



COLLEGE OF ENGINEERING  
SCHOOL OF AEROSPACE ENGINEERING

AE 6705: INTRODUCTION TO MECHATRONICS

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## LAB9

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## Question 1

Generate a step input with 100% duty cycle and measure the open-loop motor response by capturing sampled motor speed values and storing it in an array. Print out this array to the CCS console after the motor reaches steady state. Repeat this experiment for different speed changes (i.e. 20%, 40%, 60%, and 80% duty cycles) so that the results can be compared.

### Solution:

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RPM Raw Data
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```
,20%,40%,60%,80%,100%
RPM[0] ,163.24028,20.781232,45.546093,69.42585,126.74398
RPM[1] ,40.5289,36.906185,111.857941,235.407257,38.57468
RPM[2] ,72.675148,55.860237,236.520813,38.162495,43.653309
RPM[3] ,121.448868,130.994232,36.253265,41.428871,46.249653
RPM[4] ,37.338886,191.5728,38.379265,42.826981,55.35928
RPM[5] ,40.446934,233.429031,38.932102,50.541294,57.267784
RPM[6] ,40.913593,34.27039,45.434349,51.541592,57.241558
RPM[7] ,57.307163,34.880013,46.040974,51.266788,65.850777
RPM[8] ,58.28923,34.580883,45.55439,58.893406,66.658447
RPM[9] ,55.304173,39.704994,52.165363,59.018532,65.070923
RPM[10] ,80.193268,39.720764,52.132729,57.544594,74.162704
RPM[11] ,78.617134,38.730053,50.710445,65.206703,73.42218
RPM[12] ,70.692062,43.710548,57.123844,64.717186,71.134583
RPM[13] ,107.136276,43.395679,56.7285,62.57885,80.3479
RPM[14] ,100.726227,41.964329,54.723106,70.255028,79.214981
RPM[15] ,87.99807,47.121387,61.418129,69.348824,76.231895
RPM[16] ,140.727554,46.525078,60.63607,66.863464,85.427132
RPM[17] ,128.239288,44.759193,58.160404,74.583092,83.85125
RPM[18] ,106.113113,49.97052,64.986351,73.153618,80.412506
RPM[19] ,182.616867,49.097111,63.751751,70.225418,89.703087
RPM[20] ,160.566788,47.068153,61.080502,78.34613,87.95163
RPM[21] ,125.471779,52.604416,68.11129,76.62912,83.76696
RPM[22] ,242.250473,51.472614,66.640678,73.132217,93.598839
RPM[23] ,201.047455,49.247021,63.573425,81.30162,91.025848
RPM[24] ,149.523026,54.729092,70.602226,79.378471,86.957382
RPM[25] ,315.8591,53.362331,68.994751,75.735382,96.731483
RPM[26] ,251.006531,51.02092,65.695045,84.175926,94.269424
RPM[27] ,176.867706,56.689907,72.940186,82.413872,89.719177
RPM[28] ,458.299713,55.194283,71.246078,78.395271,99.463898
RPM[29] ,323.418488,52.621025,67.687157,86.806427,96.918976
RPM[30] ,205.340866,58.221352,74.783875,84.67485,91.980316
RPM[31] ,577.372986,56.715633,72.75975,80.477226,101.834007
RPM[32] ,379.078827,54.083828,69.195267,89.302559,99.424339
RPM[33] ,228.000458,59.859333,76.66436,86.806427,94.127441
RPM[34] ,850.348633,58.323223,74.361244,82.454643,104.385178
RPM[35] ,454.549988,55.304173,70.622177,91.042427,101.297615
```

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 RPM[50], 33.355904, 59.730614, 76.394958, 98.194221, 108.933556  
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RPM[150],35.132446,72.548607,92.507866,107.343277,116.850899

---

