Platelet

Team Reference Material

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Graph Theory

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- 1.7.5 Link-Cut Tree
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- 1.10 KM 算法
- 1.11 支配树
- 1.11.1 DAG
- 1.11.2 一般图
- 1.12 弦图
- 1.13 网络流

Math

2.1 int64 相乘取模

2.2 扩展欧几里得 (gy)

```
// return gcd(a, b)
   // ax+by=gcd(a,b)
   template <typename T>
   T extend_gcd(T a, T b, T &x, T &y) {
       if (b == 0) \{
           x = 1, y = 0;
           return a;
       T res = extend_gcd(b, a % b, x, y);
9
       T t = y;
10
       y = x - a / b * y;
11
       x = t;
12
       return res;
13
   // return minimal positive integer x so that ax+by=c
  // or -1 if such x does not exist
  template <typename T>
18
   inline T solve_equ(T a, T b, T c) {
19
       T x, y, d;
20
       d = extend_gcd(a, b, x, y);
21
       if (c % d)
22
           return -1;
23
       T t = c / d;
24
25
       x *= t;
       y *= t;
26
       T k = b / d;
27
       x = (x \% k + k) \% k;
28
       return x;
29
30
   // return minimal positive integer x so that ax==b \pmod{p}
31
   // or -1 if such x does not exist
32
   template <typename T>
33
   inline T solve(T a, T b, T p) {
34
       a = (a \% p + p) \% p;
35
       b = (b \% p + p) \% p;
       return solve_equ(a, p, b);
37
```

8 CHAPTER 2. MATH

2.3 中国剩余定理

- 2.4 组合数
- 2.4.1 Lucas 定理
- 2.4.2 组合数合数取模
- 2.5 高斯消元
- 2.6 Miller Rabin & Pollard Rho (gy)

```
* In Java, use BigInteger.isProbablePrime(int certainty) to replace miller_rabin(BigInteger
    \rightarrow number)
   * Test Set / First Wrong Answer
   * 2 / 2,047
   * 2, 3 / 1,373,653
   * 31, 73 / 9,080,191
   * 2, 3, 5 / 25,326,001
   * 2, 3, 5, 7 / 3,215,031,751 (> Int.MAX_VALUE)
   * 2, 7, 61 / 4,759,123,141
   * 2, 13, 23, 1662803 / 1,122,004,669,633
10
   * 2, 3, 5, 7, 11 / 2,152,302,898,747
11
   * 2, 3, 5, 7, 11, 13 / 3,474,749,660,383
12
   * 2, 3, 5, 7, 11, 13, 17 / 341,550,071,728,321
13
   * 2, 3, 5, 7, 11, 13, 17, 19, 23 / 3,825,123,056,546,413,051
14
   * 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37 / 318,665,857,834,031,151,167,461 (> Long.MAX_VALUE)
15
   * 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41 / 3,317,044,064,679,887,385,961,981
16
17
   #include <cstdint>
18
   #include <cstdlib>
19
   #include <vector>
20
22 const int test_case_size = 12;
23 const int test_cases[test_case_size] = {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37};
25 int64_t multiply_mod(int64_t x, int64_t y, int64_t p) {
       int64_t t = (x * y - (int64_t) ((long double) x / p * y + 1e-3) * p) % p;
26
       return t < 0? t + p: t;
27
30 int64_t add_mod(int64_t x, int64_t y, int64_t p) {
      return (Oull + x + y) % p;
31
32 }
33
  int64_t power_mod(int64_t x, int64_t exp, int64_t p) {
34
       int64_t ans = 1;
35
       while (exp) {
36
          if (exp & 1)
37
              ans = multiply_mod(ans, x, p);
38
          x = multiply_mod(x, x, p);
39
           exp >>= 1;
40
       }
41
42
       return ans;
43 | }
44
bool miller_rabin_check(int64_t prime, int64_t base) {
       int64_t number = prime - 1;
```

```
for (; ~number & 1; number >>= 1)
47
            continue;
48
        int64_t result = power_mod(base, number, prime);
49
        for (; number != prime - 1 && result != 1 && result != prime - 1; number <<= 1)
50
            result = multiply_mod(result, result, prime);
51
        return result == prime - 1 || (number & 1) == 1;
52
   }
53
54
    bool miller_rabin(int64_t number) {
55
        if (number < 2)
56
            return false;
57
        if (number < 4)
58
            return true;
59
        if (~number & 1)
60
            return false:
61
        for (int i = 0; i < test_case_size && test_cases[i] < number; i++)</pre>
62
            if (!miller_rabin_check(number, test_cases[i]))
63
                return false;
64
        return true;
65
   }
66
67
    int64_t gcd(int64_t x, int64_t y) {
        return y == 0 ? x : gcd(y, x % y);
69
70
71
    int64_t pollard_rho_test(int64_t number, int64_t seed) {
72
        int64_t x = rand() % (number - 1) + 1, y = x;
73
        int head = 1, tail = 2;
74
        while (true) {
75
76
            x = multiply_mod(x, x, number);
77
            x = add_mod(x, seed, number);
78
            if (x == y)
79
                return number;
            int64_t answer = gcd(std::abs(x - y), number);
80
            if (answer > 1 && answer < number)
81
                return answer:
82
            if (++head == tail) {
83
                y = x;
84
                tail <<= 1;
85
            }
86
        }
87
   }
88
89
    void factorize(int64_t number, std::vector<int64_t> &divisor) {
90
91
        if (number > 1) {
            if (miller_rabin(number)) {
92
                divisor.push_back(number);
93
            } else {
94
                int64_t factor = number;
95
                while (factor >= number)
96
                     factor = pollard_rho_test(number, rand() % (number - 1) + 1);
97
                factorize(number / factor, divisor);
98
                factorize(factor, divisor);
99
            }
100
        }
101
   }
102
103
   #include <cstdio>
104
   int main() {
105
        static int64_t tar;
106
        static std::vector<int64_t> factors;
107
```

10 CHAPTER 2. MATH

```
while (scanf("%1ld", &tar)) {
    printf("%d\n", miller_rabin(tar));
    factors.clear();
    factorize(tar, factors);
    for (int64_t i : factors)
        printf("%1ld\n", i);
    }
    return 0;
}
```

- 2.7 $O(m^2 \log n)$ 线性递推
- 2.8 Polynomial
- 2.8.1 FFT
- 2.8.2 NTT & 多项式求逆
- 2.9 拉格朗日插值
- 2.10 杜教筛
- 2.11 BSGS
- 2.11.1 BSGS
- 2.11.2 扩展 BSGS
- 2.12 直线下整点个数
- 2.13 单纯形
- 2.14 辛普森积分

2.15 常用数列定理

- 第一类 Stirling Number
- 第二类 Stirling Number
- Catalan Number c_n 表示长度为 2n 的合法括号序的数量 $c_1=1,\,c_{n+1}=\sum\limits_{i=1}^nc_i\times c_{n+1-i}$ $c_n=\frac{\binom{2n}n}{n+1}$
- Bell Number
- Bernoulli Number

