3 可并堆 (ct)

```
struct Node {
       Node *ch[2];
2
       11 val; int size;
       inline void update()
       {
            size = ch[0] \rightarrow size + ch[1] \rightarrow size + 1;
       }
   } mem[maxn], *rt[maxn];
  Node *merge(Node *a, Node *b)
9
10
       if (a == mem) return b;
11
       if (b == mem) return a;
12
       if (a -> val < b -> val) std::swap(a, b);
13
       // a -> pushdown();
14
       std::swap(a -> ch[0], a -> ch[1]);
15
       a -> ch[1] = merge(a -> ch[1], b);
16
       a -> update();
17
       return a;
18
19
```

5.4 zkw 线段树 (ct)

```
// must be 0-based !
inline void build()

for (int i = M - 1; i; --i) tr[i] = dmax(tr[i << 1], tr[i << 1 | 1]);

inline void Change(int x, int v)

x += M; tr[x] = v; x >>= 1;
for (; x; x >>= 1) tr[x] = dmax(tr[x << 1], tr[x << 1 | 1]);
}
</pre>
```

```
11 inline int Query(int s, int t)
12 {
       int ret = -0x7fffffff;
13
       for (s = s + M - 1, t = t + M + 1; s ^ t ^ 1; s >>= 1, t >>= 1)
14
15
           if (~s & 1) cmax(ret, tr[s ^ 1]);
16
           if (t & 1) cmax(ret, tr[t ^ 1]);
17
18
       return ret;
19
20
21
  int main()
22
       int n; scanf("%d", &n);
23
       for (M = 1; M < n; M <<= 1);
24
       for (int i = 0; i < n; ++i)
25
           scanf("%d", &tr[i + M]);
26
       for (int i = n; i < M; ++i) tr[i + M] = -0x7ffffffff;
27
       build();
28
       int q; scanf("%d", &q);
29
       for (; q; --q)
           int 1, r; scanf("%d%d", &1, &r); --1, --r;
32
           printf("%d\n", Query(1, r));
33
       }
34
       return 0;
35
36
```

5.5 Splay (ct)

指针版

```
struct Node *null;
   struct Node {
       Node *ch[2], *fa;
       int val; bool rev;
       inline bool type()
            return fa -> ch[1] == this;
       inline void pushup()
10
11
       }
       inline void pushdown()
12
       {
            if (rev)
14
15
                 ch[0] -> rev ^= 1;
16
                 ch[1] -> rev ^= 1;
17
                 std::swap(ch[0], ch[1]);
18
                 rev ^= 1;
19
            }
20
       }
21
       inline void rotate()
23
            bool d = type(); Node *f = fa, *gf = f -> fa;
24
            (fa = gf, f \rightarrow fa != null) ? fa \rightarrow ch[f \rightarrow type()] = this : 0;
25
            (f \rightarrow ch[d] = ch[!d]) != null ? ch[!d] \rightarrow fa = f : 0;
26
            (ch[!d] = f) -> fa = this;
27
            f -> pushup();
28
29
```

5.5. SPLAY (CT) 33

```
inline void splay()

for (; fa != null; rotate())

if (fa -> fa != null)

(type() == fa -> type() ? fa : this) -> rotate();

pushup();

}

mem[maxn];
```

