

# Ray Tracing: shading

## **CS 4620 Lecture 6**

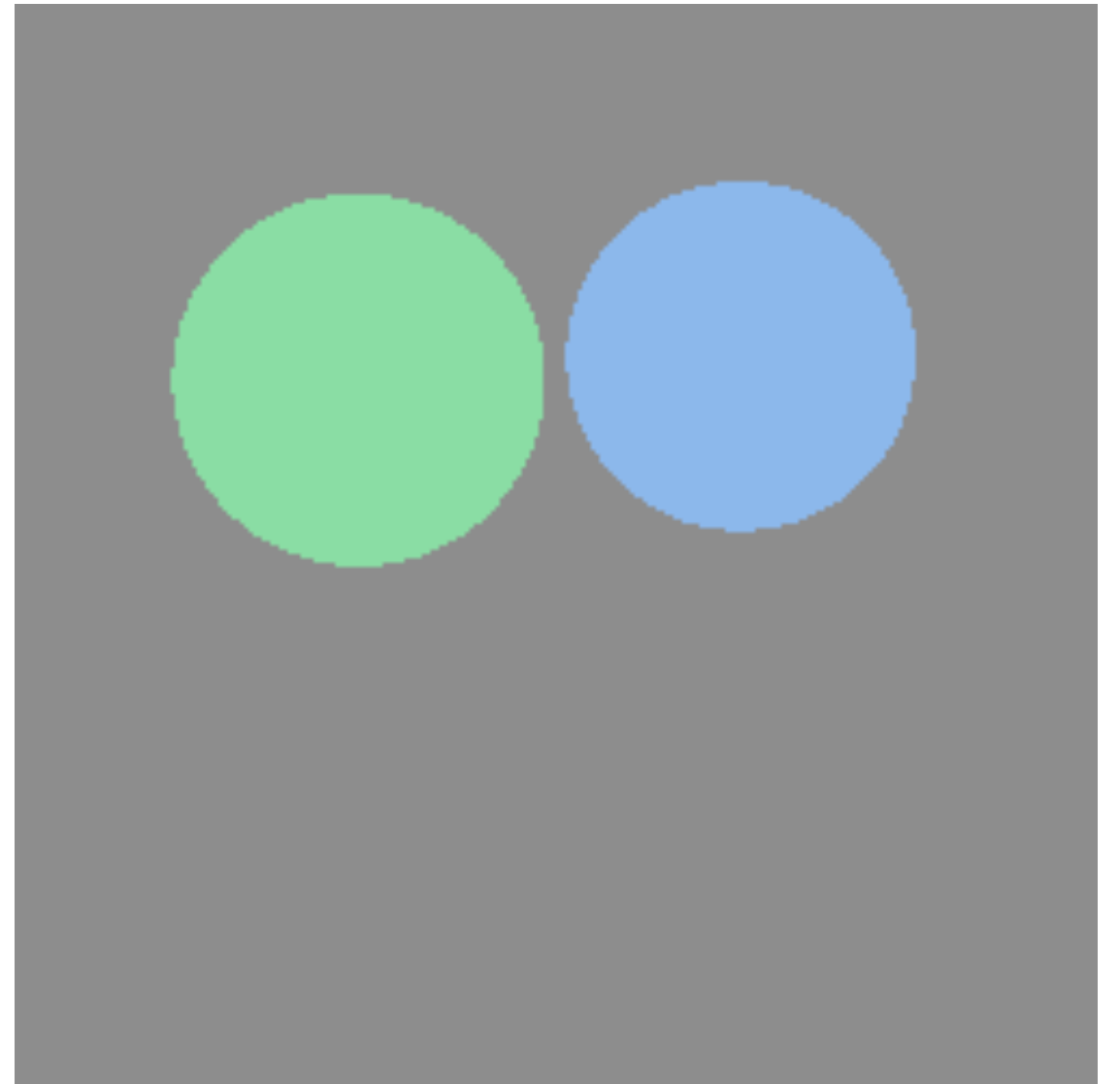
# Image so far

- **With eye ray generation and scene intersection**

```
for 0 <= iy < ny
  for 0 <= ix < nx {
    ray = camera.getRay(ix, iy);
    c = scene.trace(ray, 0, +inf);
    image.set(ix, iy, c);
  }

...

Scene.trace(ray, tMin, tMax) {
  surface, t = surfs.intersect(ray, tMin, tMax);
  if (surface != null) return surface.color();
  else return black;
}
```

