21bit0481-asst-3

September 20, 2023

```
[]: '''Assignment 15 sep
     Perform Data preprocessing on Titanic dataset
     1.Data Collection.
        Please download the dataset from
        https://www.kaggle.com/datasets/yasserh/titanic-datase
     2.Data Preprocessing
            Import the Libraries.
           Importing the dataset.
         o Checking for Null Values.
         o Data Visualization.
         o Outlier Detection
           Splitting Dependent and Independent variables
         o Perform Encoding
           Feature Scaling.
            Splitting Data into Train and Test'''
    \#\#Import the Libraries
[2]: import numpy as np
     import pandas as pd
     import matplotlib.pyplot as plt
     import seaborn as sns
    ##Import the dataset
[3]: df=pd.read_csv('Titanic-Dataset.csv')
     df
[3]:
         PassengerId Survived Pclass
                              0
                                      3
                    1
     0
     1
                              1
                                      1
     2
                    3
                              1
                                      3
     3
                    4
                              1
                                      1
```

4

886

887

888

5

887

888

889

0

0

1

0

3

2

1

```
890
889
                                   1
                           1
890
             891
                           0
                                   3
                                                      Name
                                                                Sex
                                                                      Age
                                                                            SibSp
0
                                 Braund, Mr. Owen Harris
                                                               male
                                                                     22.0
                                                                                1
1
     Cumings, Mrs. John Bradley (Florence Briggs Th... female 38.0
                                                                              1
2
                                  Heikkinen, Miss. Laina
                                                            female
                                                                                0
                                                                     26.0
3
          Futrelle, Mrs. Jacques Heath (Lily May Peel)
                                                            female
                                                                     35.0
                                                                                1
4
                                Allen, Mr. William Henry
                                                                     35.0
                                                               male
                                                                                0
. .
                                   Montvila, Rev. Juozas
                                                                                0
886
                                                               male
                                                                     27.0
887
                            Graham, Miss. Margaret Edith
                                                            female
                                                                     19.0
                                                                                0
888
               Johnston, Miss. Catherine Helen "Carrie"
                                                             female
                                                                      NaN
                                                                                1
889
                                   Behr, Mr. Karl Howell
                                                               male
                                                                     26.0
                                                                                0
890
                                     Dooley, Mr. Patrick
                                                                                0
                                                               male
                                                                     32.0
     Parch
                       Ticket
                                   Fare Cabin Embarked
0
         0
                    A/5 21171
                                 7.2500
                                           NaN
         0
                                           C85
                                                       С
1
                     PC 17599
                                71.2833
2
         0
            STON/02. 3101282
                                 7.9250
                                           NaN
                                                       S
3
         0
                       113803
                                53.1000
                                          C123
                                                       S
4
         0
                       373450
                                 8.0500
                                           NaN
                                                       S
         0
                                13.0000
                                                       S
886
                       211536
                                           NaN
887
         0
                       112053
                                30.0000
                                           B42
                                                       S
                   W./C. 6607
888
         2
                                23.4500
                                           NaN
                                                       S
                                                       С
889
         0
                       111369
                                30.0000
                                          C148
890
                       370376
                                 7.7500
                                           NaN
                                                       Q
```

[891 rows x 12 columns]

##Checking for Null Values

[4]: df.isnull().sum()

[4]: PassengerId 0 Survived 0 Pclass 0 Name 0 Sex 0 Age 177 SibSp 0 Parch 0 Ticket 0 Fare 0 Cabin 687 Embarked 2

dtype: int64

[5]: #inference: There are 3 columns which have null values-Age, Cabin, Embarked

 $\#\# \mathrm{Data}$ Visualisation

[6]: df.head()

[6]:	PassengerId	Survived	Pclass	١
0	1	0	3	
1	2	1	1	
2	3	1	3	
3	4	1	1	
1	E	^	၁	

	Name Sex A	lge SibS	5p \
0	Braund, Mr. Owen Harris male 22	2.0	1
1	Cumings, Mrs. John Bradley (Florence Briggs Th female 38.0) 1	
2	Heikkinen, Miss. Laina female 26	3.0	0
3	Futrelle, Mrs. Jacques Heath (Lily May Peel) female 35	5.0	1
4	Allen. Mr. William Henry male 35	5.0	0