数组版

```
// BZOJ - 1500 维修数列
   int fa[maxn], ch[maxn][2], a[maxn], size[maxn], cnt;
   int sum[maxn], lmx[maxn], rmx[maxn], mx[maxn], v[maxn], id[maxn], root;
  bool rev[maxn], tag[maxn];
  inline void update(R int x)
5
6
       R \text{ int } ls = ch[x][0], rs = ch[x][1];
       size[x] = size[ls] + size[rs] + 1;
       sum[x] = sum[ls] + sum[rs] + v[x];
       mx[x] = gmax(mx[ls], mx[rs]);
10
       cmax(mx[x], lmx[rs] + rmx[ls] + v[x]);
       lmx[x] = gmax(lmx[ls], sum[ls] + v[x] + lmx[rs]);
       rmx[x] = gmax(rmx[rs], sum[rs] + v[x] + rmx[ls]);
13
14
   }
   inline void pushdown(R int x)
15
16
   {
       R \text{ int } ls = ch[x][0], rs = ch[x][1];
17
       if (tag[x])
18
19
           rev[x] = tag[x] = 0;
20
           if (ls) tag[ls] = 1, v[ls] = v[x], sum[ls] = size[ls] * v[x];
21
           if (rs) tag[rs] = 1, v[rs] = v[x], sum[rs] = size[rs] * v[x];
22
23
           if (v[x] >= 0)
24
           {
               if (ls) lmx[ls] = rmx[ls] = mx[ls] = sum[ls];
25
               if (rs) lmx[rs] = rmx[rs] = mx[rs] = sum[rs];
26
           }
27
           else
28
           {
29
               if (ls) lmx[ls] = rmx[ls] = 0, mx[ls] = v[x];
30
               if (rs) lmx[rs] = rmx[rs] = 0, mx[rs] = v[x];
31
           }
32
       }
33
       if (rev[x])
34
35
       {
           rev[x] ^= 1; rev[ls] ^= 1; rev[rs] ^= 1;
36
           swap(lmx[ls], rmx[ls]);swap(lmx[rs], rmx[rs]);
37
           swap(ch[ls][0], ch[ls][1]); swap(ch[rs][0], ch[rs][1]);
38
39
40
   inline void rotate(R int x)
41
42
       R int f = fa[x], gf = fa[f], d = ch[f][1] == x;
43
       if (f == root) root = x;
44
       (ch[f][d] = ch[x][d ^ 1]) > 0 ? fa[ch[f][d]] = f : 0;
45
       (fa[x] = gf) > 0 ? ch[gf][ch[gf][1] == f] = x : 0;
46
       fa[ch[x][d ^ 1] = f] = x;
47
       update(f);
48
49
50 inline void splay(R int x, R int rt)
```

```
51 {
       while (fa[x] != rt)
53
            R int f = fa[x], gf = fa[f];
54
            if (gf != rt) rotate((ch[gf][1] == f) ^ (ch[f][1] == x) ? x : f);
55
            rotate(x);
56
57
       update(x);
58
59
   void build(R int 1, R int r, R int rt)
60
61
       if (1 > r) return;
62
       R int mid = 1 + r >> 1, now = id[mid], last = id[rt];
63
       if (1 == r)
64
       Ł
65
            sum[now] = a[1];
66
            size[now] = 1;
67
            tag[now] = rev[now] = 0;
68
            if (a[1] >= 0) lmx[now] = rmx[now] = mx[now] = a[1];
69
            else lmx[now] = rmx[now] = 0, mx[now] = a[1];
70
       }
71
72
       else
       {
73
            build(1, mid - 1, mid);
74
            build(mid + 1, r, mid);
75
       }
76
       v[now] = a[mid];
77
       fa[now] = last;
78
       update(now);
79
80
       ch[last][mid >= rt] = now;
81
   int find(R int x, R int rank)
82
83
       if (tag[x] || rev[x]) pushdown(x);
84
       R int ls = ch[x][0], rs = ch[x][1], lsize = size[ls];
85
       if (lsize + 1 == rank) return x;
86
       if (lsize >= rank)
87
           return find(ls, rank);
88
89
            return find(rs, rank - lsize - 1);
90
91 }
92 inline int prepare(R int 1, R int tot)
93 | {
       R int x = find(root, 1 - 1), y = find(root, 1 + tot);
94
95
       splay(x, 0);
       splay(y, x);
96
       return ch[y][0];
97
98
   std::queue <int> q;
99
   inline void Insert(R int left, R int tot)
100
101
       for (R int i = 1; i <= tot; ++i) a[i] = FastIn();
102
       for (R int i = 1; i <= tot; ++i)
103
            if (!q.empty()) id[i] = q.front(), q.pop();
104
            else id[i] = ++cnt;
105
       build(1, tot, 0);
106
       R int z = id[(1 + tot) >> 1];
107
       R int x = find(root, left), y = find(root, left + 1);
108
       splay(x, 0);
109
       splay(y, x);
110
       fa[z] = y;
```

5.5. SPLAY (CT) 35

```
ch[y][0] = z;
112
        update(y);
113
        update(x);
114
   }
115
   void rec(R int x)
116
   {
117
        if (!x) return ;
118
        R \text{ int } ls = ch[x][0], rs = ch[x][1];
119
        rec(ls); rec(rs); q.push(x);
120
        fa[x] = ch[x][0] = ch[x][1] = 0;
121
        tag[x] = rev[x] = 0;
^{122}
123
   inline void Delete(R int 1, R int tot)
124
125
        R int x = prepare(1, tot), f = fa[x];
126
        rec(x); ch[f][0] = 0;
127
        update(f); update(fa[f]);
128
129
   inline void Makesame (R int 1, R int tot, R int val)
130
131
        R int x = prepare(1, tot), y = fa[x];
132
133
        v[x] = val; tag[x] = 1; sum[x] = size[x] * val;
        if (val >= 0) lmx[x] = rmx[x] = mx[x] = sum[x];
134
        else lmx[x] = rmx[x] = 0, mx[x] = val;
135
        update(y); update(fa[y]);
136
137
   inline void Reverse(R int 1, R int tot)
138
139
        R int x = prepare(1, tot), y = fa[x];
140
141
        if (!tag[x])
142
            rev[x] ^= 1;
143
            swap(ch[x][0], ch[x][1]);
144
            swap(lmx[x], rmx[x]);
145
            update(y); update(fa[y]);
146
147
148
   inline void Query(R int 1, R int tot)
149
150
        R int x = prepare(1, tot);
151
        printf("%d\n",sum[x]);
152
153
   #define inf ((1 << 30))
   int main()
155
156
        R int n = FastIn(), m = FastIn(), 1, tot, val;
157
        R char op, op2;
158
        mx[0] = a[1] = a[n + 2] = -inf;
159
        for (R int i = 2; i <= n + 1; i++ )
160
        {
161
            a[i] = FastIn();
162
        }
163
        for (R int i = 1; i \le n + 2; ++i) id[i] = i;
164
        n += 2; cnt = n; root = (n + 1) >> 1;
165
        build(1, n, 0);
166
        for (R int i = 1; i <= m; i++ )
167
168
            op = getc();
169
            while (op < 'A' \mid \mid op > 'Z') op = getc();
170
            getc(); op2 = getc();getc();getc();getc();
171
            if (op == 'M' && op2 == 'X')
172
```

```
{
173
                 printf("%d\n",mx[root] );
174
            }
175
            else
176
            {
177
                 1 = FastIn() + 1; tot = FastIn();
178
                 if (op == 'I') Insert(1, tot);
179
                 if (op == 'D') Delete(1, tot);
180
                 if (op == 'M') val = FastIn(), Makesame(1, tot, val);
181
                 if (op == 'R')
182
                     Reverse(1, tot);
183
                 if (op == 'G')
184
                     Query(1, tot);
185
            }
186
        }
187
        return 0;
188
189
```

