Introduction to Mechatronics (ME/AE 6705) Lab Assignment 9

Characterizing a DC Motor Using Encoders, MSP432 LaunchPad and PWM Signals

9.1 Objective

The objectives of this lab are three fold:

- i. to build an electromechanical system using a DC motor and an encoder,
- ii. to implement an open loop controller using an MCU, and
- iii. to characterize the step response and transfer function using experimental data.

9.2 Deliverables and Grading

To get credit for this lab assignment you must:

- 1. Demonstrate proper operation of your code to TAs or instructor during office hours or demo hours. You must write your own code for this lab no lab groups are allowed. (30 points)
- 2. Submit all plots and answer all questions listed at the end of the lab assignment as a PDF file to Canvas before the due data specified on Canvas. (50 points).
- 3. Submit the commented final version of your code on Canvas (single .c file containing your main() function, do not submit header files, etc. Combine all your codes into a single file. You should only submit a single .c file.) (Pass/Fail)

9.3 Setup

This lab requires Code Composer Studio, the MSP432 LaunchPad, and an electromechanical system comprised of a DC motor and an encoder.

The lab uses onboard features of the MSP432 LaunchPad including GPIOs, Timer A, PWM, Timer Capture/Compare and interrupts. We will also use the motor driver circuit built in Lab 8.

9.4 Problem Statement

Create an electromechanical system consisting of a DC motor and an encoder sensor attached to the motor. The microcontroller will be used to apply a variable PWM signal to the motor driver circuit built in Lab 8.

This lab will characterize a fundamental property of the dynamic system – the system's *step* response. The first-order transfer function of the system can be modeled by extracting the system's *time constant* and *gain* from the step response.

A series of experiments will be performed in this lab. First, a step input will be applied by taking speed readings with a duty cycle of 100%. Speed readings will be taken in real-time until the speed stops changing (less than 2 seconds). The step response can be shown by plotting this time series, and a first-order transfer function for the DC motor can be derived based on that.

For the next experiments, the same process will be performed for all duty cycles (20-100%). The plots of step responses for different duty cycles can then be constructed.

9.5 Hardware

We reviewed the background on brushed DC motors, H-bridge ICs, flyback diodes and breadboards in Lab Assignment 8. In this lab, we will be also using the encoder attached to the DC motor.

9.5.1 Encoder

An encoder is a sensor with digital outputs that relate to rotational speed. The DC motor used in this lab is equipped with an encoder board that senses the rotation of the magnetic disc and provides a resolution of 12 counts per revolution of the motor shaft. The encoder board has 6 pins: the motor leads are connected to the M1 and M2 pins along the edge of the board; the remaining four pins are used to power the sensors and access the two quadrature outputs.

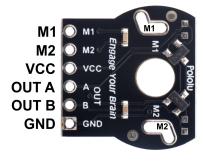


Figure 1: Encoder board.

The encoder is powered through the VCC and GND pins. To be used with the MSP432

LaunchPad, VCC should be 3.3 V, and the quadrature outputs A and B are open-drain digital signals that need to be pulled up to the 3.3V voltage of the system using two 10k resistors.

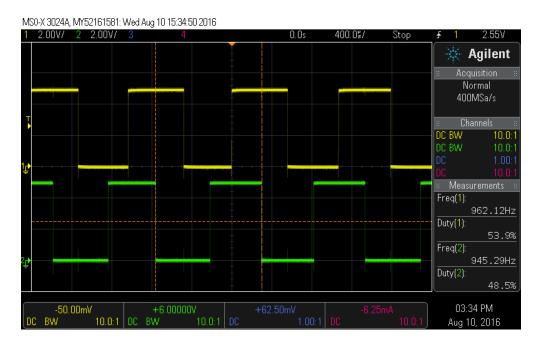


Figure 2: Scope trace of the two outputs of the encoder, period*360 is the time for one revolution (Image courtesy of Pololu). The two vertical dashed lines indicate a period of the green signal (the time between two falling edges).

The encoder produces a pair of pulse trains, called outputs A and B, that look like the signals shown in Figure 2. Each output pulses 360 times per rotation. If we measure the Period (in sec) of one of the encoder signals, we can calculate the motor speed in rpm as

$$Speed\ (rpm) = 60/(360*Period)$$

We can use the MSP432 input capture mode to make time measurements on input signals. The MSP432 microcontroller has four General Purpose Timer Modules called Timer_A. Each timer has one 16-bit timer and seven associated capture/compare registers.

In this lab, we will use Timer_A2 to create a capture input for the encoder interface. There will be an interrupt on each falling edge of output A, and the timer will measure the period of the encoder output.