	Parch	Ticket	Fare	${\tt Cabin}$	Embarked
0	0	A/5 21171	7.2500	NaN	S
1	0	PC 17599	71.2833	C85	C
2	0	STON/02. 3101282	7.9250	${\tt NaN}$	S
3	0	113803	53.1000	C123	S
4	0	373450	8.0500	${\tt NaN}$	S

[7]: df.info()

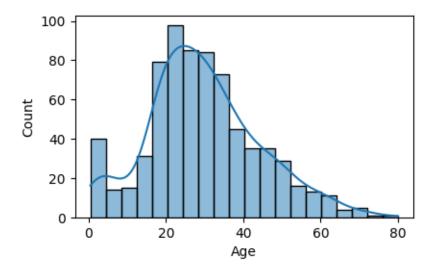
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 891 entries, 0 to 890
Data columns (total 12 columns):

#	Column	Non-Null Count	Dtype
0	PassengerId	891 non-null	int64
1	Survived	891 non-null	int64
2	Pclass	891 non-null	int64
3	Name	891 non-null	object
4	Sex	891 non-null	object
5	Age	714 non-null	float64
6	SibSp	891 non-null	int64
7	Parch	891 non-null	int64
8	Ticket	891 non-null	object
9	Fare	891 non-null	float64
10	Cabin	204 non-null	object
11	Embarked	889 non-null	object

dtypes: float64(2), int64(5), object(5)
memory usage: 83.7+ KB

```
[8]: plt.figure(figsize=(10, 6))
  plt.subplot(2, 2, 1)
  sns.histplot(df['Age'], bins=20, kde=True)
  plt.xlabel('Age')
  plt.ylabel('Count')
```

[8]: Text(0, 0.5, 'Count')



```
[9]: corr=df.corr() corr
```

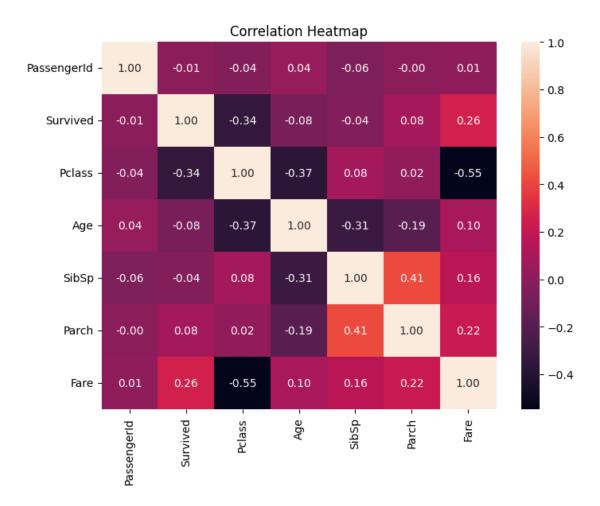
<ipython-input-9-7d5195e2bf4d>:1: FutureWarning: The default value of
numeric_only in DataFrame.corr is deprecated. In a future version, it will
default to False. Select only valid columns or specify the value of numeric_only
to silence this warning.

corr=df.corr()

[9]:		PassengerId	Survived	Pclass	Age	SibSp	Parch	\
	PassengerId	1.000000	-0.005007	-0.035144	0.036847	-0.057527	-0.001652	
	Survived	-0.005007	1.000000	-0.338481	-0.077221	-0.035322	0.081629	
	Pclass	-0.035144	-0.338481	1.000000	-0.369226	0.083081	0.018443	
	Age	0.036847	-0.077221	-0.369226	1.000000	-0.308247	-0.189119	
	SibSp	-0.057527	-0.035322	0.083081	-0.308247	1.000000	0.414838	
	Parch	-0.001652	0.081629	0.018443	-0.189119	0.414838	1.000000	
	Fare	0.012658	0.257307	-0.549500	0.096067	0.159651	0.216225	