2.16 积分表

Geometry

- 3.1 点、直线、圆
- 3.2 点到凸包切线
- 3.3 直线凸包交点
- 3.4 凸包游戏
- 3.5 半平面交
- 3.6 旋转卡壳
- 3.7 判断圆是否有交
- 3.8 最小圆覆盖
- 3.9 最小球覆盖
- 3.10 $O(n^2 \log n)$ 圆交面积和重心
- 3.11 圆与多边形交
- 3.12 $O(n \log n)$ 凸多边形内的最大圆
- 3.13 三角形的五心
- 3.14 三维凸包
- 3.15 三维绕轴旋转
- 3.16 几何公式

String

- 4.1 KMP
- 4.2 AC 自动机
- 4.3 后缀数组
- 4.4 后缀自动机
- 4.5 Manacher
- 4.6 回文自动机
- 4.7 最小表示法

Data Structure

5.1 莫队 (ct)

```
Title: Modui
   // Date: 26.02.2016
 4 // Test:BZOJ-2038
       Complexity: O(n^3/2)
   //
           莫队算法——将所有询问储存起来,然后分块暴力处理。
           时间复杂度为 O (n× 根号 n)。
9
10
   #include <cstdio>
11
   #include <cstring>
12
   #include <algorithm>
13
   #include <cmath>
14
15
   #ifdef WIN32
16
           #define LL "%I64d"
17
   #else
18
           #define LL "%lld"
19
   #endif
20
21
   #ifdef CT
22
           #define debug(...) printf(__VA_ARGS__)
23
           #define debug(...)
   #endif
27
   #define R register
28
   \#define \ \ getc() \ \ (S==T886(T=(S=B)+fread(B,1,1<<15,stdin),S==T)?E0F:*S++)
29
   \#define\ gmax(\_a, \_b)\ ((\_a) > (\_b)\ ?\ (\_a)\ :\ (\_b))
   \#define\ gmin(\_a,\ \_b)\ ((\_a)\ <\ (\_b)\ ?\ (\_a)\ :\ (\_b))
31
   #define cmax(_a, _b) (_a < (_b) ? _a = (_b) : 0)
32
   #define cmin(_a, _b) (_a > (_b) ? _a = (_b) : 0)
33
   char B[1<<15],*S=B,*T=B;</pre>
34
   inline int FastIn()
35
36
           R char ch;R int cnt=0;R bool minus=0;
37
           while (ch=getc(),(ch < ^{'}0' || ch > ^{'}9') && ch != ^{'}-^{'});
38
           ch == '-' ?minus=1:cnt=ch-'0';
39
           while (ch=getc(),ch >= '0' && ch <= '9') cnt = cnt * 10 + ch - '0';
40
           return minus?-cnt:cnt;
41
42 }
```

```
43 #define maxn 50010
int col[maxn],num[maxn],size,pos[maxn];
45 long long up[maxn],dw[maxn],ans;
46 struct Query{
           int l,r,id;
47
  }q[maxn];
48
   inline bool cmp(const Query &i,const Query &j){
49
           return pos[i.l]!=pos[j.l] ? (i.l<j.l) : (pos[i.l]&1 ? i.r<j.r : i.r>j.r);
50
51
   inline long long gcd(R long long a,R long long b){
52
           R long long tmp;
53
           while (b){
54
                    tmp=b;
55
                    b=a\%b;
56
                    a=tmp;
57
           }
58
           return a;
59
60
   inline void update(R int x,R int d){
61
           ans-=num[col[x]]*num[col[x]];
62
           num[col[x]]+=d;
63
           ans+=num[col[x]]*num[col[x]];
65
   int main()
66
   ₹
67
           R int n=FastIn(),m=FastIn();size=(int)sqrt(n*1.0);
68
           for (R int i=1;i<=n;i++) col[i]=FastIn(),pos[i]=(i-1)/size+1;</pre>
69
           for (R int i=1;i<=m;i++){</pre>
70
                    q[i].l=FastIn();q[i].r=FastIn();q[i].id=i;
71
           }
72
73
           std::sort(q+1,q+m+1,cmp);
74
           R int l=1,r=0;
           for (R int i=1;i<=m;i++){
75
                    R int id_now=q[i].id;
76
                    if (q[i].l==q[i].r){
77
                             up[id_now]=0;dw[id_now]=1;continue;
78
                    }
79
                    for (;r<q[i].r;r++) update(r+1,1);</pre>
80
                    for (;r>q[i].r;r--) update(r,-1);
81
                    for (;l<q[i].1;l++) update(1,-1);
82
                    for (;l>q[i].1;l--) update(l-1,1);
83
                    R long long aa,bb,cc;
85
                    aa=ans-q[i].r+q[i].l-1;
                    bb=(long long)(q[i].r-q[i].l+1)*(q[i].r-q[i].l);
86
87
                    cc=gcd(aa,bb);aa/=cc;bb/=cc;
                    up[id_now]=aa;dw[id_now]=bb;
88
89
           for (R int i=1;i<=m;i++) printf("%lld/%lld\n",up[i],dw[i] );</pre>
90
           return 0;
91
92
```

5.2 ST 表 (ct)

```
#include <cstdio>

#define dmax(_a, _b) ((_a) > (_b) ? (_a) : (_b))

#define maxn 200010
int a[maxn], f[20][maxn], n;
```

5.3. 可并堆 (CT) 15

```
7 int Log[maxn];
   void build()
9
   {
10
           for (int i = 1; i <= n; ++i) f[0][i] = a[i];
11
12
            int lim = Log[n];
13
            for (int j = 1; j \le \lim_{j \to \infty} ++j)
14
15
                     int *fj = f[j], *fj1 = f[j - 1];
16
                     for (int i = 1; i \le n - (1 \le j) + 1; ++i)
17
                             fj[i] = dmax(fj1[i], fj1[i + (1 << (j - 1))]);
18
            }
19
20
   int Query(int 1, int r)
21
22
            int k = Log[r - 1 + 1];
23
            return dmax(f[k][1], f[k][r - (1 << k) + 1]);
24
25
   int main()
26
27
           scanf("%d", &n);
28
           Log[0] = -1;
29
            for (int i = 1; i <= n; ++i)
30
            {
31
                     scanf("%d", &a[i]);
32
                    Log[i] = Log[i >> 1] + 1;
33
            }
34
            build();
35
36
            int q;
            scanf("%d", &q);
37
38
            for (; q; --q)
39
                     int 1, r; scanf("%d%d", &1, &r);
40
                    printf("%d\n", Query(1, r) );
41
            }
^{42}
43
```

5.3 可并堆 (ct)

```
struct Node {
           Node *ch[2];
2
           11 val; int size;
3
            inline void update()
4
5
                    size = ch[0] \rightarrow size + ch[1] \rightarrow size + 1;
           }
   } mem[maxn], *rt[maxn];
  Node *merge(Node *a, Node *b)
9
10
            if (a == mem) return b;
11
            if (b == mem) return a;
12
            if (a -> val < b -> val) std::swap(a, b);
13
            std::swap(a -> ch[0], a -> ch[1]);
14
           a -> ch[1] = merge(a -> ch[1], b);
15
           a -> update();
16
17
           return a;
```

5.4 线段树 (ct)

