

# Derivatives: An Overview

Based on the book "Options, Futures & Other Derivatives" by John C. Hull

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# Part I

## Preliminaries

*In this introductory part we cover some basic concept that we will need later on to discuss the main topics of this report.*

*First, we introduce markets on a high level, discussing the various types of market out there and the subjects acting on them. After that, we introduce basic concept about interest rates, fundamental for the theory of derivative pricing.*

### 1 Markets

#### 1.1 Types of derivatives markets

Financial securities can be exchanged on Exchange-Traded or Over-The-Counter markets (OTC).

In the former, the Exchange provides standardized contracts to traders. Traders do not have to worry about credit risk since the exchange clearing house acts as an intermediary body and takes care of that for both parts of the contract. Usually, this is done by requiring a margin (deposit funds) for both traders.

On the other hand, OTC markets are the ones in which the majority of the derivatives trade takes part. The main participants in OTC derivatives markets are banks, large financial institutions, and corporations.

Once an OTC trade has been agreed upon, the two parties can either present it to a central counterparty (CCP) or clear the trade bilaterally. A CCP is like an exchange clearing house.

Often, banks act as market makers for the most common instruments. Thus, they quote bid and ask prices for them. Nowadays OCT markets are heavily regulated to improve transparency and reduce systemic risk, but before 2007 regulations were little to none.

#### 1.2 Contracts on derivatives markets

The following are some important types of contracts that one can encounter when dealing with derivatives.

##### 1.2.1 Forwards

A forward contract is an agreement between two parties to buy/sell an asset at a certain time in the future for a certain price, and they are usually traded OTC. When the contract acts at an immediate time, we often refer to those contracts as spot contracts.

Parties can assume a long (resp. short) position if they want to buy (resp. sell) the underlying asset. The other party necessarily assumes the other position.

The payoff of a forward for one unit of the asset is:

$$\text{sign}(P)(S_T - K)$$

where  $S_T$  is the spot price of the asset at maturity  $T$ ,  $K$  is the delivery price of the forward,  $P$  is positive if we have a long position, negative otherwise.

Note that the payoff is equal to the total gain or loss from the contract since the cost of entering a forward contract is zero.

##### 1.2.2 Futures

Like a forward contract, a futures contract is an agreement between two parties to buy or sell an asset at a certain time in the future for a certain price. Unlike forward contracts, futures contracts are normally traded on an exchange. To make trading possible, the exchange specifies standardized features of the contract and there is an exchange clearing house between the parties.

Two large exchanges on which futures contracts are traded are the Chicago Board of Trade (CBOT) and the Chicago Mercantile Exchange (CME), which have now merged to form the CME Group.

### 1.2.3 Options

Options can be traded in both types of markets. We shall distinguish between the kinds of options:

A first distinction can be made on the right that the option gives to the holder:

*Call option* = gives the holder the right to **buy** the underlying asset by a certain date for a certain price

*Put option* = gives the holder the right to **sell** the underlying asset by a certain date for a certain price

Another distinction is the time one can exercise the option. if at time  $t_0$  we buy an option with maturity  $T$ . Then the option is: *American* if it can be exercised at any time  $t \in [t_0, T]$ , *European* if it can be exercised only at time  $t = T$

Note that one does not necessarily have to exercise the option. It acts like a sort of "insurance" on the price of an underlying asset. Thus, there is a cost to acquire an option. On top of that, Exchanges or institutions OTC quote bid and ask prices with a much larger spread than that for the underlying stock and it depends on the volume of trading.

Given the distinctions we made so far, we can identify four types of positions:

It is possible to *buy* or *sell a call* and *buy* or *sell a put*. In jargon, selling the option is often referred to as *writing the option*.

As a side note, it can be useful to know that In the United States, an option contract is a contract to buy or sell 100 shares.

## 1.3 Subjects acting on derivatives markets

In a market, we can identify three categories of traders: hedgers, speculators, and arbitrageurs.