Fare

```
PassengerId 0.012658
      Survived
                   0.257307
      Pclass
                  -0.549500
      Age
                   0.096067
      SibSp
                   0.159651
      Parch
                   0.216225
      Fare
                   1.000000
[10]: df.isnull().any()
[10]: PassengerId
                     False
      Survived
                     False
      Pclass
                     False
      Name
                     False
      Sex
                     False
      Age
                      True
      SibSp
                     False
     Parch
                     False
      Ticket
                     False
     Fare
                     False
      Cabin
                      True
      Embarked
                      True
      dtype: bool
[11]: df.isnull().sum()
[11]: PassengerId
                       0
      Survived
                       0
      Pclass
                       0
     Name
                       0
      Sex
                       0
      Age
                     177
      SibSp
                       0
      Parch
                       0
      Ticket
                       0
      Fare
                       0
      Cabin
                     687
      Embarked
                       2
      dtype: int64
[12]: plt.figure(figsize=(8, 6))
      sns.heatmap(corr, annot=True, fmt=".2f")
      plt.title('Correlation Heatmap')
[12]: Text(0.5, 1.0, 'Correlation Heatmap')
```



##Handling Null Values

Imputing null values of age and emabarked

```
[13]: median_age=df['Age'].median()
df['Age'].fillna(median_age,inplace=True)
```

```
[14]: mode_embarked=df['Embarked'].mode()[0]
df['Embarked'].fillna(mode_embarked,inplace=True)
```

Dropping the column Cabin having large Null Values

```
[15]: df.drop('Cabin',axis=1,inplace=True)
```

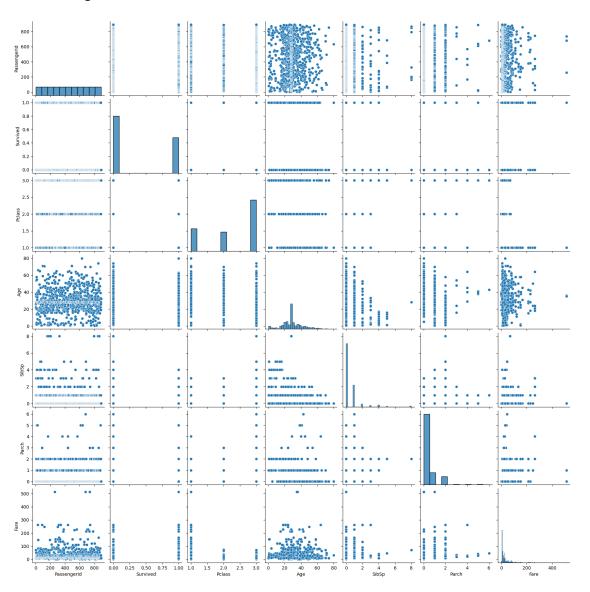
```
[16]: df.isnull().sum()
```

[16]: PassengerId 0
Survived 0
Pclass 0

Name 0 Sex 0 Age 0 SibSp 0 Parch 0 Ticket 0 Fare 0 Embarked 0 dtype: int64

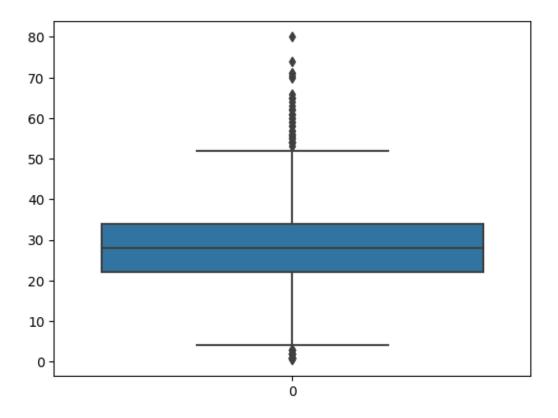
[17]: sns.pairplot(df)