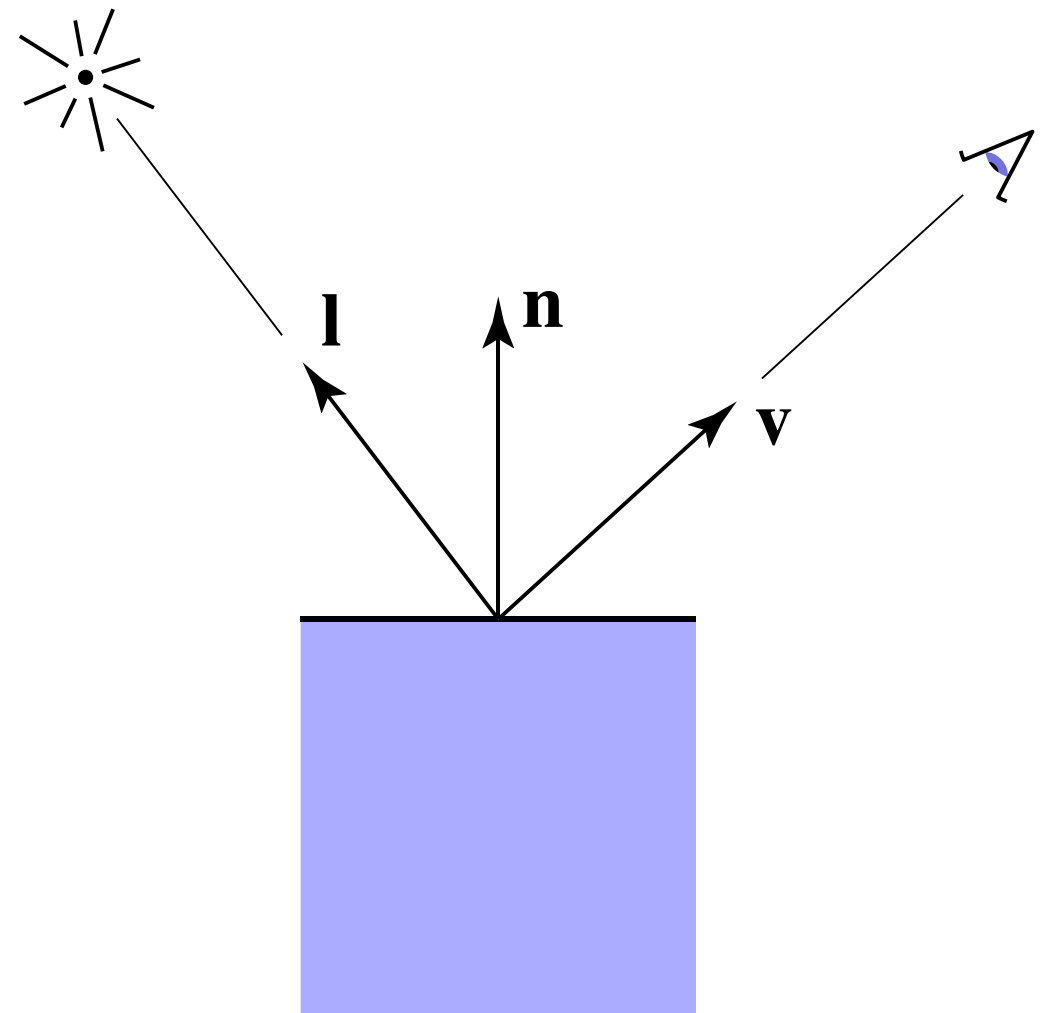


# Shading

- **Compute light reflected toward camera**

- **Inputs:**

- eye direction
- light direction  
(for each of many lights)
- surface normal
- surface parameters  
(color, roughness, ...)



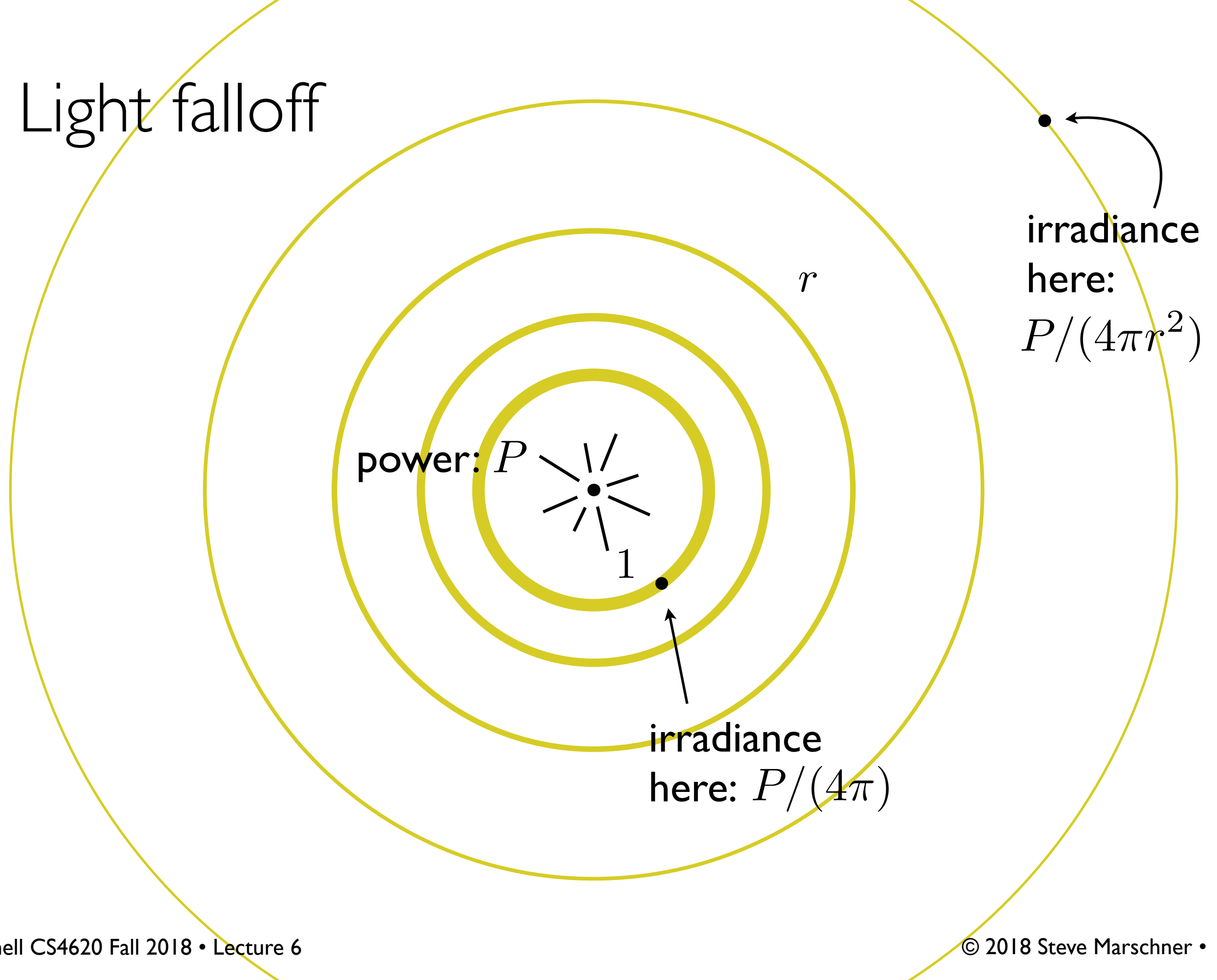
# Shading philosophy

- **Goals of shading depend on purpose of image**
  - visualization, CAD: maximize visual clarity
  - visual effects, advertising: maximize resemblance to reality
  - animation, games: somewhere in between
- **Basic starting point: physics of light reflection**
  - a set of useful approximations to real surfaces
  - can remove things for simplicity/clarity
  - can add things for increased accuracy/realism