### 1.3.1 Hedgers

Hedgers use derivatives to reduce the risk that they face from potential future movements in a market variable.

They can use both forwards or options. The fundamental difference between them when hedging is that Forward contracts are designed to neutralize risk by fixing the price that the hedger will pay or receive for the underlying asset. Option contracts, by contrast, provide insurance. They offer a way for investors to protect themselves against adverse price movements in the future while still allowing them to benefit from favorable price movements.

An example of hedging using such contract is by fixing the currency conversion rate at present day to neutralize currency conversion risk.

### 1.3.2 Speculators

Speculators use derivatives to bet on the future direction of a market variable.

They can decide to use forwards over buying directly the underlying asset at the spot price and selling it afterward. If one makes the calculations, it turns out that using forwards results in a worse outcome in both cases (right & wrong prediction of the market direction). The reason is simple: if one buys the asset at a spot price, a great amount of liquidity is needed. On the other hand, the future requires only a fraction of the liquidity (that is, the margin) and one can leverage the position. Also, one should account for the "risk-free" interest rate earned or paid for the liquidity that is not immediately used in the case of the forward. (*See section ?? for a definition of "risk-free"*).

There is a difference between options and futures: when a speculator uses futures, the potential loss as well as the potential gain is very large. When options are purchased, no matter how bad things get, the speculator's loss is limited to the amount paid for the options.

### 1.3.3 Arbitrageurs

Arbitrageurs take offsetting positions in two or more instruments — even in different markets — to lock in a riskless profit.

In general, (mathematical) arbitrage opportunities cannot last for long. For this reason, in the book most of the arguments concerning derivatives are made under the assumption that no arbitrage opportunity exist.

## 2 Interest Rates

### 2.1 Types of Rate

One important factor influencing interest rates is credit risk. This is the risk that there will be a default by the borrower of funds. The extra amount added to a risk-free interest rate to allow for credit risk is known as a credit spread.

**Treasury Rates** Rates an investor earns on Treasury bills and Treasury bonds (more in general, bonds from a developed country). It is usually assumed that there is no chance that the government of a developed country will default on an obligation denominated in its own currency. A developed country's Treasury rates are therefore regarded as risk-free.

**Overnight Rates** At the end of a day, some financial institutions typically have surplus funds in their accounts with the central bank while others have requirements for funds, given the requirements of reserves that the central bank makes. This leads to borrowing and lending overnight. There are many rates, depending on the country of interest: effective federal funds rate (US), SONIA (UK), ESTER (EU), etc...

**Repo Rates** Unlike the overnight federal funds rate, repo rates are secured borrowing rates. In a repo (or repurchase agreement), a financial institution that owns securities agrees to sell the securities for a certain price and buy them back at a later time for a slightly higher price. The interest rate is referred to as the *repo rate*. If structured carefully, a repo involves very little credit risk.

### 2.2 Reference Rates

In a financial transaction, the parties frequently enter into contracts where the future interest rate paid or received is set equal to the value of an agreed reference interest rate.

**LIBOR** = London Interbank Offered Rate.

It is set by asking a panel of global banks to provide quotes estimating the unsecured rates of interest at which they could borrow from other banks just prior to 11 a.m. (U.K. time). Thus, they are estimates of unsecured borrowing rates for creditworthy banks.

A problem with LIBOR is that there is not enough borrowing between banks for a bank's estimates to be determined by market transactions. As a result, it can be subject to manipulation. Bank regulators are uncomfortable with this and have developed plans to phase out the use of LIBOR.

**New Reference** The plan is to base reference rates on the overnight rates (like ESTER). [Note that in the US the rate used will be SOFR, based on repo rates, thus they are secured rates].

Longer rates such as three-month rates, six-month rates, or one-year rates can be determined from overnight rates by compounding them daily:

$$\left[ \left( \prod_{i=1}^n 1 + r_i \hat{d}_i \right) - 1 \right] * \frac{360}{D}$$

With  $d_i$  = number of days to which  $r_i$  is applied,  $\hat{d}_i = \frac{d_i}{D}$ , and  $D = \sum_i d_i$ .  
e.g. rate on friday is assumed to be applied also on saturday and sunday.