[17]: <seaborn.axisgrid.PairGrid at 0x7d24298e68f0>



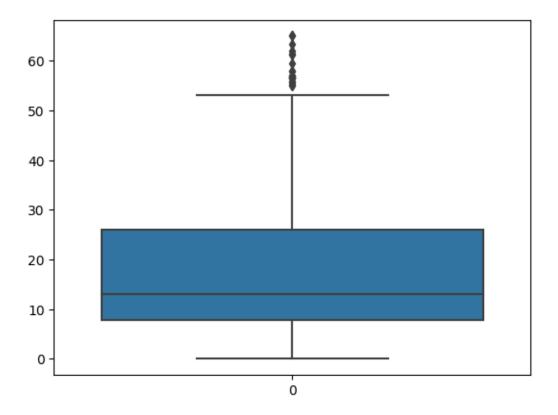
```
[18]: Q1 = df['Age'].quantile(0.25)
      Q3 = df['Age'].quantile(0.75)
      IQR = Q3 - Q1
      lower_bound = Q1 - 1.5 * IQR
      upper_bound = Q3 + 1.5 * IQR
      outliers = (df['Age'] < lower_bound) | (df['Age'] > upper_bound)
      print("Indices of potential outliers:")
      print(df[outliers].index)
     Indices of potential outliers:
     Int64Index([ 7, 11, 15, 16, 33, 54, 78, 94, 96, 116, 119, 152, 164,
                 170, 172, 174, 183, 195, 205, 232, 252, 268, 275, 280, 297, 305,
                 326, 340, 366, 381, 386, 438, 456, 467, 469, 479, 483, 487, 492,
                 493, 530, 545, 555, 570, 587, 625, 626, 630, 642, 644, 647, 659,
                 672, 684, 694, 745, 755, 772, 788, 803, 824, 827, 829, 831, 851,
                 879],
                dtype='int64')
[19]: Q1 = df['Fare'].quantile(0.25)
      Q3 = df['Fare'].quantile(0.75)
      IQR = Q3 - Q1
      lower_bound = Q1 - 1.5 * IQR
      upper_bound = Q3 + 1.5 * IQR
      outliers = (df['Fare'] < lower_bound) | (df['Fare'] > upper_bound)
      print(df[outliers].index)
     Int64Index([ 1, 27, 31, 34, 52, 61, 62, 72, 88, 102,
                 792, 802, 820, 829, 835, 846, 849, 856, 863, 879],
                dtype='int64', length=116)
[20]: from scipy import stats
      mean fare=np.mean(df['Fare'])
      median_fare=np.median(df['Fare'])
      mode fare=stats.mode(df['Fare'])
      print('Mean',mean_fare)
      print('Median',median_fare)
      print('Mode',mode_fare)
     Mean 32.204207968574636
     Median 14.4542
     Mode ModeResult(mode=8.05, count=43)
[21]: Q1 = df['Fare'].quantile(0.25)
      Q3 = df['Fare'].quantile(0.75)
      IQR = Q3 - Q1
      lower_bound = Q1 - 1.5 * IQR
      upper_bound = Q3 + 1.5 * IQR
```

```
df = df[(df['Fare'] >= lower_bound) & (df['Fare'] <= upper_bound)]</pre>
[22]: mean_fare=np.mean(df['Fare'])
      median_fare=np.median(df['Fare'])
      mode_fare=stats.mode(df['Fare'])
      print('Mean',mean_fare)
      print('Median',median_fare)
      print('Mode',mode_fare)
     Mean 17.82209070967742
     Median 13.0
     Mode ModeResult(mode=8.05, count=43)
[23]: mean_age=np.mean(df['Age'])
      median_age=np.median(df['Age'])
      mode_age=stats.mode(df['Age'])
      print('Mean',mean_age)
      print('Median',median_age)
      print('Mode',mode_age)
     Mean 28.748709677419356
     Median 28.0
     Mode ModeResult(mode=28.0, count=186)
[24]: sns.boxplot(df.Age)
[24]: <Axes: >
```



[25]: sns.boxplot(df.Fare)