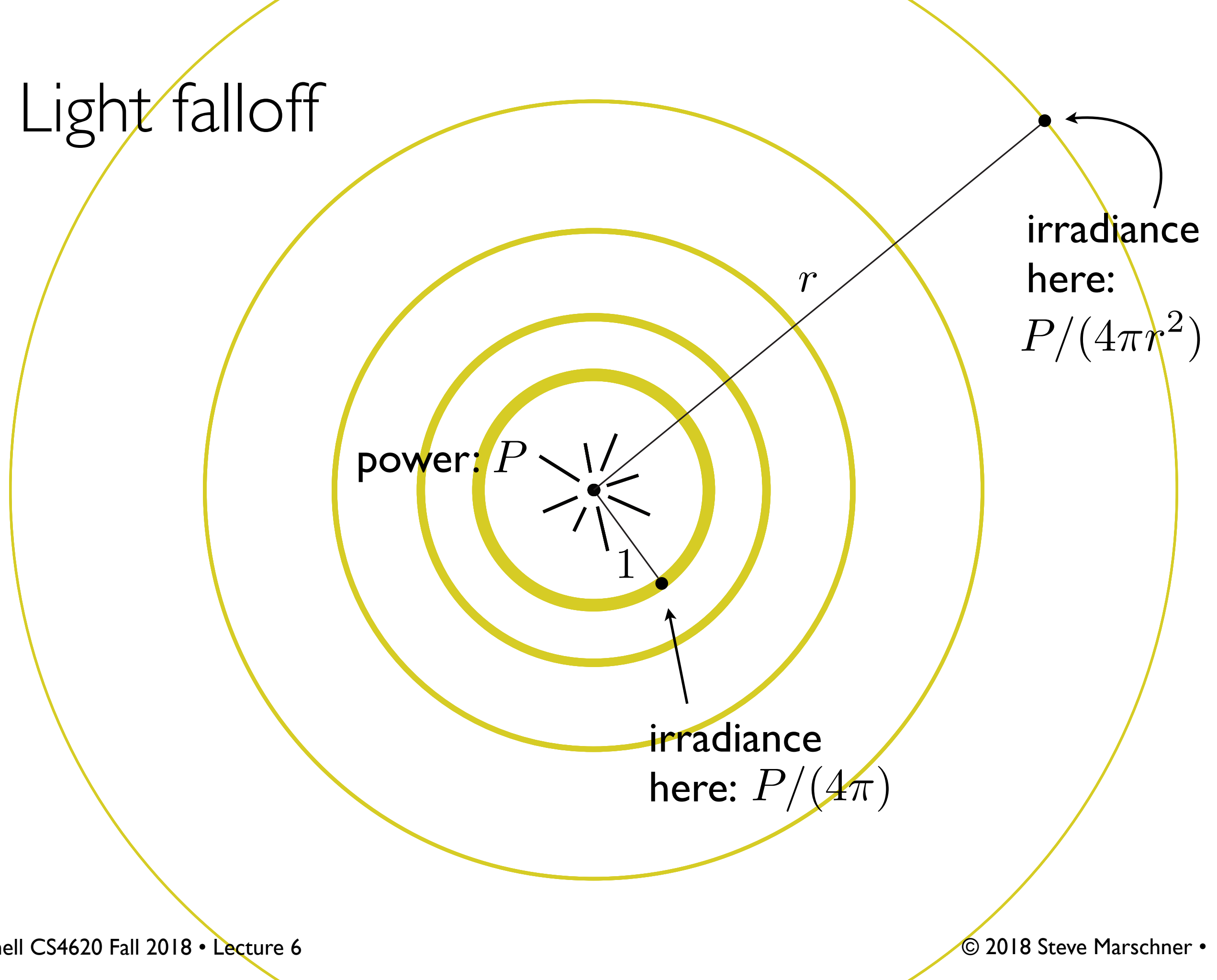
# Light

- **Think of light as a flow of particles through space**
  - disregarding wave nature: polarization, interference, diffraction
  - for now disregarding color: only how much light
- **Sources of light**
  - point sources (a flashlight) ← we will stick to this for now.
  - directional sources (the sun)
  - area sources (a fluorescent tube)
  - environment sources (the sky)

# Light falloff



# Light falloff



# Irradiance from isotropic point source

- **A sphere surrounding the source receives all the power**
- **A small, flat surface of area  $A$  facing the source receives a fraction (area of surface) / (area of sphere) of that power:**

$$P_A = P \frac{A}{4\pi r^2}$$

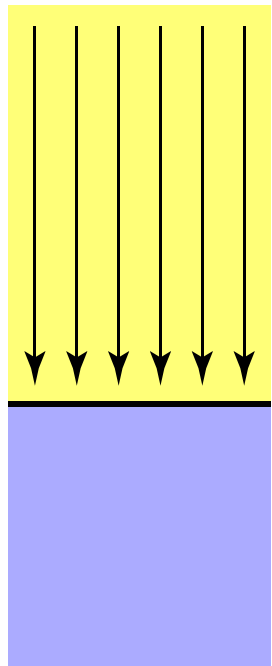
- **Irradiance is power per unit area:**

