Platelet

Team Reference Material

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Chapter 1

Graph Theory

- 1.1 2-SAT
- 1.2 双连通分量
- 1.2.1 点双连通分量
- 1.2.2 边双连通分量
- 1.3 K 短路 (lhy)

```
const int MAXNODE = MAXN + MAXM * 2;
   bool used[MAXN];
   int n, m, cnt, S, T, Kth, N, TT;
   int rt[MAXN], seq[MAXN], adj[MAXN], from[MAXN], dep[MAXN];
   LL dist[MAXN], w[MAXM], ans[MAXK];
   struct GivenEdge{
        int u, v, w;
        GivenEdge() {};
        \label{eq:continuity} \mbox{GivenEdge(int $\underline{\ }$ u, int $\underline{\ }$ v, int $\underline{\ }$ w) : u(\underline{\ }$ u), v(\underline{\ }$ v(\underline{\ }$ w), $w(\underline{\ }$ w)$ $\{\}$;}
   }edge[MAXM];
10
   struct Edge{
11
        int v, nxt, w;
        Edge() {};
        Edge(int _v, int _nxt, int _w) : v(_v), nxt(_nxt), w(_w) \{\};
15 }e[MAXM];
   inline void addedge(int u, int v, int w)
16
17
        e[++cnt] = Edge(v, adj[u], w); adj[u] = cnt;
18
19
   void dij(int S)
20
21
        for(int i = 1; i <= N; i++)</pre>
22
23
             dist[i] = INF;
24
             dep[i] = 0x3f3f3f3f;
25
             used[i] = false;
26
             from[i] = 0;
27
```

```
static priority_queue<pair<LL, int>, vector<pair<LL, int> >, greater<pair<LL, int> > hp;
29
       while(!hp.empty())hp.pop();
30
       hp.push(make_pair(dist[S] = 0, S));
31
       dep[S] = 1;
32
       while(!hp.empty())
33
34
           pair<LL, int> now = hp.top();
35
           hp.pop();
36
           int u = now.second;
37
           if(used[u])continue;
38
           else used[u] = true;
39
           for(int p = adj[u]; p; p = e[p].nxt)
40
41
               int v = e[p].v;
42
               if(dist[u] + e[p].w < dist[v])</pre>
43
44
                   dist[v] = dist[u] + e[p].w;
45
                   dep[v] = dep[u] + 1;
46
                   from[v] = p;
47
                   hp.push(make_pair(dist[v], v));
48
               }
49
           }
50
       }
51
       for(int i = 1; i <= m; i++)</pre>
                                       w[i] = 0;
52
       for(int i = 1; i <= N; i++)</pre>
53
           if(from[i])w[from[i]] = -1;
54
       for(int i = 1; i <= m; i++)</pre>
55
56
           57
58
               w[i] = -dist[edge[i].u] + (dist[edge[i].v] + edge[i].w);
59
           }
60
           else
61
62
           {
               w[i] = -1;
63
           }
64
       }
65
  }
66
  inline bool cmp_dep(int p, int q)
68
       return dep[p] < dep[q];</pre>
70
  }
71
   struct Heap{
      LL key;
72
       int id, lc, rc, dist;
73
       Heap() {};
74
       Heap(LL k, int i, int 1, int r, int d) : key(k), id(i), lc(l), rc(r), dist(d) {};
75
       inline void clear()
76
77
           key = 0;
78
           id = lc = rc = dist = 0;
79
  }hp[MAXNODE];
s2 inline int merge_simple(int u, int v)
  {
83
       if(!u)return v;
84
       if(!v)return u;
85
       if(hp[u].key > hp[v].key)
```

1.3. K 短路 (LHY) 7

```
{
87
            swap(u, v);
88
        }
89
        hp[u].rc = merge_simple(hp[u].rc, v);
90
        if(hp[hp[u].lc].dist < hp[hp[u].rc].dist)</pre>
91
92
            swap(hp[u].lc, hp[u].rc);
93
94
        hp[u].dist = hp[hp[u].rc].dist + 1;
95
        return u;
96
97
   inline int merge_full(int u, int v)
98
99
        if(!u)return v;
100
        if(!v)return u;
101
        if(hp[u].key > hp[v].key)
102
        {
103
            swap(u, v);
104
        }
105
        int nownode = ++cnt;
106
        hp[nownode] = hp[u];
107
        hp[nownode].rc = merge_full(hp[nownode].rc, v);
108
        if(hp[hp[nownode].lc].dist < hp[hp[nownode].rc].dist)</pre>
109
        {
110
            swap(hp[nownode].lc, hp[nownode].rc);
111
112
        hp[nownode].dist = hp[hp[nownode].rc].dist + 1;
113
        return nownode;
114
115
116
   priority_queue<pair<LL, int>, vector<pair<LL, int> >, greater<pair<LL, int> > Q;
   int main()
117
118
        while(scanf("%d%d", &n, &m) != EOF)
119
120
            scanf("%d%d%d", &S, &T, &Kth, &TT);
121
            for(int i = 1; i <= m; i++)</pre>
122
            {
123
                 int u, v, w;
124
                 scanf("%d%d%d", &u, &v, &w);
125
                 edge[i] = \{u, v, w\};
126
            }
^{127}
            N = n;
128
            memset(adj, 0, sizeof(*adj) * (N + 1));
129
            cnt = 0;
130
            for(int i = 1; i <= m; i++)
131
                 addedge(edge[i].v, edge[i].u, edge[i].w);
132
            dij(T);
133
            if(dist[S] > TT)
134
135
                 puts("Whitesnake!");
136
137
                 continue;
            }
138
            for(int i = 1; i <= N; i++)</pre>
139
                 seq[i] = i;
140
            sort(seq + 1, seq + N + 1, cmp_dep);
141
            cnt = 0;
142
            memset(adj, 0, sizeof(*adj) * (N + 1));
143
```

```
memset(rt, 0, sizeof(*rt) * (N + 1));
144
            for(int i = 1; i <= m; i++)</pre>
145
                 addedge(edge[i].u, edge[i].v, edge[i].w);
146
            rt[T] = cnt = 0;
147
            hp[0].dist = -1;
148
            for(int i = 1; i <= N; i++)</pre>
149
150
                 int u = seq[i], v = edge[from[u]].v;
151
                 rt[u] = 0;
152
                 for(int p = adj[u]; p; p = e[p].nxt)
153
154
                     if(~w[p])
155
                     {
156
                          hp[++cnt] = Heap(w[p], p, 0, 0, 0);
157
                          rt[u] = merge_simple(rt[u], cnt);
158
                     }
159
160
                 if(i == 1)continue;
161
                 rt[u] = merge_full(rt[u], rt[v]);
162
163
            while(!Q.empty())Q.pop();
164
             Q.push(make_pair(dist[S], 0));
165
             edge[0].v = S;
166
             for(int kth = 1; kth <= Kth; kth++)</pre>
167
             {
168
                 if(Q.empty())
169
                 {
170
                     ans[kth] = -1;
171
                     continue;
172
173
                 pair<LL, int> now = Q.top(); Q.pop();
174
175
                 ans[kth] = now.first;
                 int p = now.second;
176
                 if(hp[p].lc)
177
                 {
178
                     Q.push(make_pair(+hp[hp[p].lc].key + now.first - hp[p].key, hp[p].lc));
179
                 }
180
                 if(hp[p].rc)
181
                 {
182
                     Q.push(make_pair(+hp[hp[p].rc].key + now.first - hp[p].key, hp[p].rc));
183
                 }
184
                 if(rt[edge[hp[p].id].v])
185
186
                 {
                     Q.push(make_pair(hp[rt[edge[hp[p].id].v]].key + now.first, rt[edge[hp[p].id].v]));
187
188
            }
189
            if (ans[Kth] == -1 \mid \mid ans[Kth] > TT)
190
             {
191
                 puts("Whitesnake!");
192
             }
193
             else
194
             {
195
                 puts("yareyaredawa");
196
            }
197
        }
198
   }
199
```

