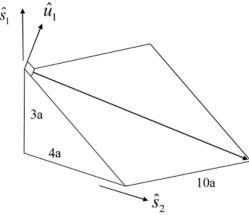
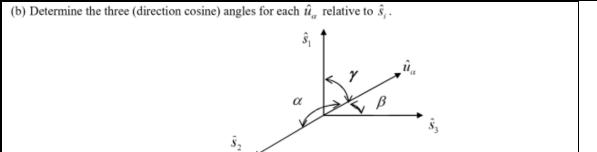
1. The block below is a right triangular wedge. Vector bases  $\hat{u}$  and  $\hat{s}$  are dextral, orthonormal triads and fixed in the block. Note that  $\bar{H} = H\,\hat{u}_3$  and  $\hat{u}_1$  is normal to the top surface.



(a) Determine the direction cosine matrix that relates  $\hat{u}$  and  $\hat{s}$ . Note that the relationship can be written in the forms

$$\begin{bmatrix} \hat{s}_1 \\ \hat{s}_2 \\ \hat{s} \end{bmatrix} = L \begin{bmatrix} \hat{u}_1 \\ \hat{u}_2 \\ \hat{u} \end{bmatrix} \quad \text{or} \quad \begin{bmatrix} \hat{s}_1 & \hat{s}_2 & \hat{s}_3 \end{bmatrix} = \begin{bmatrix} \hat{u}_1 & \hat{u}_2 & \hat{u}_3 \end{bmatrix} C$$

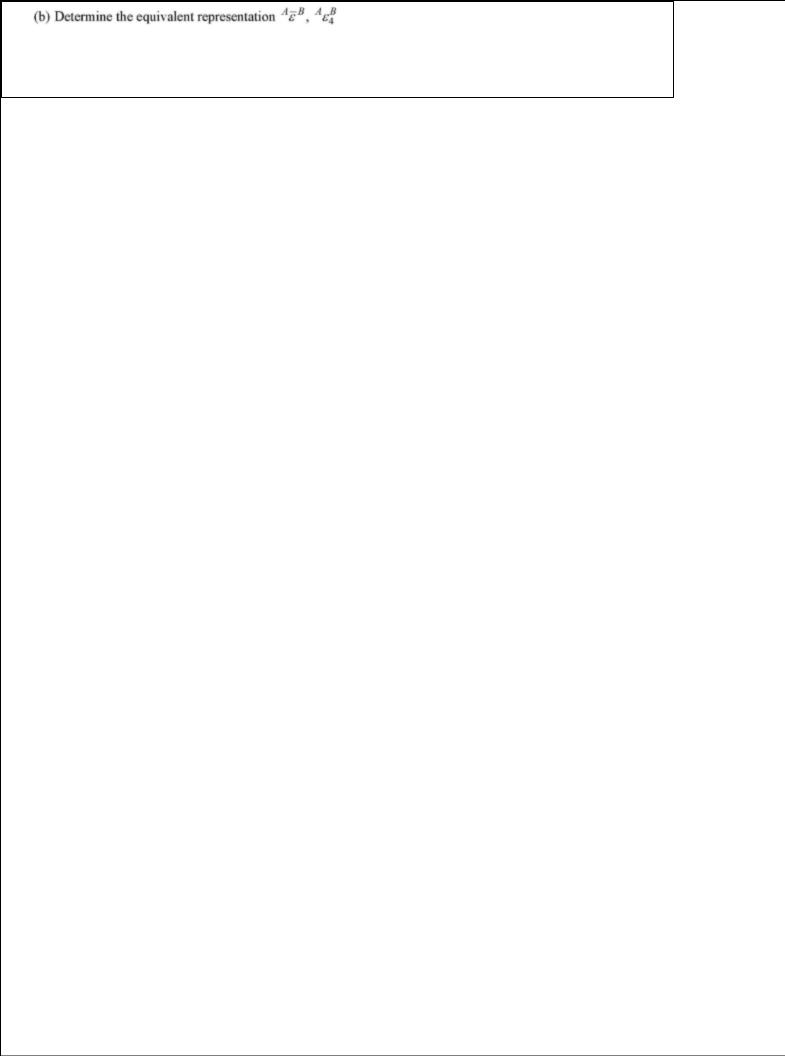
Write out both L and C. Evaluate the measure numbers and test the orthogonality conditions.



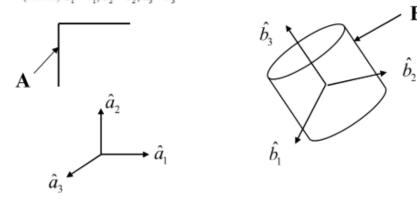
**Problem 2:** Given that the rigid body B from problem 2 moves relative to A, suppose its orientation is known at a given instant. Let this new orientation be given as

$${}^{A}C^{B} = \begin{bmatrix} .4638 & .3607 & .8091 \\ -.6082 & -.0052 \\ -.6442 & -.4897 & .5876 \end{bmatrix}$$

(a) Determine the missing element in the  ${}^AC^B$ Verify that all orthogonality conditions are satisfied. What is the accuracy?