The second encoder signal (output B) can be connected to a GPIO to detect the motor direction: A falling edge for output A and a high signal for B signifies one direction, while a falling edge for output A and a low signal for B signifies the other direction. The direction associated with each case can be tested by running the motor and visually noting the direction of rotation for the tested case.

9.5.2 Circuit Schematic

Figure 3 shows the circuit we use to interface the brushed DC motor and the encoder with the MSP432 LaunchPad. You have already assembled part of this circuit (everything except the encoder) on the breadboard in Lab Assignment 8.

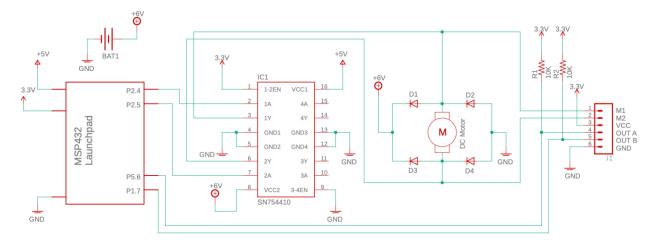


Figure 3: Circuit diagram for the H-bridge interface with motor and encoder.

Two $10K\Omega$ pull-up resistors ¹ are connected to the encoder output pins (pin A and pin B), as the outputs are open-drain digital signals.

The encoder outputs of the DC motor are connected to P5.6 and P1.7 as shown on the schematic. Note that P5.6 corresponds to TA2.1 which can be used as Capture/Compare Input 1A (CCI1A, that is Register 1 Input A) for Timer_A2.

Note: Part of the circuit shown in Figure 3 is the same as the motor driver circuit built in Lab 8.

Note: Remember to connect a common ground between the LaunchPad and the driver circuit.

Warning: While driving the motors using the H-bridge circuit, continue to check the temperature of the MSP432 and SN754410 ICs. If it is getting hot, disconnect the LaunchPad immediately and debug the circuit.

9.6 Electormechanical System Modeling

As discussed in the class, the open-loop transfer function of a DC motor plant is given by:

$$P(s) = \frac{\omega(s)}{U(s)} = \frac{K}{(Js+b)(Ls+R) + K^2} \qquad (rad/sec/V)$$
 (1)

¹Resistor color codes: brown-black-orange (10 $K\Omega$)

Often times, the motor inductance can be neglected (assuming L is too small), and the motor transfer function is written as a first order transfer function.

The plant *input* is the voltage (or the duty cycle of the PWM signal) that drives the motor, and the plant output is the motor speed (which can be measured as the period of the encoder output signal).

For a motor with unknown parameters, the transfer function can be obtained by either a systematic or an experimental approach.

9.6.1 Systematic approach

With this approach, the motor parameters including inertia J, damping b, inductance L, resistance R and motor torque constant K need to be measured or calculated.

Given the fact that the torque produced by the rotor (τ_m) is directly proportional to the current (i) in the armsture windings through the torque constant of the motor (K):

$$\tau_m = K \times i,\tag{2}$$

this approach requires advanced lab equipment for torque measurements. Therefore, for the purpose of this lab assignment, we will use an experimental approach to estimate the transfer function of the DC motor.

9.6.2 Experimental approach

In this lab, the transfer function will be *estimated* by extracting key parameters from a measured *step response*. The plant input will be a *step function* (a change in duty cycle of the PWM signal). The step change in duty cycle is produced by the MSP432 LaunchPad. The resulting response at the plant output is also recorded by the microcontroller and stored in an array of its internal memory, which can be examined by the debugger.

Suppose the plant's step response looks like a simple exponential, as illustrated in Figure 4. This suggests that the plant can be modeled as a *first-order* system with input u(t), measured output signal y(t), time constant τ , and gain K. The model is given by the linear ordinary differential equation:

$$Ku(t) = \tau \frac{dy(t)}{dt} + y(t)$$

Solving this equation produces the step response for time t > 0:

$$y(t) = K\Delta u(1 - e^{-\frac{t}{\tau}})$$

where Δu is the step change in the input. The gain K is simply the change in y divided by the change in u, computed when the system has reached steady state (i.e. for large t).

The time constant τ is the time needed for the output to make 63.2% (e^{-1}) of the change from its initial to its final value.