The new reference rates are regarded as risk-free because they are derived from one-day loans to creditworthy financial institutions. LIBOR, by contrast, incorporates a credit spread. Since credit spreads increase in stressed market conditions, the new risk-free reference rates may also be augmented by credit spread measures in the future.

Also, LIBOR rates are forward looking. They are determined at the beginning of the period to which they will apply. The new reference rates are backward looking: The rate applicable to a particular period is not known until the end of the period when all the relevant overnight rates have been observed.

### 2.3 Risk-free Rate

the usual approach to valuing derivatives involves setting up a riskless portfolio and arguing that the return on the portfolio should be the risk-free rate.

For that purpose, Treasury rates are artificially low. Therefore, The risk-free reference rates created from from overnight rates are the ones used in valuing derivatives.

## 2.4 Measure interest rates - Compounding

The compounding frequency defines the units in which an interest rate is measured. A rate expressed with one compounding frequency can be converted into an equivalent rate with a different compounding frequency.

Given an amount  $A$  invested for  $n$  years at interest rate  $R$ :

**Discrete compounding** The interest rate is compounded  $m$  times a year. Then at the end of the period we get:

$$A \left( 1 + \frac{R}{m} \right)^{mn}$$

When  $m = 1$  the rate is the *equivalent annual interest rate*.

If we want to derive the equivalent rate given a compounding  $m_2$ , we can just solve

$$A \left( 1 + \frac{R_1}{m_1} \right)^{m_1 n} = A \left( 1 + \frac{R_2}{m_2} \right)^{m_2 n} \implies R_2 = m_2 \left[ \left( 1 + \frac{R_1}{m_1} \right)^{\frac{m_1}{m_2}} - 1 \right]$$

**Continuous compounding** At the limit  $\lim_{m \rightarrow 0}$ , we get that  $A$ , at the end of the period, becomes

$$Ae^{Rn}$$

For practical purposes, one can think of it as being equivalent to daily compounding. To get the equivalent rate with discrete compounding  $m$ , we solve:

$$Ae^{R_c n} = A \left( 1 + \frac{R_m}{m} \right)^{mn} \implies R_m = m(e^{\frac{R_c}{m}} - 1)$$

On the other hand, continuous compounding is widely used for derivative pricing. From now on, every interest rate is to be intended as continuously compounded, if not specified.

If we want to discount the rate, we simply compute  $Ae^{-Rn}$

## 2.5 Zero-Rates

The **n-year zero-coupon interest rate** is the rate of interest earned on an investment that starts today and lasts for  $n$  years. All the interest and principal is realized at the end of  $n$  years. *There are no intermediate payments.* Sometimes it is also called the  $n$ -year spot rate, the  $n$ -year zero rate, or just the  $n$ -year zero. In the market, most rates are not pure zero rates.

## 2.6 Bond Pricing

A bond's principal — or face/par value — is the amount that is paid at the end of its life. Thus, the theoretical price of a bond should be the present value plus the (discounted) cash flow that will come from the bond ownership over time.

To discount cashflows, one can use the same rate as the bond's one, but a more accurate approach is to use a different zero-rate for each cash flow.

**Bond Price** The bond price can be calculated as:

$$B = \sum_{i=1}^N c_i e^{-z_{fi} * fi}$$

$c_i$  is the value of the coupon that the bond pays at period  $i$ ,  $f$  is the frequency of the coupon (annual, semiannual, etc...), and  $z_{fi}$  is the zero-rate with maturity  $fi$ .

For every coupon, we pick a different zero-rate and we compound it for its respective maturity. [Note that  $c_N$  is equal to the face value of the bond plus the last coupon, if present].