[25]: <Axes: >



[34]:	df										
[34]:		PassengerId	Survived	Pclass	\						
	0	1	0	3							
	2	3	1	3							
	3	4	1	1							
	4	5	0	3							
	5	6	0	3							
		•••	•••								
	886	887	0	2							
	887	888	1	1							
	888	889	0	3							
	889	890	1	1							
	890	891	0	3							
						Name	Sex	Age	SibSp	Parch	\
	0		В	Braund, Mr. Owen Harris			male	22.0	1	0	
	2		Heikkinen, Miss. Laina			Laina	female	26.0	0	0	
	3	Futrelle, Mr	s. Jacques	s. Jacques Heath (Lily May Peel)			female	35.0	1	0	
	4		Al	len, Mr.	William	Henry	male	35.0	0	0	
	5			Мо	ran, Mr.	James	male	28.0	0	0	

```
888
                                                                     28.0
                                                                                       2
               Johnston, Miss. Catherine Helen "Carrie"
                                                            female
                                                                                1
      889
                                    Behr, Mr. Karl Howell
                                                                     26.0
                                                                                0
                                                                                       0
                                                               male
      890
                                      Dooley, Mr. Patrick
                                                               male 32.0
                                                                                0
                                                                                       0
                      Ticket
                                  Fare Embarked
      0
                   A/5 21171
                               7.2500
                                              S
      2
           STON/02. 3101282
                               7.9250
                                              S
      3
                      113803 53.1000
                                              S
                                              S
      4
                      373450
                               8.0500
      5
                      330877
                               8.4583
                                              Q
      . .
                         •••
                                              S
      886
                      211536
                              13.0000
      887
                      112053
                              30.0000
                                              S
      888
                  W./C. 6607
                                              S
                              23.4500
                                              С
      889
                      111369
                              30.0000
      890
                      370376
                               7.7500
                                              Q
      [775 rows x 11 columns]
     ##Seperate dependent and independent variables
[26]: Y=df['Survived']
      X=df.drop('Survived', axis=1)
     ##Perform Encoding
[27]: from sklearn.preprocessing import LabelEncoder
      le=LabelEncoder()
      X["Sex"] = le.fit_transform(X["Sex"])
      X["Sex"].value_counts()
[27]: 1
           531
      0
           244
      Name: Sex, dtype: int64
[28]: df
[28]:
           PassengerId
                         Survived Pclass
      0
                      1
                                 0
                                         3
      2
                      3
                                 1
                                         3
                      4
      3
                                 1
                                         1
      4
                      5
                                 0
                                         3
      5
                      6
                                 0
                                         3
      . .
                                         2
      886
                    887
                                 0
      887
                    888
                                 1
                                         1
```

Montvila, Rev. Juozas

Graham, Miss. Margaret Edith female 19.0

886

887

male 27.0

0

0

0

```
889
      888
                                0
                                         3
      889
                    890
                                1
                                         1
      890
                    891
                                0
                                         3
                                                      Name
                                                               Sex
                                                                           SibSp
                                                                                  Parch
                                                                      Age
      0
                                 Braund, Mr. Owen Harris
                                                              male
                                                                    22.0
                                                                               1
                                                                                       0
      2
                                  Heikkinen, Miss. Laina female
                                                                    26.0
                                                                               0
                                                                                       0
           Futrelle, Mrs. Jacques Heath (Lily May Peel)
                                                                                       0
      3
                                                            female
                                                                    35.0
                                                                               1
                                Allen, Mr. William Henry
      4
                                                                    35.0
                                                                               0
                                                                                       0
                                                              male
      5
                                         Moran, Mr. James
                                                              male
                                                                     28.0
                                                                               0
                                                                                       0
      . .
                                                                 •••
                                                                       •••
      886
                                    Montvila, Rev. Juozas
                                                              male
                                                                    27.0
                                                                               0
                                                                                       0
      887
                            Graham, Miss. Margaret Edith
                                                            female 19.0
                                                                               0
                                                                                       0
      888
               Johnston, Miss. Catherine Helen "Carrie"
                                                            female
                                                                    28.0
                                                                               1
                                                                                       2
      889
                                    Behr, Mr. Karl Howell
                                                                    26.0
                                                                               0
                                                                                       0
                                                              male
                                      Dooley, Mr. Patrick
      890
                                                                                       0
                                                              male 32.0
                                                                               0
                      Ticket
                                 Fare Embarked
      0
                   A/5 21171
                               7.2500
                                              S
      2
           STON/02. 3101282
                               7.9250
      3
                      113803 53.1000
                                              S
      4
                      373450
                               8.0500
                                              S
      5
                      330877
                               8.4583
                                              Q
      . .
      886
                      211536
                              13.0000
                                              S
                                              S
      887
                      112053
                              30.0000
      888
                                              S
                 W./C. 6607
                              23.4500
      889
                      111369
                              30.0000
                                              С
      890
                      370376
                               7.7500
                                              Q
      [775 rows x 11 columns]
[29]: X.Embarked.value_counts()
[29]: S
           584
      С
           116
      Q
            75
      Name: Embarked, dtype: int64
[30]: Embarked=pd.get_dummies(X["Embarked"],drop_first=True)
      Embarked
[30]:
              S
           0
              1
      0
      2
           0 1
      3
           0 1
```

