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d = sym('d',[5,1])
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$$d = \begin{pmatrix} d_1 \\ d_2 \\ d_3 \\ d_4 \\ d_5 \end{pmatrix}$$

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I = eye(5)
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$$I = 5 \times 5 \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

```
B = I + d*d'
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$$B = \begin{pmatrix} d_1 \overline{d_1} + 1 & d_1 \overline{d_2} & d_1 \overline{d_3} & d_1 \overline{d_4} & d_1 \overline{d_5} \\ d_2 \overline{d_1} & d_2 \overline{d_2} + 1 & d_2 \overline{d_3} & d_2 \overline{d_4} & d_2 \overline{d_5} \\ d_3 \overline{d_1} & d_3 \overline{d_2} & d_3 \overline{d_3} + 1 & d_3 \overline{d_4} & d_3 \overline{d_5} \\ d_4 \overline{d_1} & d_4 \overline{d_2} & d_4 \overline{d_3} & d_4 \overline{d_4} + 1 & d_4 \overline{d_5} \\ d_5 \overline{d_1} & d_5 \overline{d_2} & d_5 \overline{d_3} & d_5 \overline{d_4} & d_5 \overline{d_5} + 1 \end{pmatrix}$$

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[C D] = eig(B)
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$$C = \begin{pmatrix} -\frac{\overline{d_2}}{\overline{d_1}} & -\frac{\overline{d_3}}{\overline{d_1}} & -\frac{\overline{d_4}}{\overline{d_1}} & -\frac{\overline{d_5}}{\overline{d_1}} & \frac{d_1}{d_5} \\ 1 & 0 & 0 & 0 & \frac{d_2}{d_5} \\ 0 & 1 & 0 & 0 & \frac{d_3}{d_5} \\ 0 & 0 & 1 & 0 & \frac{d_4}{d_5} \\ 0 & 0 & 0 & 1 & 1 \end{pmatrix}$$

D =

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & d_1 \overline{d_1} + d_2 \overline{d_2} + d_3 \overline{d_3} + d_4 \overline{d_4} + d_5 \overline{d_5} + 1 \end{pmatrix}$$

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norm(C(:,5))
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ans =

$$\sqrt{\frac{|d_1|^2}{|d_5|^2} + \frac{|d_2|^2}{|d_5|^2} + \frac{|d_3|^2}{|d_5|^2} + \frac{|d_4|^2}{|d_5|^2} + 1}$$