

05 Mesh Animation

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Basic surface deformation methods

Blend shapes: make a mesh by combining several meshes

Mesh skinning: deform a mesh based on an underlying skeleton

Both use simple linear algebra

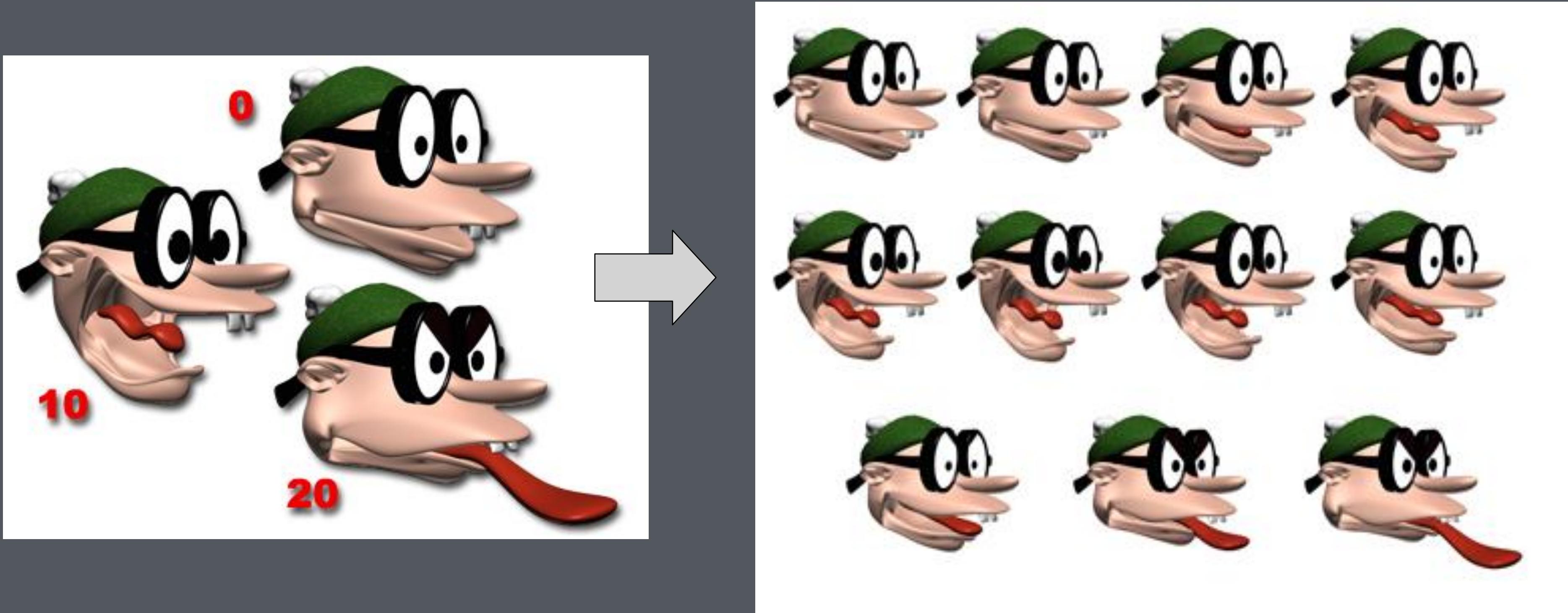
- Easy to implement—first thing to try
- Fast to run—used in games