$$E = P_A / A = \frac{P}{4\pi r^2} = \frac{P}{4\pi} \frac{1}{r^2}$$

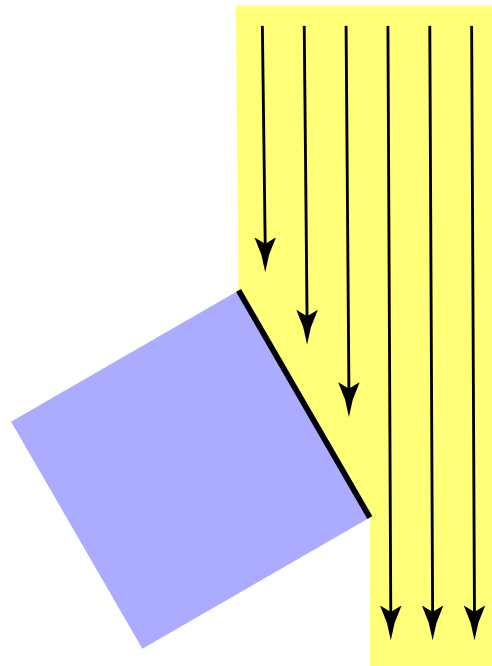
↑      ↑  
intensity   geometry factor



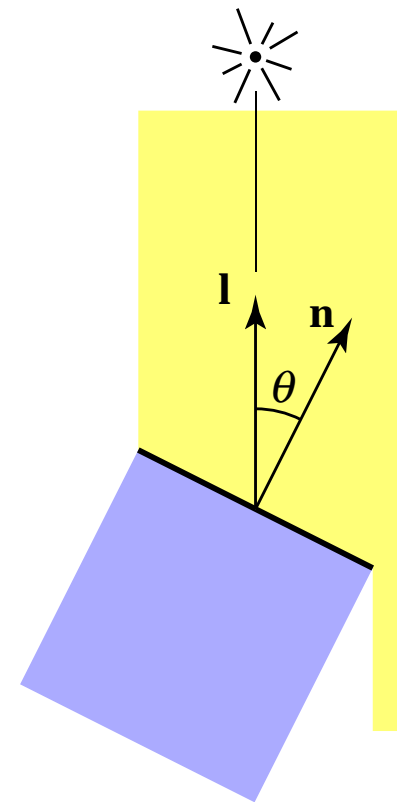
# Lambert's cosine law



Top face of cube  
receives a certain  
amount of light



Top face of  
60° rotated cube  
intercepts half the light



In general, light per unit  
area is proportional to  
 $\cos \theta = \mathbf{l} \cdot \mathbf{n}$

# Irradiance from isotropic point source

- **A surface of area  $A$  facing at an angle to the source receives a factor of  $\cos \theta$  less light:**

$$P_A = P \frac{A \cos \theta}{4\pi r^2}$$

- **Irradiance is power per unit area:**

$$E = P_A / A = \frac{P}{4\pi} \frac{\cos \theta}{r^2}$$

↑  
intensity

↑  
geometry factor

# Diffuse reflection

- **Simplest reflection model**
- **Reflected light is independent of view direction**
- **Reflected light is proportional to irradiance**
  - constant of proportionality is the diffuse reflection coefficient

$$L_d = k_d E$$

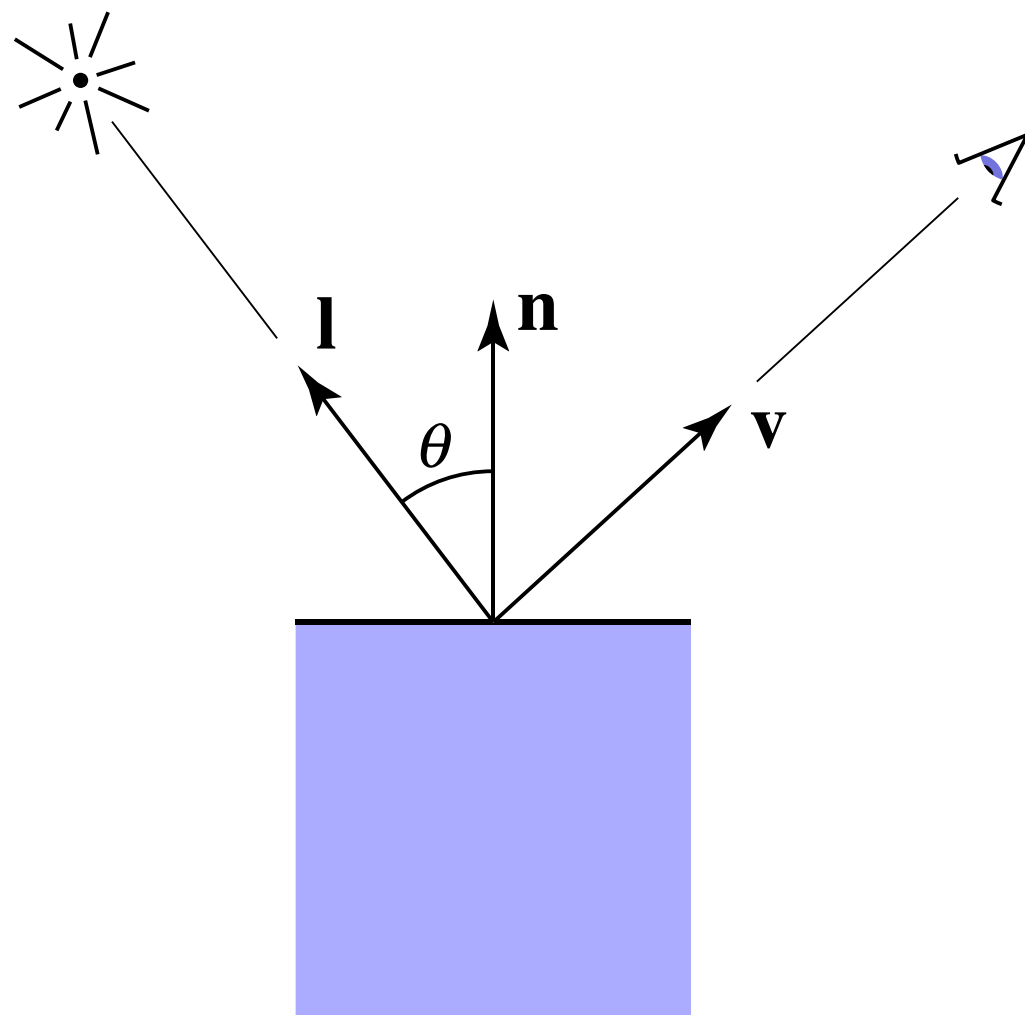
- **More useful to think in terms of reflectance**
  - reflectance is the fraction reflected (between 0 and 1)