1.4. 最大团 9

1.4 最大团

1.5 一般图最大匹配

- 1.6 树
- 1.6.1 虚树
- 1.6.2 矩阵树定理
- 1.6.3 点分治
- 1.6.4 Prufer 编码
- 1.6.5 Link-Cut Tree (ct)

```
struct Node *null;
   struct Node {
2
       Node *ch[2], *fa, *pos;
       int val, mn, l, len; bool rev;
       // min_val in chain
       inline bool type()
       {
            return fa -> ch[1] == this;
       }
9
       inline bool check()
10
       {
11
            return fa -> ch[type()] == this;
12
13
       inline void pushup()
14
15
16
            pos = this; mn = val;
            ch[0] \rightarrow mn < mn ? mn = ch[0] \rightarrow mn, pos = ch[0] \rightarrow pos : 0;
17
            ch[1] \rightarrow mn < mn ? mn = ch[1] \rightarrow mn, pos = ch[1] \rightarrow pos : 0;
18
            len = ch[0] -> len + ch[1] -> len + 1;
19
20
       inline void pushdown()
21
22
            if (rev)
23
24
                 ch[0] -> rev ^= 1;
25
                 ch[1] -> rev ^= 1;
                 std::swap(ch[0], ch[1]);
27
                 rev ^= 1;
28
            }
29
       }
30
       inline void pushdownall()
31
32
            if (check()) fa -> pushdownall();
33
            pushdown();
34
35
       inline void rotate()
36
37
            bool d = type(); Node *f = fa, *gf = f -> fa;
38
            (fa = gf, f \rightarrow check()) ? fa \rightarrow ch[f \rightarrow type()] = this : 0;
39
            (f \rightarrow ch[d] = ch[!d]) != null ? ch[!d] \rightarrow fa = f : 0;
40
            (ch[!d] = f) -> fa = this;
41
            f -> pushup();
42
43
       inline void splay(bool need = 1)
44
```

```
{
45
           if (need) pushdownall();
46
           for (; check(); rotate())
47
                if (fa -> check())
48
                    (type() == fa -> type() ? fa : this) -> rotate();
49
           pushup();
50
51
       inline Node *access()
52
53
           Node *i = this, *j = null;
54
           for (; i != null; i = (j = i) -> fa)
55
56
               i -> splay();
57
               i \rightarrow ch[1] = j;
58
                i -> pushup();
59
60
61
           return j;
       }
62
       inline void make_root()
63
64
           access();
           splay();
66
           rev ^= 1;
67
       }
68
       inline void link(Node *that)
69
70
           make_root();
71
           fa = that;
72
           splay(0);
73
74
       inline void cut(Node *that)
75
76
           make_root();
77
           that -> access();
78
           that -> splay(0);
79
           that -> ch[0] = fa = null;
80
           that -> pushup();
81
82
83 | } mem[maxn];
84 inline Node *query(Node *a, Node *b)
85 {
       a -> make_root(); b -> access(); b -> splay(0);
87
       return b -> pos;
88 | }
s9 inline int dist(Node *a, Node *b)
90 | {
       a -> make_root(); b -> access(); b -> splay(0);
91
       return b -> len;
92
93
```

1.7. 仙人掌 11

- 1.6.6 树上倍增
- 1.6.7 数链剖分
- 1.7 仙人掌
- 1.8 帯花树
- 1.9 KM 算法
- 1.10 支配树
- 1.10.1 DAG
- 1.10.2 一般图
- 1.11 弦图
- 1.12 网络流
- 1.13 最小割
- 1.14 最大流
- 1.15 费用流

1.16 有上下界的网络流 (Durandal)

B(u,v) 表示边 (u,v) 流量的下界,C(u,v) 表示边 (u,v) 流量的上界,设 F(u,v) 表示边 (u,v) 的实际流量设 G(u,v) = F(u,v) - B(u,v),则 $0 \le G(u,v) \le C(u,v) - B(u,v)$

• 无源汇的上下界可行流

建立超级源点 S^* 和超级汇点 T^* ,对于原图每一条边 (u,v) 在新网络中连如下三条边: $S^* \to v$,容量为 B(u,v); $u \to T^*$,容量为 B(u,v); $u \to v$,容量为 C(u,v) - B(u,v)。最后求新网络的最大流,判断从 超级源点 S^* 出发的边是否都满流即可,边 (u,v) 的最终解中的实际流量为 G(u,v) + B(u,v)。

- 有源汇的上下界可行流 从汇点 T 到源点 S 连一条上界为 ∞ ,下界为 0 的边。按照无源汇的上下界可行流一样做即可,流量即为 $T\to S$ 边上的流量。
- 有源汇的上下界最大流
 - 在有源汇的上下界可行流中,从汇点 T 到源点 S 的边改为连一条上界为 ∞,下界为 x 的边。x 满足二分性质,找到最大的 x 使得新网络存在有源汇的上下界可行流即为原图的最大流。
 - 从汇点 T 到源点 S 连一条上界为 ∞,下界为 0 的边,变成无源汇的网络。按照无源汇的上下界可行流的方法,建立超级源点 S^* 与超级汇点 T^* ,求一遍 S^* → T^* 的最大流,再将从汇点 T 到源点 S 的这条边拆掉,求一次 S → T 的最大流即可。
- 有源汇的上下界最小流
 - 在有源汇的上下界可行流中,从汇点 T 到源点 S 的边改为连一条上界为 x,下界为 0 的边。x 满足二分性质,找到最小的 x 使得新网络存在有源汇的上下界可行流即为原图的最大流。
 - 按照无源汇的上下界可行流的方法,建立超级源点 S^* 与超级汇点 T^* ,求一遍 S^* \to T^* 的最大流,但是注意不加上汇点 T 到源点 S 的这条边,即不使之改为无源汇的网络去求解。求完后,再加上那条汇点 T 到源点 S 的边,上界为 ∞ 的边。因为这条边的下界为 0,所以 S^* , T^* 无影响,再求

一次 $S^* \to T^*$ 的最大流。若超级源点 S^* 出发的边全部满流,则 $T \to S$ 边上的流量即为原图的最小流,否则无解。

- 1.16.1 zkw 费用流
- 1.17 差分约束

Chapter 2

Math

2.1 int64 相乘取模 (Durandal)

```
int64_t mul(int64_t x, int64_t y, int64_t p) {
   int64_t t = (x * y - (int64_t) ((long double) x / p * y + 1e-3) * p) % p;
   return t < 0 ? t + p : t;
}</pre>
```

2.2 扩展欧几里得 (gy)

```
// return gcd(a, b)
   // ax+by=gcd(a,b)
   int extend_gcd(int a, int b, int &x, int &y) {
       if (b == 0) \{
           x = 1, y = 0;
5
6
           return a;
       int res = extend_gcd(b, a % b, x, y);
       int t = y;
9
       y = x - a / b * y;
10
       x = t;
11
       return res;
12
13
   // return minimal positive integer x so that ax+by=c
   // or -1 if such x does not exist
   int solve_equ(int a, int b, int c) {
17
       int x, y, d;
       d = extend_gcd(a, b, x, y);
18
       if (c % d)
19
          return -1;
20
       int t = c / d;
21
       x *= t;
22
       y *= t;
23
       int k = b / d;
24
       x = (x \% k + k) \% k;
25
26
       return x;
27
   // return minimal positive integer x so that ax==b \pmod{p}
   // or -1 if such x does not exist
29
30 int solve(int a, int b, int p) {
      a = (a \% p + p) \% p;
31
       b = (b \% p + p) \% p;
```

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```
return solve_equ(a, p, b);

34
}
```

2.3 中国剩余定理 (Durandal)

返回是否可行,余数和模数结果为 r_1 , m_1

```
bool CRT(int &r1, int &m1, int r2, int m2) {
    int x, y, g = extend_gcd(m1, m2, x, y);
    if ((r2 - r1) % g != 0) return false;
    x = 111 * (r2 - r1) * x % m2;
    if (x < 0) x += m2;
    x /= g;
    r1 += m1 * x;
    m1 *= m2 / g;
    return true;
}</pre>
```

2.4 线性同余不等式 (Durandal)

必须满足 $0 \le d < m$, $0 \le l \le r < m$, 返回 $\min\{x \ge 0 \mid l \le x \cdot d \mod m \le r\}$, 无解返回 -1

```
int64_t calc(int64_t d, int64_t m, int64_t l, int64_t r) {
   if (1 == 0) return 0;
   if (d == 0) return -1;
   if (d * 2 > m) return calc(m - d, m, m - r, m - l);
   if ((1 - 1) / d < r / d) return (1 - 1) / d + 1;
   int64_t k = calc((-m % d + d) % d, d, l % d, r % d);
   if (k == -1) return -1;
   return (k * m + l - 1) / d + 1;
}</pre>
```

2.5 组合数

2.6 高斯消元

2.7 Miller Rabin & Pollard Rho (gy)

```
*\ In\ Java,\ use\ BigInteger.is Probable Prime (int\ certainty)\ to\ replace\ miller\_rabin (BigInteger)
    \rightarrow number)
   * Test Set / First Wrong Answer
   * 2 / 2,047
   * 2, 3 / 1,373,653
   * 31, 73 / 9,080,191
   * 2, 3, 5 / 25,326,001
   * 2, 3, 5, 7 / 3,215,031,751 (> Int.MAX_VALUE)
   * 2, 7, 61 / 4,759,123,141
   * 2, 13, 23, 1662803 / 1,122,004,669,633
   * 2, 3, 5, 7, 11 / 2,152,302,898,747
   * 2, 3, 5, 7, 11, 13 / 3,474,749,660,383
   * 2, 3, 5, 7, 11, 13, 17 / 341,550,071,728,321
   * 2, 3, 5, 7, 11, 13, 17, 19, 23 / 3,825,123,056,546,413,051
14
   * 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37 / 318,665,857,834,031,151,167,461 (> Long.MAX_VALUE)
16 * 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41 / 3,317,044,064,679,887,385,961,981
```