The simplest tools in the offline animation toolbox

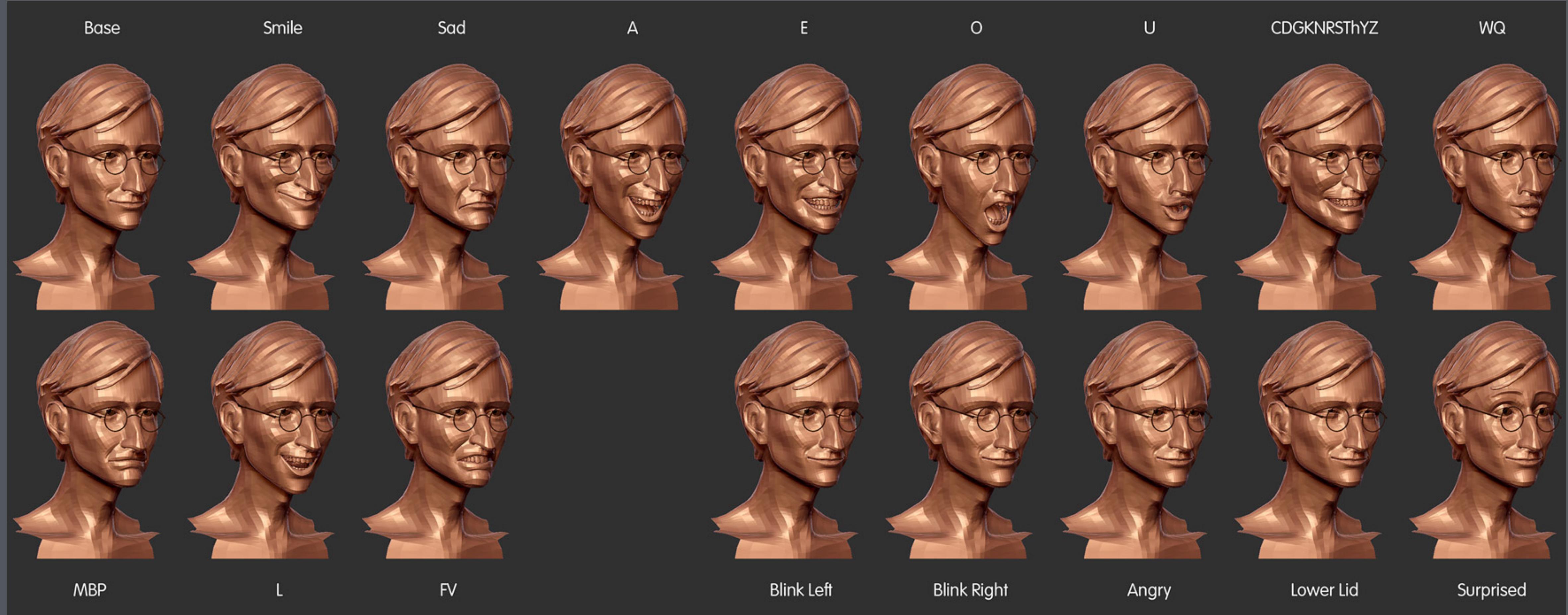
Blend shapes

Simply interpolate linearly among several key poses

- Aka. blend shapes or morph targets



Blend shapes



Blend shapes math

Simple setup

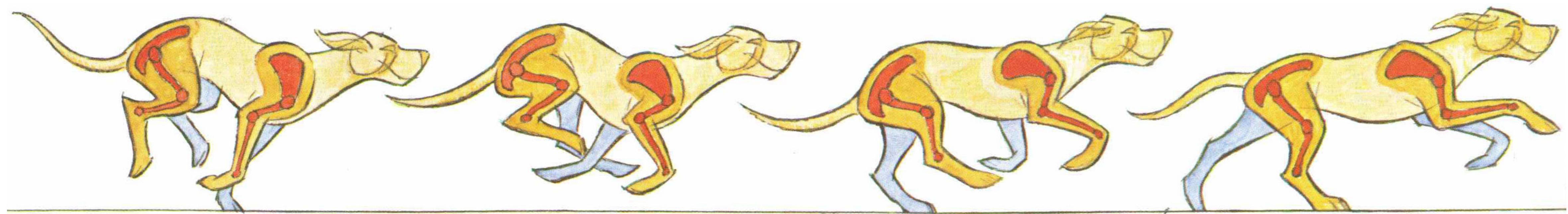
- User provides key shapes: a position for every control point in every shape
 - p_{ij} for point i , shape j
- Per frame: user provides a weight w_j for each key shape
 - Must sum to 1.0