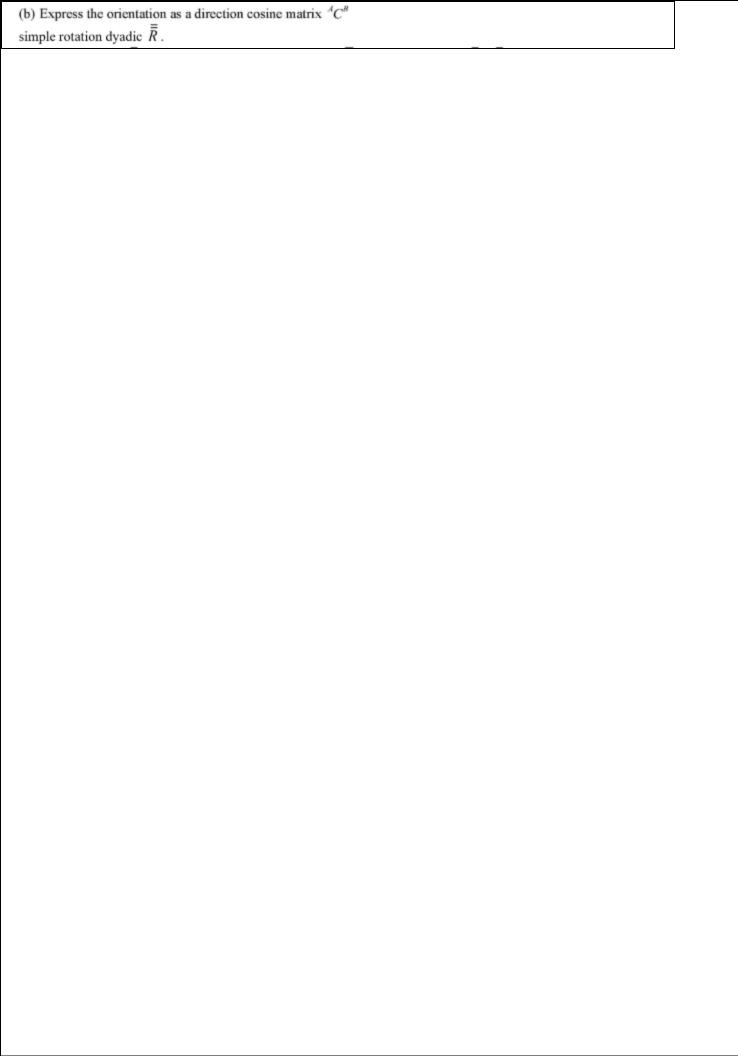
**Problem 3:** Assume that a rigid body B (e.g., a rigid spacecraft) can move with respect to a frame A. Let unit vectors  $\hat{b}$  be fixed in body B; unit vectors  $\hat{a}$  are fixed in A. At the initial time,  $\hat{a}_i = \hat{b}_i$  (that is,  $\hat{a}_1 = \hat{b}_1$ ,  $\hat{a}_2 = \hat{b}_2$ ,  $\hat{a}_3 = \hat{b}_3$ 



At some later time, the orientation of B in A is described in terms of the simple rotation:

$${}^{A}\overline{L}^{B} = -1\hat{a}_{1} + 2\hat{a}_{2} + 2\hat{a}_{3}$$
 ${}^{A}\theta^{B} = -120^{\circ}$ 

(a) Sketch  $\hat{\lambda}$  (and  $\overline{L}$ ) in 3-D. Add the direction of  $\theta$  to the sketch.



(c) Define a vector  $\overline{k}$  that is fixed in  $\hat{a}$  initially such that  $\overline{k}=1\hat{a}_1-2\hat{a}_2$ . Label  $\overline{k}=\overline{k}_a$  to reflect the vector prior to the rotation; then,  $\overline{k}=\overline{k}_b$  represents the vector after the rotation. The vector  $\overline{k}_b$  is fixed in the body B such that  $\overline{k}_a=\overline{k}_b$  at the initial time. After the simple rotation, express  $\overline{k}_b$  in terms of unit vectors  $\hat{b}$ ;  $\hat{a}$ . (Use the simple rotation theorem!) Since  $\overline{k}_a=1\hat{a}_1-2\hat{a}_2$ , does  $\overline{k}_b=1\hat{b}_1-2\hat{b}_2$   $\overline{k}_b=1\hat{a}_1-2\hat{a}_2$ ? After the rotation, should the measure numbers be the same in both  $\hat{a}$  and  $\hat{b}$ ?