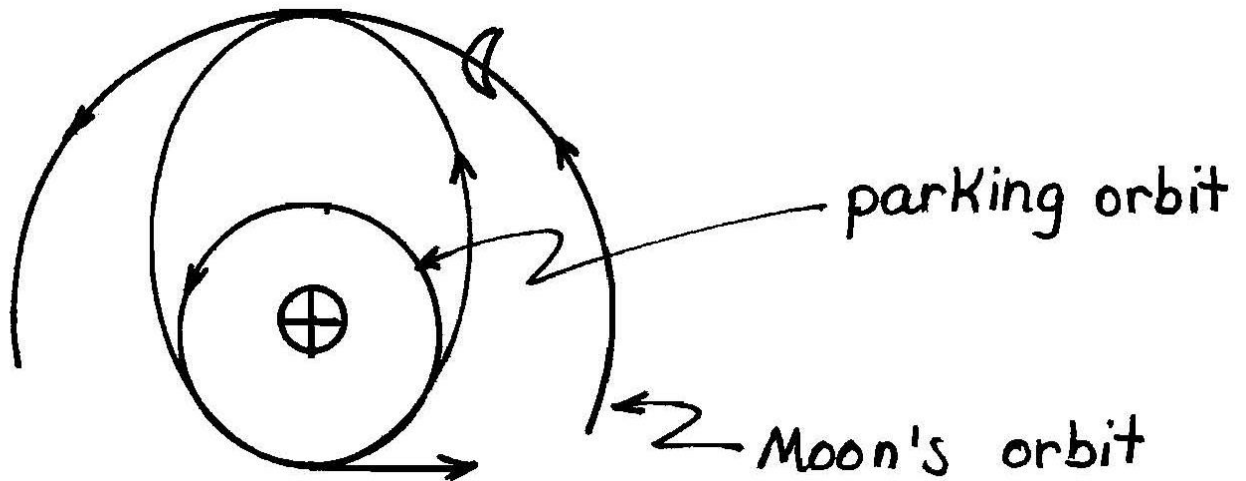


Example: Free-Return Trajectories

Consider circumlunar trajectories

Assume 

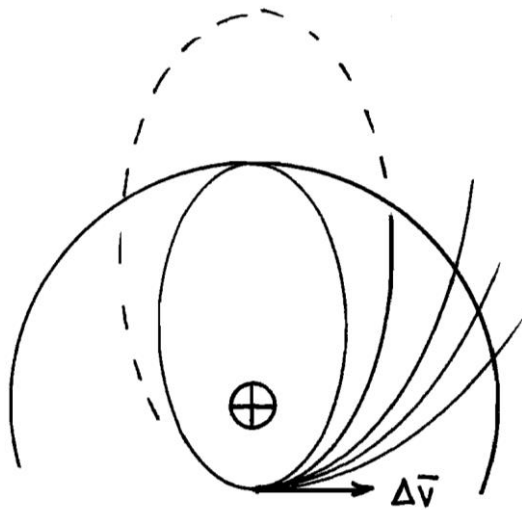
Note: patched-conic approach less accurate in this problem than for interplanetary



If \mathbb{C} has no gravity

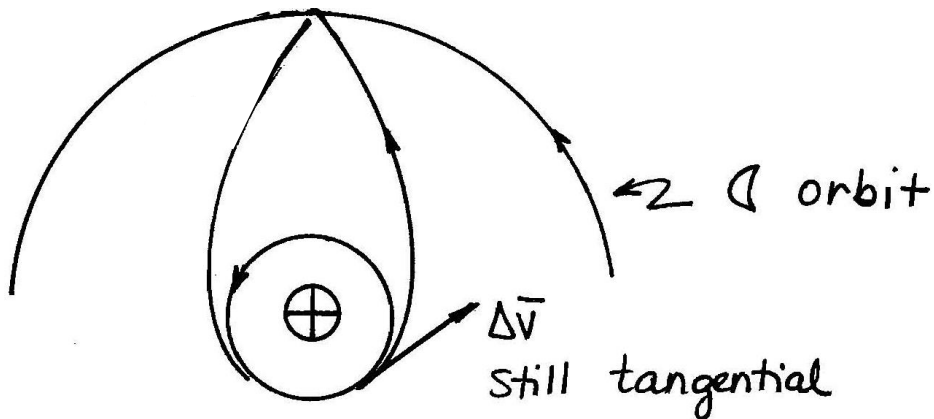
1. Jump to ellipse from parking orbit
2. At \mathbb{C} , with no $\Delta \bar{v}$, remains on transfer ellipse
3. Returns to \oplus at radius of parking orbit