Computation of deformed shape

$$\mathbf{p}'_i = \sum_j w_j \mathbf{p}_{ij}$$

Works well for relatively small motions

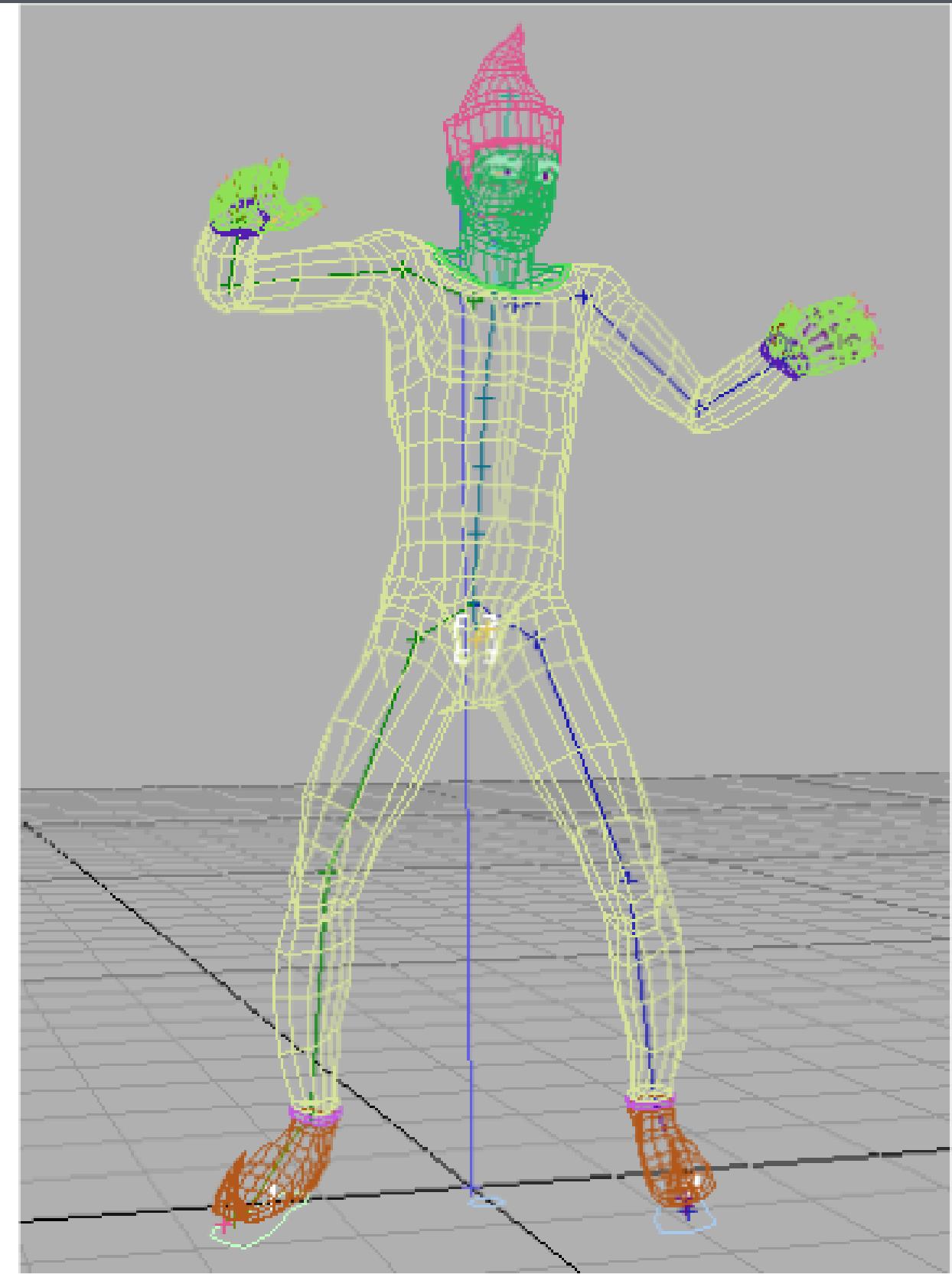
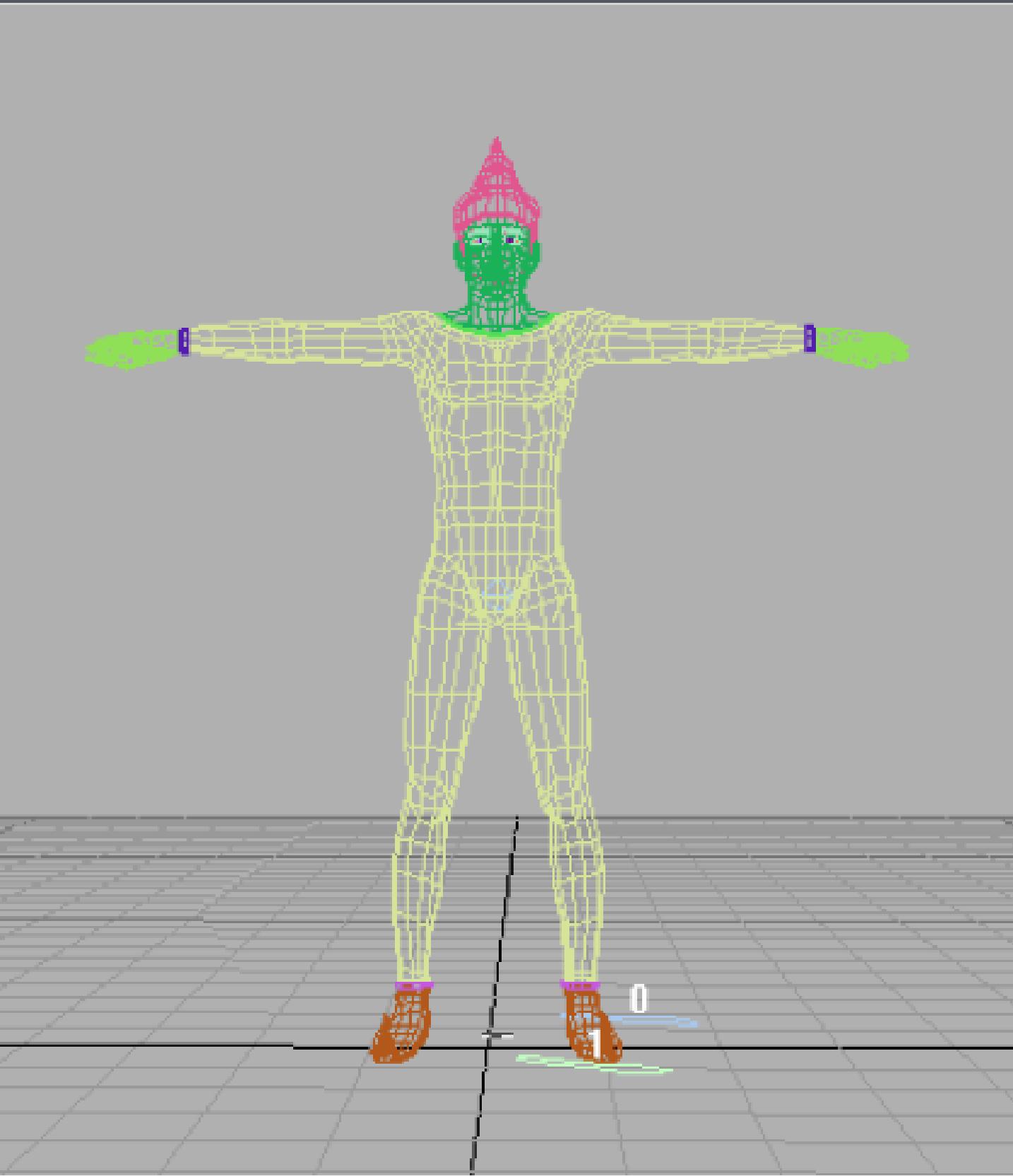
- Often used for facial animation
- Runs in real time; popular for games