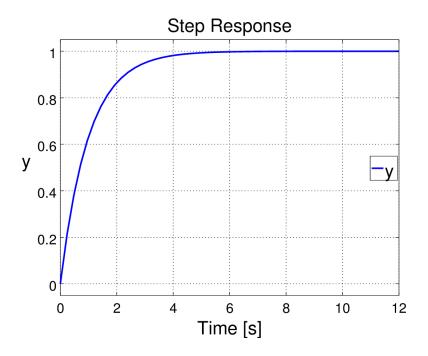


Figure 4: First order step response.

Knowing the time constant and gain, the transfer function of this first-order system can be written as:

$$G(s) = \frac{Y(s)}{U(s)} = \frac{K}{\tau s + 1} \tag{3}$$

MATLAB/Simulink can be used to verify the experimental data via the model, which is that of a first order system driven by a step input. If the experimental data fits a first order behavior, then using the computed values of K and τ in the Simulink model should produce a simulated response that matches the experimental result.

9.7 Software

Note: To setup a new project for CCS with driverlib, create an "Empty Project (with main.c)" similar to lab 2, copy only the "driverlib" folder provided with lab 2 and paste it into the new project, and specify the search path for the C preprocessor.

The first task for the software is to use Timer_A2 to measure period from the encoder. Set up Timer_A2 to create a capture input for the encoder interface. There needs to be an interrupt on each *falling edge* of output A (connected to P5.6), and the encoder output can be measured by comparing the "capture/compare count" from the previous falling edge to the current falling edge.

Note: Once the Timer_A2 Capture mode is initialized for the Register 1 and Input A, the INT_TA2_N timer interrupt needs to be enabled, which results in triggering the TA2_N_IRQHandler() interrupt service routine at each timer interrupt.

Note: The timer capture/compare count can be accessed using the DriverLib function: Timer_A_getCaptureCompareCount(...). Please consult with the DriverLib User's Guide for more details on the associated input and output arguments.

The second task is to use the encoder period to determine the motor speed. Since there are 360 pulses per rotation, the Speed in rpm can be calculated as

$$Speed\ (rpm) = 60/(360 * Period)$$

If you choose the DCO and SMCLK at 3 MHz (with prescale of 1), the period measurement resolution will be 333 ns. The second input of the encoder can be used to determine which direction the motor is spinning (optional). You will write software that counts the number of timer ticks between two consecutive encoder pulses as the motor spins, and store them in an array, as described in the following.

Write a program that starts with applying a PWM signal with zero duty cycle to the motor. The PWM signal can be generated using Timer_AO, similar to Lab 8. Pressing the S1 pushbutton on the LaunchPad should adjust a desired speed variable to different PWM duty cycles (in 20% increments) (while maintaining the motor off). Pressing the S2 pushbutton should then instantaneously drive the motor with the desired speed (according to the specified PWM duty cycle), thus producing the required step input.

As soon as the step input is produced, the program should log the motor speed by measuring the period of encoder pulses. This can be done by storing the *timer ticks* at each timer/capture interrupt caused by the encoder output A into a buffer. Record data until speed is stabilized (for about 1000 samples, or about 1 to 2 seconds). This represents the step response of the system. After the motor has reached steady state, convert the stored timer ticks to *speed values* (in RPM) and *timestamps* and print out the array of sampled speed values along with their timestamps into the CCS console. This allows one to plot the step response ("speed" vs. time). The motor time constant and gain parameters can then be extracted from the plot.

Apply different control inputs and record the resulting step responses and steady state speeds. Start at 20% duty cycle. Record encoder measurements until they stop changing, and print out the data into the CCS console. Repeat these steps for duty cycles 40-100%, in 20% increments. Compute the average steady state speed for each duty cycle applied.

9.8 Questions

- 1. Generate a step input with 100% duty cycle and measure the open-loop motor response by capturing sampled motor speed values and storing it in an array. Print out this array to the CCS console after the motor reaches steady state. Repeat this experiment for different speed changes (i.e. 20%, 40%, 60% and 80% duty cycles) so that the results can be compared.
- 2. Use a program such as MATLAB, Excel, etc. to plot the motor responses for each tested case versus time. Use the response corresponding to 100% duty cycle to measure the

motor time constant and gain K. Write the open-loop transfer function for this case. This transfer function will describe the input-output relationship between the motor speed and input duty cycle. In addition, compare the step responses for each test case. What do you notice happening as the duty cycle increases? What is the reason for this?

- 3. Verify the measured time constant and gain by creating and running a Simulink model for a first order system. Use this to simulate a step input. Your simulated response should be similar to your experimental results.
- 4. Calculate the transfer function using step responses resulted from other duty cycles. Is the resulting transfer function the same for all the experiments? If not, discuss why.

Make sure to cover each of the questions above fully, as points will be deducted for incomplete answers.