\mathbb{C} does possess gravity



Consider:

1. make transfer ellipse larger
2. $\Delta \bar{v}$ still tangential (most efficient)
3. apogee $\geq r_{\mathbb{C}}$
4. reach \mathbb{C} sooner at different angle



If pass \mathbb{C} such that

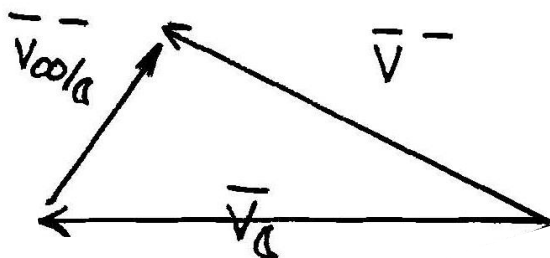
$$v_r^+ = -v_r^-$$

$$v_\theta^+ = +v_\theta^-$$



end up on same trajectory for \oplus return

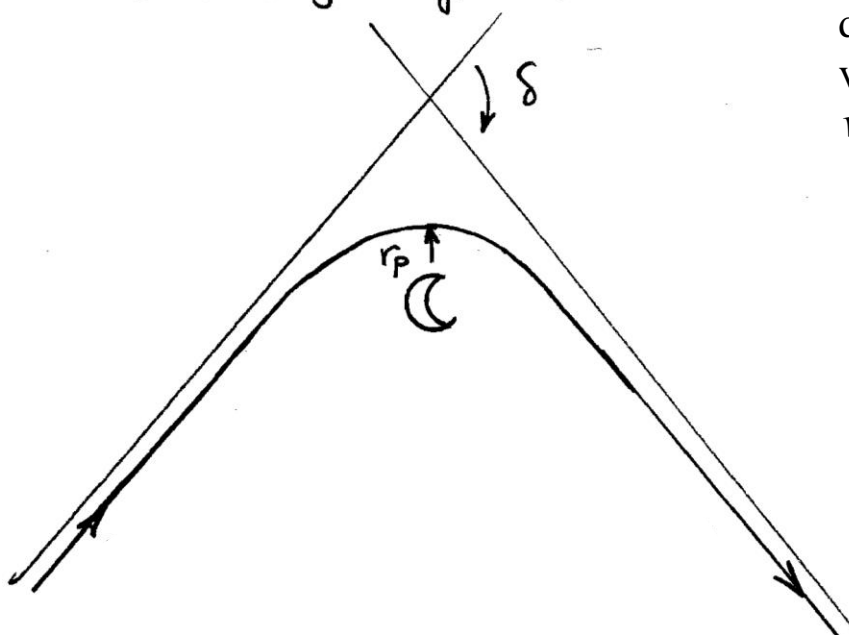
Vector Diagram



Same relative velocity equation:

$$\vec{v}^- = \vec{v}_{\infty/a} + \vec{v}_a$$

Local trajectory



Flyby angle determined by value of v_∞ and r_p

Notes:

1. Early Apollo flights → free-return

Typical 3-day outbound leg

Pass ahead of \mathbb{C} so s/c could enter 3-day return leg if failure occurs

Apollo 11 (for landing) 3 day out; 2.5 day return (if insertion did not occur would not return to vicinity of Earth)

2. Apollo 17 altered its initial free-return translunar trajectory to get a more precise landing

$$r_{p/\mathbb{C}} = 1849 \text{ (111 altitude) / passed ahead}$$

Entered lunar orbit

3. Apollo 13

Had made a mid-course correction to leave free-return path before experiencing failure that aborted \mathbb{C} landing

Lunar module engines used after explosion to modify trajectory and return to \oplus

Apollo 13 → same trajectory / failure enroute to \mathbb{C} / lunar module descent engines did fire

$$\text{Lunar approach: } v_r = +.244 \quad v_\theta = 0$$