5.4.1 ZKW 线段树

```
// Title:ZKW Segment Tree
// Date:19.11.2015
4 // Complexity:
5 //
        Build Tree: O(N)
   //
         Query: O(logN)
        Change: O(logN)
   //
9 | #include < cstdio >
10 | #include < cmath >
11 | #define maxn 100000
12 #define R register
13 int T[1<<18|1],n,m,M;
14
inline int FastIn()
16 {
           R char ch=getchar();R int cnt=0;R bool minus=0;
           while ((ch<'0'||ch>'9')\&\&ch!='-') ch=getchar();
           if (ch=='-') minus=1,ch=getchar();
           while (ch>='0'&&ch<='9') cnt=cnt*10+ch-'0',ch=getchar();
20
           return minus?-cnt:cnt;
21
22
23
  inline void Build_Tree()
24
25
           for (R int i=M-1;i>=1;i--)
26
             T[i]=T[2*i]+T[2*i+1];
27
28
30 inline int Query(int s,int t)
31
       R int Ans;
32
           for (Ans=0,s=s+M-1,t=t+M+1;s^t^1;s>>=1,t>>=1)
33
34
                    if (\sims&1) Ans+=T[s^1];
35
                    if (t&1) Ans+=T[t^1];
36
37
           return Ans;
41 inline void Change(int x,int NewValue)
42
           R int i=M+x;
43
           for (T[i]=NewValue,i>>=1;i;i>>=1)
44
             T[i]=T[2*i]+T[2*i+1];
45
46
47
   int main()
48
49
           n=FastIn();m=FastIn();
           for (M=1; M \le n; M \le =1);
51
           for (R int i=0;i<n;i++)</pre>
52
             T[M+i]=FastIn();
53
           Build_Tree();
54
           for (R int i=1;i<=m;i++)</pre>
55
```

5.4. 线段树 (CT) 17

```
R char cmd=getchar();
57
                     if (cmd=='Q')
58
                     {
59
                             R int a=FastIn()-1,b=FastIn()-1;
60
                             printf("%d\n",Query(a,b));
61
                     }
62
                     if (cmd=='M')
63
64
                              R int a=FastIn()-1,b=FastIn();
65
                              Change(a,b);
66
                     }
67
            }
68
            return 0;
69
70
```

5.4.2 主席树

```
Title: Functional Segment Tree
   // Date:16.12.2015
   // Complexity:O((n+m)logn)
   // Test:YZOJ-1991
   #include<cstdio>
   #include<algorithm>
   #define maxt 2000010
   #define maxn 100010
9
   #define R register
10
   inline int FastIn(){
11
           R char ch=getchar();R int cnt=0;
12
           while (ch<'0'||ch>'9') ch=getchar();
13
           while (ch>='0'\&\&ch<='9') cnt=cnt*10+ch-'0', ch=getchar();
14
15
           return cnt;
16
17
   int ls[maxt],
18
       rs[maxt],
19
           count[maxt],
20
           root[maxn],
21
           tot;
22
23
   int num[maxn],rank[maxn],n,m,r[maxn];
24
   bool cmp(const int &i,const int &j){
26
           return num[i]<num[j];</pre>
27
28
29
   inline void Insert(int last,int left,int right,int pre)
30
31
           count[++tot]=count[last]+1;
32
           if (left==right) return;
33
           R int mid=(left+right)>>1;
34
           if (pre>mid){
35
                    rs[tot]=tot+1;
36
                    Insert(rs[last],mid+1,right,pre);
37
           }
38
           else{
39
                    ls[tot]=tot+1;
40
                    rs[tot]=rs[last];
41
                    Insert(ls[last],left,mid,pre);
42
           }
43
```

```
44 | }
45
  inline int Query(int a,int b,int k)
46
47
           R int l=1,r=n,mid,f1=a,f2=b,cnt,kk=k;
48
           while (l<r){
49
                    mid=(1+r)>>1; cnt=count[ls[f2]]-count[ls[f1]];
50
                    if (cnt>=kk) f1=ls[f1],f2=ls[f2],r=mid;
51
                    else f1=rs[f1],f2=rs[f2],l=mid+1,kk-=cnt;
52
           }
53
           return 1;
54
55
56
  int main()
57
   ₹
58
           n=FastIn();m=FastIn();R int i,a,b,k;
59
           for (i=1;i<=n;i++) num[i]=FastIn(),rank[i]=i;</pre>
60
           std::sort(rank+1,rank+n+1,cmp);
61
           std::sort(num+1,num+n+1);
62
           for (i=1;i<=n;i++) r[rank[i]]=i;</pre>
63
           for (i=1;i<=n;i++) {
                    root[i]=tot+1;
65
                    Insert(root[i-1],1,n,r[i]);
66
           }
67
           for (i=1;i<=m;i++){
68
                    a=FastIn();b=FastIn();k=FastIn();
69
                    printf("%d\n",num[Query(root[a-1],root[b],k)]);
70
71
           return 0;
72
73
```

5.5 平衡树 (ct)