```
*/
17
   const int test_case_size = 12;
18
   const int test_case[test_case_size] = {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37};
19
   int64_t multiply_mod(int64_t x, int64_t y, int64_t p) {
20
       int64_t t = (x * y - (int64_t) ((long double) x / p * y + 1e-3) * p) % p;
21
       return t < 0? t + p: t;
22
23
   int64_t add_mod(int64_t x, int64_t y, int64_t p) {
24
       return (Oull + x + y) % p;
25
26
   int64_t power_mod(int64_t x, int64_t exp, int64_t p) {
27
       int64_t ans = 1;
28
       while (exp) {
29
           if (exp & 1)
30
               ans = multiply_mod(ans, x, p);
31
           x = multiply_mod(x, x, p);
32
           exp >>= 1;
33
34
35
       return ans;
   }
36
   bool miller_rabin_check(int64_t prime, int64_t base) {
37
       int64_t number = prime - 1;
38
       for (; ~number & 1; number >>= 1)
39
           continue;
40
       int64_t result = power_mod(base, number, prime);
41
42
       for (; number != prime - 1 && result != 1 && result != prime - 1; number <<= 1)
43
           result = multiply_mod(result, result, prime);
44
       return result == prime - 1 || (number & 1) == 1;
   }
45
   bool miller_rabin(int64_t number) {
46
       if (number < 2)</pre>
47
           return false;
48
       if (number < 4)
49
           return true;
50
       if (~number & 1)
51
52
       for (int i = 0; i < test_case_size && test_cases[i] < number; i++)
53
           if (!miller_rabin_check(number, test_cases[i]))
54
55
               return false;
56
       return true;
   }
57
   int64_t gcd(int64_t x, int64_t y) {
58
       return y == 0 ? x : gcd(y, x % y);
59
60
   int64_t pollard_rho_test(int64_t number, int64_t seed) {
61
       int64_t x = rand() % (number - 1) + 1, y = x;
62
       int head = 1, tail = 2;
63
64
       while (true) {
           x = multiply_mod(x, x, number);
65
           x = add_mod(x, seed, number);
66
           if (x == y)
67
               return number;
68
           int64_t answer = gcd(std::abs(x - y), number);
69
           if (answer > 1 && answer < number)</pre>
```

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```
return answer;
           if (++head == tail) {
               y = x;
73
               tail <<= 1;
74
75
       }
76
77
   void factorize(int64_t number, std::vector<int64_t> &divisor) {
78
       if (number > 1) {
79
           if (miller_rabin(number)) {
80
               divisor.push_back(number);
81
           } else {
82
               int64_t factor = number;
83
               while (factor >= number)
84
                    factor = pollard_rho_test(number, rand() % (number - 1) + 1);
85
               factorize(number / factor, divisor);
86
               factorize(factor, divisor);
87
88
       }
89
```

- $2.8 \quad O(m^2 \log n)$ 线性递推
- 2.9 Polynomial
- 2.9.1 FFT
- 2.9.2 NTT & 多项式求逆
- 2.10 拉格朗日插值
- 2.11 杜教筛
- 2.12 BSGS
- 2.12.1 BSGS
- 2.12.2 扩展 BSGS
- 2.13 直线下整点个数 (gy)

必须满足 $a\geq 0,\,b\geq 0,\,m>0\,,\,$ 返回 $\sum\limits_{i=0}^{n-1}rac{a+bi}{m}$

```
int64_t count(int64_t n, int64_t a, int64_t b, int64_t m) {
   if (b == 0)
      return n * (a / m);
   if (a >= m)
      return n * (a / m) + count(n, a % m, b, m);
   if (b >= m)
      return (n - 1) * n / 2 * (b / m) + count(n, a, b % m, m);
   return count((a + b * n) / m, (a + b * n) % m, m, b);
}
```

2.14. 单纯形 17

2.14 单纯形

2.15 辛普森积分

常用数列定理 (gy) 2.16

• 第一类 Stirling number 用 $s(n,k) = (-1)^{n-k} {n \brack k}$ 表示第一类 Stirling number ${n+1\brack k} = n{n\brack k} + {n\brack n}, k>0$ ${0\brack 0} = 1, {n\brack 0} = {0\brack n} = 0, n>0$ ${n\brack k}$ 为将 n 个元素分成 k 个环的方案数

• 第二类 Stirling number 用 $S(n,k) = {n \atop k}$ 表示第二类 Stirling number ${n+1 \brace k} = k \begin{Bmatrix} n \rbrace \\ k \end{Bmatrix} + {n \brace k-1}, k > 0$ ${0 \brace 0} = 1, {n \brack 0} = {0 \brack n} = 0, n > 0$ ${n \brace k} = \frac{1}{k!} \sum_{j=0}^{k} (-1)^{k-j} {k \choose j} j^n$

 $\binom{n}{k}$ 为将 n 个元素划分成 k 个非空集合的方案数

• Catalan Number c_n 表示长度为 2n 的合法括号序的数量 $c_1 = 1, c_{n+1} = \sum_{i=1}^{n} c_i \times c_{n+1-i}$ $c_n = \frac{\binom{2n}{n}}{n+1}$

• Bell number

$$B_n$$
 表示基数为 n 的集合的划分方案数
$$B_i = \begin{cases} 1 & i = 0\\ \sum\limits_{k=0}^{n} \binom{n}{k} B_k & i > 0 \end{cases}$$

$$B_n = \sum\limits_{k=0}^{n} \binom{n}{k}$$

• Bernoulli number
$$\sum_{j=0}^{m} {m+1 \choose j} B_j = 0, m > 0$$

$$B_i = \begin{cases} 1 & i = 0 \\ \sum\limits_{j=0}^{i-1} {i+1 \choose j} \\ -\frac{j=0}{i+1} & i > 0 \end{cases}$$

$$\sum_{k=1}^{n} k^m = \frac{1}{m+1} \sum_{k=0}^{m} {m+1 \choose k} B_k n^{m+1-k}$$

• Lagrange polynomial 给定次数为 n 的多项式函数 L(x) 上的 n+1 个点 $(x_0,y_0),(x_1,y_1),\ldots,(x_n,y_n)$ 则 $L(x)=\sum\limits_{j=0}^n y_j\prod\limits_{0\leq m\leq n,m\neq j}\frac{x-x_m}{x_j-x_m}$

Chapter 3

Geometry

3.1 点、直线、圆 (gy)

```
using number = long double;
const number eps = 1e-8;
3 number _sqrt(number x) {
      return std::sqrt(std::max(x, (number) 0));
5 }
  number _asin(number x) {
      x = std::min(x, (number) 1), x = std::max(x, (number) -1);
      return std::asin(x);
9
  number _acos(number x) {
10
       x = std::min(x, (number) 1), x = std::max(x, (number) -1);
11
       return std::acos(x);
12
13
14 int sgn(number x) {
       return (x > eps) - (x < -eps);
15
16
  int cmp(number x, number y) {
17
       return sgn(x - y);
18
  }
19
  struct point {
20
      number x, y;
       point() {}
       point(number x, number y) : x(x), y(y) {}
       number len2() const {
24
          return x * x + y * y;
25
26
       number len() const {
27
           return _sqrt(len2());
28
29
       point unit() const {
30
           return point(x / len(), y / len());
       point rotate90() const {
33
           return point(-y, x);
34
35
       friend point operator+(const point &a, const point &b) {
36
           return point(a.x + b.x, a.y + b.y);
```

