Triangle meshes 2

CS 4620 Lecture 3

Practical encoding of meshes

OBJ file format

- widely used format for polygon meshes
- supports the usual attributes: position, normal, texture coordinate
- allows triangles or polygons (only triangles and quads widely supported)
- particularly flexible about controlling continuity of attributes
- comes with a crude mechanism for adding materials

Demo

- simple file with one triangle
- effects of normals and texture coords
- exploration of continuity and discontinuity

Simple computations with meshes

Smoothing

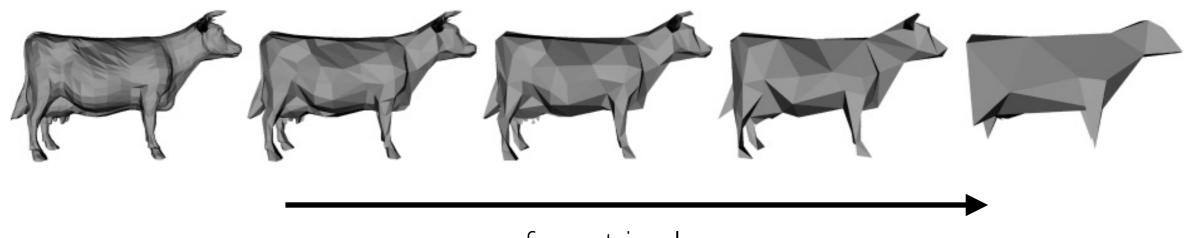
- Idea I: move each vertex to the average of all neighboring vertices
- Idea 2: move each vertex partway towards the avg. of its neighbors
- there are many fancier ways to do this but with similar flavor

Computing normals

- Idea I: faces already have normals; just use those.
- Idea 2: set normal @ each vertex to the average of the neighboring triangles' normals
- Idea 3: ...to a weighted avg. of the neighboring triangles' normals
 - weight by area
 - weight by angle

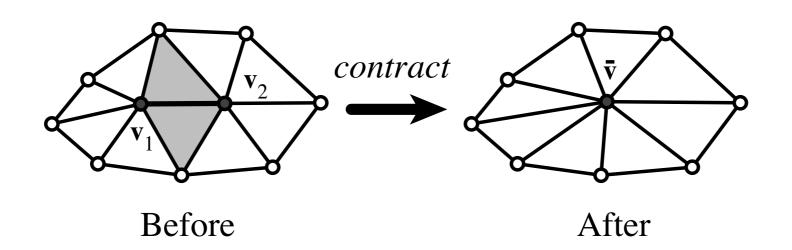
Ops. that change mesh topology

Mesh simplification



fewer triangles

popular approach based on edge-collapse operations:



Queries on meshes

For face, find all:

- vertices
- edges
- neighboring faces
- For vertex, find all: ←
 - incident edges
 - incident triangles
 - neighboring vertices

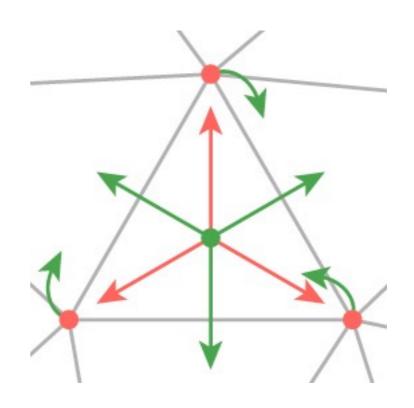
• For edge, find:

- two adjacent faces
- two adjacent vertices

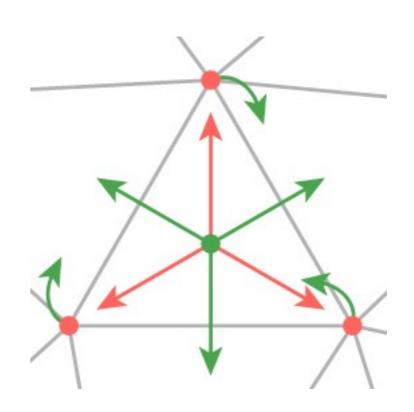
useful for smoothing/normal operations, if you want to compute them one vertex at a time (all at once is easier!)