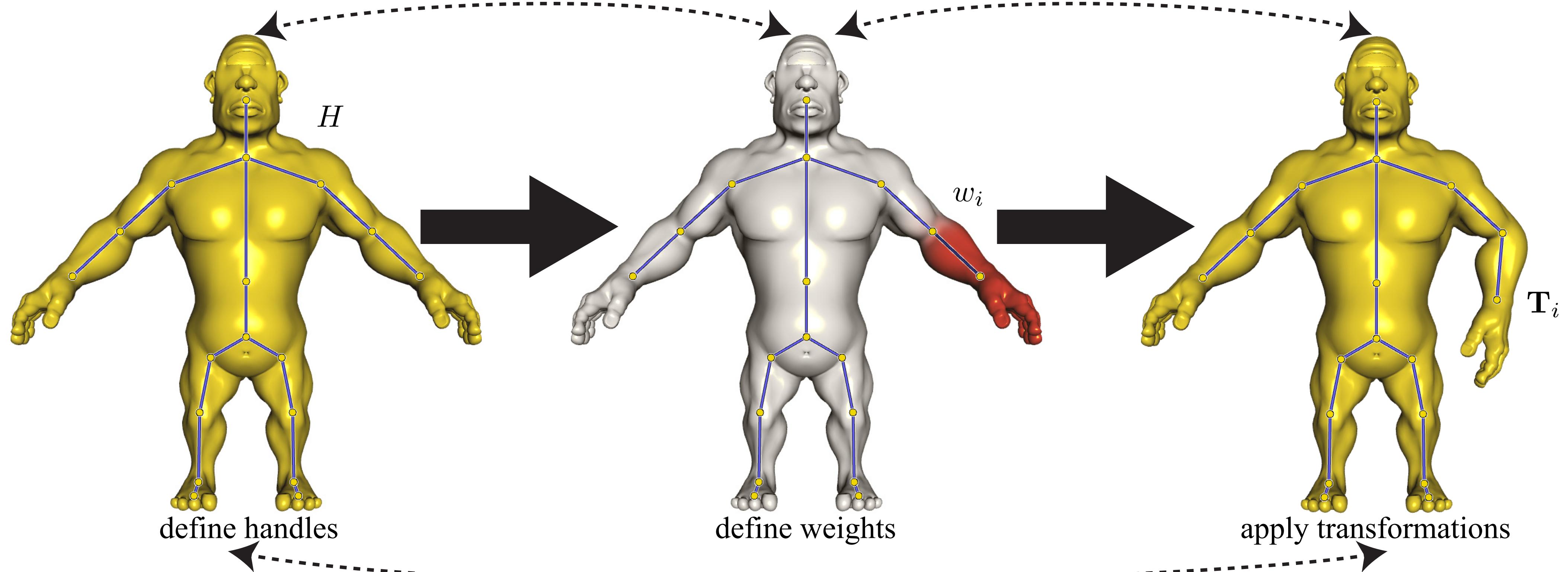
P. Blair, *Cartoon Animation*.