3.1. 点、直线、圆 (GY)

```
38
       friend point operator-(const point &a, const point &b) {
39
           return point(a.x - b.x, a.y - b.y);
40
41
       friend point operator*(const point &a, number b) {
42
           return point(a.x * b, a.y * b);
43
44
       friend point operator/(const point &a, number b) {
45
           return point(a.x / b, a.y / b);
46
47
       friend number dot(const point &a, const point &b) {
48
49
           return a.x * b.x + a.y * b.y;
50
       friend number det(const point &a, const point &b) {
51
           return a.x * b.y - a.y * b.x;
52
53
       friend number operator == (const point &a, const point &b) {
54
           return cmp(a.x, b.x) == 0 && cmp(a.y, b.y) == 0;
55
56
   };
57
   number dis2(const point &a, const point &b) {
       return (a - b).len2();
59
60
   number dis(const point \&a, const point \&b) {
61
       return (a - b).len();
62
   }
63
   struct line {
64
       point a, b;
65
66
       line() {}
67
       line(point a, point b) : a(a), b(b) {}
       point value() const {
           return b - a;
69
70
  };
71
   bool point_on_line(const point &p, const line &l) {
72
       return sgn(det(p - 1.a, p - 1.b)) == 0;
73
  }
74
   // including endpoint
75
  bool point_on_ray(const point &p, const line &l) {
77
       return sgn(det(p - 1.a, p - 1.b)) == 0 &&
78
           sgn(dot(p - 1.a, 1.b - 1.a)) >= 0;
79
   // including endpoints
80
   bool point_on_seg(const point &p, const line &1) {
81
       return sgn(det(p - 1.a, p - 1.b)) == 0 &&
82
           sgn(dot(p - 1.a, 1.b - 1.a)) >= 0 &&
83
           sgn(dot(p - 1.b, 1.a - 1.b)) >= 0;
84
85
   bool seg_has_intersection(const line &a, const line &b) {
86
       if (point_on_seg(a.a, b) || point_on_seg(a.b, b) ||
87
               point_on_seg(b.a, a) || point_on_seg(b.b, a))
88
           return /* including endpoints */ true;
89
       return sgn(det(a.a - b.a, b.b - b.a)) * sgn(det(a.b - b.a, b.b - b.a)) < 0
90
           && sgn(det(b.a - a.a, a.b - a.a)) * sgn(det(b.b - a.a, a.b - a.a)) < 0;
91
92
   point intersect(const line &a, const line &b) {
93
       number s1 = det(a.b - a.a, b.a - a.a);
94
       number s2 = det(a.b - a.a, b.b - a.a);
```

```
return (b.a * s2 - b.b * s1) / (s2 - s1);
   l٦
97
   point projection(const point &p, const line &1) {
        return 1.a + (1.b - 1.a) * dot(p - 1.a, 1.b - 1.a) / (1.b - 1.a).len2();
99
100
   number dis(const point &p, const line &l) {
101
        return std::abs(dot(p - 1.a, 1.b - 1.a)) / (1.b - 1.a).len();
102
103
   point symmetry_point(const point &a, const point &o) {
104
        return o + o - a;
105
106
   point reflection(const point &p, const line &l) {
107
        return symmetry_point(p, projection(p, 1));
108
   }
109
   struct circle {
110
       point o;
111
        number r;
112
        circle() {}
113
        circle(point o, number r) : o(o), r(r) {}
114
115 };
    bool intersect(const line &1, const circle &a, point &p1, point &p2) {
        number x = dot(1.a - a.o, 1.b - 1.a);
117
        number y = (1.b - 1.a).len2();
118
        number d = x * x - y * ((1.a - a.o).len2() - a.r * a.r);
119
        if (sgn(d) < 0) return false;</pre>
120
        point p = 1.a - (1.b - 1.a) * (x / y), delta = (1.b - 1.a) * (_sqrt(d) / y);
121
        p1 = p + delta, p2 = p - delta;
122
        return true;
125
    bool intersect(const circle &a, const circle &b, point &p1, point &p2) {
        if (a.o == b.o \&\& cmp(a.r, b.r) == 0)
           return /* value for coincident circles */ false;
127
        number s1 = (b.o - a.o).len();
128
        if (cmp(s1, a.r + b.r) > 0 \mid \mid cmp(s1, std::abs(a.r - b.r)) < 0)
129
            return false;
130
        number s2 = (a.r * a.r - b.r * b.r) / s1;
131
        number aa = (s1 + s2) / 2, bb = (s1 - s2) / 2;
132
        point p = (b.o - a.o) * (aa / (aa + bb)) + a.o;
133
        point delta = (b.o - a.o).unit().rotate90() * _sqrt(a.r * a.r - aa * aa);
134
        p1 = p + delta, p2 = p - delta;
135
        return true;
136
137
    bool tangent(const point &p0, const circle &c, point &p1, point &p2) {
138
        number x = (p0 - c.o).len2();
139
        number d = x - c.r * c.r;
140
        if (sgn(d) < 0) return false;</pre>
141
        if (sgn(d) == 0)
142
            return /* value for point_on_line */ false;
143
        point p = (p0 - c.o) * (c.r * c.r / x);
144
145
        point delta = ((p0 - c.o) * (-c.r * \_sqrt(d) / x)).rotate90();
        p1 = c.o + p + delta;
146
        p2 = c.o + p - delta;
147
        return true;
148
149
   bool ex_tangent(const circle &a, const circle &b, line &l1, line &l2) {
150
        if (cmp(std::abs(a.r - b.r), (b.o - a.o).len()) == 0) {
151
            point p1, p2;
152
            intersect(a, b, p1, p2);
153
            11 = 12 = line(p1, p1 + (a.o - p1).rotate90());
154
```

3.1. 点、直线、圆 (GY) 21

```
return true;
155
        } else if (cmp(a.r, b.r) == 0) {
156
            point dir = b.o - a.o;
157
            dir = (dir * (a.r / dir.len())).rotate90();
158
            11 = line(a.o + dir, b.o + dir);
159
            12 = line(a.o - dir, b.o - dir);
160
            return true;
161
        } else {
162
            point p = (b.o * a.r - a.o * b.r) / (a.r - b.r);
163
            point p1, p2, q1, q2;
164
            if (tangent(p, a, p1, p2) && tangent(p, b, q1, q2)) {
165
                11 = line(p1, q1);
166
                12 = line(p2, q2);
167
                return true;
168
            } else {
169
                return false;
170
            }
171
        }
172
173
   bool in_tangent(const circle &a, const circle &b, line &l1, line &l2) {
174
        if (cmp(a.r + b.r, (b.o - a.o).len()) == 0) {
175
176
            point p1, p2;
            intersect(a, b, p1, p2);
177
            11 = 12 = line(p1, p1 + (a.o - p1).rotate90());
178
            return true;
179
        } else {
180
            point p = (b.o * a.r + a.o * b.r) / (a.r + b.r);
181
            point p1, p2, q1, q2;
182
            if (tangent(p, a, p1, p2) && tangent(p, b, q1, q2)) {
183
                11 = line(p1, q1);
184
                12 = line(p2, q2);
185
186
                return true;
            } else {
187
                return false;
188
            }
189
        }
190
191 }
```

- 3.2 点到凸包切线
- 3.3 直线凸包交点
- 3.4 凸包游戏
- 3.5 半平面交
- 3.6 旋转卡壳
- 3.7 判断圆是否有交
- 3.8 最小圆覆盖
- 3.9 最小球覆盖
- $3.10 O(n^2 \log n)$ 圆交面积和重心
- 3.11 圆与多边形交
- 3.12 $O(n \log n)$ 凸多边形内的最大圆
- 3.13 三角形的五心
- 3.14 三维凸包
- 3.15 三维绕轴旋转
- 3.16 几何公式

Chapter 4

String

- 4.1 KMP
- 4.2 AC 自动机
- 4.3 后缀数组
- 4.4 后缀自动机
- 4.5 Manacher
- 4.6 回文自动机
- 4.7 最小表示法

Chapter 5

Data Structure

5.1 莫队 (ct)

```
int size;
   struct Query {
      int 1, r, id;
       inline bool operator < (const Queuy &that) const {return 1 / size != that.1 / size ? 1 < that.1
        \hookrightarrow: ((1 / size) & 1 ? r < that.r : r > that.r);}
5 | } q[maxn];
6 int main()
7 | {
       size = (int) sqrt(n * 1.0);
       std::sort(q + 1, q + m + 1);
       int 1 = 1, r = 0;
10
       for (int i = 1; i <= m; ++i)
           for (; r < q[i].r; ) add(++r);
14
           for (; r > q[i].r; ) del(r--);
           for (; 1 < q[i].1; ) del(1++);
15
           for (; 1 > q[i].1; ) add(--1);
16
17
               write your code here.
18
19
20
       return 0;
21
```

5.2 ST 表 (ct)

```
int a[maxn], f[20][maxn], n;
int Log[maxn];

void build()
{
    for (int i = 1; i <= n; ++i) f[0][i] = a[i];

    int lim = Log[n];
    for (int j = 1; j <= lim; ++j)
    {
        int *fj = f[j], *fj1 = f[j - 1];
        for (int i = 1; i <= n - (1 << j) + 1; ++i)
        fj[i] = dmax(fj1[i], fj1[i + (1 << (j - 1))]);
}
</pre>
```