**Bond Yield** A bond's yield is the single discount rate that, if applied to all cashflows, gives a bond price equal to its market price. If we let  $M$  be the market price of the bond, we write:

$$\sum_{i=1}^N c_i e^{-y^* f_i} = M$$

Which can be solved using numerical methods (i.e. [Newton-Raphson](#))

**Par Yield** The par yield for a certain bond maturity is the coupon rate that causes the bond price to equal its par value.

$$\sum_{i=1}^{N-1} c e^{-z_{f_i}^* f_i} + (Par\ Value + c) e^{-z_{f_N}^* f_N} = Par\ Value$$

## 2.7 Determination of Zero Rates

A chart showing the zero rate as a function of maturity is known as the zero curve. A common assumption is that the zero curve is linear between the points determined using the bootstrap method.

**Bootstrap method** In practice, we do not usually have bonds with maturities equal to exactly 1.5 years, 2 years, 2.5 years, and so on. One approach is to interpolate between the bond price data before it is used to calculate the zero curve. Assume a piecewise linear curve with corners at these times. Use an iterative “trial and error” procedure to determine the rate at time  $t_1$  that matches the price of the first instrument, then use a similar procedure to determine the rate at time  $t_2$  that matches the price of the second instrument, and so on. For any trial rate, the rates used for coupons are determined by linear interpolation. A more sophisticated approach is to use polynomial or exponential functions, rather than linear functions, for the zero curve between times  $t_i$  and  $t_{i+1}$  for all  $i$ . The functions are chosen so that they price the bonds correctly and so that the gradient of the zero curve does not change at any of the  $t_i$ . This is referred to as using a spline function for the zero curve.

## 2.8 Forward Rates

Forward interest rates are the rates of interest implied by current zero rates for periods of time in the future. e.g. when considering a 2-years timespan, it is the rate for year 2 that, when combined with the zero-rate for year 1, gives the zero-rate at 2 years from today (compounded for 2 years).

$$A(1 + z_1)(1 + \mathbf{x}) = A(1 + z_2)^2$$

When interest rates are continuously compounded and rates in successive time periods are combined, the overall equivalent rate is simply the average rate during the whole period.

Assume  $R_1$ ,  $R_2$  are zero rates for maturities  $T_1$  and  $T_2$ , respectively.  $R_F$  is the forward interest rate for the period of time between  $T_1$  and  $T_2$ . Then:

$$R_F = \frac{R_2 T_2 - R_1 T_1}{T_2 - T_1} \implies R_F = R_2 + (R_2 - R_1) \frac{T_1}{T_2 - T_1} \implies R_F = R + \frac{\partial R}{\partial T} \text{ as } T_2 \rightarrow T_1$$

Where  $R$  is the zero-rate for a maturity of  $T$  and  $R_F$  is the *instantaneous forward rate* for a maturity of  $T$ . This is the forward rate applicable to a very short future time period that begins at time  $T$ . Defining  $P(0, T) = e^{-RT}$ , the equation becomes

$$R_F = -\frac{\partial}{\partial T} \ln P(0, T)$$

This shows that, if the zero curve is upward sloping between  $T_1$  and  $T_2$  so that  $R_2 > R_1$ , then  $R_F > R_2$  (i.e., the forward rate for a period of time ending at  $T_2$  is greater than the  $T_2$  zero rate) and viceversa.

If a large investor thinks that rates in the future will be different from today's forward rates, there are many trading strategies that the investor can explore. One of these involves entering into a contract known as a forward rate agreement (FRA).

## 2.9 Forward Rate Agreements

...

### 2.10 Duration

The duration of a bond measures how long the holder of the bond has to wait before receiving the present value of the cash payments. For instance, a zero-coupon bond that lasts  $n$  years has a duration of  $n$  years.

Recalling from the formula for the bond price  $B$  and bond yield  $y$ , with cashflows  $c_i$ :

$$B = \sum_{i=1}^N c_i e^{-y \cdot t_i}$$

Then the *duration* is defined as:

$$D = \sum_{i=1}^N t_i \left[ \frac{c_i e^{-y \cdot t_i}}{B} \right]$$

In square brackets is the ratio of the present value of the cashflow at time  $t_i$  to the bond price.