Mesh skinning

A simple way to deform a surface to follow a skeleton



[Sébastien Dominié | NVIDIA]



Mesh skinning math: setup

Surface has control points p_i

- Triangle vertices, spline control points, subdiv base vertices

Each bone has a transformation matrix M_j

- Normally a rigid motion

Every point–bone pair has a weight w_{ij}

- In practice only nonzero for small # of nearby bones
- The weights are provided by the user

Points are transformed by a blended transformation

- Various ways to blend exist

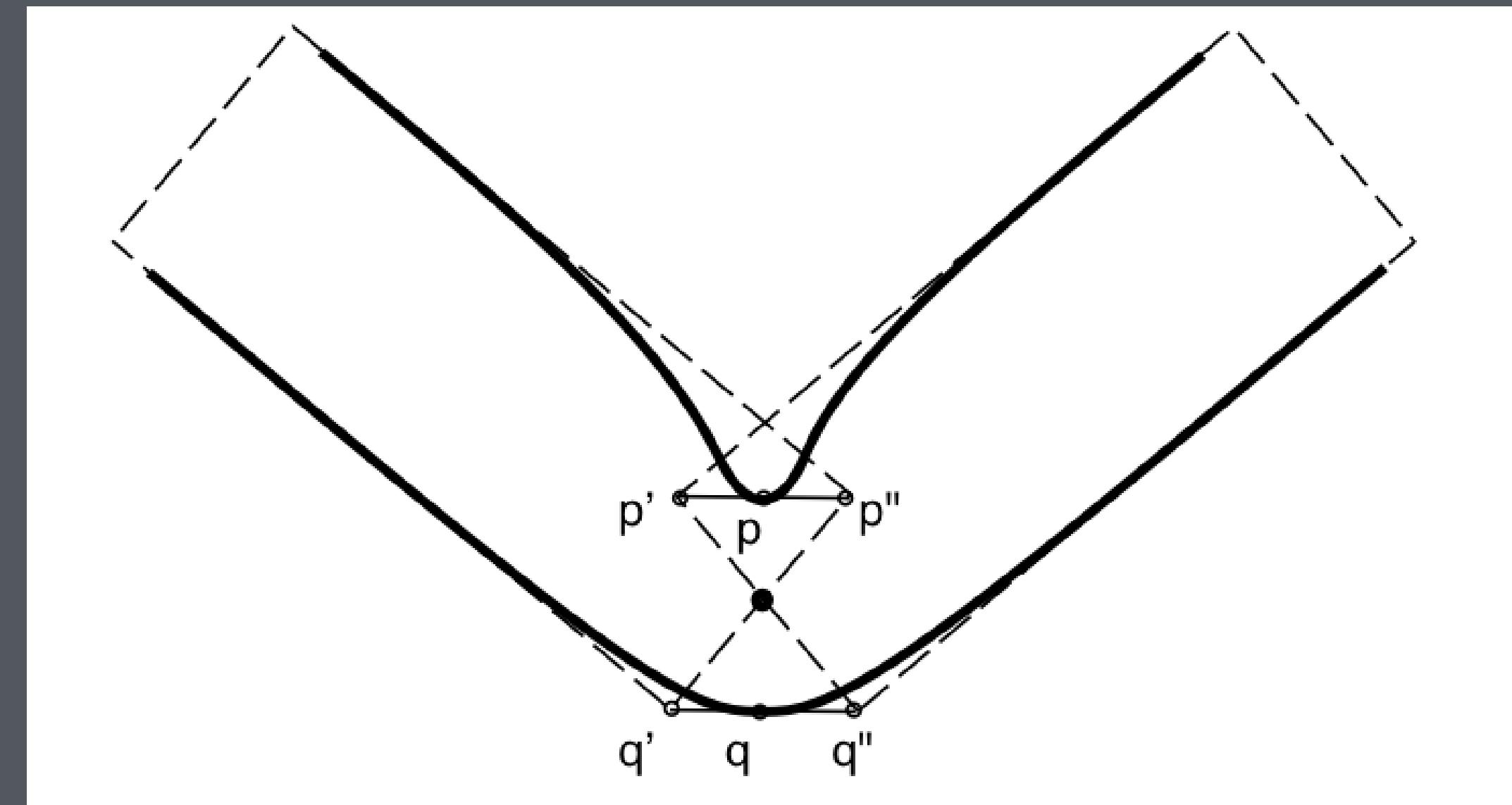
Linear blend skinning

Simplest mesh skinning method

Deformed position of a point is a weighted sum

- of the positions determined by each bone's transform alone
- weighted by that vertex's weight for that bone

$$\begin{aligned} \mathbf{p}'_i &= \sum_j w_{ij} M_j \mathbf{p}_i \\ &= \left(\sum_j w_{ij} M_j \right) \mathbf{p}_i \end{aligned}$$