5.3. 可并堆 (CT) 25

```
14 int Query(int 1, int r)
15 {
       int k = Log[r - 1 + 1];
16
       return dmax(f[k][1], f[k][r - (1 << k) + 1]);
17
   }
18
   int main()
19
   {
20
       scanf("%d", &n);
21
       Log[0] = -1;
22
       for (int i = 1; i <= n; ++i)
23
24
           scanf("%d", &a[i]);
25
           Log[i] = Log[i >> 1] + 1;
26
       }
27
       build();
28
       int q;
29
       scanf("%d", &q);
30
       for (; q; --q)
31
32
           int 1, r; scanf("%d%d", &1, &r);
33
           printf("%d\n", Query(1, r));
34
35
36
```

5.3 可并堆 (ct)

```
struct Node {
       Node *ch[2];
2
       11 val; int size;
       inline void update()
       {
            size = ch[0] \rightarrow size + ch[1] \rightarrow size + 1;
       }
   } mem[maxn], *rt[maxn];
  Node *merge(Node *a, Node *b)
9
10
       if (a == mem) return b;
11
       if (b == mem) return a;
12
       if (a -> val < b -> val) std::swap(a, b);
13
       // a -> pushdown();
14
       std::swap(a -> ch[0], a -> ch[1]);
15
       a -> ch[1] = merge(a -> ch[1], b);
16
       a -> update();
17
       return a;
18
19
```

5.4 zkw 线段树 (ct)

```
// must be 0-based !
inline void build()

for (int i = M - 1; i; --i) tr[i] = dmax(tr[i << 1], tr[i << 1 | 1]);

inline void Change(int x, int v)

x += M; tr[x] = v; x >>= 1;
for (; x; x >>= 1) tr[x] = dmax(tr[x << 1], tr[x << 1 | 1]);
}
</pre>
```

```
11 inline int Query(int s, int t)
12 {
       int ret = -0x7fffffff;
13
       for (s = s + M - 1, t = t + M + 1; s ^ t ^ 1; s >>= 1, t >>= 1)
14
15
           if (~s & 1) cmax(ret, tr[s ^ 1]);
16
           if (t & 1) cmax(ret, tr[t ^ 1]);
17
18
19
       return ret;
20
  int main()
21
22
       int n; scanf("%d", &n);
23
       for (M = 1; M < n; M <<= 1);
24
       for (int i = 0; i < n; ++i)
25
           scanf("%d", &tr[i + M]);
26
       for (int i = n; i < M; ++i) tr[i + M] = -0x7ffffffff;
27
       build();
28
       int q; scanf("%d", &q);
29
       for (; q; --q)
           int 1, r; scanf("%d%d", &1, &r); --1, --r;
32
           printf("%d\n", Query(1, r));
33
34
       return 0;
35
36
```

5.5 主席树

5.6 Splay (ct)

指针版

```
struct Node *null;
   struct Node {
       Node *ch[2], *fa;
       int val; bool rev;
       inline bool type()
       {
            return fa -> ch[1] == this;
       inline void pushup()
10
       {
       }
11
       inline void pushdown()
12
13
            if (rev)
14
15
                 ch[0] -> rev ^= 1;
16
                 ch[1] -> rev ^= 1;
17
                 std::swap(ch[0], ch[1]);
18
19
                 rev ^= 1;
            }
20
       }
21
       inline void rotate()
22
23
            bool d = type(); Node *f = fa, *gf = f -> fa;
24
            (fa = gf, f \rightarrow fa != null) ? fa \rightarrow ch[f \rightarrow type()] = this : 0;
25
            (f \rightarrow ch[d] = ch[!d]) != null ? ch[!d] \rightarrow fa = f : 0;
26
```

5.6. SPLAY (CT) 27

```
(ch[!d] = f) -> fa = this;
27
           f -> pushup();
28
       }
29
       inline void splay()
30
31
           for (; fa != null; rotate())
32
                if (fa -> fa != null)
33
                    (type() == fa -> type() ? fa : this) -> rotate();
34
           pushup();
35
36
   } mem[maxn];
37
```

数组版

```
// BZOJ - 1500 维修数列
  int fa[maxn], ch[maxn][2], a[maxn], size[maxn], cnt;
int sum[maxn], lmx[maxn], rmx[maxn], mx[maxn], v[maxn], id[maxn], root;
  bool rev[maxn], tag[maxn];
5 inline void update(R int x)
6
       R \text{ int } ls = ch[x][0], rs = ch[x][1];
       size[x] = size[ls] + size[rs] + 1;
       sum[x] = sum[ls] + sum[rs] + v[x];
10
       mx[x] = gmax(mx[ls], mx[rs]);
11
       cmax(mx[x], lmx[rs] + rmx[ls] + v[x]);
       lmx[x] = gmax(lmx[ls], sum[ls] + v[x] + lmx[rs]);
12
       rmx[x] = gmax(rmx[rs], sum[rs] + v[x] + rmx[ls]);
13
14
   inline void pushdown(R int x)
15
16
       R \text{ int } ls = ch[x][0], rs = ch[x][1];
17
       if (tag[x])
18
19
20
           rev[x] = tag[x] = 0;
           if (ls) tag[ls] = 1, v[ls] = v[x], sum[ls] = size[ls] * v[x];
21
           if (rs) tag[rs] = 1, v[rs] = v[x], sum[rs] = size[rs] * v[x];
22
           if (v[x] >= 0)
23
           {
24
               if (ls) lmx[ls] = rmx[ls] = mx[ls] = sum[ls];
25
               if (rs) lmx[rs] = rmx[rs] = mx[rs] = sum[rs];
26
           }
27
           else
28
           {
               if (ls) lmx[ls] = rmx[ls] = 0, mx[ls] = v[x];
30
               if (rs) lmx[rs] = rmx[rs] = 0, mx[rs] = v[x];
31
           }
32
       }
33
       if (rev[x])
34
35
           rev[x] ^= 1; rev[ls] ^= 1; rev[rs] ^= 1;
36
           swap(lmx[ls], rmx[ls]);swap(lmx[rs], rmx[rs]);
37
           swap(ch[ls][0], ch[ls][1]); swap(ch[rs][0], ch[rs][1]);
38
39
40
   inline void rotate(R int x)
41
42
       R int f = fa[x], gf = fa[f], d = ch[f][1] == x;
43
       if (f == root) root = x;
44
       (ch[f][d] = ch[x][d ^ 1]) > 0 ? fa[ch[f][d]] = f : 0;
45
       (fa[x] = gf) > 0 ? ch[gf][ch[gf][1] == f] = x : 0;
46
       fa[ch[x][d ^ 1] = f] = x;
47
```

```
update(f);
48
49 }
50 inline void splay(R int x, R int rt)
51 | {
        while (fa[x] != rt)
52
53
            R int f = fa[x], gf = fa[f];
54
            if (gf != rt) rotate((ch[gf][1] == f) ^ (ch[f][1] == x) ? x : f);
55
            rotate(x);
56
57
        update(x);
58
59
   void build(R int 1, R int r, R int rt)
60
61 | {
        if (1 > r) return;
62
        R int mid = 1 + r >> 1, now = id[mid], last = id[rt];
63
        if (1 == r)
64
65
            sum[now] = a[1];
66
            size[now] = 1;
67
            tag[now] = rev[now] = 0;
            if (a[1] \ge 0) lmx[now] = rmx[now] = mx[now] = a[1];
69
            else lmx[now] = rmx[now] = 0, mx[now] = a[1];
70
        }
71
        else
72
        {
73
            build(1, mid - 1, mid);
74
            build(mid + 1, r, mid);
75
76
77
        v[now] = a[mid];
        fa[now] = last;
78
79
        update(now);
        ch[last][mid >= rt] = now;
80
81
  int find(R int x, R int rank)
82
83
        if (tag[x] || rev[x]) pushdown(x);
84
        R int ls = ch[x][0], rs = ch[x][1], lsize = size[ls];
85
        if (lsize + 1 == rank) return x;
86
        if (lsize >= rank)
87
            return find(ls, rank);
88
        else
90
            return find(rs, rank - lsize - 1);
91 }
92 inline int prepare(R int 1, R int tot)
93 | {
        R int x = find(root, 1 - 1), y = find(root, 1 + tot);
94
        splay(x, 0);
95
        splay(y, x);
96
        return ch[y][0];
97
98
   std::queue <int> q;
   inline void Insert(R int left, R int tot)
100
101
        for (R int i = 1; i <= tot; ++i ) a[i] = FastIn();</pre>
102
        for (R int i = 1; i <= tot; ++i )</pre>
103
            if (!q.empty()) id[i] = q.front(), q.pop();
104
            else id[i] = ++cnt;
105
        build(1, tot, 0);
106
        R int z = id[(1 + tot) >> 1];
107
        R int x = find(root, left), y = find(root, left + 1);
```