5.5.1 Splay

```
// Title : Splay Tree
3 // Date : 11.01.2016
 4 // Complexity : O(nlogn) (期望)
5 // Test : BZ0J-1251
6 /*
   */
   #include <cstdio>
9 #include <cstring>
10 #include <algorithm>
   #include <cmath>
11
12
   #ifdef WIN32
13
            #define LL "%I64d"
14
   #else
15
            #define LL "%lld"
16
   \#endif
17
18
   #ifdef CT
19
            \textit{\#define debug(...)} \ \textit{printf(\_VA\_ARGS}\_\_)
20
   #else
^{21}
            #define debug(...)
22
   #endif
23
```

```
25 #define R register
  \#define\ getc()\ (S==T&G(T=(S=B)+fread(B,1,1<<15,stdin),S==T)?E0F:*S++)
   \#define\ gmax(\_a,\ \_b)\ ((\_a)\ >\ (\_b)\ ?\ (\_a)\ :\ (\_b))
27
   \#define\ gmin(\_a,\ \_b)\ ((\_a)\ <\ (\_b)\ ?\ (\_a)\ :\ (\_b))
28
   \#define\ cmax(\_a,\ \_b)\ (\_a < (\_b)\ ?\ \_a = (\_b)\ :\ 0)
29
   #define cmin(a, b) (a > (b) ? a = (b) : 0)
30
   char B[1<<15],*S=B,*T=B;</pre>
31
   inline int FastIn()
32
33
           R char ch;R int cnt=0;R bool minus=0;
34
           while (ch=getc(),(ch < '0' || ch > '9') && ch != '-');
35
           ch == '-' ?minus=1:cnt=ch-'0';
36
           while (ch=getc(),ch >= '0' && ch <= '9') cnt = cnt * 10 + ch - '0';
37
           return minus?-cnt:cnt:
38
39
   #define maxn 50010
40
  int n,Q,root;
41
42 int fa[maxn], ch[maxn][2], id[maxn], size[maxn];
   int tag[maxn], mx[maxn], num[maxn];
43
   bool rev[maxn];
44
   inline void update(int x){
45
           R int ls=ch[x][0],rs=ch[x][1];
46
           mx[x]=num[x];
47
           cmax(mx[x],mx[ls]);cmax(mx[x],mx[rs]);
48
           size[x]=size[ls]+size[rs]+1;
49
   }//更新
50
   void build(int l,int r,int rt){
51
           if (1>r) return;
52
           R int mid=l+r>>1;
53
           fa[mid]=rt;
54
55
           if (mid<rt) ch[rt][0]=mid;</pre>
56
           else ch[rt][1]=mid;
57
           build(1,mid-1,mid);
           build(mid+1,r,mid);
58
           update(mid);
59
  }//建树
60
   inline void pushdown(int x){
61
           R int ls=ch[x][0],rs=ch[x][1];
62
           if (tag[x]){
63
                    R int lazy=tag[x];
64
                    if (ls) tag[ls]+=lazy,num[ls]+=lazy,mx[ls]+=lazy;
65
                    if (rs) tag[rs]+=lazy,num[rs]+=lazy,mx[rs]+=lazy;
66
67
                   tag[x]=0;
68
           }
           if (rev[x]){
69
                    if (ls) rev[ls]^=1;
70
                    if (rs) rev[rs]^=1;
71
                    ch[x][1]=ls;ch[x][0]=rs;
72
                   rev[x]=0;
73
74
   }//具体下传的过程
75
   inline void rotate(int x){//把 x 向上旋转到 x 的父亲
76
           R int f=fa[x],gf=fa[f],d=(ch[f][1]==x);//f 表示 x 的父亲, gf 是祖父, d 是 x 在其父亲的位置
77
           if (f==root) root=x,ch[0][0]=x;
78
           (ch[f][d]=ch[x][d<sup>1</sup>])>0 ? fa[ch[f][d]]=f : 0;//把 x 的儿子中与 d 相反的节点来代替 x 的位置
79
           (fa[x]=gf)>0 ? ch[gf][ch[gf][1]==f]=x : 0;//把 x 代替 f 的位置
80
           fa[ch[x][d^1]=f]=x;//把 f 接到 x 的下面
81
           update(f);//更新 f 节点
82
83
   inline void splay(int x,int rt){//把 x 旋转到 rt
           while (fa[x]!=rt){
```

```
R int f=fa[x],gf=fa[f];
86
                    if (gf!=rt) rotate((ch[gf][1]==f)^(ch[f][1]==x)? x :f);//如果祖孙三代是相同方向就转
87
                      →父亲,不然转自己
                    rotate(x);
88
89
            update(x);
90
91
   int find(int x,int rank){
92
            if (tag[x]||rev[x]) pushdown(x);
93
            R int ls=ch[x][0],rs=ch[x][1],lsize=size[ls];
94
            if (lsize+1==rank) return x;
95
            if (lsize>=rank) return find(ls,rank);
96
            else return find(rs,rank-lsize-1);
97
   }//找第 k 小
98
   inline int prepare(int l,int r){
99
           R int x=find(root,l-1);
100
            splay(x,0);
101
            x=find(root,r+1);
102
            splay(x,root);
103
            return ch[x][0];
104
   }//把 l-1 旋到根, r+1 旋到右儿子, 然后返回 r+1 的左儿子, 返回一个包含 [l, r] 的节点
   inline void add(int l,int r,int w){
            R int x=prepare(1,r);
107
            tag[x] += w, num[x] += w, mx[x] += w;
108
   }//区间加
109
   inline void rever(int 1,int r){
110
            R int x=prepare(1,r);
111
           rev[x]^=1;
112
   }//区间翻转
113
   inline void query(int l,int r){
114
115
           R int x=prepare(1,r);
            printf("%d\n",mx[x] );
116
   }//区间查询最大值
   inline int split(R int k){
118
           R int ls;
119
            if (k<size[root])</pre>
120
            {
121
                    R int kth=find(root,k+1);
122
                    splay(kth);ls=ch[kth][0];
123
                    fa[ls]=0;ch[kth][0]=0;
124
                    size[kth] -=size[ls];
125
            }
126
127
            else{
128
                    ls=root;root=0;
            }
129
            return ls;
130
   }//删除数列
131
   inline void merge(R int nwrt){
132
            if (!root) {root=nwrt;return;}
133
            R int nw=find(root,1);
134
            splay(nw);fa[nwrt]=nw;ch[nw][0]=nwrt;
135
            size[nw] +=size[nwrt];
136
   }//合并数列
137
   int main()
138
139
            n=FastIn()+2;Q=FastIn();R int i,1,r,v,cmd;mx[0]=-233333333;
140
            build(1,n,0);root=(1+n)>>1;
141
            for (;Q--;){
142
                    cmd=FastIn();l=FastIn()+1;r=FastIn()+1;
143
                    if (cmd==1) v=FastIn(),add(1,r,v);
144
                    else if (cmd==2) rever(1,r);
145
```

```
146 else query(1,r);
147 }
148 return 0;
149 }
```

