# AAE 334: Aerodynamics

HW7: Wing Stability Analysis
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Download the files in the HW7 folder on Blackboard. To review use of XFLR5 for stability analysis see the video 'XFLR5 Demo for AAE 334 Stability Lecture' by Professor Sullivan, which is available on the AAE 334 Course Content page on Blackboard. After performing the calculations or running the analyses described below, enter the results in the appropriate column in the Excel file "AAE334 Homework 7 Data and Answer Sheet". Print a copy of the completed spreadsheet to turn in with your homework.

#### 1. Problem #1

- a. [25 pts] Using the formulas in the notes, calculate the stability quantities on the "Homework sheet" tab of the Excel file "AAE334 Homework 7 Data and Answer Sheet". Show your handwritten work on separate sheets of paper.
- b. [25 pts] Run XFLR5 using the file "AAE 334 telemaster stability Homework #7.xfl" and compare your answers (i.e., calculate the percent difference). (Note that the xfl file already has the geometry of the airplane included. In addition, the analysis of the wing alone has already been done. However, you will have to run the necessary analysis of the airplane.)
- 2. Problem #2 Rerun xFLR5 with a velocity V=20 m/sec.
  - a. [25 pts] Trim the aircraft by moving the CG so the aircraft is stable at the proper trim point.
  - b. [25 pts] Trim the aircraft by changing the tail angle so the aircraft is stable at the proper trim point. (Use the original CG location.)

\*The spreadsheet with the final answers is at the end

$$\begin{array}{ll} & Q_{00} & Q_{00} & = \frac{1}{2} P_{00} V_{00}^{2} \\ & = \frac{1}{2} \left( |_{225} \frac{pq}{pq_{3}} \right) \left( |_{34} \frac{m}{5} \right)^{2} \\ & = \frac{1}{10949805} P_{00} \end{array}$$

CL assuming steady-level flight
$$C_L = \frac{W}{905m} = \frac{46.71N}{(109.9605pm)(0.86m^2)} = 0.4949$$

Angles from the MACA 2412 lift curve (in Appendix)
$$CL = 0.4949 \rightarrow Ce = CL \cdot b = 1.183$$

$$Q_{2L} = -2 dy = -0.0349 rad$$

Dyn P: 9,00 - 109.9805 Pa

Re # wing: Re,w = 321048.79

Re # tail : Re,+ = 215561.33

lift coeff: CL = 0,4949 - from graph que -20 = -0.0349 rad

Rac wing: ( (Xac) w = Ctr = 0.09 m

Pac tail: (xac) - C+ = 0.0602 m

ao: for Ci: 0.4949 → Slope ≈ 270

\* Xcg: The angle of incidence of the wing (mr. 7 to plane)

in = 4.50 = 0.0785 rad

The angle of incidence of the tail (wint to mean chord of ming)

11 = 1 = 2° = 2.5° = 0.0436 rad

Using there the lift coefficients of the why and tail respectively

becomes  $C_{LN} = 2\pi (Q - \lambda_N) \cdots O$   $C_{LN}, C_{LN}, Q \rightarrow un | enoughs$   $C_{L1} = 2\pi (Q - \lambda_1) \cdots O$ 

and from equilibrium

W= Lw+ L+

W = 900 Sm Cin + 900 St Cit

W = Poo (Sm Cim + St Cit) ... 3.

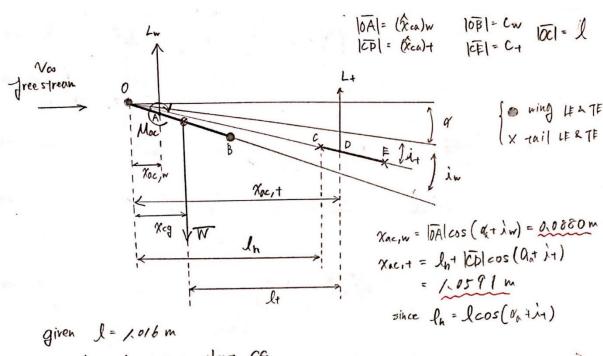
solve the system equations D@3 (using MATLAB)

→ Cin: 0,3550 - Ln= 900 Su Cin = 33,5728 N

CL1 = 0.5740 - L-1 = 800 St CL1 = 13.1372N

and Q = 0.1350

- 9a = 9-921 = 0.1699 rad (absolute angle of attack)



non from the numero about CG

solving this neget

$$\chi_{cg} = 0.19.74m$$
  $\chi_{cg} = \frac{\chi_{cg}}{C} = 0.5483$ 

► Cia since

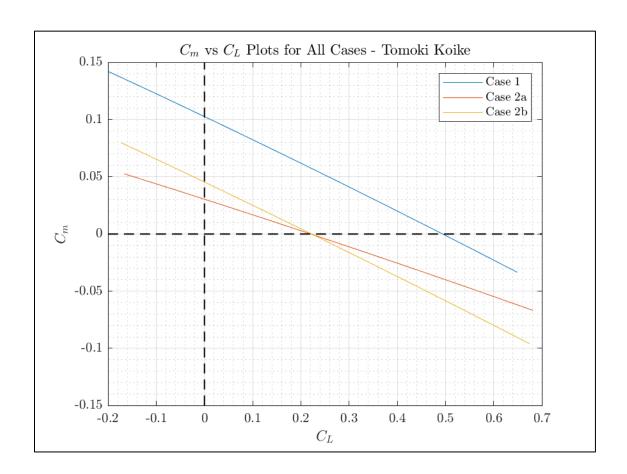
$$V_h \qquad \text{shee} \qquad V_h = \frac{s_+ f_+}{SE} = 0.5780$$