5.6. SPLAY (CT) 29

```
splay(x, 0);
109
        splay(y, x);
110
        fa[z] = y;
111
        ch[y][0] = z;
112
        update(y);
113
        update(x);
114
115
   void rec(R int x)
116
117
        if (!x) return;
118
        R \text{ int } ls = ch[x][0], rs = ch[x][1];
119
        rec(ls); rec(rs); q.push(x);
120
        fa[x] = ch[x][0] = ch[x][1] = 0;
121
        tag[x] = rev[x] = 0;
122
   l٦
123
124 inline void Delete(R int 1, R int tot)
   {
125
        R int x = prepare(1, tot), f = fa[x];
126
        rec(x); ch[f][0] = 0;
127
        update(f); update(fa[f]);
128
129
   inline void Makesame(R int 1, R int tot, R int val)
130
131
        R int x = prepare(1, tot), y = fa[x];
132
        v[x] = val; tag[x] = 1; sum[x] = size[x] * val;
133
        if (val >= 0) lmx[x] = rmx[x] = mx[x] = sum[x];
134
        else lmx[x] = rmx[x] = 0, mx[x] = val;
135
        update(y); update(fa[y]);
136
137
   inline void Reverse(R int 1, R int tot)
138
139
        R int x = prepare(1, tot), y = fa[x];
140
141
        if (!tag[x])
142
            rev[x] ^= 1;
143
            swap(ch[x][0], ch[x][1]);
144
            swap(lmx[x], rmx[x]);
145
            update(y); update(fa[y]);
146
147
148
   inline void Query(R int 1, R int tot)
149
150
151
        R int x = prepare(1, tot);
        printf("%d\n",sum[x]);
152
153
   #define inf ((1 << 30))
154
   int main()
155
   {
156
        R int n = FastIn(), m = FastIn(), 1, tot, val;
157
        R char op, op2;
158
        mx[0] = a[1] = a[n + 2] = -inf;
159
        for (R int i = 2; i <= n + 1; i++)
160
161
            a[i] = FastIn();
162
        }
163
        for (R int i = 1; i <= n + 2; ++i) id[i] = i;
164
        n += 2; cnt = n; root = (n + 1) >> 1;
165
        build(1, n, 0);
166
        for (R int i = 1; i <= m; i++ )
167
        {
168
            op = getc();
169
```

```
while (op < 'A' \mid \mid op > 'Z') op = getc();
170
            getc(); op2 = getc();getc();getc();getc();
171
            if (op == 'M' && op2 == 'X')
^{172}
            {
173
                 printf("%d\n",mx[root] );
174
            }
175
            else
176
            {
177
                 1 = FastIn() + 1; tot = FastIn();
178
                 if (op == 'I') Insert(1, tot);
179
                 if (op == 'D') Delete(1, tot);
180
                 if (op == 'M') val = FastIn(), Makesame(1, tot, val);
181
                 if (op == 'R')
182
                     Reverse(1, tot);
183
                 if (op == 'G')
184
                     Query(1, tot);
185
186
        }
187
        return 0;
188
189
```

5.7 Treap (ct)

```
struct Treap {
       Treap *ls, *rs;
2
       int size;
       bool rev;
       inline void update()
6
7
           size = ls -> size + rs -> size + 1;
9
       inline void set_rev()
10
           rev ^= 1;
11
           std::swap(ls, rs);
^{12}
13
       inline void pushdown()
14
15
           if (rev)
16
17
                ls -> set_rev();
19
                rs -> set_rev();
                rev = 0;
20
21
22
  } mem[maxn], *root, *null = mem;
23
  struct Pair {
24
       Treap *fir, *sec;
25
  };
26
  Treap *build(R int 1, R int r)
27
28
       if (1 > r) return null;
       R \text{ int } mid = 1 + r >> 1;
       R Treap *now = mem + mid;
31
       now \rightarrow rev = 0;
32
       now -> ls = build(1, mid - 1);
33
       now -> rs = build(mid + 1, r);
34
       now -> update();
35
```

5.7. TREAP (CT) 31

```
return now;
36
  }
37
  inline Treap *Find_kth(R Treap *now, R int k)
38
39
       if (!k) return mem;
40
       if (now -> ls -> size >= k) return Find_kth(now -> ls, k);
41
       else if (now -> ls -> size + 1 == k) return now;
42
       else return Find_kth(now -> rs, k - now -> ls -> size - 1);
43
44
   Treap *merge(R Treap *a, R Treap *b)
45
46
       if (a == null) return b;
47
       if (b == null) return a;
48
       if (rand() \% (a -> size + b -> size) < a -> size)
49
50
           a -> pushdown();
51
           a -> rs = merge(a -> rs, b);
52
           a -> update();
53
           return a;
54
       }
55
       else
56
       {
57
           b -> pushdown();
58
           b -> ls = merge(a, b -> ls);
59
           b -> update();
60
           return b;
61
62
63
   Pair split(R Treap *now, R int k)
64
65
       if (now == null) return (Pair) {null, null};
66
       R Pair t = (Pair) {null, null};
67
       now -> pushdown();
68
       if (k <= now -> ls -> size)
69
70
           t = split(now -> ls, k);
71
           now -> ls = t.sec;
72
           now -> update();
73
           t.sec = now;
74
       }
75
       else
76
       {
77
78
           t = split(now \rightarrow rs, k - now \rightarrow ls \rightarrow size - 1);
79
           now -> rs = t.fir;
80
           now -> update();
           t.fir = now;
81
82
       return t;
83
84
   inline void set_rev(int 1, int r)
85
86
       R Pair x = split(root, 1 - 1);
87
       R Pair y = split(x.sec, r - 1 + 1);
88
       y.fir -> set_rev();
89
       root = merge(x.fir, merge(y.fir, y.sec));
90
91
```

5.8 可持久化平衡树 (ct)

```
char str[maxn];
2 struct Treap
   {
       Treap *ls, *rs;
       char data; int size;
       inline void update()
           size = ls -> size + rs -> size + 1;
10 } *root[maxn], mem[maxcnt], *tot = mem, *last = mem, *null = mem;
inline Treap* new_node(char ch)
12 {
       *++tot = (Treap) {null, null, ch, 1};
13
       return tot;
14
15 }
16 struct Pair
17 {
       Treap *fir, *sec;
18
19 };
inline Treap *copy(Treap *x)
21 {
       if (x == null) return null;
22
       if(x > last) return x;
23
       *++tot = *x;
24
       return tot;
25
26
  Pair Split(Treap *x, int k)
27
28
       if (x == null) return (Pair) {null, null};
29
30
       Pair y;
       Treap *nw = copy(x);
31
       if (nw \rightarrow ls \rightarrow size >= k)
32
33
           y = Split(nw -> ls, k);
34
           nw -> ls = y.sec;
35
           nw -> update();
36
           y.sec = nw;
37
       }
38
       else
39
       {
           y = Split(nw \rightarrow rs, k - nw \rightarrow ls \rightarrow size - 1);
41
           nw -> rs = y.fir;
           nw -> update();
43
           y.fir = nw;
44
45
       return y;
46
47
  Treap *Merge(Treap *a, Treap *b)
48
49
       if (a == null) return b;
50
       if (b == null) return a;
       Treap *nw;
52
       if (rand() \% (a -> size + b -> size) < a -> size)
53
           nw = copy(a);
55
           nw -> rs = Merge(nw -> rs, b);
56
57
       else
```

```
59
        {
            nw = copy(b);
60
            nw -> ls = Merge(a, nw -> ls);
61
62
        nw -> update();
63
        return nw;
64
65
   Treap *Build(int 1, int r)
66
67
        if (1 > r) return null;
68
        R int mid = 1 + r >> 1;
69
        Treap *nw = new_node(str[mid]);
70
        nw -> ls = Build(1, mid - 1);
71
        nw -> rs = Build(mid + 1, r);
72
        nw -> update();
73
        return nw;
74
75 }
76
   int now;
   inline void Insert(int k, char ch)
77
78
        Pair x = Split(root[now], k);
79
80
        Treap *nw = new_node(ch);
        root[++now] = Merge(Merge(x.fir, nw), x.sec);
81
82
   inline void Del(int 1, int r)
83
84
        Pair x = Split(root[now], 1 - 1);
85
        Pair y = Split(x.sec, r - 1 + 1);
86
        root[++now] = Merge(x.fir, y.sec);
87
88
89
    inline void Copy(int 1, int r, int 11)
90
        Pair x = Split(root[now], 1 - 1);
91
        Pair y = Split(x.sec, r - 1 + 1);
92
        Pair z = Split(root[now], 11);
93
        Treap *ans = y.fir;
94
        root[++now] = Merge(Merge(z.fir, ans), z.sec);
95
   }
96
   void Print(Treap *x, int 1, int r)
97
98
        if (!x) return;
99
        if (1 > r) return;
100
101
        R int mid = x \rightarrow ls \rightarrow size + 1;
        if (r < mid)</pre>
102
103
        {
            Print(x -> ls, l, r);
104
            return ;
105
        }
106
        if (1 > mid)
107
108
            Print(x -> rs, l - mid, r - mid);
109
            return ;
110
111
        Print(x -> ls, l, mid - 1);
112
        printf("%c", x \rightarrow data);
113
        Print(x -> rs, 1, r - mid);
114
115 }
void Printtree(Treap *x)
117 {
        if (!x) return;
118
        Printtree(x -> ls);
119
```

```
printf("%c", x \rightarrow data);
120
        Printtree(x -> rs);
121
122 }
123 int main()
124 {
        srand(time(0) + clock());
125
        null -> ls = null -> rs = null; null -> size = 0; null -> data = 0;
126
        int n = F();
127
        gets(str + 1);
128
        int len = strlen(str + 1);
129
        root[0] = Build(1, len);
130
        while (1)
131
132
             last = tot;
133
             R char opt = getc();
134
             while (opt < 'A' \mid \mid opt > 'Z')
135
136
                 if (opt == EOF) return 0;
137
                 opt = getc();
138
             }
139
             if (opt == 'I')
140
141
                 R int x = F();
^{142}
                 R char ch = getc();
143
                 Insert(x, ch);
144
145
             else if (opt == 'D')
146
147
                 R int 1 = F(), r = F();
148
149
                 Del(1, r);
             }
150
             else if (opt == 'C')
151
152
                 R int x = F(), y = F(), z = F();
153
                 Copy(x, y, z);
154
             }
155
             else if (opt == 'P')
156
157
                 R \text{ int } x = F(), y = F(), z = F();
158
                 Print(root[now - x], y, z);
159
                 puts("");
160
             }
161
162
163
        return 0;
164
```