5.6 Treap (ct)

```
struct Treap {
       Treap *ls, *rs;
       int size;
       bool rev;
       inline void update()
       {
           size = ls -> size + rs -> size + 1;
9
       inline void set_rev()
10
           rev ^= 1;
11
           std::swap(ls, rs);
12
13
       inline void pushdown()
14
^{15}
           if (rev)
16
17
                ls -> set_rev();
18
               rs -> set_rev();
19
                rev = 0;
20
           }
21
       }
23 | } mem[maxn], *root, *null = mem;
24 struct Pair {
       Treap *fir, *sec;
25
26 };
  Treap *build(R int 1, R int r)
27
28
       if (1 > r) return null;
29
       R int mid = 1 + r >> 1;
30
       R Treap *now = mem + mid;
31
32
       now \rightarrow rev = 0;
       now \rightarrow ls = build(1, mid - 1);
       now -> rs = build(mid + 1, r);
34
       now -> update();
35
       return now;
36
37 }
38 inline Treap *Find_kth(R Treap *now, R int k)
```

5.7. 可持久化平衡树 (CT)

```
39 {
       if (!k) return mem;
40
       if (now -> ls -> size >= k) return Find_kth(now -> ls, k);
41
       else if (now -> ls -> size + 1 == k) return now;
42
       else return Find_kth(now -> rs, k - now -> ls -> size - 1);
43
44
   Treap *merge(R Treap *a, R Treap *b)
45
46
47
       if (a == null) return b;
       if (b == null) return a;
48
       if (rand() % (a -> size + b -> size) < a -> size)
49
50
           a -> pushdown();
51
           a -> rs = merge(a -> rs, b);
52
           a -> update();
53
           return a;
54
       }
55
       else
56
       {
57
           b -> pushdown();
58
           b -> ls = merge(a, b -> ls);
59
           b -> update();
60
           return b;
61
62
63
  Pair split(R Treap *now, R int k)
64
65
       if (now == null) return (Pair) {null, null};
66
       R Pair t = (Pair) {null, null};
67
       now -> pushdown();
68
       if (k \le now -> ls -> size)
69
70
           t = split(now -> ls, k);
71
           now -> ls = t.sec;
72
           now -> update();
73
           t.sec = now;
74
       }
75
       else
76
77
            t = split(now \rightarrow rs, k - now \rightarrow ls \rightarrow size - 1);
78
           now -> rs = t.fir;
79
           now -> update();
80
81
           t.fir = now;
       }
82
       return t;
83
84
   }
   inline void set_rev(int 1, int r)
85
86
       R Pair x = split(root, 1 - 1);
87
       R Pair y = split(x.sec, r - 1 + 1);
88
       y.fir -> set_rev();
89
       root = merge(x.fir, merge(y.fir, y.sec));
90
91
```

5.7 可持久化平衡树 (ct)

```
char str[maxn];
struct Treap
{
```

```
Treap *ls, *rs;
       char data; int size;
       inline void update()
6
           size = ls -> size + rs -> size + 1;
9
10 } *root[maxn], mem[maxcnt], *tot = mem, *last = mem, *null = mem;
inline Treap* new_node(char ch)
12
       *++tot = (Treap) {null, null, ch, 1};
13
14
       return tot;
15
  struct Pair
16
17
       Treap *fir, *sec;
18
19 };
  inline Treap *copy(Treap *x)
20
21 {
       if (x == null) return null;
22
       if(x > last) return x;
23
       *++tot = *x;
       return tot;
25
26 }
27 Pair Split(Treap *x, int k)
28
       if (x == null) return (Pair) {null, null};
29
       Pair y;
30
       Treap *nw = copy(x);
31
       if (nw \rightarrow ls \rightarrow size >= k)
32
33
           y = Split(nw -> ls, k);
34
           nw -> ls = y.sec;
35
           nw -> update();
36
           y.sec = nw;
37
       }
38
       else
39
40
           y = Split(nw \rightarrow rs, k - nw \rightarrow ls \rightarrow size - 1);
41
           nw -> rs = y.fir;
42
           nw -> update();
43
44
           y.fir = nw;
45
       }
       return y;
46
47
  |}
  Treap *Merge(Treap *a, Treap *b)
48
49
       if (a == null) return b;
50
       if (b == null) return a;
51
       Treap *nw;
52
       if (rand() \% (a -> size + b -> size) < a -> size)
53
54
55
           nw = copy(a);
           nw -> rs = Merge(nw -> rs, b);
56
       }
57
       else
58
       {
59
           nw = copy(b);
60
           nw -> ls = Merge(a, nw -> ls);
61
62
       nw -> update();
63
       return nw;
```

```
65 }
   Treap *Build(int 1, int r)
66
67
        if (1 > r) return null;
68
        R int mid = 1 + r >> 1;
69
        Treap *nw = new_node(str[mid]);
70
        nw -> ls = Build(1, mid - 1);
71
        nw -> rs = Build(mid + 1, r);
72
        nw -> update();
73
        return nw;
74
75
76
   int now;
   inline void Insert(int k, char ch)
77
78
        Pair x = Split(root[now], k);
79
        Treap *nw = new_node(ch);
80
        root[++now] = Merge(Merge(x.fir, nw), x.sec);
81
82
   inline void Del(int 1, int r)
83
84
        Pair x = Split(root[now], 1 - 1);
85
        Pair y = Split(x.sec, r - 1 + 1);
86
        root[++now] = Merge(x.fir, y.sec);
87
88
   inline void Copy(int 1, int r, int 11)
89
90
        Pair x = Split(root[now], 1 - 1);
91
        Pair y = Split(x.sec, r - 1 + 1);
92
        Pair z = Split(root[now], 11);
93
94
        Treap *ans = y.fir;
        root[++now] = Merge(Merge(z.fir, ans), z.sec);
95
96
   void Print(Treap *x, int 1, int r)
97
98
        if (!x) return ;
99
        if (1 > r) return;
100
        R int mid = x \rightarrow ls \rightarrow size + 1;
101
        if (r < mid)</pre>
102
        {
103
            Print(x -> ls, l, r);
104
            return ;
105
        }
106
107
        if (1 > mid)
108
        {
109
            Print(x -> rs, l - mid, r - mid);
            return ;
110
111
        Print(x -> ls, l, mid - 1);
112
        printf("%c", x -> data );
113
        Print(x -> rs, 1, r - mid);
114
115
   void Printtree(Treap *x)
116
117
        if (!x) return;
118
        Printtree(x -> ls);
119
        printf("%c", x \rightarrow data);
120
        Printtree(x -> rs);
121
122 }
123 int main()
124 {
        srand(time(0) + clock());
```

```
null -> ls = null -> rs = null; null -> size = 0; null -> data = 0;
126
        int n = F();
127
        gets(str + 1);
128
        int len = strlen(str + 1);
129
        root[0] = Build(1, len);
130
        while (1)
131
132
             last = tot;
133
            R char opt = getc();
134
             while (opt < 'A' \mid \mid opt > 'Z')
135
136
                 if (opt == EOF) return 0;
137
                 opt = getc();
138
             }
139
             if (opt == 'I')
140
141
                 R int x = F();
142
                 R char ch = getc();
143
                 Insert(x, ch);
144
145
             else if (opt == 'D')
146
147
                 R int 1 = F(), r = F();
148
                 Del(1, r);
149
             }
150
             else if (opt == 'C')
151
152
                 R \text{ int } x = F(), y = F(), z = F();
153
                 Copy(x, y, z);
154
             }
155
             else if (opt == 'P')
157
                 R \text{ int } x = F(), y = F(), z = F();
                 Print(root[now - x], y, z);
159
                 puts("");
160
161
        }
162
        return 0;
163
164
```