$$C_{Mq} = C_{LQ} \left( \tilde{\chi}_{cq} - \tilde{\chi}_{ac} \right) - \left( C_{LQ} \right)_T \left( 1 - \frac{\partial c}{\partial q} \right) V_h$$

$$= -0.5346$$

$$\widetilde{\chi}_{n} = \widetilde{\chi}_{nc} + \frac{(c_{cq})}{C_{cq}} \left(1 - \frac{2\epsilon}{\partial \alpha}\right) V_{nc}$$

$$= 0.8069$$



#### MATLAB CODE

#### AAE334 HW7 MATLAB CODE

```
clear all; close all; clc;

fdir = 'C:\Users\Tomo\Desktop\studies\2020-Spring\AAE334\matlab\outputs\HW7';

set(groot, 'defaulttextinterpreter',"latex");

set(groot, 'defaultAxesTickLabelInterpreter',"latex");

set(groot, 'defaultLegendInterpreter',"latex");
```

## problem 1-a

```
% Defining necessary properties
v inf = 13.4; % freestream velocity [m/s]
rho_inf = 1.225; % freestream air density [kg/m3]
q inf = 0.5*rho inf*v inf^2; % freestream dynamic pressure [Pa]
S_w = 0.86; % wing area [m2]
S t = 0.208; % tail area [m2]
ch_w = 0.36; % chord length of wing [m]
ch t = 0.241; % chord length of tail [m]
l = 1.016; % distance from the LE of the wing to the LE of the tail [m]
ch mean = ch w; % mean chord length of the wing [m]
epsilon = 0;
e_a = 0.4; % D(epsilon)/Da
W = 46.71; % weight of the plane [N]
% Calculating the x_cg (center of gravity of the plane)
% Necessary angles [rad]
a zl = deg2rad(-2.1) % zero lift angle
i w = deg2rad(4.5) % incident angle of the wing
i_t = i_w - deg2rad(2) % incident angle of the tail wrt the plane
% find a, C_Lw, and C_Lt
[C_Lw, C_Lt, a] = CLw_CLt_AoA(W, i_w, i_t, q_inf, S_w, S_t)
a a = a - a zl % absolute angle of attack
% the lifts for the wing and tail
L w = q inf*S w*C Lw % wing [N]
L_t = q_inf*S_t*C_Lt % tail [N]
% aerodynamic center positions (wrt the LE of the wing)
xhat ac w = ch w/4 \% wing [m]
xhat_ac_t = ch_t/4 % tail [m]
```

```
lh = l*cos(a a + i t);
x_ac_w = xhat_ac_w*cos(a_a + i_w)
x_ac_t = lh + xhat_ac_t*cos(a_a + i_t)
x_ac_til = 0.25;
% moment coefficient about the aerodynamic center of the wing
C Mac w = -0.05;
% moment about the aerodynamic center of the wing [N-m]
Mac_w = q_inf*S_w*ch_mean*C_Mac_w
% solve
syms var1
eqn1 = Mac_w + L_w*(var1 - x_ac_w) - L_t*(x_ac_t - var1) + W*var1 == 0;
x cg = double(solve(eqn1, var1))
x_{cg_til} = x_{cg/ch_mean}
% C La
C_La_w = C_Lw/a_a
% C_La_t
C_La_t = C_Lt/(a_a)
% l_t distance from the x_cg to the aerodynamic center of the tail
l_t = x_ac_t - x_cg
Vh = S_t*l_t/S_w/ch_mean
% C Mo
C_Mo = C_Mac_w + C_La_t*(epsilon + i_t)*Vh
% C Ma
C_Ma = C_La_w*(x_cg_til - x_ac_til) - C_La_t*(1 - e_a)*Vh
x_n_{til} = x_ac_{til} + C_La_t/C_La_w*(1 - e_a)*Vh
x n = x n til*ch mean
SM = x_n_{til} - x_cg_{til}
problem 1-b
```

```
% importing data
data_1b = readmatrix("inputs\hw7\hw7_Cm_vs_Cl_case1_2_2.csv");
% Calculating the static margin
SM_1b = calc_SM_from_xflr(data_1b)
```

```
data_1b2 = readmatrix("inputs\hw7\hw7_Cm_vs_alpha_case1_2.csv");
% Calculating the C_M0 (*for the angle of attack add 2.1 degrees to adjust
% to the absolute angle of attack)
[C_Mo_1b, C_Ma_1b] = calc_CMo_and_CMa_from_xlfr(data_1b2, -2.1, rad2deg(i_w))
```