5.9 CDQ 分治 (ct)

```
struct event
{
    int x, y, id, opt, ans;
} t[maxn], q[maxn];

void cdq(int left, int right)
{
    if (left == right) return;
    R int mid = left + right >> 1;
    cdq(left, mid);
    cdq(mid + 1, right);
    //分成若干个子问题
```

5.10. BITSET (CT) 35

```
12
       ++now:
       for (int i = left, j = mid + 1; j <= right; ++j)</pre>
13
14
           for (; i <= mid && q[i].x <= q[j].x; ++i)
15
               if (!q[i].opt)
16
                    add(q[i].y, q[i].ans);
17
           //考虑前面的修改操作对后面的询问的影响
18
           if (q[j].opt)
19
               q[j].ans += query(q[j].y);
20
21
22
       R int i, j, k = 0;
       //以下相当于归并排序
23
       for (i = left, j = mid + 1; i <= mid \&\& j <= right; )
24
25
           if (q[i].x \le q[j].x)
26
               t[k++] = q[i++];
27
           else
28
               t[k++] = q[j++];
29
30
       for (; i <= mid; )</pre>
31
           t[k++] = q[i++];
32
33
       for (; j <= right; )</pre>
           t[k++] = q[j++];
34
       for (int i = 0; i < k; ++i)
35
           q[left + i] = t[i];
36
37
```

5.10 Bitset (ct)

```
namespace Game {
   \#define\ maxn\ 300010
   #define maxs 30010
  uint b1[32][maxs], b2[32][maxs];
   int popcnt[256];
6 inline void set(R uint *s, R int pos)
       s[pos >> 5] = 1u << (pos & 31);
   }
9
   inline int popcount(R uint x)
10
11
       return popcnt[x >> 24 & 255]
            + popcnt[x >> 16 & 255]
13
            + popcnt[x >> 8 & 255]
                            & 255];
15
            + popcnt[x
16
   void main() {
17
       int n, q;
18
       scanf("%d%d", &n, &q);
19
       char *s1 = new char[n + 1];
20
       char *s2 = new char[n + 1];
21
       scanf("%s%s", s1, s2);
22
       uint *anss = new uint[q];
23
       for (R int i = 1; i < 256; ++i) popcnt[i] = popcnt[i >> 1] + (i & 1);
24
       #define modify(x, _p)\
25
       {\
26
```

```
for (R \ int \ j = 0; \ j < 32 \& j <= _p; \ ++j) \setminus
27
               set(b##x[j], _p - j);\
28
29
       for (R int i = 0; i < n; ++i)
30
           if (s1[i] == '0') modify(1, 3 * i)
31
           else if (s1[i] == '1') modify(1, 3 * i + 1)
32
           else modify(1, 3 * i + 2)
33
       for (R int i = 0; i < n; ++i)
34
           if (s2[i] == '1') modify(2, 3 * i)
           else if (s2[i] == '2') modify(2, 3 * i + 1)
36
           else modify(2, 3 * i + 2)
37
       for (int Q = 0; Q < q; ++Q) {
38
           R int x, y, 1;
39
           scanf("%d%d%d", &x, &y, &1); x *= 3; y *= 3; 1 *= 3;
40
           uint *f1 = b1[x \& 31], *f2 = b2[y \& 31], ans = 0;
41
           R int i = x >> 5, j = y >> 5, p, lim;
42
           for (p = 0, lim = 1 >> 5; p + 8 < lim; p += 8, i += 8, j += 8)
43
44
               ans += popcount(f1[i + 0] & f2[j + 0]);
               ans += popcount(f1[i + 1] & f2[j + 1]);
46
               ans += popcount(f1[i + 2] & f2[j + 2]);
47
               ans += popcount(f1[i + 3] & f2[j + 3]);
48
               ans += popcount(f1[i + 4] & f2[j + 4]);
49
               ans += popcount(f1[i + 5] & f2[j + 5]);
50
               ans += popcount(f1[i + 6] & f2[j + 6]);
51
               ans += popcount(f1[i + 7] & f2[j + 7]);
52
53
           for (; p < lim; ++p, ++i, ++j) ans += popcount(f1[i] & f2[j]);
54
           R uint S = (1u \ll (1 \& 31)) - 1;
55
           ans += popcount(f1[i] & f2[j] & S);
56
           anss[Q] = ans;
57
       }
58
       output_arr(anss, q * sizeof(uint));
59
60 }
61 }
```

Chapter 6

Others

6.1 vimrc (gy)

```
se et ts=4 sw=4 sts=4 nu sc sm lbr is hls mouse=a
  sy on
  ino <tab> <c-n>
  ino <s-tab> <tab>
  au winnew * winc L
  nm <f6> ggVG"+y
  nm <f7> :w<cr>:make<cr>
  nm <f8> :!@@<cr>
  nm <f9> :!@@ < in<cr>
10 nm <s-f9> :!(time @@ < in &>> out) &>> out<cr>:sp out<cr>
  au filetype cpp cm @@ ./a.out | se cin fdm=syntax mp=g++\ %\ -std=c++11\ -Wall\ -Wextra\ -02
11
12 map <c-p> :ha<cr>
  se pheader=%n\ %f
au filetype java cm @@ java %< | se cin fdm=syntax mp=javac\ %
au filetype python cm @@ python % | se si fdm=indent
  au bufenter *.kt setf kotlin
```

6.2 STL 释放内存 (Durandal)

```
template <typename T>
   __inline void clear(T &container) {
    container.clear();
    T(container).swap(container);
}
```

6.3 开栈 (Durandal)

```
register char *_sp __asm__("rsp");
int main() {
    const int size = 400 << 20; // 400 MB
    static char *sys, *mine(new char[size] + size - 4096);
    sys = _sp; _sp = mine;
    _main(); // main method
    _sp = sys;</pre>
```

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```
s return 0;
9 }
```

6.4 Java Template (gy)

```
import java.io.BufferedReader;
   import java.io.IOException;
   import java.io.InputStreamReader;
   import java.math.BigDecimal;
  import java.math.BigInteger;
  import java.math.RoundingMode;
  import java.util.ArrayDeque;
  import java.util.ArrayList;
9 import java.util.Arrays;
import java.util.Comparator;
import java.util.Deque;
import java.util.LinkedList;
import java.util.List;
14 import java.util.Scanner;
import java.util.StringTokenizer;
16 public class Template {
17
       // Input
       private static BufferedReader reader;
18
       private static StringTokenizer tokenizer;
19
       private static String next() {
20
21
           try {
               while (tokenizer == null || !tokenizer.hasMoreTokens())
22
                   tokenizer = new StringTokenizer(reader.readLine());
23
           } catch (IOException e) {
25
               // do nothing
26
           return tokenizer.nextToken();
27
       }
28
       private static int nextInt() {
29
           return Integer.parseInt(next());
30
31
       private static double nextDouble() {
           return Double.parseDouble(next());
34
       private static BigInteger nextBigInteger() {
35
           return new BigInteger(next());
36
37
       public static void main(String[] args) {
38
           reader = new BufferedReader(new InputStreamReader(System.in));
39
           Scanner scanner = new Scanner(System.in);
40
           while (scanner.hasNext())
42
               scanner.next();
       }
43
       // BigInteger & BigDecimal
44
       private static void bigDecimal() {
45
           BigDecimal a = BigDecimal.valueOf(1.0);
46
           BigDecimal b = a.setScale(50, RoundingMode.HALF_EVEN);
```