5.5.2 非旋转 Treap

```
// Title : Treap (unrotated)
   // Date : 13.04.2016
      Test : BZ0J-3224
  //
      Complexity: O(nlogn)(期望)
   //
6
   /*
           对于序列上的一些操作的问题—
           解决办法:平衡树 Treap
9
10
11 #include <cstdio>
12 #include <cstring>
13 #include <algorithm>
  #include <cmath>
   #ifdef WIN32
           #define LL "%I64d"
17
   #else
18
           #define LL "%lld"
19
   #endif
20
21
   #ifdef CT
22
           #define debug(...) printf(__VA_ARGS__)
23
           #define setfile()
24
   #else
25
26
           #define debug(...)
           #define filename ""
27
           \#define\ setfile()\ freopen(filename".in",\ "r",\ stdin);\ freopen(filename".out",\ "w",\ stdout);
28
   #endif
29
30
  #define R register
31
32 #define qetc() (S == T \& G (T = (S = B) + fread(B, 1, 1 << 15, stdin), S == T) ? EOF : *S++)
33 \#define\ dmax(a, b)\ ((a) > (b) ? (a) : (b))
34 \#define\ dmin(\_a, \_b)\ ((\_a) < (\_b)\ ?\ (\_a)\ :\ (\_b))
  #define cmax(a, b) (a < (b) ? a = (b) : 0
  #define cmin(_a, _b) (_a > (_b) ? _a = (_b) : 0)
_{37} char B[1 << 15], *S = B, *T = B;
  inline int FastIn()
38
39
           R char ch; R int cnt = 0; R bool minus = 0;
40
           while (ch = getc(), (ch < ^{'}0' || ch > ^{'}9') && ch != ^{'}-') ;
41
           ch == '-' ? minus = 1 : cnt = ch - '0';
42
           while (ch = getc(), ch >= '0' && ch <= '9') cnt = cnt * 10 + ch - '0';
43
           return minus ? -cnt : cnt;
44
45
   const int Ta = 1 << 16 | 3, Tb = 33333331;</pre>
46
   int Tc;
  inline int randint() {return Tc = Ta * Tc + Tb;}
  struct Treap
49
50
           int data, key, size;
51
           Treap *ls, *rs;
52
           Treap(int _val):data(_val), key(randint()), ls(NULL), rs(NULL), size(1){}
53
```

```
inline void update()
             {
55
                      size = (ls ? ls -> size : 0) + (rs ? rs -> size : 0) + 1;
56
             }
57
58 | }*root;
59 inline int Size(Treap *x)
60 | {
            return x ? x \rightarrow size : 0;
61
62
    //为了防止访问到空节点, 定义一个函数来访问 size
   struct Pair
64
65
             Treap *fir, *sec;
66
67 | };
68 Treap *Merge(Treap *a, Treap *b)
69
             if (!a) return b;
70
             if (!b) return a;
71
             if (a \rightarrow key < b \rightarrow key)
72
73
                      a \rightarrow rs = Merge(a \rightarrow rs, b);
                      a -> update();
 75
                      return a;
76
             }
77
             else
78
             {
79
                      b -> ls = Merge(a, b -> ls);
 80
                      b -> update();
81
                      return b;
82
83
    //按照 a, b 的顺序来合并两棵 Treap
86 Pair Split(Treap *x, int k)
87 | {
             if (!x) return (Pair){NULL, NULL};
88
             Pair y; y.fir = NULL; y.sec = NULL;
89
             if (Size(x \rightarrow ls) >= k)
90
91
                      y = Split(x \rightarrow ls, k);
92
                      x \rightarrow ls = y.sec;
93
                      x -> update();
94
                      y.sec = x;
             }
96
97
             else
             {
98
                      y = Split(x \rightarrow rs, k - Size(x \rightarrow ls) - 1);
99
                      x \rightarrow rs = y.fir;
100
                      x -> update();
101
                      y.fir = x;
102
             }
103
             return y;
104
105
    //将前 k 个的点分离出来
106
107 inline int Find(R int k)
108
             Pair x = Split(root, k - 1);
109
             Pair y = Split(x.sec, 1);
110
             Treap *ans = y.fir;
111
             root = Merge(Merge(x.fir, ans), y.sec);
112
             return ans -> data;
113
114 }
```

```
115 //找到第 k 小的 data 值
int Get(Treap *x, R int val)
117 {
             if (!x) return 0;
118
             return val \langle x - \rangle data ? Get(x - \rangle ls, val) : Get(x - \rangle rs, val) + Size(x - \rangle ls) + 1;
119
120
    //找到 val 的排名
121
   inline void Insert(R int val)
122
123
            R int k = Get(root, val);
124
            Pair x = Split(root, k);
125
            Treap *pre = new Treap(val);
126
            root = Merge(Merge(x.fir, pre), x.sec);
^{127}
   l٦
128
    //插入
129
130 inline void Delete(R int val)
131 {
            R int k = Get(root, val);
132
            Pair x = Split(root, k - 1);
133
            Pair y = Split(x.sec, 1);
134
            root = Merge(x.fir, y.sec);
135
136
137 //单点删除
   inline int upper(R int val)
138
139
            R int ans = 1e9;
140
            Treap *tmp = root;
141
            while (tmp)
142
143
                      if (tmp -> data > val)
144
145
                      {
                               cmin(ans, tmp -> data);
146
                               tmp = tmp \rightarrow ls;
147
                      }
148
                      else
149
                               tmp = tmp -> rs;
150
             }
151
            return ans;
152
153
   inline int lower(R int val)
154
155
            R int ans = -1e9;
156
157
            Treap *tmp = root;
             while (tmp)
158
159
             {
                      if (tmp -> data < val)</pre>
160
                      {
161
                               cmax(ans, tmp -> data);
162
                               tmp = tmp -> rs;
163
                      }
164
                      else tmp = tmp -> ls;
165
             }
166
167
            return ans;
168
    void print(Treap *x)
169
170
             if (!x) return;
171
             print(x -> ls);
172
            printf("%d ",x -> data );
173
            print(x -> rs);
174
175 }
```

```
176 | int main()
   |{
177
            root = NULL;
178
            for (R int Q = FastIn(); Q; --Q)
179
180
                     R int opt = FastIn(), x = FastIn();
181
                     if (opt == 1) Insert(x);
182
                     else if (opt == 2) Delete(x);
183
                     else if (opt == 3)
184
185
                              R int ans = Get(root, x);
186
                              while (ans > 1 && Find(ans - 1) == x) ans--;
187
                              printf("%d\n", ans );
188
                     }
189
                     else if (opt == 4) printf("d\n", Find(x));
190
                     else if (opt == 5) printf("%d\n",lower(x) );
191
                     else printf("%d\n",upper(x) );
192
            }
193
            return 0;
194
195
196
    input:
197
   10
198
199 1 106465
200 4 1
201 1 317721
   1 460929
202
   1 644985
203
    1 84185
204
205
    1 89851
   6 81968
    1 492737
    5 493598
209
210 output:
211 106465
212 84185
213 492737
214
215 input2:
217 1 1
218 1 1
219 1 1
220 1 2
221 3 1
   output2:
222
    1
223
224
```