## Question 2

Use a program such as MATLAB, Excel, etc. to plot the motor responses for each tested case versus time. Use the response corresponding to 100% duty cycle to measure the motor time constant and gain  $K$ . Write the open-loop transfer function for this case. This transfer function will describe the input-output relationship for each test case. What do you notice happening as the duty cycle increases? What is the reason for this?

---

### Solution:

From the step response of 100% duty cycle in Figure 1, we can compute the parameters of the transfer function which are the time constant and gain where gain is the steady state RPM value and the time constant is the time that took for the response to reach approximately 63% of the steady state value.

Time Constant $\tau$	Gain $K$
0.0753	123.3266

Table 1: Time constant and gain of first order system from data

Thus, the open loop transfer function for this system becomes

$$G(s) = \frac{123.3266}{0.0753s + 1}.$$

Furthermore, from Figure 1 we can see that as the duty cycle increases the fluctuations that occur at the beginning of the response becomes attenuated. This is due to a phenomenon called windup which causes the RPM to rise drastically and sporadically for when the duty cycle is low. This is due to saturation and not having an anti-windup scheme in our system.

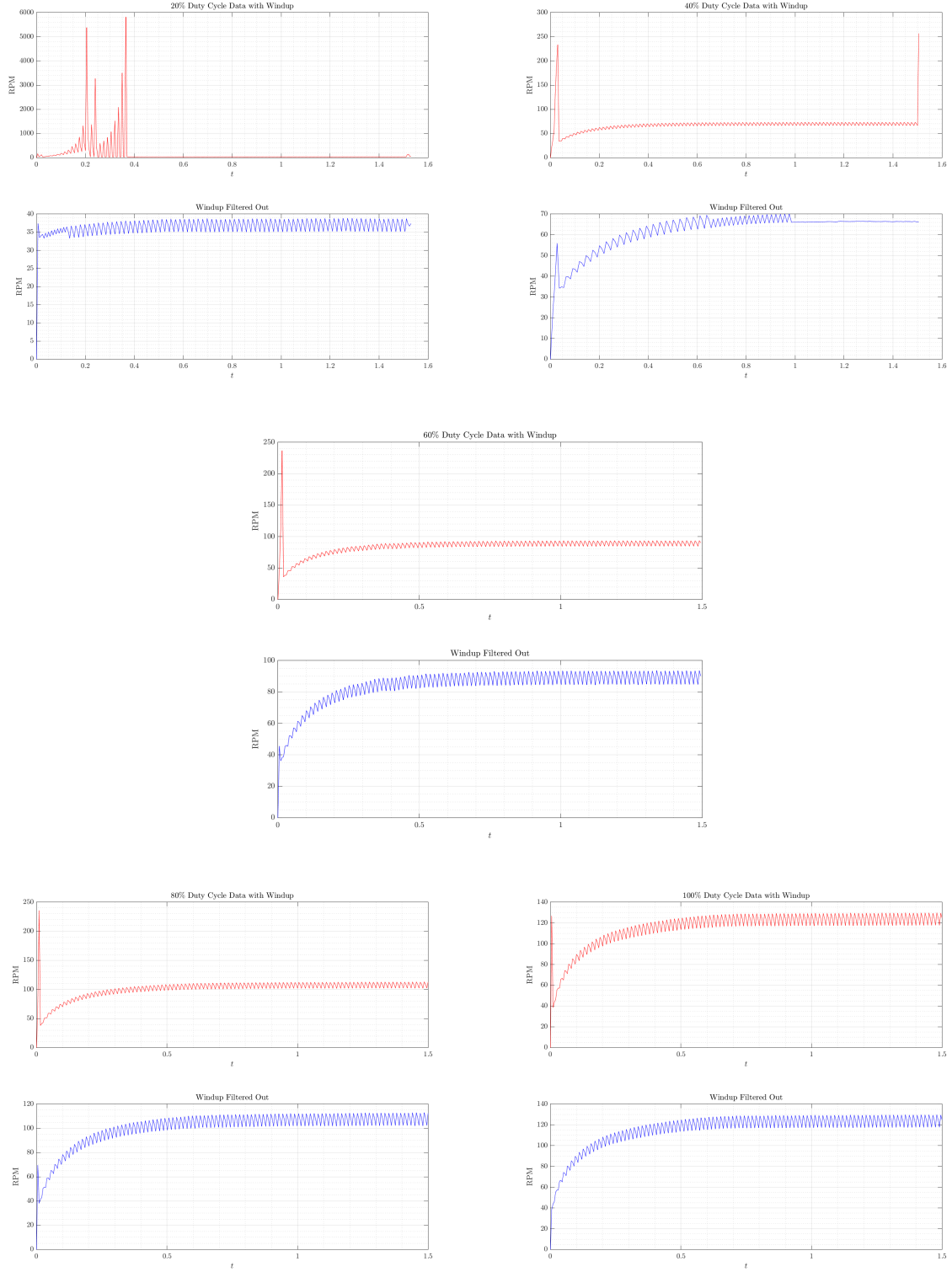


Figure 1: Step response for each corresponding duty cycles



### Question 3

Verify the measured time constant and gain by creating and running a Simulink model for a first order system. Use this to simulate a step input. Your simulated response should be similar to your experimental results.

---

#### Solution:

Using the Simulink model below

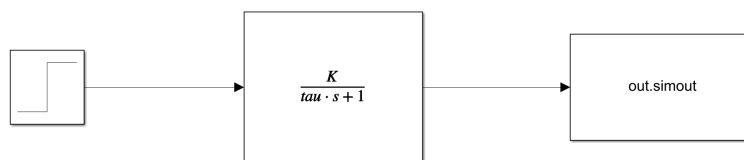


Figure 2: Simulink model of first order system

we obtain the following result

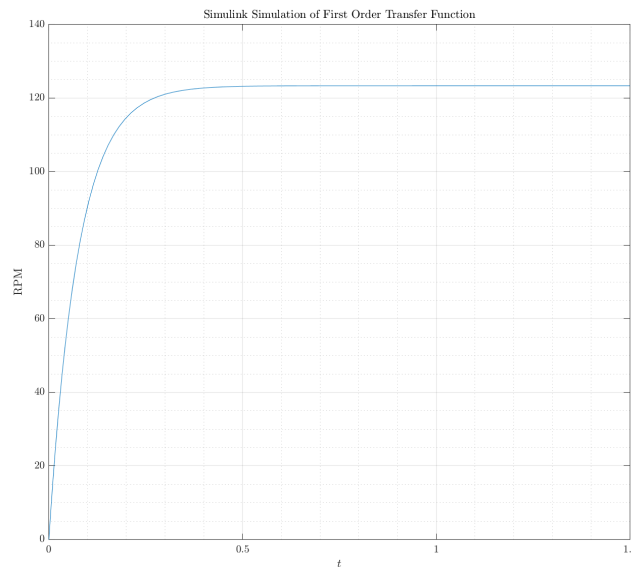


Figure 3: Simulink model of first order system

## Question 4

Calculate the transfer function using step responses resulted from other duty cycles. Is the resulting transfer function the same for all the experiments? If not, discuss why.

---

### Solution:

Using MATLAB we compute the other transfer functions with their gains and time constants. The result is tabulated as follows.

Time Constant $\tau$	Gain $K$	Transfer Function
$\approx 0$ ( $\epsilon$ )	37.0432/0.2	$\frac{185.216}{\epsilon s + 1}$
0.0821	66.5705/0.4	$\frac{166.4263}{0.0821s + 1}$
0.0654	89.0193/0.6	$\frac{148.3655}{0.0654s + 1}$
0.0953	107.0021/0.8	$\frac{133.7526}{0.0953s + 1}$
0.0753	123.3266	$\frac{123.3266}{0.0753s + 1}$

Table 2: Time constant and gain of first order system for all cases

We can observe from this table that the transfer functions each have a different gain value as well as a time constant. For each duty cycle there is a slight error or deviation between the theoretical value and the actual value that is output from the system due to factors such as disturbances and errors. For the case of 20% duty cycle there was a lot of errors due to winding and it even had a rapid rise that made it difficult to measure the time constant value. These limitations due to the digital system along with the disturbances and errors caused this deviation of transfer functions for each duty cycle case.

## Appendix

### 5.1 MATLAB Code