4

```
886 0 1
      887 0
      888 0 1
      889 0
      890 1 0
      [775 rows x 2 columns]
     ##Splitting into training and testing set
[31]: from sklearn.model_selection import train_test_split
      X_train, X_test, Y_train, Y_test = train_test_split(X, Y, test_size=0.2,_
       →random state=0)
      X_train.shape,X_test.shape,Y_train.shape,Y_test.shape
[31]: ((620, 10), (155, 10), (620,), (155,))
     ##Feature Scaling.
[36]: from sklearn.preprocessing import MinMaxScaler
      numeric_columns = ['Age', 'Fare', 'Pclass', 'SibSp', 'Parch']
      X_train_numeric = X_train[numeric_columns]
      X_test_numeric = X_test[numeric_columns]
      sc=MinMaxScaler()
      X_train_scaled=sc.fit_transform(X_train_numeric)
      X_test_scaled=sc.transform(X_test_numeric)
      X_train_scaled
      X_test_scaled
[36]: array([[0.34656949, 0.11923077, 1.
                                                 , 0.
                                                              , 0.
                                                                          ],
             [0.22090978, 0.22237231, 1.
                                                  , 0.
                                                              , 0.16666667],
             [0.34656949, 0.12384615, 1.
                                                 , 0.
                                                              , 0.
                                                                          ],
             [0.68585072, 0.24615385, 0.5
                                                 . 0.
                                                              . 0.
                                                                          ٦.
                                                              , 0.
             [0.34656949, 0.11121846, 1.
                                                 , 0.
                                                                          ],
             [0.27117366, 0.11153846, 1.
                                                 , 0.
                                                              , 0.
                                                                          ],
             [0.28373963, 0.23147385, 0.5
                                                 , 0.
                                                              , 0.
                                                                          ],
             [0.63558683, 0.40846154, 0.
                                                 , 0.
                                                              , 0.
                                                                          ],
             [0.05755215, 0.29628154, 1.
                                                 , 0.4
                                                              , 0.16666667],
             [0.33400352, 0.12192308, 1.
                                                 , 0.
                                                              , 0.
                                                                          ],
             [0.52249309, 0.8
                                                              , 0.
                                                                          ],
                                   , 0.
                                                 , 0.2
             [0.48479517, 0.12192308, 1.
                                                              , 0.
                                                 , 0.
                                                                          ],
                                                              , 0.
             [0.24604172, 0.15147385, 1.
                                                                          ],
                                                 , 0.
             [0.01985423, 0.42923077, 1.
                                                  , 0.6
                                                              , 0.33333333],
             [0.34656949, 0.11961538, 1.
                                                 , 0.
                                                              , 0.
                                                                          ],
             [0.03242021, 0.24461538, 1.
                                                 , 0.2
                                                              , 0.16666667],
```

5

```
, 0. ],
[0.34656949, 0.11993538, 1. , 0.
[0.40939935, 0.07692308, 0.
                             , 0.
                                       , 0.
                              , 0.
                                        , 0.5
[0.2963056 , 0.29628154, 1.
                             , 0.
                                       , 0.
[0.44709726, 0.12147385, 1.
                                        , 0.16666667],
[0.00728826, 0.17128154, 1.
                             , 0.2
                                        , 0.
[0.39683338, 0.86916615, 1.
                             , 0.
[0.25860769, 0.24769231, 1.
                             , 0.
                                        , 0.
[0.37170143, 0.2 , 0.5
                             , 0.
                                       , 0.
[0.34656949, 0.12147385, 1.
                             , 0.
                                        , 0.
                                                   ٦.
[0.30887158, 0.11115385, 1.
                             , 0.
                                        , 0.
[0.27117366, 0.11923077, 1.
                             , 0.
                                       , 0.
                             , 0.
                                        , 0.
[0.34656949, 0.11923077, 1.
[0.34656949, 0.12384615, 1.
                             , 0.
                                       , 0.
                            , 0.2
                                       , 0.16666667],
[0.30887158, 0.46153846, 0.5
                             , 0.
                                       , 0.
[0.37170143, 0.12384615, 1.
                             , 0.
                                       , 0.
[0.34656949, 0.13403846, 1.
                             , 0.8
                                       , 0.33333333],
[0.04498618, 0.48115385, 1.
                             , 0.
[0.7361146 , 0.11153846, 1.
                                       , 0.
                             , 0.2
[0.34656949, 0.30718 , 1.
[0.4722292 , 0.13326923, 1.
                             , 0.
                                       , 0.
                             , 0.2
                                        , 0.
[0.23347575, 0.12083385, 1.
                             , 0.
                                       , 0.
[0.34656949, 0.11121846, 1.
[0.54762503, 0.12384615, 1.
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