5.5.3 可持久化平衡树

```
用来解决超级编辑器等问题。
9
            优势: 好写好调好理解的平衡树
10
            缺点:写不好看的话常数大。(相较于 SBT 来说,甚至有可能会比 splay 慢),需手写 rand
11
12
   #include <cstdio>
13
   #include <cstring>
14
   #include <algorithm>
15
   #include <cmath>
16
17
   #ifdef WIN32
18
            #define LL "%I64d"
19
20
   #else
           #define LL "%lld"
21
   #endif
22
23
   #ifdef CT
24
           #define debug(...) printf(__VA_ARGS__)
25
           #define setfile()
26
   #else
27
           #define debug(...)
28
           #define filename ""
29
           #define setfile() freopen(filename".in", 'r', stdin); freopen(filename".out", 'w', stdout)
30
   #endif
31
32
   #define R register
33
   //\#define\ qetc()\ (S==TEG)(T=(S=B)+fread(B,1,1<<15,stdin),S==T)?E0F:*S++)
34
   #define getc() getchar()
35
   \#define\ dmax(\_a, \_b)\ ((\_a) > (\_b)\ ?\ (\_a)\ :\ (\_b))
36
   #define dmin(_a, _b) ((_a) < (_b) ? (_a) : (_b))
37
   #define cmax(a, b) (a < (b) ? a = (b) : 0)
#define cmin(a, b) (a > (b) ? a = (b) : 0)
38
39
   #define cabs(_x) ((_x)<0?(_x):(_x))
40
   char B[1<<15],*S=B,*T=B;</pre>
  inline int FastIn()
42
43
           R char ch;R int cnt=0;R bool minus=0;
44
           while (ch=getc(),(ch < ^{'}0' || ch > ^{'}9') && ch != ^{'}-^{'});
45
           ch == '-' ?minus=1:cnt=ch-'0';
46
           while (ch=getc(), ch >= '0' \&\& ch <= '9') cnt = cnt * 10 + ch - '0';
47
           return minus?-cnt:cnt;
48
49
   #define maxn 100010
51
   char str[maxn];
   struct Treap
52
53
           char data;
54
           int size;
55
           Treap *ls, *rs;
56
           Treap(char _ch): data(_ch), size(1), ls(NULL), rs(NULL){}
57
           inline void update()
58
59
           {
                    size = (ls ? ls -> size : 0) + (rs ? rs -> size : 0) + 1;
60
           7
61
   }*root[maxn];
62
   inline int Size(Treap *x)
63
64
           return x ? x \rightarrow size : 0;
65
  }
66
  struct Pair
67
   {
68
           Treap *fir, *sec;
69
```

```
70 };
71 inline Treap *copy(Treap *x)
72 | {
             if (!x) return NULL;
73
             Treap *nw = new Treap(x -> data);
74
             nw \rightarrow ls = x \rightarrow ls;
75
             nw \rightarrow rs = x \rightarrow rs;
76
             nw \rightarrow size = x \rightarrow size;
77
             return nw;
78
79
   Pair Split(Treap *x, int k)
80
81
             if (!x) return (Pair){NULL, NULL};
82
             Pair y; y.fir = NULL; y.sec = NULL;
83
             Treap *nw = copy(x);
84
             if (Size(nw -> ls) >= k)
85
             {
86
                      y = Split(nw -> ls, k);
87
                      nw \rightarrow ls = y.sec;
88
                      nw -> update();
89
                      y.sec = nw;
             }
91
             else
92
             {
93
                      y = Split(nw \rightarrow rs, k - Size(nw \rightarrow ls) - 1);
94
                      nw -> rs = y.fir;
95
                      nw -> update();
96
                      y.fir = nw;
97
98
99
             return y;
100
    const int Ta = 1 << 16 | 3, Tb = 33333331;</pre>
101
    unsigned int Tc;
   inline unsigned int randint(){return Tc = Ta * Tc + Tb;}
104 Treap *Merge(Treap *a, Treap *b)
105
             Treap *nw;
106
             if (!a) return nw = copy(b);
107
             if (!b) return nw = copy(a);
108
             if (randint() % (Size(a) + Size(b)) < Size(a))</pre>
109
             {
110
                      nw = copy(a);
111
112
                      nw -> rs = Merge(nw -> rs, b);
             }
113
114
             else
             {
115
                      nw = copy(b);
116
                      nw -> ls = Merge(a, nw -> ls);
117
118
             nw -> update();
119
             return nw;
120
121
   Treap *Build(int 1, int r)
122
123
             if (1 > r) return NULL;
124
             R \text{ int } mid = 1 + r >> 1;
125
             Treap *nw = new Treap(str[mid]);
126
             nw -> ls = Build(1, mid - 1);
127
             nw -> rs = Build(mid + 1, r);
128
             nw -> update();
129
             return nw;
130
```

```
131 }
   int now;
132
   inline void Insert(R int k, R char ch)
133
134
            Pair x = Split(root[now], k);
135
            Treap *nw = new Treap(ch);
136
            root[++now] = Merge(Merge(x.fir, nw), x.sec);
137
138
    inline void Del(R int 1, R int r)
139
140
            Pair x = Split(root[now], 1 - 1);
141
            Pair y = Split(x.sec, r - 1 + 1);
142
            root[++now] = Merge(x.fir, y.sec);
143
   }
144
   inline void Copy(R int 1, R int r, R int 11)
145
146
            Pair x = Split(root[now], 1 - 1);
147
            Pair y = Split(x.sec, r - 1 + 1);
148
            Pair z = Split(root[now], 11);
149
            Treap *ans = y.fir;
150
            root[++now] = Merge(Merge(z.fir, ans), z.sec);
151
152
   inline void Print(Treap *x, R int 1, R int r)
153
154
            if (!x) return ;
155
            if (1 > r) return;
156
            R int mid = Size(x \rightarrow ls) + 1;
157
            if (r < mid)</pre>
158
            {
159
                     Print(x -> ls, l, r);
160
161
                     return ;
            }
162
            if (1 > mid)
163
            {
164
                     Print(x -> rs, 1 - mid, r - mid);
165
                     return ;
166
            }
167
            Print(x -> ls, l, mid - 1);
168
            printf("%c",x -> data );
169
            Print(x -> rs, 1, r - mid);
170
171 }
   inline void Printtree(Treap *x)
172
173
   {
174
            if (!x) return;
175
            Printtree(x -> ls);
            printf("%c",x \rightarrow data);
176
            Printtree(x -> rs);
177
178
    int main()
179
180
               setfile();
181
            R int n = FastIn();
182
            gets(str + 1);
183
            R int len = strlen(str + 1);
184
            root[0] = Build(1, len);
185
            while (1)
186
187
                     R char opt = getc();
188
                     while (opt < 'A' \mid \mid opt > 'Z')
189
                     {
190
                              if (opt == EOF) return 0;
191
```

```
opt = getc();
192
                     }
193
                     if (opt == 'I')
194
                     {
195
                              R int x = FastIn();
196
                              R char ch = getc();
197
                              Insert(x, ch);
198
199
                     else if (opt == 'D')
200
                              R int 1 = FastIn(), r = FastIn();
                              Del(1, r);
203
                     }
204
                     else if (opt == 'C')
205
206
                              R int x = FastIn(), y = FastIn(); z = FastIn();
207
                              Copy(x, y, z);
208
                     }
209
                     else if (opt == 'P')
210
211
                              R int x = FastIn(), y = FastIn(), z = FastIn();
                                printf("%d %d %d n", x, y, z);
213
                              Print(root[now - x], y, z);
214
                              puts("");
215
216
                       Printtree(root[now]);
217
                       puts("");
218
219
            return 0;
220
```

5.6 CDQ 分治 (ct)

```
// Title: cdq 分治
  // Date : 18.04.2016
  // Test : BZ0J-1176
      Complexity : O(nlog^2n)
  //
          对于三维偏序等问题—
          解决办法: 离线询问, 分治降维, 剩下一维用随便什么树乱搞。这样就不用写树套树啦!
11 #include <cstdio>
12 #include <cstring>
  #include <algorithm>
  #include <cmath>
14
15
  #ifdef WIN32
16
         #define LL "%I64d"
17
  #else
18
          #define LL "%lld"
19
  #endif
20
21
  #ifdef CT
22
          #define debug(...) printf(__VA_ARGS__)
23
          #define setfile()
24
  #else
25
          #define debug(...)
```