$$L_d = \frac{R_d}{\pi} E$$

- will have to explain the factor of pi later

# Lambertian shading

- **Shading independent of view direction**



irradiance from source

diffuse reflectance

$$L_d = \frac{R}{\pi} \frac{\max(0, \mathbf{n} \cdot \mathbf{l})}{r^2} I$$

diffusely reflected radiance

diffuse coefficient

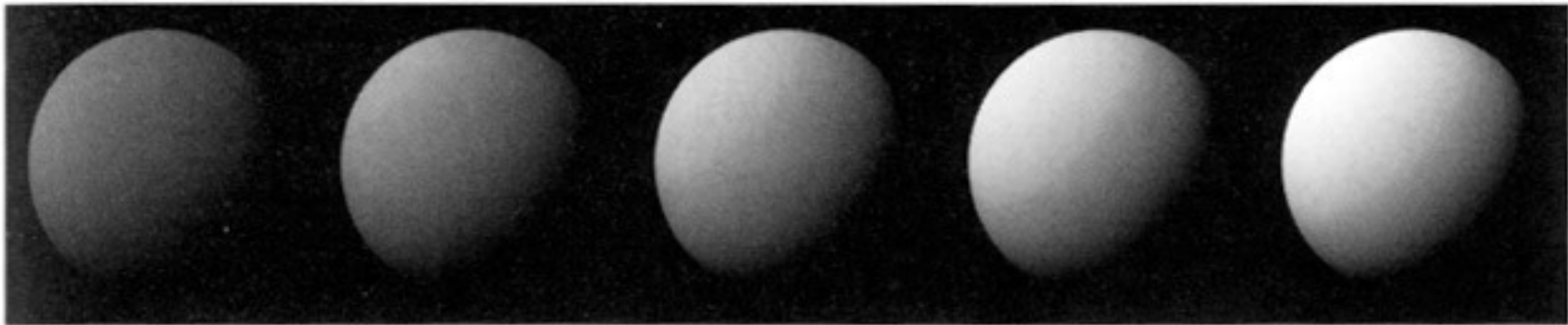
distance to source

intensity of source

The diagram shows the derivation of the Lambertian shading equation. It starts with the irradiance from the source, which is the intensity of the source  $I$  divided by the square of the distance to the source  $r^2$ . This is then multiplied by the diffuse reflectance  $R$  and the cosine of the angle between the normal and the light direction,  $\max(0, \mathbf{n} \cdot \mathbf{l})$ . The result is the diffusely reflected radiance  $L_d$ , which is divided by  $\pi$  to account for the Lambertian distribution of the reflected light.