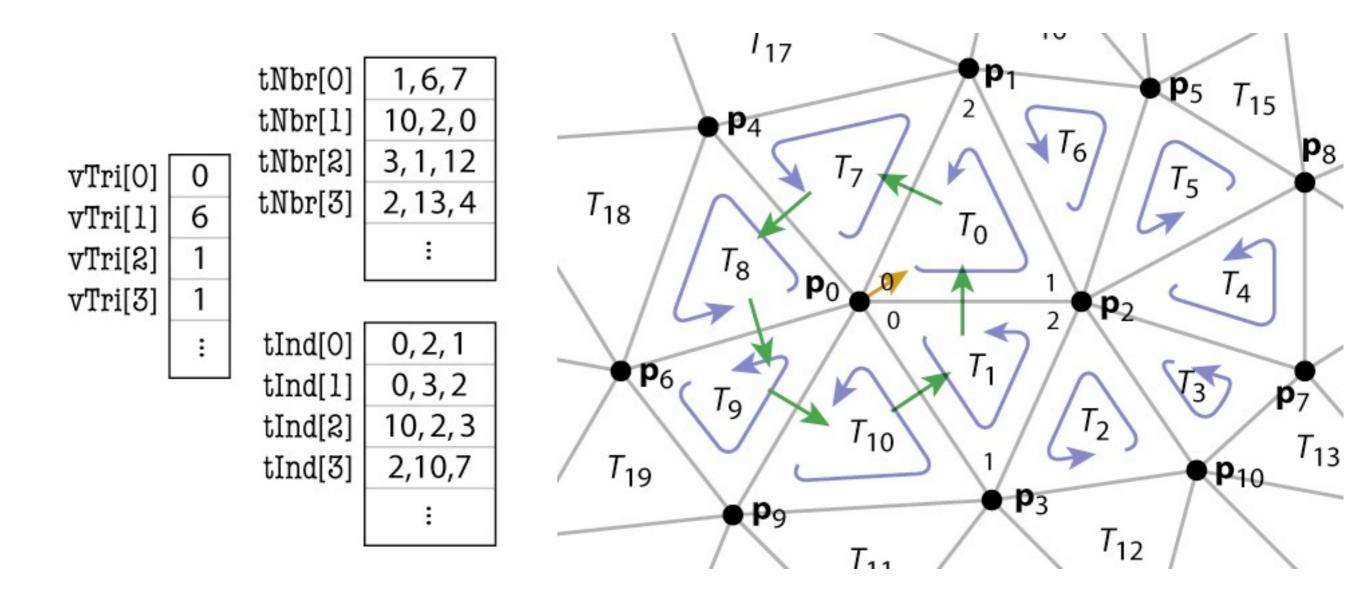
most of these ops. required to implement edge-collapse-based simplification

- Extension to indexed triangle set
- Triangle points to its three neighboring triangles
- Vertex points to a single neighboring triangle
- Can now enumerate triangles around a vertex



