

(b)

process A:

$$pV = C = pV_1 = (1 \times 10^5 \text{ Pa})(0.1 \text{ m}^3) = 1 \times 10^5 \text{ Pa} \cdot \text{m}^3$$

$$p = \frac{C}{V}$$

$$W_A = \int_1^2 p dV = \int_{V_1}^{V_2} \frac{C}{V} dV = C \ln \frac{V_2}{V_1} = (1 \times 10^5 \text{ Pa} \cdot \text{m}^3) \ln \left(\frac{1.0 \text{ m}^3}{0.1 \text{ m}^3} \right)$$

$$\approx 2.302 \times 10^5 \text{ J} = 230.2 \text{ kJ}$$

$$W_A = 230 \text{ kJ}$$

process B:

1 \rightarrow 3 isovolumetric so no work

$$3 \rightarrow 2 \quad p(V) = \alpha V + \beta \quad \dots \textcircled{1}$$

$$\alpha = \frac{(2 \times 10^5 - 1 \times 10^5) \text{ Pa}}{(0.1 - 1.0) \text{ m}^3} \approx -1.11 \times 10^5 \frac{\text{Pa}}{\text{m}^3}$$

plug in p_2, V_2 into $\textcircled{1}$

$$\beta = 1 \times 10^5 + \left(1.11 \times 10^5 \frac{\text{Pa}}{\text{m}^3} \right) (1.0 \text{ m}^3) = 2.11 \times 10^5 \text{ Pa}$$

$$p(V) = \alpha V + \beta$$

$$W_B = \int_3^2 p(V) dV = \int_{V_1}^{V_2} (\alpha V + \beta) dV = \frac{\alpha}{2} (V_2^2 - V_1^2) + \beta (V_2 - V_1)$$

$$= \frac{1}{2} \left(-1.11 \times 10^5 \frac{\text{Pa}}{\text{m}^3} \right) (1.0^2 - 0.1^2) (\text{m}^6) + (2.11 \times 10^5 \text{ Pa}) (1.0 - 0.1) (\text{m}^3)$$

$$= 134955 \text{ J} = 134.955 \text{ kJ}$$

$$W_B = 135 \text{ kJ}$$

(c)

$$Q_A = \Delta U + W_A = (U_2 - U_1) + W_A$$

$$= (200 \text{ kJ} - 400 \text{ kJ}) + 230 \text{ kJ}$$

$$= -30.0 \text{ kJ}$$

$$Q_B = \Delta U + W_B = (U_2 - U_1) + W_B$$

$$= -200 \text{ kJ} + 135 \text{ kJ}$$

$$= -65.0 \text{ kJ}$$

$$Q_A = -30.0 \text{ kJ}$$

$$Q_B = -65.0 \text{ kJ}$$