```
BigDecimal c = b.abs();
48
            // if scale omitted, b.scale is used
49
           BigDecimal d = c.divide(b, 50, RoundingMode.HALF_EVEN);
50
            // since Java 9
51
            BigDecimal e = d.sqrt(new MathContext(50, RoundingMode.HALF_EVEN));
52
           BigDecimal x = new BigDecimal(BigInteger.ZERO);
53
           BigInteger y = BigDecimal.ZERO.toBigInteger(); // RoundingMode.DOWN
54
           y = BigDecimal.ZERO.setScale(0, RoundingMode.HALF_EVEN).unscaledValue();
55
56
       // sqrt for Java 8
57
       private static BigDecimal sqrt(BigDecimal a, int scale, RoundingMode mode) {
58
            if (a.equals(BigDecimal.ZERO))
59
                return BigDecimal.ZERO;
60
            a = a.setScale(scale, mode);
61
           BigDecimal ans = a;
62
           BigDecimal TWO = BigDecimal.valueOf(2L);
63
           for (int i = 1; i <= scale; i++)
64
                ans = ans.add(a.divide(ans, scale, mode)).divide(TWO, scale, mode);
65
66
           return ans:
       }
67
       private static BigInteger sqrt(BigInteger a) {
68
           BigInteger about = BigInteger.ZERO.setBit(a.bitLength() / 2);
69
           return sqrt(new BigDecimal(a.toString()), new BigDecimal(about.toString())).setScale(0,
70

→ RoundingMode.FLOOR).unscaledValue();
71
       private static BigDecimal sqrt(BigDecimal a, BigDecimal initial) {
72
73
            if (a.equals(BigDecimal.ZERO))
74
                return BigDecimal.ZERO;
75
            a = a.setScale(50, RoundingMode.HALF_EVEN);
76
           BigDecimal ans = initial;
           for (int i = 1; i <= 10; i++)
77
                ans = ans.add(a.divide(ans, RoundingMode.HALF_EVEN)).divide(BigDecimal.valueOf(2),
78
                  \hookrightarrow RoundingMode.HALF_EVEN);
           return ans:
79
       }
80
       // ArrayList
81
       private static void arrayList() {
82
           List<Integer> list = new ArrayList<>();
83
            // Generic array is banned
85
           List[] lists = new List[100];
86
           lists[0] = new ArrayList<Integer>();
            /\!/ for List<Integer>, remove(Integer) stands for element, while remove(int) stands for
87
              \hookrightarrow index
            list.remove(list.get(1));
88
            list.remove(list.size() - 1);
89
            list.clear();
90
       }
91
       // Queue
92
       private static void queue() {
93
           LinkedList<Integer> queue = new LinkedList<>();
94
            // return the value without popping
95
            queue.peek();
96
            // pop and return the value
97
            queue.poll();
98
            Deque<Integer> deque = new ArrayDeque<>();
99
            deque.peekFirst();
100
```

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```
deque.peekLast();
101
            deque.pollFirst();
102
        }
103
        // Others
104
        private static void others() {
105
            Arrays.sort(new int[10]);
106
            Arrays.sort(new Integer[10], (a, b) -> {
107
                 if (a.equals(b)) return 0;
108
                 if (a > b) return -1;
109
                 return 1;
110
            });
111
            Arrays.sort(new Integer[10], Comparator.comparingInt((a) -> (int) a).reversed());
112
            long a = 1_000_000_000_000_000_000L;
113
            int b = Integer.MAX_VALUE;
114
            int c = 'a';
115
116
117
```

6.5 Big Fraction (gy)

```
fun gcd(a: Long, b: Long): Long = if (b == OL) a else gcd(b, a % b)
   class Fraction(val a: BigInteger, val b: BigInteger) {
       constructor(a: Long, b: Long) : this(BigInteger.valueOf(a / gcd(a, b)), BigInteger.valueOf(b /
         \hookrightarrow \gcd(a, b)))
       operator fun plus(o: Fraction): Fraction {
           var gcd = b.gcd(o.b)
           val tempProduct = (b / gcd) * (o.b / gcd)
           var ansA = a * (o.b / gcd) + o.a * (b / gcd)
           val gcd2 = ansA.gcd(gcd)
           ansA \neq gcd2
           gcd /= gcd2
10
           return Fraction(ansA, gcd * tempProduct)
11
12
       operator fun minus(o: Fraction): Fraction {
13
           var gcd = b.gcd(o.b)
14
           val tempProduct = (b / gcd) * (o.b / gcd)
15
           var ansA = a * (o.b / gcd) - o.a * (b / gcd)
16
17
           val gcd2 = ansA.gcd(gcd)
           ansA /= gcd2
18
           gcd /= gcd2
19
           return Fraction(ansA, gcd * tempProduct)
20
21
       operator fun times(o: Fraction): Fraction {
22
           val gcd1 = a.gcd(o.b)
23
           val gcd2 = b.gcd(o.a)
24
           return Fraction((a / gcd1) * (o.a / gcd2), (b / gcd2) * (o.b / gcd1))
26
       }
```

6.6 模拟退火 (ct)

```
db ans_x, fans;
inline double rand01() {return rand() / 2147483647.0;}
```

6.7. 三分 (CT) 41

```
inline double randp() {return (rand() & 1 ? 1 : -1) * rand01();}
  inline double f(double x)
5 {
6
           write your function here.
7
8
       if (maxx < fans) {fans = maxx; ans_x = x;}</pre>
9
       return maxx;
10
11
   int main()
12
13
       srand(time(NULL) + clock());
14
       db x = 0, fnow = f(x);
15
       fans = 1e30;
16
       for (db T = 1e4; T > 1e-4; T *= 0.997)
17
18
           db nx = x + randp() * T, fnext = f(nx);
19
           db delta = fnext - fnow;
20
           if (delta < 1e-9 || exp(-delta / T) > rand01())
21
22
                x = nx;
23
24
               fnow = fnext;
           }
25
       }
26
       return 0;
27
28
```

6.7 三分 (ct)

```
inline db cubic_search()
{
    double 1 = -1e4, r = 1e4;
    for (int i = 1; i <= 100; ++i)
    {
        double ll = (l + r) * 0.5;
        double rr = (ll + r) * 0.5;
        if (check(ll) < check(rr)) r = rr;
        else l = ll;
    }
    return (l + r) * 0.5;
}</pre>
```

6.8 博弈论模型 (gy)

• Wythoff's game

给定两堆石子,每次可以从任意一堆中取至少一个石子,或从两堆中取相同的至少一个石子,取走最后石子的胜

先手胜当且仅当石子数满足:

```
\lfloor (b-a) \times \phi \rfloor = a, (a \le b, \phi = \frac{\sqrt{5}+1}{2})
```

先手胜对应的石子数构成两个序列:

Lower Wythoff sequence: $a_n = \lfloor n \times \phi \rfloor$

Upper Wythoff sequence: $b_n = \lfloor n \times \phi \rfloor$

• Fibonacci nim

给定一堆石子,第一次可以取至少一个、少于石子总数数量的石子,之后每次可以取至少一个、不超过 上次取石子数量两倍的石子,取走最后石子的胜

先手胜当且仅当石子数为斐波那契数

6.9 积分表

- $a^x \to \frac{a^x}{\ln a}$
- $\sin x \to -\cos x$
- $\cos x \to \sin x$
- $\tan x \to -\ln \cos x$
- $\sec x \to \ln \tan(\frac{x}{2} + \frac{\pi}{4})$
- $\csc x \to \ln \tan \frac{x}{2}$
- $\sin^2 x \to \frac{x}{2} \frac{1}{2}\sin x \cos x$
- $\cos^2 x \to \frac{x}{2} + \frac{1}{2}\sin x \cos x$
- $\tan^2 x \to \tan x x$
- $\sec^2 x \to \tan x$
- $\csc^2 x \to -\tan x$
- $\arcsin x \to \frac{1}{\sqrt{1-x^2}}$
- $\arccos x \to -\frac{1}{\sqrt{1-x^2}}$
- $\arctan x \to \frac{1}{1+x^2}$