5.6. CDQ 分治 (CT) 29

```
#define filename ""
27
            #define setfile() freopen(filename".in", "r", stdin); freopen(filename".out", "w", stdout);
28
   #endif
29
30
   #define R register
31
   \#define\ getc()\ (S == T\ \&\&\ (T = (S = B) + fread(B,\ 1,\ 1 << 15,\ stdin),\ S == T)\ ?\ EOF\ :\ *S++)
32
   \#define\ dmax(\_a, \_b)\ ((\_a) > (\_b)\ ?\ (\_a)\ :\ (\_b))
33
   #define \ dmin(_a, _b) \ ((_a) < (_b) ? (_a) : (_b))
34
   #define cmax(a, b) (a < (b) ? a = (b) : 0
35
   #define cmin(_a, _b) (_a > (_b) ? _a = (_b) : 0)
char B[1 << 15], *S = B, *T = B;
36
37
   inline int FastIn()
38
39
           R char ch; R int cnt = 0; R bool minus = 0;
40
           while (ch = getc(), (ch < ^{'}0' || ch > ^{'}9') && ch != ^{'}-^{'});
41
            ch == '-' ? minus = 1 : cnt = ch - '0';
42
            while (ch = getc(), ch >= '0' && ch <= '9') cnt = cnt * 10 + ch - '0';
43
           return minus ? -cnt : cnt;
44
45
   #define maxn 200010
46
   #define maxm 2000010
   struct event
49
50
            int x, y, pos, opet, ans;
            inline bool operator < (const event &that) const {return pos < that.pos ;}</pre>
51
   }t[maxn], q[maxn];
52
   #define lowbit(\underline{x}) ((\underline{x}) & -(\underline{x}))
53
   int bit[maxm], last[maxm], s, w, cnt, now;
54
   inline void add(R int x, R int val)
55
56
            for (; x \le w; x += lowbit(x))
57
58
                     if (last[x] != now)
59
                             bit[x] = 0;
60
                    bit[x] += val;
61
                    last[x] = now;
62
            }
63
64
   inline int query(R int x)
65
66
           R int ans = 0;
67
            for (; x ; x = lowbit(x))
68
69
            {
                     if (last[x] == now)
70
71
                              ans += bit[x];
            }
72
73
            return ans;
74
   void cdq(R int left, R int right)
75
76
            if (left == right) return ;
77
            R int mid = left + right >> 1;
78
            cdq(left, mid); cdq(mid + 1, right);
79
            //分成若干个子问题
80
            ++now:
81
            for (R int i = left, j = mid + 1; j <= right; ++j)
82
83
                    for (; i \le mid \&\& q[i].x \le q[j].x; ++i)
84
                              if (!q[i].opet)
85
                                       add(q[i].y, q[i].ans);
86
                     //考虑前面的修改操作对后面的询问的影响
87
```

```
if (q[j].opet)
                              q[j].ans += query(q[j].y);
89
            }
90
            R int i, j, k = 0;
91
            //以下相当于归并排序
92
            for (i = left, j = mid + 1; i <= mid && j <= right; )</pre>
93
94
                     if (q[i].x \ll q[j].x)
95
                              t[k++] = q[i++];
96
97
                     else
                              t[k++] = q[j++];
98
99
            for (; i <= mid; )</pre>
100
                     t[k++] = q[i++];
101
            for (; j <= right; )</pre>
102
                     t[k++] = q[j++];
103
            for (R int i = 0; i < k; ++i)
104
                     q[left + i] = t[i];
105
106
   int main()
107
    {
108
              setfile();
109
            s = FastIn();
110
            w = FastIn();
111
            while (1)
112
113
                     R int opt = FastIn();
114
                     if (opt == 1)
115
116
                              R int x = FastIn(), y = FastIn(), a = FastIn();
117
                              q[++cnt] = (event)\{x, y, cnt, 0, a\};
118
119
                     if (opt == 2)
120
                     {
121
                              R int x = FastIn() - 1, y = FastIn() - 1, a = FastIn(); b = FastIn();
122
                              q[++cnt] = (event) \{x, y, cnt, 1, x * y * s\};
123
                              q[++cnt] = (event) \{a, b, cnt, 2, a * b * s\};
124
                              q[++cnt] = (event) \{x, b, cnt, 2, x * b * s\};
125
                              q[++cnt] = (event) \{a, y, cnt, 2, a * y * s\};
126
                     }
127
                     if (opt == 3) break;
128
            }
129
130
            cdq(1, cnt);
131
            std::sort(q + 1, q + cnt + 1);
            for (R int i = 1; i <= cnt; ++i)
132
                     if (q[i].opet == 1)
133
                              printf("%d\n",q[i].ans + q[i + 1].ans - q[i + 2].ans - q[i + 3].ans), i +=
134
            return 0;
135
136
```

Others

6.1 vimrc (gy)

```
se et ts=4 sw=4 sts=4 nu sc sm lbr is hls mouse=a
  sy on
  ino <tab> <c-n>
   ino <s-tab> <tab>
   au winnew * winc L
   nm <f6> ggVG"+y
   nm <f7> :w<cr>:make<cr>
   nm <f8> :!00<cr>
   nm <f9> :!@@ < in<cr>
   nm <s-f9> :!(time @@ < in &>> out) &>> out<cr>:sp out<cr>
11
12
   au filetype cpp cm @@ ./a.out | se cin fdm=syntax mp=g++\ %\ -std=c++11\ -Wall\ -Wextra\ -02
13
14
   map <c-p> :ha<cr>
15
   se pheader=%n\ %f
16
17
   au filetype java cm @@ java %< | se cin fdm=syntax mp=javac\ %
   au filetype python cm @@ python % | se si fdm=indent
   au bufenter *.kt setf kotlin
   au filetype kotlin cm @@ kotlin _%<Kt | se si mp=kotlinc\ %
```

6.2 Java Template (gy)

```
import java.io.BufferedReader;
import java.io.IOException;
import java.io.InputStreamReader;
import java.math.BigDecimal;
import java.math.BigInteger;
import java.math.RoundingMode;
import java.util.ArrayDeque;
import java.util.ArrayList;
import java.util.Arrays;
import java.util.Comparator;
import java.util.Deque;
import java.util.LinkedList;
import java.util.LinkedList;
import java.util.List;
import java.util.Scanner;
import java.util.Scanner;
import java.util.StringTokenizer;
```

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```
public class Template {
       // Input
18
       private static BufferedReader reader;
19
       private static StringTokenizer tokenizer;
20
21
       private static String next() {
22
           try {
23
                while (tokenizer == null || !tokenizer.hasMoreTokens())
24
                    tokenizer = new StringTokenizer(reader.readLine());
25
           } catch (IOException e) {
26
                // do nothing
27
28
           return tokenizer.nextToken();
29
       }
30
31
       private static int nextInt() {
32
           return Integer.parseInt(next());
33
34
35
       private static double nextDouble() {
36
           return Double.parseDouble(next());
37
38
39
       private static BigInteger nextBigInteger() {
40
           return new BigInteger(next());
41
42
43
       public static void main(String[] args) {
44
           reader = new BufferedReader(new InputStreamReader(System.in));
45
46
           Scanner scanner = new Scanner(System.in);
47
           while (scanner.hasNext())
48
                scanner.next();
       }
49
50
       // BigInteger & BigDecimal
51
       private static void bigDecimal() {
52
           BigDecimal a = BigDecimal.valueOf(1.0);
53
           BigDecimal b = a.setScale(50, RoundingMode.HALF_EVEN);
54
           BigDecimal c = b.abs();
55
            // if scale omitted, b.scale is used
56
           BigDecimal d = c.divide(b, 50, RoundingMode.HALF_EVEN);
57
            // since Java 9
58
           BigDecimal e = d.sqrt(new MathContext(50, RoundingMode.HALF_EVEN));
60
           BigDecimal x = new BigDecimal(BigInteger.ZERO);
           BigInteger y = BigDecimal.ZERO.toBigInteger(); // RoundingMode.DOWN
61
           y = BigDecimal.ZERO.setScale(0, RoundingMode.HALF_EVEN).unscaledValue();
62
63
64
       // sqrt for Java 8
65
       private static BigDecimal sqrt(BigDecimal a, int scale, RoundingMode mode) {
66
            if (a.equals(BigDecimal.ZERO))
67
                return BigDecimal.ZERO;
68
           a = a.setScale(scale, mode);
69
70
           BigDecimal ans = a;
           BigDecimal TWO = BigDecimal.valueOf(2L);
71
           for (int i = 1; i <= scale; i++)</pre>
72
                ans = ans.add(a.divide(ans, scale, mode)).divide(TWO, scale, mode);
73
           return ans:
74
75
76
       private static BigInteger sqrt(BigInteger a) {
```