5.8 CDQ 分治 (ct)

```
struct event
2 {
      int x, y, id, opt, ans;
  } t[maxn], q[maxn];
  void cdq(int left, int right)
6
      if (left == right) return ;
      R int mid = left + right >> 1;
      cdq(left, mid);
10
      cdq(mid + 1, right);
      //分成若干个子问题
11
12
      ++now;
      for (int i = left, j = mid + 1; j <= right; ++j)
13
14
           for (; i <= mid && q[i].x <= q[j].x; ++i)
15
               if (!q[i].opt)
16
17
                   add(q[i].y, q[i].ans);
```

5.9. BITSET (CT) 41

```
//考虑前面的修改操作对后面的询问的影响
18
           if (q[j].opt)
19
               q[j].ans += query(q[j].y);
20
       }
21
       R int i, j, k = 0;
22
       //以下相当于归并排序
23
       for (i = left, j = mid + 1; i <= mid \&\& j <= right; )
24
25
           if (q[i].x \le q[j].x)
26
27
               t[k++] = q[i++];
           else
28
               t[k++] = q[j++];
29
       }
30
       for (; i <= mid; )
31
           t[k++] = q[i++];
32
       for (; j <= right; )</pre>
33
           t[k++] = q[j++];
34
       for (int i = 0; i < k; ++i)
35
           q[left + i] = t[i];
36
37
```

5.9 Bitset (ct)

```
namespace Game {
   #define maxn 300010
   #define maxs 30010
  uint b1[32][maxs], b2[32][maxs];
   int popcnt[256];
5
   inline void set(R uint *s, R int pos)
6
       s[pos >> 5] = 1u << (pos & 31);
8
   }
   inline int popcount(R uint x)
10
11
       return popcnt[x >> 24 & 255]
^{12}
            + popcnt[x >> 16 & 255]
13
            + popcnt[x >> 8 & 255]
14
            + popcnt[x
                            & 255];
15
16
   void main() {
17
       int n, q;
       scanf("%d%d", &n, &q);
19
       char *s1 = new char[n + 1];
20
       char *s2 = new char[n + 1];
21
       scanf("%s%s", s1, s2);
22
       uint *anss = new uint[q];
23
       for (R int i = 1; i < 256; ++i) popcnt[i] = popcnt[i >> 1] + (i & 1);
24
25
       #define modify(x, _p)\
26
           for (R int j = 0; j < 32 && j <= p; ++j)\
27
               set(b##x[j], p - j); \
28
29
       for (R int i = 0; i < n; ++i)
30
           if (s1[i] == '0') modify(1, 3 * i)
31
           else if (s1[i] == '1') modify(1, 3 * i + 1)
32
```

```
else modify(1, 3 * i + 2)
       for (R int i = 0; i < n; ++i)
34
           if (s2[i] == '1') modify(2, 3 * i)
35
           else if (s2[i] == '2') modify(2, 3 * i + 1)
36
           else modify(2, 3 * i + 2)
37
       for (int Q = 0; Q < q; ++Q) {
38
           R int x, y, 1;
39
           scanf("%d%d%d", &x, &y, &1); x *= 3; y *= 3; 1 *= 3;
40
           uint *f1 = b1[x \& 31], *f2 = b2[y \& 31], ans = 0;
41
           R int i = x >> 5, j = y >> 5, p, lim;
42
           for (p = 0, lim = 1 >> 5; p + 8 < lim; p += 8, i += 8, j += 8)
43
44
               ans += popcount(f1[i + 0] & f2[j + 0]);
^{45}
               ans += popcount(f1[i + 1] & f2[j + 1]);
46
               ans += popcount(f1[i + 2] \& f2[j + 2]);
47
               ans += popcount(f1[i + 3] & f2[j + 3]);
48
               ans += popcount(f1[i + 4] & f2[j + 4]);
49
               ans += popcount(f1[i + 5] & f2[j + 5]);
50
               ans += popcount(f1[i + 6] & f2[j + 6]);
51
               ans += popcount(f1[i + 7] & f2[j + 7]);
52
           }
53
           for (; p < lim; ++p, ++i, ++j) ans += popcount(f1[i] & f2[j]);
54
           R uint S = (1u \ll (1 \& 31)) - 1;
55
           ans += popcount(f1[i] & f2[j] & S);
56
           anss[Q] = ans;
57
58
59
       output_arr(anss, q * sizeof(uint));
60
61 }
```