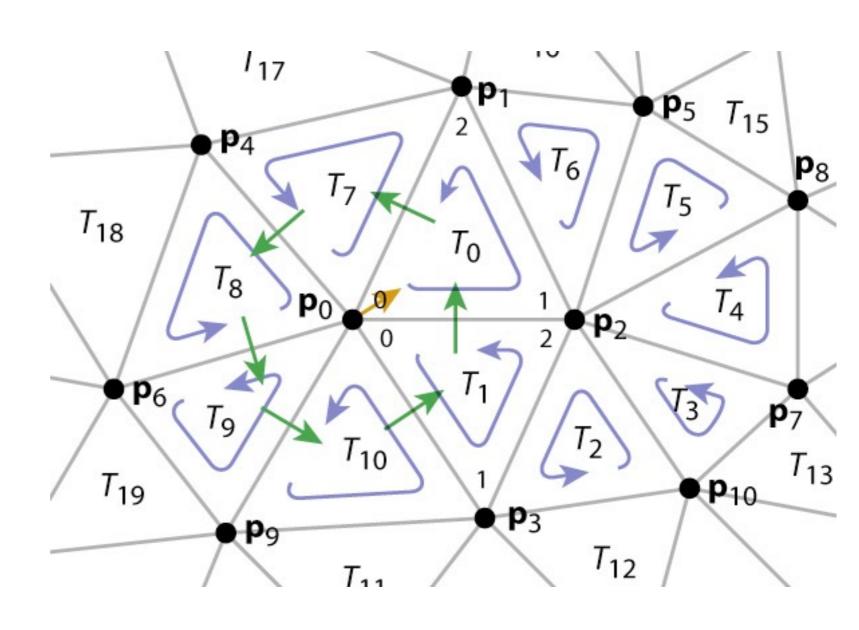
```
Triangle {
 Triangle nbr[3];
  Vertex vertex[3];
// t.neighbor[i] is adjacent
// across the edge from i to i+l
Vertex {
 // ... per-vertex data ...
 Triangle t; // any adjacent tri
// ... or ...
Mesh {
 // ... per-vertex data ...
 int tInd[nt][3]; // vertex indices
 int tNbr[nt][3]; // indices of neighbor triangles
 int vTri[nv]; // index of any adjacent triangle
```





```
TrianglesOfVertex(v) {
    t = v.t;
    do {
        find t.vertex[i] == v;
        t = t.nbr[pred(i)];
        } while (t != v.t);
    }

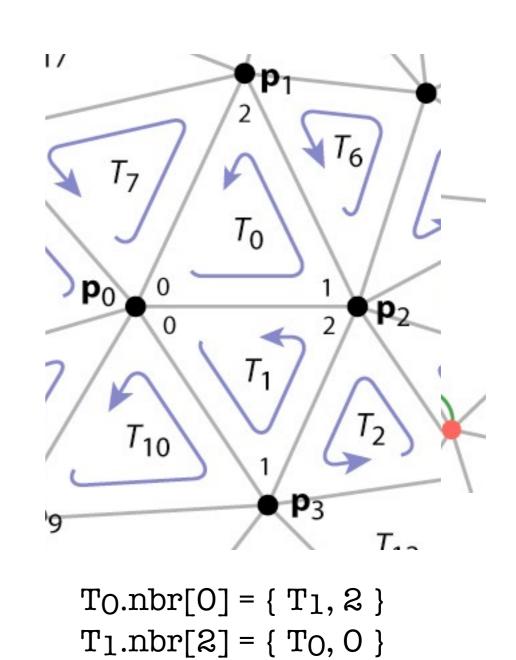
pred(i) = (i+2) % 3;
succ(i) = (i+1) % 3;
```



- indexed mesh was 36 bytes per vertex
- add an array of triples of indices (per triangle)
 - $int[n_T][3]$: about 24 bytes per vertex
 - 2 triangles per vertex (on average)
 - (3 indices x 4 bytes) per triangle
- add an array of representative triangle per vertex
 - $-\inf[n_V]$: 4 bytes per vertex
- total storage: 64 bytes per vertex
 - still not as much as separate triangles