```
BigInteger about = BigInteger.ZERO.setBit(a.bitLength() / 2);
78
             return sqrt(new BigDecimal(a.toString()), new BigDecimal(about.toString())).setScale(0,
79
               \hookrightarrow RoundingMode.FLOOR).unscaledValue();
        }
80
81
        private static BigDecimal sqrt(BigDecimal a, BigDecimal initial) {
82
             if (a.equals(BigDecimal.ZERO))
83
                 return BigDecimal.ZERO;
84
             a = a.setScale(50, RoundingMode.HALF_EVEN);
85
             BigDecimal ans = initial;
86
             for (int i = 1; i <= 10; i++)
87
                 ans = ans.add(a.divide(ans, RoundingMode.HALF_EVEN)).divide(BigDecimal.valueOf(2),
                   \hookrightarrow \texttt{RoundingMode.HALF\_EVEN)} \; ;
             return ans;
89
        }
90
91
        // ArrayList
92
        private static void arrayList() {
93
            List<Integer> list = new ArrayList<>();
94
             // Generic array is banned
95
            List[] lists = new List[100];
96
             lists[0] = new ArrayList<Integer>();
97
             // for List<Integer>, remove(Integer) stands for element, while remove(int) stands for
98
               \rightarrow index
             list.remove(list.get(1));
99
             list.remove(list.size() - 1);
100
             list.clear();
101
102
103
        // Queue
104
105
        private static void queue() {
             LinkedList<Integer> queue = new LinkedList<>();
106
107
             // return the value without popping
108
             queue.peek();
             // pop and return the value
109
             queue.poll();
110
             Deque<Integer> deque = new ArrayDeque<>();
111
             deque.peekFirst();
112
             deque.peekLast();
113
             deque.pollFirst();
114
        }
115
116
117
        // Others
118
        private static void others() {
119
             Arrays.sort(new int[10]);
             Arrays.sort(new Integer[10], (a, b) -> {
120
                 if (a.equals(b)) return 0;
121
                 if (a > b) return -1;
122
                 return 1;
123
             });
124
             Arrays.sort(new Integer[10], Comparator.comparingInt((a) -> (int) a).reversed());
125
             long a = 1_000_000_000_000_000_000L;
126
             int b = Integer.MAX_VALUE;
127
             int c = 'a';
128
129
130
```

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6.3 Big Fraction (gy)

```
fun gcd(a: Long, b: Long): Long = if (b == OL) a else gcd(b, a % b)
   class Fraction(val a: BigInteger, val b: BigInteger) {
       constructor(a: Long, b: Long) : this(BigInteger.valueOf(a / gcd(a, b)), BigInteger.valueOf(b /
         \hookrightarrow \gcd(a, b)))
       operator fun plus(o: Fraction): Fraction {
6
           var gcd = b.gcd(o.b)
           val tempProduct = (b / gcd) * (o.b / gcd)
           var ansA = a * (o.b / gcd) + o.a * (b / gcd)
9
           val gcd2 = ansA.gcd(gcd)
10
           ansA /= gcd2
11
           gcd /= gcd2
12
           return Fraction(ansA, gcd * tempProduct)
13
14
15
       operator fun minus(o: Fraction): Fraction {
16
           var gcd = b.gcd(o.b)
17
           val tempProduct = (b / gcd) * (o.b / gcd)
18
           var ansA = a * (o.b / gcd) - o.a * (b / gcd)
19
           val gcd2 = ansA.gcd(gcd)
20
           ansA /= gcd2
21
           gcd /= gcd2
22
           return Fraction(ansA, gcd * tempProduct)
23
24
25
       operator fun times(o: Fraction): Fraction {
26
27
           val gcd1 = a.gcd(o.b)
28
           val gcd2 = b.gcd(o.a)
           return Fraction((a / gcd1) * (o.a / gcd2), (b / gcd2) * (o.b / gcd1))
29
30
```

6.4 模拟退火 (ct)

```
#include <cstdio>
  #include <cmath>
   #include <cstdlib>
4 #include <ctime>
6 #define R register
   \#define\ cmax(\_a, \_b)\ (\_a < (\_b)\ ?\ \_a = (\_b)\ :\ 0)
   #define maxn 10010
9 struct Poi {
           double x, y, m;
10
11 }p[maxn];
12
   double ans_x, ans_y, fans;
13
   inline double randO1() {return rand() / 2147483647.0;}
   inline double randp() {return (rand() & 1 ? 1 : -1) * rand01();}
inline double sqr(R double x) {return x * x;}
inline double f(R double x, R double y)
18 {
           R double maxx = 0;
19
            for (R int i = 1; i \le n; ++i)
20
                    \max += \operatorname{sqrt}(\operatorname{sqr}(x - p[i].x) + \operatorname{sqr}(y - p[i].y)) * p[i].m;
```

6.5. 三分 (CT) 35

```
if (maxx < fans) {fans = maxx; ans_x = x; ans_y = y;}</pre>
22
           return maxx;
23
  }
24
   int main()
25
26
           srand(time(NULL) + clock());
27
           scanf("%d", &n);
28
           R double x = 0, y = 0, tot = 0;
29
           for (R int i = 1; i \le n; ++i)
30
                    scanf("%lf%lf", &p[i].x, &p[i].y, &p[i].m), x += p[i].x * p[i].m, y += p[i].y *
31
                      \hookrightarrow p[i].m, tot += p[i].m;
           fans = 1e30; x \neq tot; y \neq tot;
32
           R double fnow = f(x, y);
33
           for (R double T = 1e4; T > 1e-4; T *= 0.997)
34
35
                    R double nx = x + randp() * T, ny = y + randp() * T, fnext = f(nx, ny);
36
                    R double delta = fnext - fnow;
37
                    if (delta < 1e-9 || exp(-delta / T) > rand01())
38
39
                             x = nx; y = ny; fnow = fnext;
40
                    }
41
42
           printf("%.31f %.31f\n", ans_x, ans_y);
43
           return 0;
44
45
```

6.5 三分 (ct)

```
#define maxn 200010
   #define inf 1e9
   int a[maxn], n;
   inline double check(R double x)
5
           R double tmp, tmp1 = 0, tmp2 = 0, maxx = -inf, minn = -inf;
6
           for (R int i = 1; i <= n; ++i)
            {
                    tmp = (double) a[i] - x;
9
10
                    tmp1 += tmp;
11
                    cmax(maxx, tmp1);
12
                    tmp1 < 0 ? tmp1 = 0 : 0;
13
                    tmp2 -= tmp;
                    cmax(minn, tmp2);
16
                    tmp2 < 0 ? tmp2 = 0 : 0;
17
18
           return dmax(maxx, minn);
19
20
   int main()
21
22
           n = F();
23
           for (R int i = 1; i <= n; ++i) a[i] = F();
24
           R double 1 = -1e4, r = 1e4;
25
           for (R int i = 1; i <= 100; ++i)
26
27
                    R \text{ double } 11 = (1 + r) * 0.5;
28
                    R \text{ double } rr = (11 + r) * 0.5;
29
                    if (check(ll) < check(rr)) r = rr;</pre>
30
                    else 1 = 11;
31
```

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```
32
           printf("%.61f\n", check((1 + r) * 0.5));
33
           return 0;
34
35
```

博弈论模型 (gy) 6.6

• Wythoff's game

给定两堆石子,每次可以从任意一堆中取至少一个石子,或从两堆中取相同的至少一个石子,取走最后 石子的胜

先手胜当且仅当石子数满足:

 $\lfloor (b-a) \times \phi \rfloor = a, (a \le b, \phi = \frac{\sqrt{5}+1}{2})$

先手胜对应的石子数构成两个序列:

Lower Wythoff sequence: $a_n = \lfloor n \times \phi \rfloor$ Upper Wythoff sequence: $b_n = \lfloor n \times \phi^2 \rfloor$

• Fibonacci nim

给定一堆石子,第一次可以取至少一个、少于石子总数数量的石子,之后每次可以取至少一个、不超过 上次取石子数量两倍的石子, 取走最后石子的胜

先手胜当且仅当石子数为斐波那契数