# Lambertian shading

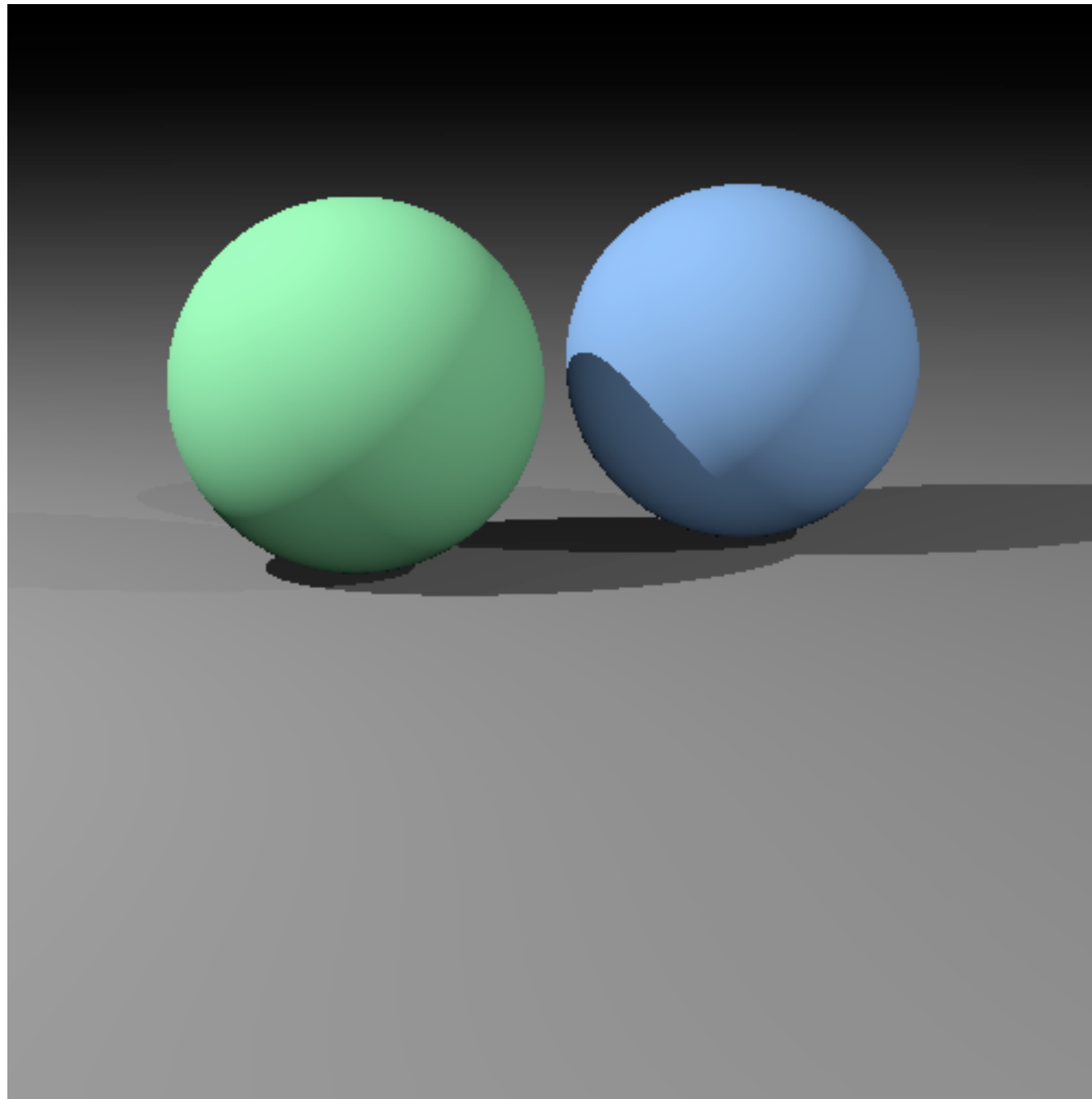
- **Produces matte appearance**



$k_d \longrightarrow$

[Foley et al.]

# Diffuse shading

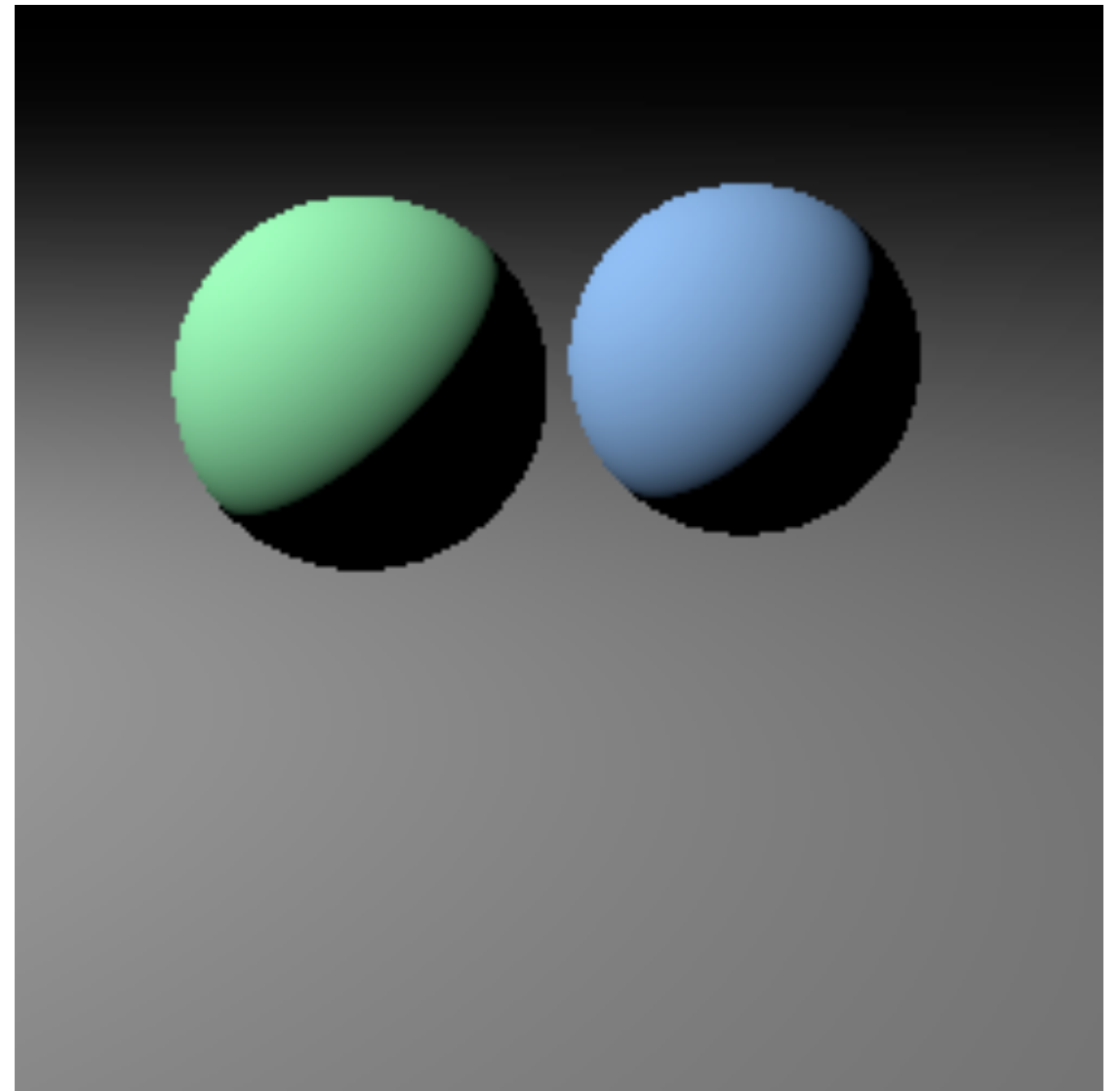


# Image so far

```
Scene.trace(Ray ray, tMin, tMax) {  
    surface, t = hit(ray, tMin, tMax);  
    if surface is not null {  
        point = ray.evaluate(t);  
        normal = surface.getNormal(point);  
        return surface.shade(ray, point,  
                               normal, light);  
    }  
    else return backgroundColor;  
}
```

...

```
Surface.shade(ray, point, normal, light) {  
    v = -normalize(ray.direction);  
    l = normalize(light.pos - point);  
    // compute shading  
}
```