Chapter 6

Others

6.1 vimrc (gy)

```
se et ts=4 sw=4 sts=4 nu sc sm lbr is hls mouse=a
  sy on
  ino <tab> <c-n>
  ino <s-tab> <tab>
  au bufwinenter * winc L
  nm <f6> ggVG"+y
  nm <f7> :w<cr>:make<cr>
  nm <f8> :!@<cr>
  nm <f9> :!@ < in<cr>
  nm <s-f9> :!(time @ < in &> out) &>> out<cr>:sp out<cr>
  au filetype cpp cm @ ./a.out | se cin fdm=syntax mp=g++\ %\ -std=c++11\ -Wall\ -Wextra\
    \hookrightarrow -Wconversion\ -02
12 map <c-p> :ha<cr>
  se pheader=%N@%F popt=number:y
  au filetype java cm @ java %< | se cin fdm=syntax mp=javac\ %
  au filetype python cm @ python % | se si fdm=indent
  au bufenter *.kt setf kotlin
  au filetype kotlin cm @ kotlin _%<Kt | se si mp=kotlinc\ %
```

6.2 STL 释放内存 (Durandal)

```
template <typename T>
   __inline void clear(T &container) {
    container.clear();
    T(container).swap(container);
}
```

6.3 开栈 (Durandal)

```
register char *_sp __asm__("rsp");
int main() {
   const int size = 400 << 20; // 400 MB
   static char *sys, *mine(new char[size] + size - 4096);
   sys = _sp; _sp = mine;
   _main(); // main method</pre>
```

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```
7
    _sp = sys;
8
    return 0;
9
```

6.4 O3 (gy)

```
__attribute__((optimize("-03"))) int main() { return 0; }
```

6.5 Java Template (gy)

```
import java.io.*;
  import java.math.*;
  import java.util.*;
  public class Template {
       // Input
5
       private static BufferedReader reader;
       private static StringTokenizer tokenizer;
       private static String next() {
           try {
10
               while (tokenizer == null || !tokenizer.hasMoreTokens())
                   tokenizer = new StringTokenizer(reader.readLine());
11
           } catch (IOException e) {
12
               // do nothing
13
14
           return tokenizer.nextToken();
15
16
       private static int nextInt() {
17
           return Integer.parseInt(next());
18
19
       private static double nextDouble() {
20
           return Double.parseDouble(next());
21
22
       private static BigInteger nextBigInteger() {
23
           return new BigInteger(next());
24
25
       public static void main(String[] args) {
26
           reader = new BufferedReader(new InputStreamReader(System.in));
27
           Scanner scanner = new Scanner(System.in);
           while (scanner.hasNext())
29
30
               scanner.next();
       }
31
       // BigInteger & BigDecimal
32
       private static void bigDecimal() {
33
           BigDecimal a = BigDecimal.valueOf(1.0);
34
           BigDecimal b = a.setScale(50, RoundingMode.HALF_EVEN);
35
           BigDecimal c = b.abs();
36
           // if scale omitted, b.scale is used
37
           BigDecimal d = c.divide(b, 50, RoundingMode.HALF_EVEN);
           // since Java 9
39
           BigDecimal e = d.sqrt(new MathContext(50, RoundingMode.HALF_EVEN));
40
           BigDecimal x = new BigDecimal(BigInteger.ZERO);
41
           BigInteger y = BigDecimal.ZERO.toBigInteger(); // RoundingMode.DOWN
42
           y = BigDecimal.ZERO.setScale(0, RoundingMode.HALF_EVEN).unscaledValue();
43
44
       // sqrt for Java 8
45
```

