

LAB 2 : Inverse Kinematic

Soulaïman Marsou

For this lab, I could not apply the Pieper's solution for my robot. The last 3 joints have not one common intersection.

I chose to use the manipulator M-10iA, which was already ready in the file “/Manipulator5_upute_rjesenje/LV1_manipulator5.py”.

Preparation : Computation of the Piper's solution.

The equation (4,15) gives us θ_3 :

$$\theta_3 = \arcsin((x^2 + y^2 + z^2 - d_4^2 - a_2^2) / (2*a_2*d_4))$$

We compute g_1 by using $x^2 + y^2$:

$$g_1^2 = x^2 + y^2$$

The equations (4,3) and (4,4) give us a system of equation to get **sin(θ_2)** and **cos(θ_2)** :

$$\theta_2 = \arctan2(\sin(\theta_2), \cos(\theta_2))$$

And for θ_1 , we use (4,1) and (4,2) :

$$\theta_1 = \arctan2(x/g_1, y/g_1)$$

Then we compute the matrix R_{63} =

$c_4*c_5*c_6 - s_4*s_6$	$- c_4*c_5*s_6 - s_4*c_6$	c_4*s_5
$s_4*c_5*c_6 + c_4*s_6$	$- s_4*c_5*s_6 + c_4*c_6$	s_4*s_5
$-s_5*c_6$	s_5*s_6	c_5

We finally get the values of the real R_{63} computed for our own robot and we have :

$$\theta_5 = \arccos(r_{33})$$

$$\theta_4 = \arctan2(r_{23} / s_5, r_{13} / s_5)$$

$$\theta_6 = \arctan2(r_{32} / s_5, - r_{31} / s_5)$$

$$*r_{ij} = R_{63}[i][j]$$

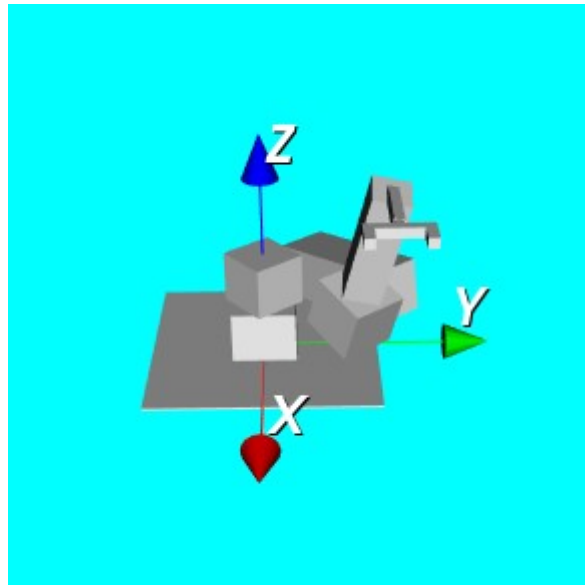
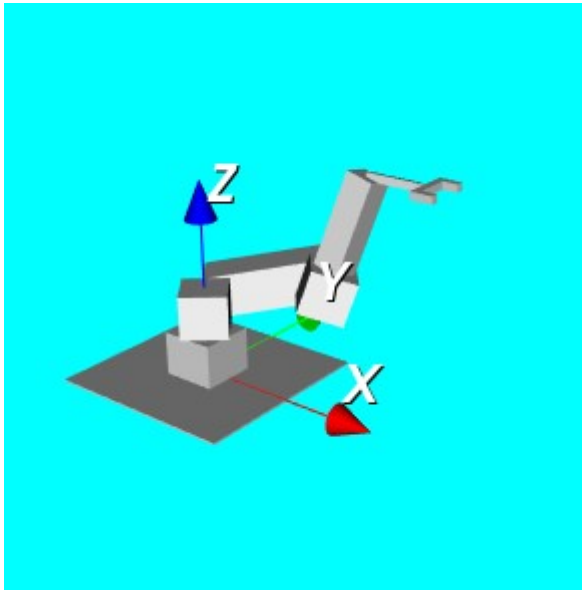
Exercice :

1. Function invik

I used the solution computed in **Preparation** to return the vector **q** of joint variable.
However, in my preparation, I don't find all the solutions, but instead, I only give one possible.
Be aware that in some position wanted, we can miss to find the only solution because of that.

2. Positioning the tool

I positionned the tool at ($x = 100\text{cm}$, $y = 50\text{cm}$, $z = 100\text{cm}$) in the following picture :

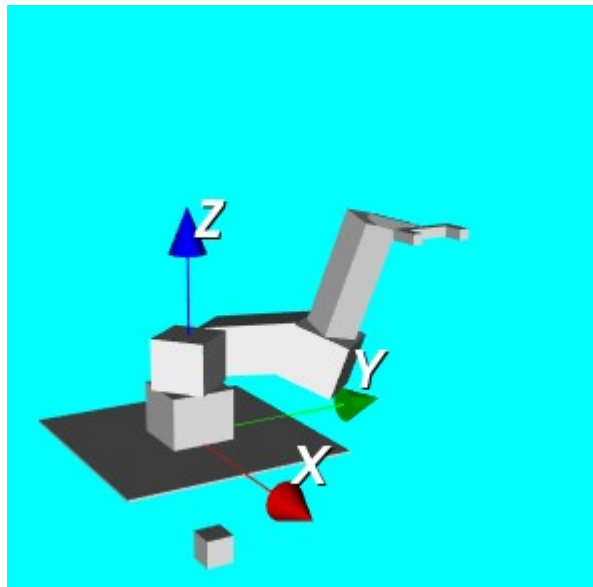
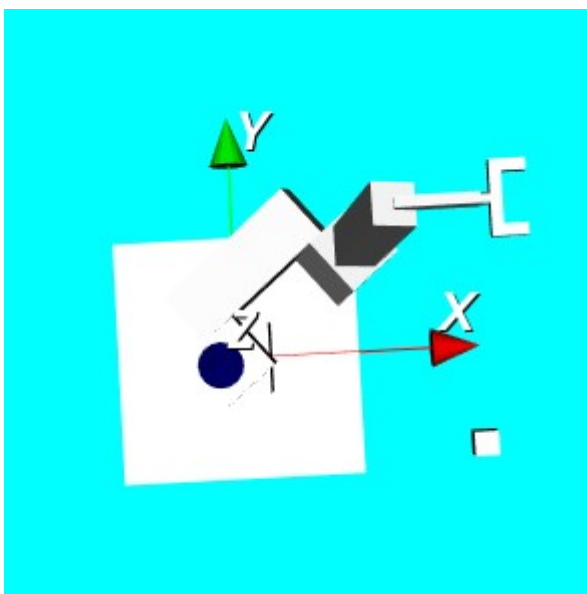


3. Cube A

With a cube A with dimensions $10\text{cm} \times 10\text{cm} \times 10\text{cm}$.

On the surface, my robot can reach only an area described by a radius of 150cm.

I chose to divide the value of the position by 3. Then, we position the cube at (100, -40).



4. Grab the cube A

Then, we execute *invkin* to position the tool to grab the cube.