### problem 2-a

```
% importing data
data_2a = readmatrix("inputs\hw7\hw7_Cm_vs_Cl_case2a.csv");
% Calculating the static margin
SM_2a = calc_SM_from_xflr(data_2a)
% Importing another data
data 2a2 = readmatrix("inputs\hw7\hw7 Cm vs alpha case2a.csv");
% Calculating the C M0 (*for the angle of attack add 2.1 degrees to adjust
% to the absolute angle of attack)
[C_Mo_2a, C_Ma_2a] = calc_CMo_and_CMa_from_xlfr(data_2a2, -2.1, rad2deg(i w))
% find a, C Lw, and C Lt
q_{inf}_{2a} = 245;
[C_Lw_2a, C_Lt_2a, a_2a] = CLw_CLt_AoA(W, i_w, i_t, q_inf_2a, S_w, S_t)
a_a_2a = a_2a - a_zl % absolute angle of attack
% the lifts for the wing and tail
L_w = q_{inf}_{2a*S_w*C_Lw_2a} \% wing [N]
L_t = q_inf_2a*S_t*C_Lt_2a % tail [N]
```

## problem 2-b

```
% importing data
data 2b = readmatrix("inputs\hw7\hw7 Cm vs Cl case2b.csv");
% Calculating the static margin
SM 2b = calc SM from xflr(data 2b)
% Importing another data
data_2b2 = readmatrix("inputs\hw7\hw7_Cm_vs_alpha_case2b.csv");
% Calculating the C_M0 (*for the angle of attack add 2.1 degrees to adjust
% to the absolute angle of attack)
[C Mo 2b, C Ma 2b] = calc CMo and CMa from xlfr(data 2b2, -2.1, rad2deg(i w))
% find a, C Lw, and C Lt
q_{inf}_{2b} = 245;
[C Lw 2b, C Lt 2b, a 2b] = CLw CLt AoA(W, i w, i t, q inf 2b, S w, S t)
a a 2b = a 2b - a zl % absolute angle of attack
% the lifts for the wing and tail
L w = q inf 2b*S w*C Lw 2b % wing [N]
L_t = q_inf_2b*S_t*C_Lt_2b % tail [N]
```

# **Plotting**

```
fig1 = figure("Renderer","painters");
```

```
plot(data_1b(:,1),data_1b(:,2))
title({'$C_m$ vs $C_L$ Plots for All Cases - Tomoki Koike'})
xlabel('$C_L$')
ylabel('$C_m$')
hold on
plot(data_2a(:,1),data_2a(:,2))
plot(data_2b(:,1),data_2b(:,2))
plot(linspace(-0.2,0.7,100),zeros([1,length(linspace(-0.2,0.7,100))]),'--
k',"LineWidth",1.0)
plot(zeros([1,length(linspace(-0.15,0.15,100))]),linspace(-0.15,0.15,100),'--
k',"LineWidth",1.0)
hold off
grid on; grid minor; box on;
legend('Case 1','Case 2a','Case 2b')
saveas(fig1, fullfile(fdir,'Cm_vs_Cl.png'))
```

#### **FUNCTIONS**

```
function SM = calc SM from xflr(data)
    % data: data points
    CL_1b = data(:,1);
    Cm_1b = data(:,2);
    % SM
    if Cm 1b(CL 1b == min(abs(CL 1b)))
        Cm_1b_0 = Cm_1b(CL_1b == min(abs(CL_1b)));
    else
        Cm_1b_0 = Cm_1b(CL_1b == -(min(abs(CL_1b))));
    end
    if CL \ 1b(Cm \ 1b == -(min(abs(Cm \ 1b))))
        CL_1b_0 = CL_1b(Cm_1b == -(min(abs(Cm_1b))));
    else
        CL_1b_0 = CL_1b(Cm_1b == (min(abs(Cm_1b))));
    end
    SM = Cm 1b 0/CL 1b 0;
end
function [C Mo, C Ma] = calc CMo and CMa from xlfr(data, a zl, i w)
    % data: data points
    % a zl: zero lift angle of attack
    % i w: wing incidence angle
    Cm = data(:,2);
    a = data(:,1) - a_zl + i_w;
    P = polyfit(a,Cm,1);
    C Ma = P(1);
    C Mo = P(2);
end
```

```
function [C_Lw, C_Lt, a] = CLw_CLt_AoA(W, i_w, i_t, q_inf, S_w, S_t)
  % system equations to find a, C_Lw, and C_Lt
  syms x1 x2 x3
  eqn1 = x1 == 2*pi*(x3 - i_w);
  eqn2 = x2 == 2*pi*(x3 - i_t);
  eqn3 = W == q_inf*(S_w*x1 + S_t*x2);
  res = solve([eqn1 eqn2 eqn3],[x1 x2 x3]);
  % the lift coefficients for the wing and tail respectively
  C_Lw = double(res.x1);
  C_Lt = double(res.x2);
  % angle of attack
  a = double(res.x3);
end
```