Triangle neighbor structure—refined

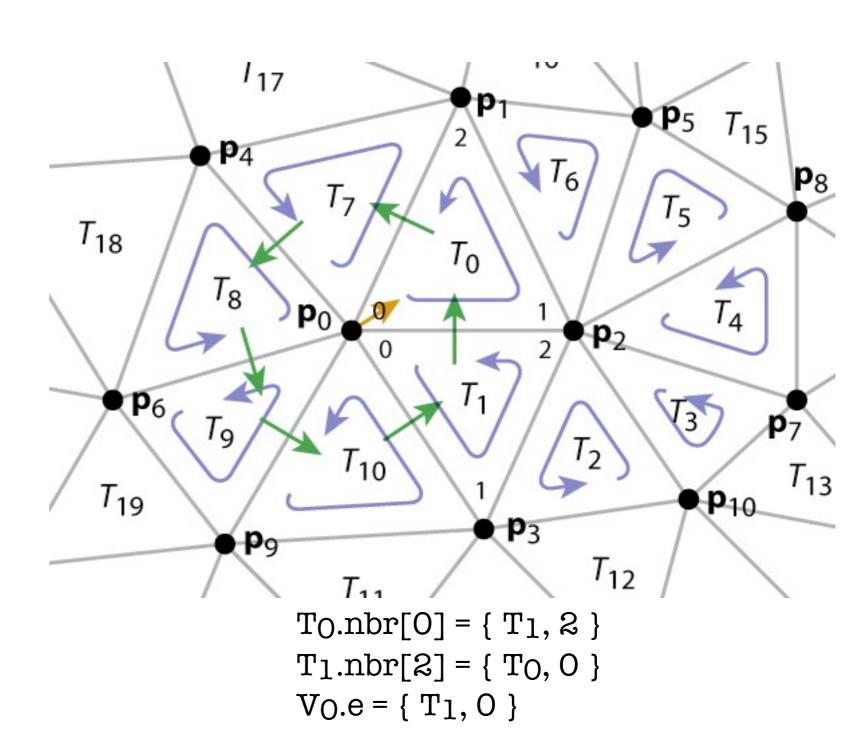
```
Triangle {
  Edge nbr[3];
  Vertex vertex[3];
// if t.nbr[i].i == j
// then t.nbr[i].t.nbr[j].t == t
Edge {
  // the i-th edge of triangle t
  Triangle t;
  int i; // in \{0,1,2\}
  // in practice t and i share 32 bits
Vertex {
  // ... per-vertex data ...
  Edge e; // any edge leaving vertex
```



 $V_0.e = \{ T_1, 0 \}$

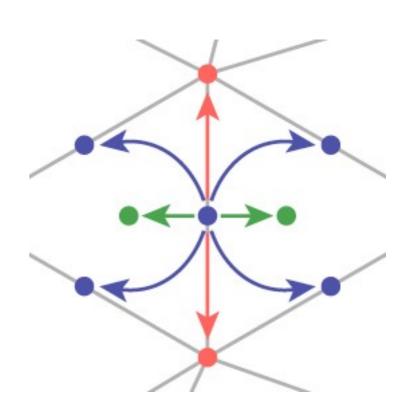
```
TrianglesOfVertex(v) {
    {t, i} = v.e;
    do {
        {t, i} = t.nbr[pred(i)];
      } while (t!= v.t);
    }

pred(i) = (i+2) % 3;
succ(i) = (i+1) % 3;
```



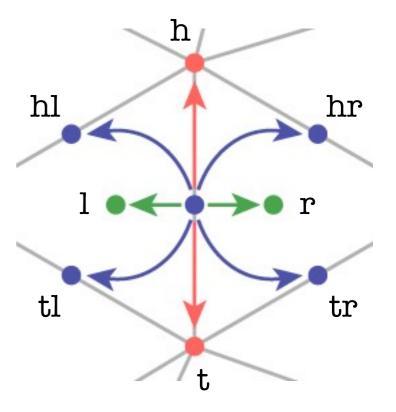
Winged-edge mesh

- Edge-centric rather than face-centric
 - therefore also works for polygon meshes
- Each (oriented) edge points to:
 - left and right forward edges
 - left and right backward edges
 - front and back vertices
 - left and right faces
- Each face or vertex points to one edge