The duration is therefore a weighted average of the times when payments are made, with the weight applied to time  $t_i$  being equal to the proportion of the bond's total present value provided by the cash flow at time  $t_i$ .

When we consider a small change in yield  $\Delta y$ , then

$$\Delta B \approx -\Delta y \sum_{i=1}^N c_i t_i e^{-y t_i}$$

From this we can retrieve the key duration relationship:

$$\Delta B \approx -\Delta y B D \implies \frac{\Delta B}{B} \approx -\Delta y D$$

Which is an approximate relationship between percentage changes in a bond price and changes in its yield. It is easy to use and is the reason why duration has become such a popular measure.

For the sake of definitions,  $DV01$  is the price change from a 1-basis-point increase in all rates, while **Gamma** is the change in  $DV01$  from a 1-basis-point increase in all rates.

**Modified Duration** can be used only when the interest rate is compounded  $m$  times per year ( $m \in \mathbb{N}$ ). In this case,

$$\Delta B = -\frac{B D \Delta y}{1 + y/m}$$

We define  $D^*$  as the *bond's modified duration*.

$$D^* = \frac{D}{1 + y/m} \implies \Delta B = -B D^* \Delta y$$

Modified duration calculation gives good accuracy for small yield changes.

Another term that is sometimes used is *dollar duration*:  $D_{\$} = D^* B$ , so that  $\Delta B = -D_{\$} \Delta y$

**Duration of a bond portfolio** The duration  $D$  of a bond portfolio is defined as a weighted average of the duration of the single bonds in the portfolio, with weights being proportional to the bond prices. Then, the previous equations apply (still for small changes in  $\Delta y$ ).

It is essential to note that, in this case, we are implicitly assuming that the yields of all bonds in the portfolio change by almost the same amount. When bonds have different maturities, this happens only when there is a parallel shift in the zero-coupon yield curve. Hence, the equations apply for small, parallel shifts of  $\Delta y$  in the zero curve.

This implies that, if the net duration of the assets in a portfolio is zero, then we eliminate exposure to parallel shifts in the yield curve, but we are still exposed to either nonparallel or large deviations.



## 2.11 Convexity

Duration applies only to small changes in yields. Two portfolios can have the same duration (gradients of the curves are equal at the origin), but react differently for large yield changes: one has more curvature than the other.

*Convexity* measures this curvature.

A measure of convexity is:

$$C = \frac{1}{B} \frac{d^2 B}{dy^2} = \frac{1}{B} \sum_{i=1}^N c_i t_i^2 e^{-y t_i}$$

Using Taylor series expansion,

$$\Delta B = \frac{dB}{dy} \Delta y + \frac{1}{2} \frac{d^2 B}{dy^2} \Delta y^2 \implies \frac{\Delta B}{B} = -D \Delta y + \frac{1}{2} C (\Delta y)^2$$

Given a duration  $D$ , the convexity of a bond portfolio tends to be greatest when the portfolio provides payments evenly over a long period of time, while is smaller when payments are concentrated around a point in time.

By choosing a portfolio of assets and liabilities with a net duration of zero and a net convexity of zero, a financial institution can make itself immune to relatively large parallel shifts in the zero curve. However, it is still exposed to nonparallel shifts.

## 2.12 Theories of The Term Structure of Interest Rates

It is natural to ask what determines the shape of the zero curve. Why is it sometimes downward sloping, sometimes upward sloping, and sometimes partly upward sloping and partly downward sloping?

There are many theories trying to explore these relationships. For instance:

**Expectations Theory** long-term interest rates should reflect expected future short-term interest rates. More precisely, a forward interest rate corresponding to a certain future period is equal to the expected future zero interest rate for that period;

**Market Segmentation Theory** there should be no relationship between short-, medium-, and long-term interest rates. Investors invest in bonds of a certain maturity and do not readily switch from one maturity to another. Thus, The short-term rate is determined by supply and demand in the short-term bond market, and so on for medium- and long-term ones;

**Liquidity Preference Theory** investors prefer to preserve their liquidity and invest funds for short periods of time, while borrowers prefer to borrow at fixed rates for long periods of time.