```
1 % AE6705 MATLAB code
2 % Tomoki Koike
3 clear all; close all; clc; % housekeeping commands
4 set(groot, 'defaulttextinterpreter','latex');
5 set(groot, 'defaultAxesTickLabelInterpreter','latex');
6 set(groot, 'defaultLegendInterpreter','latex');
7 %%
8 % Time
9 t_interr = 15000 / 3e+6;
10 %%
11 % DC 20%
12 data = csvread("dc20.csv");
13 T = t_interr * length(data);
14 data = [0; data];
15 fdata1 = data(data < 40);
16 t = linspace(0,T,length(data));
17 ft1 = linspace(0,T,length(fdata1));
18 fig = figure("Renderer","painters","Position",[60 60 950 800]);
19     subplot(2,1,1)
20     plot(t,data,'-r')
21     title('20\% Duty Cycle Data with Winding')
22     xlabel('$t$')
23     ylabel('RPM')
24     grid on; grid minor; box on;
25     subplot(2,1,2)
26     plot(ft1,fdata1,'-b')
27     title('Winding Filtered Out')
28     xlabel('$t$')
29     ylabel('RPM')
30     grid on; grid minor; box on;
31 saveas(fig,'outputs/dc20_plot.png')
32 %%
33 % DC 40%
34 data = csvread("dc40.csv");
35 T = t_interr * length(data);
36 data = [0; data];
37 fdata2 = data(data < 70);
38 t = linspace(0,T,length(data));
39 ft2 = linspace(0,T,length(fdata2));
40 fig = figure("Renderer","painters","Position",[60 60 950 800]);
```