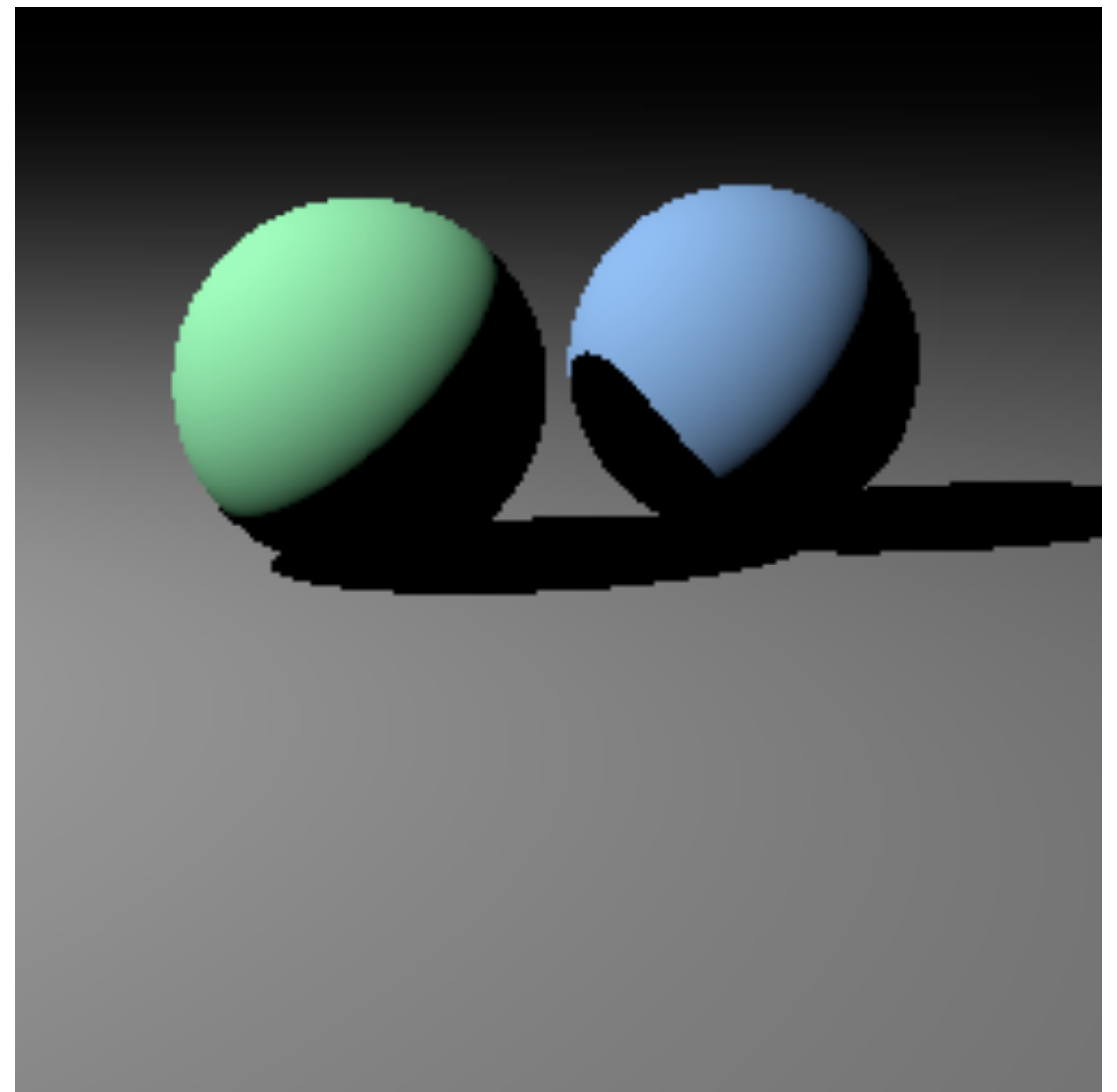
# Shadows

- **Surface is only illuminated if nothing blocks the light**
  - i.e. if the surface can “see” the light
- **With ray tracing it’s easy to check**
  - just intersect a ray with the scene!