```
// can solve scale=100 for 10000 times in about 1 second
46
       private static BigDecimal sqrt(BigDecimal a, int scale) {
47
            if (a.compareTo(BigDecimal.ZERO) < 0)</pre>
48
                return BigDecimal.ZERO.setScale(scale, RoundingMode.HALF_EVEN);
49
            int length = a.precision() - a.scale();
50
            BigDecimal ret = new BigDecimal(BigInteger.ONE, -length / 2);
51
            for (int i = 1; i <= Integer.highestOneBit(scale) + 10; i++)</pre>
52
                ret = ret.add(a.divide(ret, scale,
53
                  → RoundingMode.HALF_EVEN)).divide(BigDecimal.valueOf(2), scale,
                  → RoundingMode.HALF_EVEN);
            return ret;
54
55
       // can solve a=2^10000 for 100000 times in about 1 second
56
       private static BigInteger sqrt(BigInteger a) {
57
            int length = a.bitLength() - 1;
58
            BigInteger 1 = BigInteger.ZERO.setBit(length / 2), r = BigInteger.ZERO.setBit(length / 2);
59
            while (!1.equals(r)) {
60
                BigInteger m = 1.add(r).shiftRight(1);
61
                if (m.multiply(m).compareTo(a) < 0)</pre>
62
                    1 = m.add(BigInteger.ONE);
63
                else
64
                    r = m;
65
66
67
            return 1;
       }
68
       // Collections
69
       private static void arrayList() {
70
           List<Integer> list = new ArrayList<>();
71
72
            // Generic array is banned
73
            List[] lists = new List[100];
74
            lists[0] = new ArrayList<Integer>();
            // for List<Integer>, remove(Integer) stands for element, while remove(int) stands for
75
              \rightarrow index
            list.remove(list.get(1));
76
            list.remove(list.size() - 1);
77
            list.clear():
78
            Queue<Integer> queue = new LinkedList<>();
79
            // return the value without popping
80
            queue.peek();
81
            // pop and return the value
82
            queue.poll();
83
            Queue<Integer> priorityQueue = new PriorityQueue<>();
85
            Deque<Integer> deque = new ArrayDeque<>();
86
            deque.peekFirst();
87
            deque.peekLast();
            deque.pollFirst();
88
            TreeSet<Integer> set = new TreeSet<>();
89
            TreeSet<Integer> anotherSet = new TreeSet<>(Comparator.reverseOrder());
90
            set.ceiling(1);
91
            set.floor(1);
92
            set.lower(1);
93
            set.higher(1);
94
            set.contains(1);
95
            HashSet<Integer> hashSet = new HashSet<>();
96
            HashMap<String, Integer> map = new HashMap<>();
97
            map.put("", 1);
98
            map.get("");
99
            map.forEach((string, integer) -> System.out.println(string + integer));
100
            TreeMap<String, Integer> treeMap = new TreeMap<>();
101
            Arrays.sort(new int[10]);
102
```

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```
Arrays.sort(new Integer[10], (a, b) -> {
103
                if (a.equals(b)) return 0;
104
                if (a > b) return -1;
105
                return 1;
106
            });
107
            Arrays.sort(new Integer[10], Comparator.comparingInt((a) -> (int) a).reversed());
108
            long a = 1_000_000_000_000_000_000L;
109
            int b = Integer.MAX_VALUE;
110
            int c = 'a';
111
112
113
```

6.6 Big Fraction (gy)

```
fun gcd(a: Long, b: Long): Long = if (b == OL) a else gcd(b, a % b)
   class Fraction(val a: BigInteger, val b: BigInteger) {
       constructor(a: Long, b: Long) : this(BigInteger.valueOf(a / gcd(a, b)), BigInteger.valueOf(b /
         \hookrightarrow \gcd(a, b)))
       operator fun plus(o: Fraction): Fraction {
           var gcd = b.gcd(o.b)
           val tempProduct = (b / gcd) * (o.b / gcd)
           var ansA = a * (o.b / gcd) + o.a * (b / gcd)
           val gcd2 = ansA.gcd(gcd)
           ansA /= gcd2
           gcd /= gcd2
10
           return Fraction(ansA, gcd * tempProduct)
11
12
       operator fun minus(o: Fraction): Fraction {
14
           var gcd = b.gcd(o.b)
15
           val tempProduct = (b / gcd) * (o.b / gcd)
           var ansA = a * (o.b / gcd) - o.a * (b / gcd)
16
           val gcd2 = ansA.gcd(gcd)
17
           ansA /= gcd2
18
           gcd /= gcd2
19
           return Fraction(ansA, gcd * tempProduct)
20
21
       operator fun times(o: Fraction): Fraction {
22
           val gcd1 = a.gcd(o.b)
23
           val gcd2 = b.gcd(o.a)
24
           return Fraction((a / gcd1) * (o.a / gcd2), (b / gcd2) * (o.b / gcd1))
25
26
  }
27
```

6.7 模拟退火 (ct)

6.8. = 分(CT) 47

```
10
       return maxx;
11 }
12 int main()
   {
13
       srand(time(NULL) + clock());
14
       db x = 0, fnow = f(x);
15
       fans = 1e30;
16
       for (db T = 1e4; T > 1e-4; T *= 0.997)
17
18
           db nx = x + randp() * T, fnext = f(nx);
19
           db delta = fnext - fnow;
20
           if (delta < 1e-9 || exp(-delta / T) > rand01())
21
22
                x = nx;
23
                fnow = fnext;
24
           }
25
26
       return 0;
27
28
```

6.8 三分 (ct)

```
inline db cubic_search()
{
    double 1 = -1e4, r = 1e4;
    for (int i = 1; i <= 100; ++i)
    {
        double ll = (l + r) * 0.5;
        double rr = (ll + r) * 0.5;
        if (check(ll) < check(rr)) r = rr;
        else l = ll;
    }
    return (l + r) * 0.5;
}</pre>
```