[Lewis et al. SIGGRAPH 2000]

Linear blend skinning

Simple and fast to compute

- Can easily compute in a vertex shader

Used heavily in games

Has some issues with deformation quality

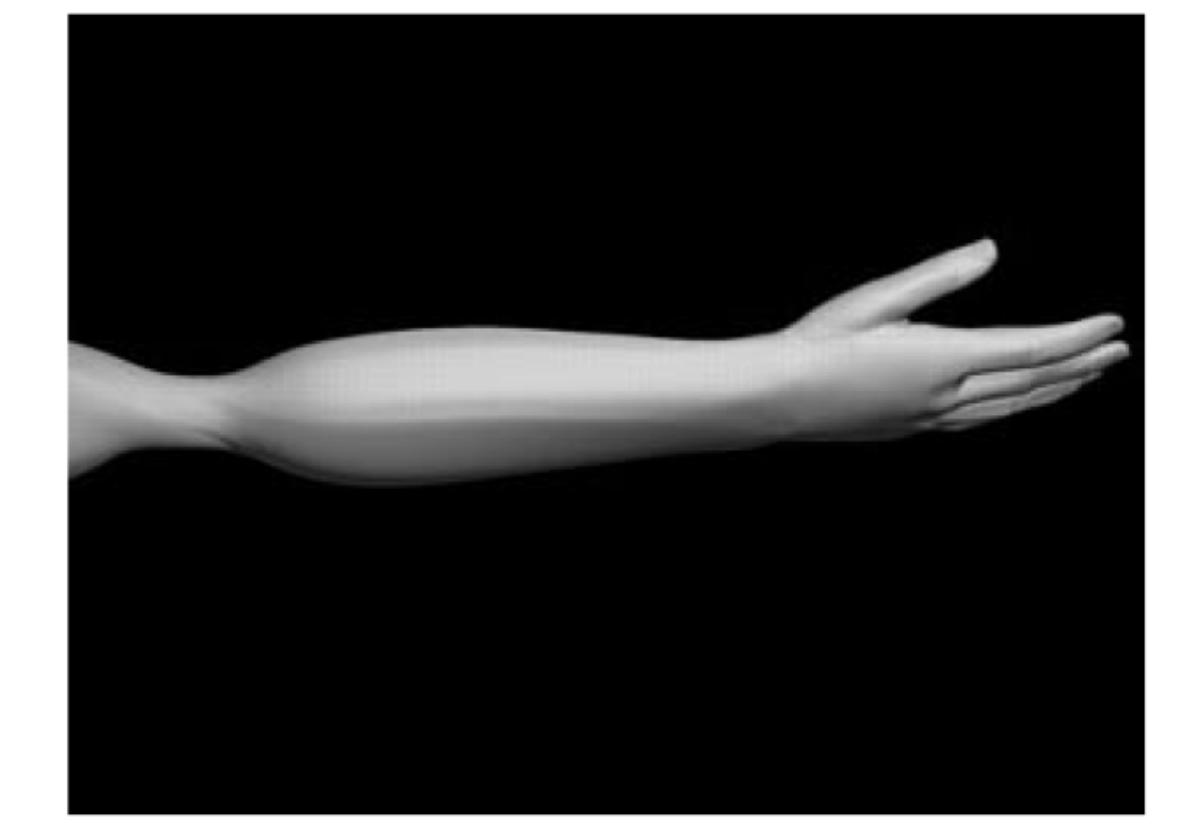
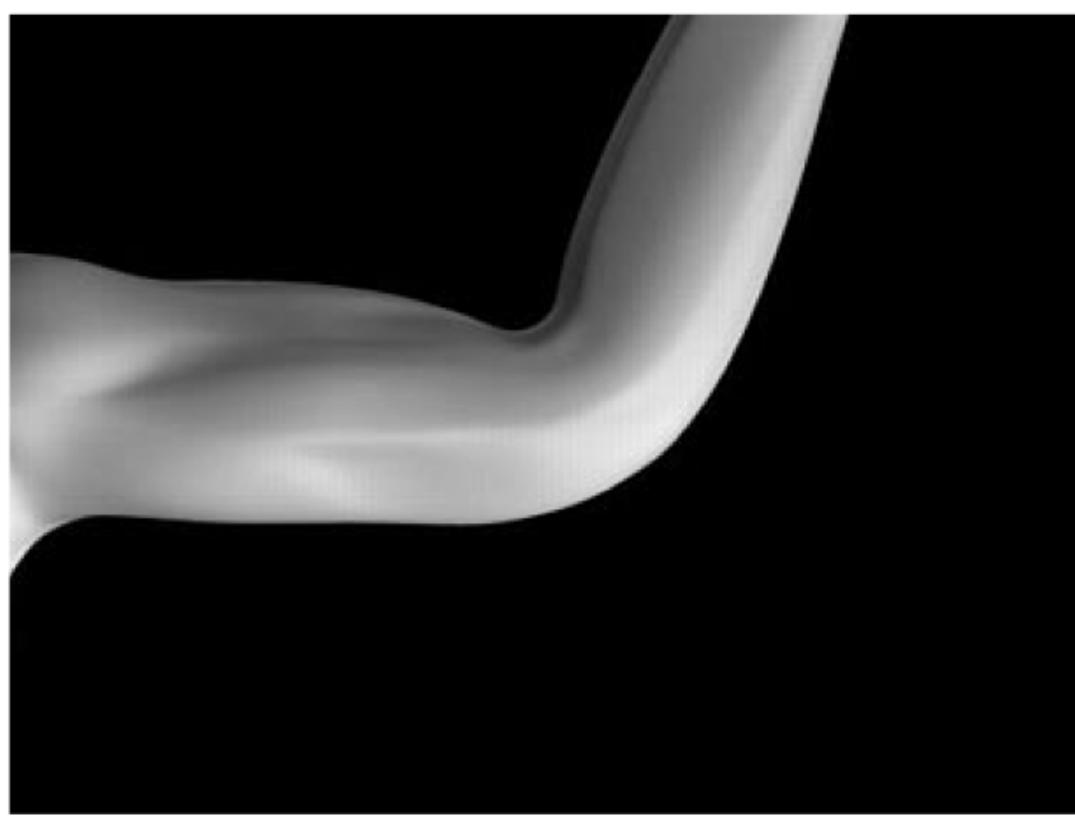
- Watch near joints between very different transforms