Winged-edge mesh

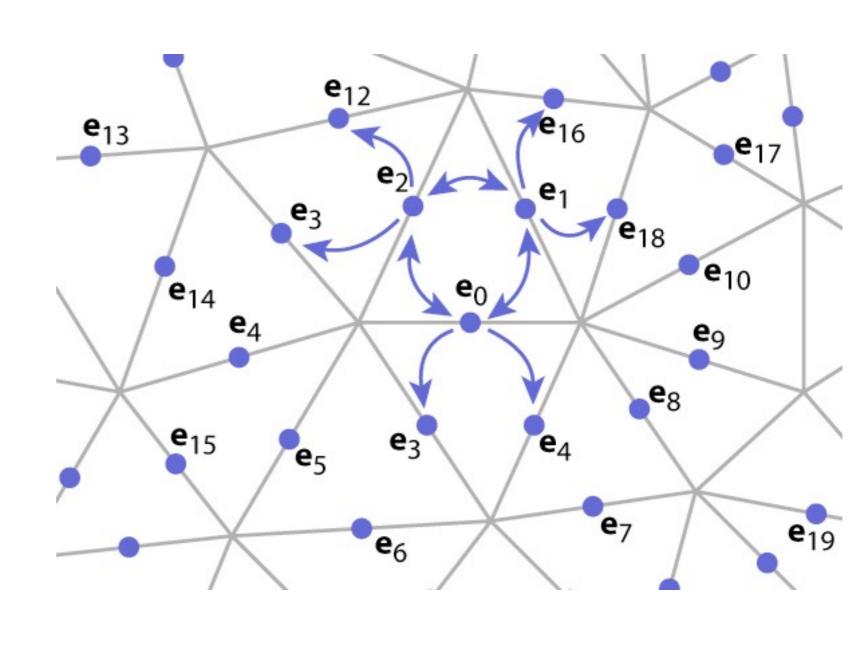
```
Edge {
 Edge hl, hr, tl, tr;
 Vertex h, t;
 Face l, r;
Face {
 // per-face data
 Edge e; // any adjacent edge
Vertex {
 // per-vertex data
 Edge e; // any incident edge
```



Winged-edge structure

```
EdgesOf Verte(x)(v) {
    e = fx.e;;
    do {
        if (e.t = fx))
            e = e.hh;;
        else
            e = e.hr;;
        } while (e != fx.e);;
    }
```

	hl	hr	tl	tr	
edge[O]	1	4	2	3	
edge[1]	18	0	16	2	
edge[0] edge[1] edge[2]	12	1	3	0	
		;			

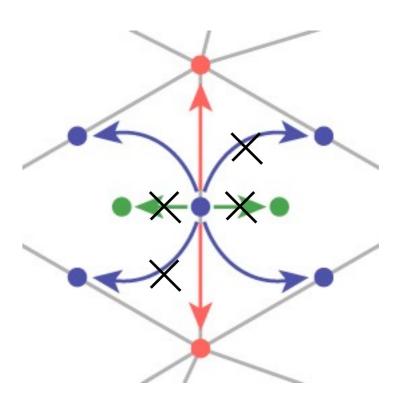


Winged-edge structure

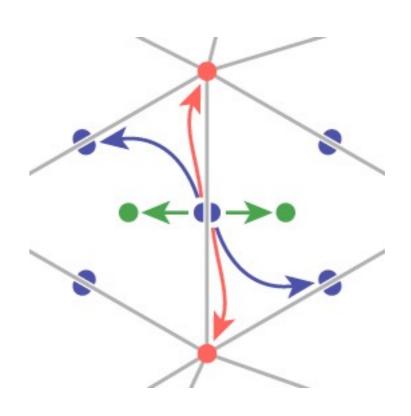
- array of vertex positions: I2 bytes/vert
- array of 8-tuples of indices (per edge)
 - head/tail left/right edges + head/tail verts + left/right tris
 - $int[n_F][8]$: about 96 bytes per vertex
 - 3 edges per vertex (on average)
 - (8 indices x 4 bytes) per edge
- add a representative edge per vertex
 - $-\inf[n_V]$: 4 bytes per vertex
- total storage: I I 2 bytes per vertex
 - but it is cleaner and generalizes to polygon meshes