6.9 Zeller Congruence (gy)

```
int day_in_week(int year, int month, int day) {
   if (month == 1 || month == 2)
        month += 12, year--;
   int c = year / 100, y = year % 100, m = month, d = day;
   int ret = (y + y / 4 + c / 4 + 5 * c + 13 * (m + 1) / 5 + d + 6) % 7;
   return ret >= 0 ? ret : ret + 7;
}
```

6.10 博弈论模型 (gy)

• Wythoff's game

给定两堆石子,每次可以从任意一堆中取至少一个石子,或从两堆中取相同的至少一个石子,取走最后 石子的胜

```
先手胜当且仅当石子数满足:
```

```
上(b-a) \times \phi = a, (a \le b, \phi = \frac{\sqrt{5}+1}{2})
先手胜对应的石子数构成两个序列:
Lower Wythoff sequence: a_n = \lfloor n \times \phi \rfloor
```

Lower Wython sequence: $a_n = \lfloor n \times \phi \rfloor$ Upper Wythoff sequence: $b_n = \lfloor n \times \phi^2 \rfloor$

• Fibonacci nim

给定一堆石子,第一次可以取至少一个、少于石子总数数量的石子,之后每次可以取至少一个、不超过 上次取石子数量两倍的石子,取走最后石子的胜 先手胜当且仅当石子数为斐波那契数

6.11 积分表

- $\sin x \to -\cos x$
- $\cos x \to \sin x$
- $\tan x \to -\ln \cos x$
- $\sec x \to \ln\left|\sin\frac{x}{2} + \cos\frac{x}{2}\right| \ln\left|-\sin\frac{x}{2} + \cos\frac{x}{2}\right|$
- $\csc x \to \ln\left|\sin\frac{x}{2}\right| \ln\left|\cos\frac{x}{2}\right|$
- $\sin^2 x \to \frac{x}{2} \frac{1}{2}\sin x \cos x$
- $\cos^2 x \to \frac{x}{2} + \frac{1}{2}\sin x \cos x$
- $\tan^2 x \to \tan x x$
- $\sec^2 x \to \tan x$
- $\csc^2 x \to -\tan x$
- $\arcsin x \to \frac{1}{\sqrt{1-x^2}}$
- $\arccos x \to -\frac{1}{\sqrt{1-x^2}}$
- $\arctan x \to \frac{1}{1+x^2}$
- $a^x \to \frac{a^x}{\ln a}$
- $\frac{1}{x^2+a^2} \to \frac{1}{|a|} \arctan \frac{x}{|a|}$
- $\frac{1}{x^2 a^2} \to \frac{1}{2} \ln|x a| \frac{1}{2} \ln|x + a|$
- $\frac{x}{ax+b} \to \frac{x}{a} \frac{b}{a^2} \ln|ax+b|$
- $\frac{x}{ax^2+c} \to \frac{1}{2a} \ln \left| ax^2 + c \right|$
- $\sqrt{c+x^2} \to \frac{x}{2}\sqrt{c+x^2} + \frac{c}{2}\ln|x+\sqrt{c+x^2}|$
- $\sqrt{c-x^2} \to \frac{x}{2}\sqrt{c-x^2} + \frac{c}{2}\arctan\frac{x}{\sqrt{c-x^2}}$
- $\frac{1}{\sqrt{c+x^2}} \to \ln\left|x + \sqrt{c+x^2}\right|$
- $\frac{1}{\sqrt{c-x^2}} \to \arctan \frac{x}{\sqrt{c-x^2}}$

6.12 公式、数列、定理

• 求和公式

$$-\sum_{k=1}^{n} (2k-1)^2 = \frac{1}{3}n(4n^2 - 1)$$
$$-\sum_{k=1}^{n} k^3 = \frac{1}{4}n^2(n+1)^2$$

$$-\sum_{k=1}^{n} (2k-1)^3 = n^2(2n^2 - 1)$$

$$-\sum_{k=1}^{n} k^4 = \frac{1}{30}n(n+1)(2n+1)(3n^2 + 3m - 1)$$

$$-\sum_{k=1}^{n} k^5 = \frac{1}{12}n^2(n+1)^2(2n^2 + 2n - 1)$$

$$-\sum_{k=1}^{n} k(k+1) = \frac{1}{3}n(n+1)(n+2)$$

$$-\sum_{k=1}^{n} k(k+1)(k+2) = \frac{1}{4}n(n+1)(n+2)(n+3)$$

$$-\sum_{k=1}^{n} k(k+1)(k+2)(k+3) = \frac{1}{5}n(n+1)(n+2)(n+3)(n+4)$$

• 错排公式

 D_n 表示 n 个元素错位排列的方案数

$$D_1 = 0, D_2 = 1$$

$$D_n = (n-1)(D_{n-2} + D_{n-1}), n \ge 3$$

$$D_n = n! \cdot (1 - \frac{1}{1!} + \frac{1}{2!} - \dots + (-1)^n \frac{1}{n!})$$