```

41     subplot(2,1,1)
42     plot(t,data,'-r')
43     title('40\% Duty Cycle Data with Winding')
44     xlabel('$t$')
45     ylabel('RPM')
46     grid on; grid minor; box on;
47     subplot(2,1,2)
48     plot(ft2,fdata2,'-b')
49     title('Winding Filtered Out')
50     xlabel('$t$')
51     ylabel('RPM')
52     grid on; grid minor; box on;
53 saveas(fig,'outputs/dc40_plot.png')
54 %%
55 % DC 60%
56 data = csvread("dc60.csv");
57 T = t_interr * length(data);
58 data = [0; data];
59 fdata3 = data(data < 100);
60 t = linspace(0,T,length(data));
61 ft3 = linspace(0,T,length(fdata3));
62 fig = figure("Renderer","painters","Position",[60 60 950 800]);
63     subplot(2,1,1)
64     plot(t,data,'-r')
65     title('60\% Duty Cycle Data with Winding')
66     xlabel('$t$')
67     ylabel('RPM')
68     grid on; grid minor; box on;
69     subplot(2,1,2)
70     plot(ft3,fdata3,'-b')
71     title('Winding Filtered Out')
72     xlabel('$t$')
73     ylabel('RPM')
74     grid on; grid minor; box on;
75 saveas(fig,'outputs/dc60_plot.png')
76 %%
77 % DC 80%
78 data = csvread("dc80.csv");
79 T = t_interr * length(data);
80 data = [0; data];
81 fdata4 = data(data < 120);
82 t = linspace(0,T,length(data));
83 ft4 = linspace(0,T,length(fdata4));
84 fig = figure("Renderer","painters","Position",[60 60 950 800]);
85     subplot(2,1,1)

```

```

86     plot(t,data,'-r')
87     title('80\% Duty Cycle Data with Winding')
88     xlabel('$t$')
89     ylabel('RPM')
90     grid on; grid minor; box on;
91     subplot(2,1,2)
92     plot(ft4,fdata4,'-b')
93     title('Winding Filtered Out')
94     xlabel('$t$')
95     ylabel('RPM')
96     grid on; grid minor; box on;
97 saveas(fig,'outputs/dc80_plot.png')
98 %%
99 % DC 100%
100 data = csvread("dc100.csv");
101 T = t_interr * length(data);
102 data = [0; data];
103 fdata5 = data;
104 fdata5(2) = [];
105 t = linspace(0,T,length(data));
106 ft5 = linspace(0,T,length(fdata5));
107 fig = figure("Renderer","painters","Position",[60 60 950 800]);
108     subplot(2,1,1)
109     plot(t,data,'-r')
110     title('100\% Duty Cycle Data with Winding')
111     xlabel('$t$')
112     ylabel('RPM')
113     grid on; grid minor; box on;
114     subplot(2,1,2)
115     plot(ft5,fdata5,'-b')
116     title('Winding Filtered Out')
117     xlabel('$t$')
118     ylabel('RPM')
119     grid on; grid minor; box on;
120 saveas(fig,'outputs/dc100_plot.png')
121 %%
122 % Computing the time constant and the gain
123 K = mean(fdata5(100:end));
124 fval = fdata5(end);
125 idx = max(find(abs(fdata5-fval)>=0.37*fval));
126 tau = ft5(idx);
127 %%
128 % Verify with simulink model
129 res = sim("motor_model.slx");
130 %%

```

```

131 fig = figure("Renderer","painters","Position",[60 60 950 800]);
132 plot(res.tout, res.simout.signals.values);
133 grid on; grid minor; box on;
134 title("Simulink Simulation of First Order Transfer Function")
135 xlabel('$t$')
136 ylabel('$RPM$')
137 saveas(fig,"outputs/model_resp.png")
138 %%
139 % Computing the time constant and gains for the other duty cycles
140 Ks = [0 0 0 0 0];
141 taus = [0 0 0 0 0];
142 fts = {ft1 ft2 ft3 ft4 ft5};
143 ct = 1;
144 for fd = {fdata1 fdata2 fdata3 fdata4 fdata5}
145     k = mean(fd{1,1}(100:end));
146     fv = fd{1,1}(end);
147     i = max(find(abs(cell2mat(fd)-fv)>=0.37*fv));
148     ftemp = fts{1,ct};
149     toe = ftemp(i);
150     Ks(ct) = k ;
151     taus(ct) = toe;
152     ct = ct + 1;
153 end

```