Linear skinning: classic problems

Surface collapses on the inside of bends and in the presence of strong twists

- Average of two rotations is not a rotation!

[Lewis et al. SG'00]



[Mohr & Gleicher SG'03]



Dual quaternion skinning

Root problem of LBS artifacts: linear blend of rigid motions is not rigid

Blending quaternions is better

- proper spherical interpolation is hard with multiple weights
- just blending and renormalizing works OK

However, blending rotation and rotation center separately performs poorly



[Kavan et al. SG '08]

Figure 6: Artifacts produced by blending rotations with respect to the origin (left) are even worse than those of linear blend skinning (right).

Dual quaternions

Combines quaternions ($1, i, j, k$) with dual numbers ($1, \epsilon$)

- resulting system has 8 dimensions: $1, i, j, k, \epsilon, \epsilon i, \epsilon j, \epsilon k$
- write it as sum of two quaternions: $\hat{q} = q_0 + \epsilon q_\epsilon$

Unit dual quaternions

- inherits quaternion constraint: $\|q_0\| = 1$
- adds one more constraint: $q_0 \cdot q_\epsilon = 0$
- a 6D manifold embedded in 8D
- represents rigid motions with nice properties

Skinning by blending dual quaternions works well

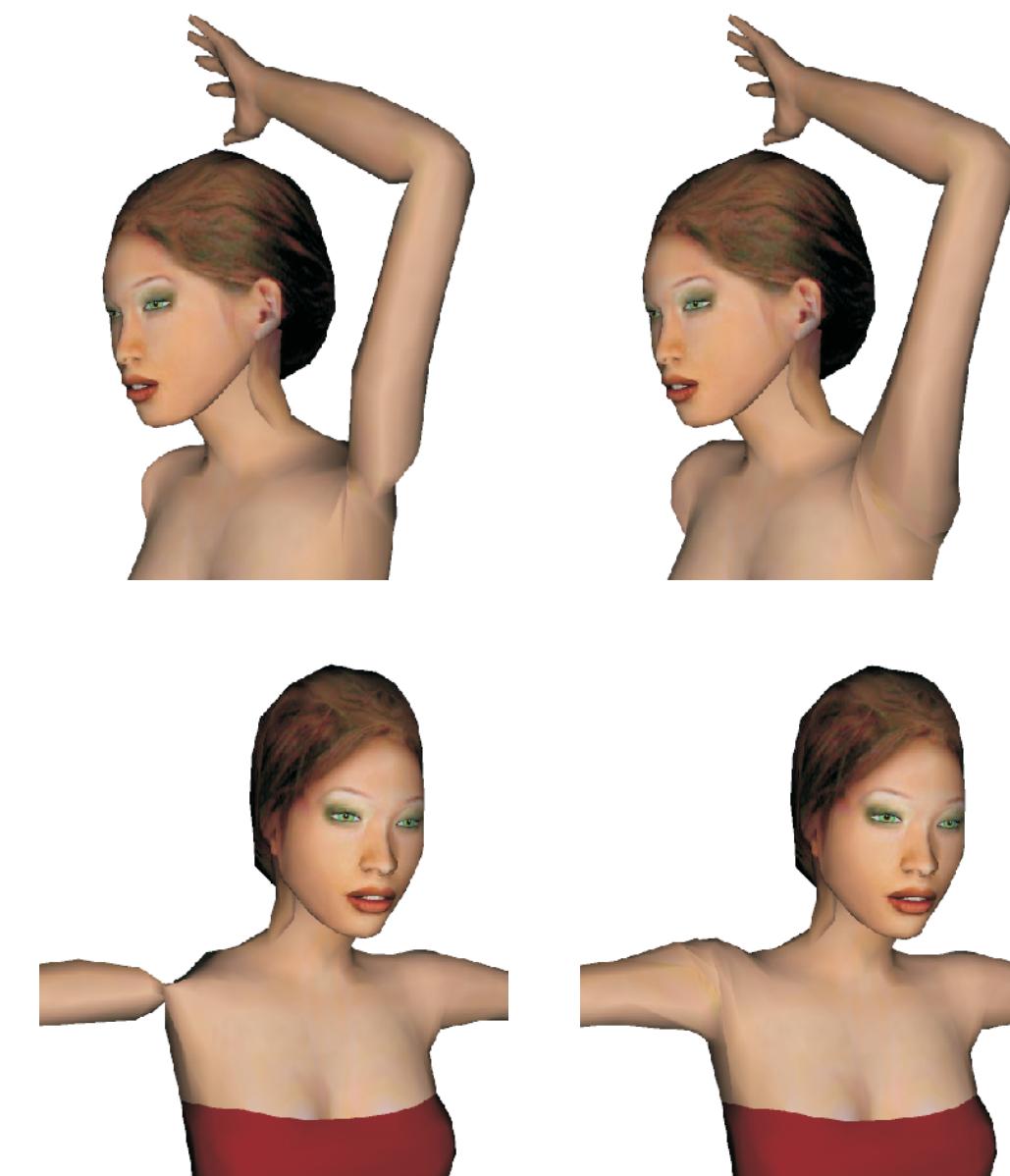
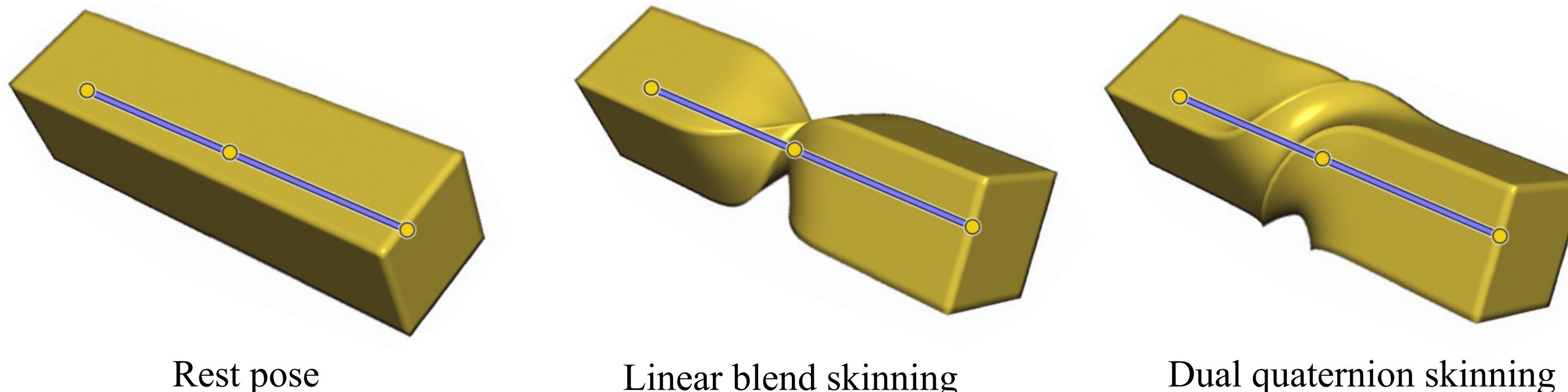


Figure 14: Comparison of linear (left) and dual quaternion (right) blending. Dual quaternions preserve rigidity of input transformations and therefore avoid skin collapsing artifacts.

[Kavan et al. SG '08]



[Kavan, SG'14 course]