• Fibonacci sequence

$$F_{0} = 0, F_{1} = 1$$

$$F_{n} = F_{n-1} + F_{n-2}$$

$$F_{n+1} \cdot F_{n-1} - F_{n}^{2} = (-1)^{n}$$

$$F_{-n} = (-1)^{n} F_{n}$$

$$F_{n+k} = F_{k} \cdot F_{n+1} + F_{k-1} \cdot F_{n}$$

$$\gcd(F_{m}, F_{n}) = F_{\gcd(m,n)}$$

$$F_{m} \mid F_{n}^{2} \Leftrightarrow nF_{n} \mid m$$

$$F_{n} = \frac{\varphi^{n} - \Psi^{n}}{\sqrt{5}}, \varphi = \frac{1 + \sqrt{5}}{2}, \Psi = \frac{1 - \sqrt{5}}{2}$$

$$F_{n} = \lfloor \frac{\varphi^{n}}{\sqrt{5}} + \frac{1}{2} \rfloor, n \ge 0$$

$$n(F) = \lfloor \log_{\varphi}(F \cdot \sqrt{5} + \frac{1}{2}) \rfloor$$

• 第一类 Stirling number

用 $s(n,k) = (-1)^{n-k} {n \brack k}$ 表示第一类 Stirling number ${n+1 \brack k} = n {n \brack k} + {n \brack n}, k > 0$ ${0 \brack 0} = 1, {n \brack 0} = {n \brack n} = 0, n > 0$ ${n \brack k}$ 为将 n 个元素分成 k 个环的方案数

• 第二类 Stirling number

用 $S(n,k) = \binom{n}{k}$ 表示第二类 Stirling number $\binom{n+1}{k} = k\binom{n}{k} + \binom{n}{k-1}, k > 0$ $\binom{0}{0} = 1, \binom{n}{0} = \binom{0}{n} = 0, n > 0$ $\binom{n}{k} = \frac{1}{k!} \sum_{j=0}^{k} (-1)^{k-j} \binom{k}{j} j^n$ $\binom{n}{k}$ 为将 n 个元素划分成 k 个非空集合的方案数

• Catalan number

 c_n 表示长度为 2n 的合法括号序的数量 $c_1=1,\,c_{n+1}=\sum\limits_{i=1}^nc_i\times c_{n+1-i}$ $c_n=\frac{\binom{2n}{n}}{n+1}$

• Bell number

 B_n 表示基数为 n 的集合的划分方案数

$$B_i = \begin{cases} 1 & i = 0\\ \sum_{k=0}^{n} \binom{n}{k} B_k & i > 0 \end{cases}$$
$$B_n = \sum_{k=0}^{n} \binom{n}{k}$$

• 五边形数定理

$$p(n)$$
 表示将 n 划分为若干个正整数之和的方案数 $p(n) = \sum_{k \in \mathbb{N}^*} (-1)^{k-1} p(n - \frac{k(3k-1)}{2})$

$$\begin{aligned} & \underset{j=0}{\mathbf{Bernoulli number}} \\ & \underset{j=0}{\overset{m}{\sum}} \binom{m+1}{j} B_j = 0, m > 0 \\ & B_i = \begin{cases} 1 & i = 0 \\ & \frac{\sum\limits_{j=0}^{i-1} \binom{i+1}{j}}{-\frac{j=0}{i+1}} & i > 0 \\ & \sum\limits_{k=1}^{n} k^m = \frac{1}{m+1} \sum\limits_{k=0}^{m} \binom{m+1}{k} B_k n^{m+1-k} \end{aligned}$$

• Möbius function

 $\mu(n) = \begin{cases} 1 & n \text{ is a square-free positive integer with an even number of prime factors} \\ -1 & n \text{ is a square-free positive integer with an odd number of prime factors} \\ 0 & n \text{ has a squared prime factor} \end{cases}$

$$\sum_{d|n} \mu(d) = \begin{cases} 1 & n = 1\\ 0 & n > 1 \end{cases}$$
$$g(n) = \sum_{d|n} f(d) \Leftrightarrow f(n) = \sum_{d|n} \mu(d)g(\frac{n}{d})$$

• Lagrange polynomial 给定次数为 n 的多项式函数 L(x) 上的 n+1 个点 $(x_0,y_0),(x_1,y_1),\ldots,(x_n,y_n)$ 则 $L(x) = \sum_{j=0}^{n} y_j \prod_{0 < m < n, m \neq j} \frac{x - x_m}{x_j - x_m}$

• 树的计数

– 有根树计数

$$a_1=1$$

$$a_{n+1}=rac{\sum\limits_{j=1}^{n} j\cdot a_j\cdot S_{n,j}}{n}$$

$$S_{n,j}=\sum\limits_{i=1}^{n/j} a_{n+1-ij}=S_{n-j,j}+a_{n+1-j}$$

$$\begin{cases} a_n - \sum_{i=1}^{n/2} a_i a_{n-i} & n \text{ is odd} \\ a_n - \sum_{i=1}^{n/2} a_i a_{n-i} + \frac{1}{2} a_{\frac{n}{2}} (a_{\frac{n}{2}} + 1) & n \text{ is even} \end{cases}$$

- 完全图生成树计数 n^{n-2}

- 矩阵-树定理

设 $\mathbf{A}[G]$ 为图 G 的邻接矩阵、 $\mathbf{D}[G]$ 为图 G 的度数矩阵,则图 G 的不同生成树的个数为 $\mathbf{C}[G]$ = $\mathbf{D}[G] - \mathbf{A}[G]$ 的任意一个 n-1 阶主子式的行列式值。

• Euler characteristic

平面图的顶点个数 V, 边数 E, 平面被划分的区域数 F, 组成图形的连通部分的数目 C 满足: V - E + F = C + 1

6.12. 公式、数列、定理

• Pick theorem

顶点为整点的简单多边形,其面积 A,内部格点数 i,边上格点数 b满足: $A = i + \frac{b}{2} - 1$

 $x_3 y_3 1$

旁心 $\left(\frac{-ax_1+bx_2+cx_3}{-a+b+c}, \frac{-ay_1+by_2+cy_3}{-a+b+c}\right)$

• 平面几何公式

 x_3 y_3