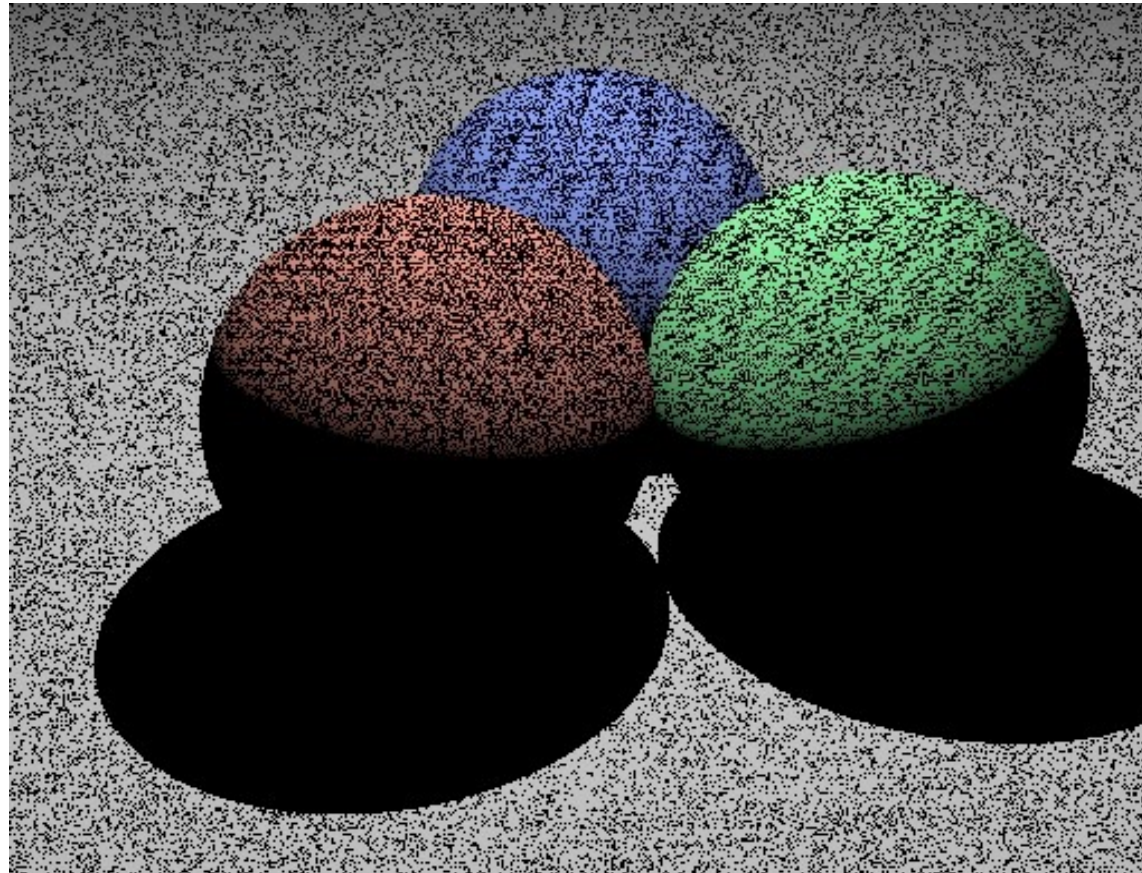
# Image so far

```
Surface.shade(ray, point, normal, light) {  
    shadRay = (point, light.pos - point);  
    if (shadRay not blocked) {  
        v = -normalize(ray.direction);  
        l = normalize(light.pos - point);  
        // compute shading  
    }  
    return black;  
}
```



# Shadow rounding errors

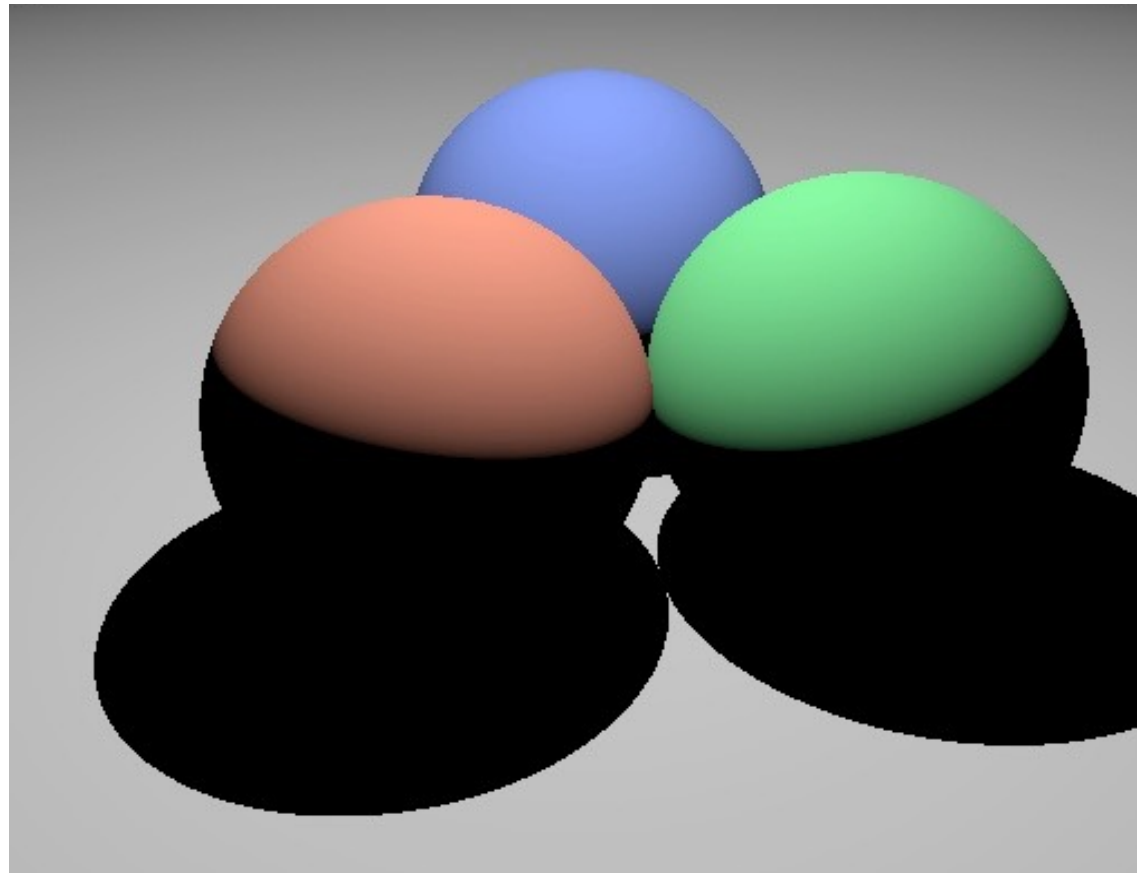
- **Don't fall victim to one of the classic blunders:**



- **What's going on?**
  - hint: at what  $t$  does the shadow ray intersect the surface you're shading?

# Shadow rounding errors

- **Solution: shadow rays start a tiny distance from the surface**



- **Do this by moving the start point, or by limiting the  $t$  range**

# Multiple lights

- **Important to fill in black shadows**
- **Just loop over lights, add contributions**
- **Ambient shading**
  - black shadows are not really right
  - one solution: dim light at camera
  - alternative: add a constant “ambient” color to the shading...

# Image so far

```
shade(ray, point, normal, lights) {  
    result = ambient;  
    for light in lights {  
        if (shadow ray not blocked) {  
            result += shading contribution;  
        }  
    }  
    return result;  
}
```