Winged-edge optimizations

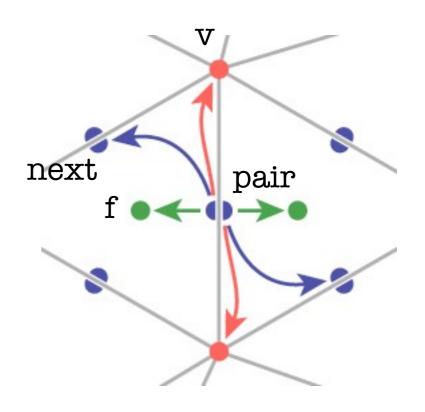
- Omit faces if not needed
- Omit one edge pointer on each side
 - results in one-way traversal



- Simplifies, cleans up winged edge
 - still works for polygon meshes
- Each half-edge points to:
 - next edge (left forward)
 - next vertex (front)
 - the face (left)
 - the opposite half-edge
- Each face or vertex points to one half-edge

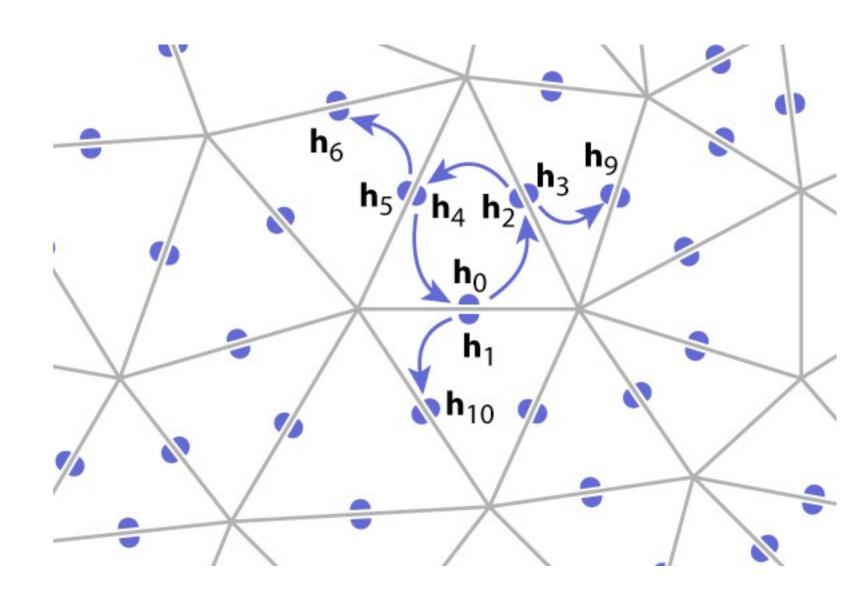


```
HEdge {
 HEdge pair, next;
 Vertex v;
 Face f;
Face {
 // per-face data
 HEdge h; // any adjacent h-edge
Vertex {
 // per-vertex data
 HEdge h; // any incident h-edge
```



```
EdgesOfWarte(x)(v) {
    h = fx.lh;;
    do {
        h = h.next;pair;
    } while (h != fx.lh);;
}
```

	pair	next
hedge[0]	1	2
hedge[1]	0	10
hedge[2]	3	4
hedge[3]	2	9
hedge[4]	5	0
hedge[5]	4	6
	:	



- array of vertex positions: I2 bytes/vert
- array of 4-tuples of indices (per h-edge)
 - next, pair h-edges + head vert + left tri
 - $-\inf[2n_E][4]$: about 96 bytes per vertex
 - 6 h-edges per vertex (on average)
 - (4 indices x 4 bytes) per h-edge
- add a representative h-edge per vertex
 - $-\inf[n_V]$: 4 bytes per vertex
- total storage: I I 2 bytes per vertex

Half-edge optimizations

- Omit faces if not needed
- Use implicit pair pointers
 - they are allocated in pairs
 - they are even and odd in an array
- Result: 2 indices per HEdge
 - HEdges are 48 bytes/vertex
 - total 64 bytes/vertex
 (same as triangle neighbor)