We will not dive further into them here, even though implications in the management of the risks associated are relevant. (p. 117-119)

## Part II

# Forwards & Futures

*In this part, we introduce forwards and futures, explaining what they are, how the markets in which they are traded work, and how to price them.*

## 3 Futures market

### 3.1 Specification of the contract

As in the introduction, futures are bought and sold on exchange-traded markets. The exchange specifies the **asset** and the **contract size**.

When the asset is a commodity, there may be variations in the quality of what is available in the marketplace. When the asset is specified, the exchange stipulate the grade or grades of the commodity that are acceptable and, in some cases, the difference in prices of the various grades.

The exchange specifies also:

- **Contract size:** Specifies the asset amount that must be delivered under one contract.
- **Delivery arrangements:** the place where delivery will be made.
- **Delivery months:** the precise period during the month when delivery can be made.
- **Price Limits and Position Limits:** for most contracts, daily price movement limits are specified, to prevent large price movements from occurring because of speculative excesses. Position limits are the maximum number of contracts that a speculator may hold.
- **Limit up/down:** price movement up/down whose magnitude is equal to the daily price limit.

### 3.2 Convergence of futures price to spot price

As the delivery period for a futures contract is approached, the futures price converges to the spot price of the underlying asset. When the delivery period is reached, the futures price equals — or is very close to — the spot price. If this was not the case, then there would exist a clear arbitrage opportunity.

### 3.3 Operations on margin accounts

The whole purpose of the following system is to ensure that funds are available to pay traders when they make a profit. In other words, protecting from **credit risk**.

Let us consider a trader who takes a long position in future contracts. The trader has to keep funds in what is known as a *margin account*. The amount that must be deposited when the contract is entered into is known as the **initial margin**. At the end of each trading day, a **daily settlement** (or *making the market*) occurs: the margin account is adjusted to reflect the trader's gain or loss. This practice is referred to as daily settlement or marking to market.

A trade is first settled at the close of the day on which it takes place. It is then settled at the close of trading on each subsequent day (since futures are settled daily, while forwards are settled at the end of their life). Daily settlement leads to funds flowing each day between traders with long positions and traders with short positions, with a net equal to zero. This daily flow of funds is known as **variation margin**.

Most individuals have to contact their brokers to trade. They are subject to a **maintenance margin**, lower than the initial margin. If the balance in the margin account falls below the maintenance margin, the trader receives a margin call and must top up the margin account to the initial margin level within a short period. If the trader does not provide this variation margin, the broker closes out the position. On the other hand, if the trader has a gain, he/she is entitled to withdraw any balance in the margin account that exceeds the initial margin.

An important side note is that most brokers pay traders interest on the balance in a margin account.

### 3.3.1 Exchange clearing house

A *clearing house* acts as an intermediary in futures transactions and it guarantees the performance of the parties to each transaction. Its main task is to keep track of all transactions happening during the day to calculate the position of every one of its members (i.e. brokers, or third parties whom are contacted by brokers on behalf of their clients). Also, minimum levels for the initial and maintenance margins are set by the exchange clearing house (Individual brokers may require greater margins).

The clearing house member is required to provide to the clearing house initial margin (or *clearing margin*). The maintenance margin is set equal to the initial margin and, at the end of each day, variation margins happen for the clearing house member. Also, when determining margin requirements, the clearing house is about 99% certain that it will be sufficient to cover any losses in the event that the member defaults and has to be closed out.

Intraday variation margin payments may also be required by a clearing house from its members in times of significant price volatility.

Finally, clearing house members are required to contribute to a **guaranty fund**. This may be used by the clearing house in the event that a member defaults and the member's margin proves insufficient to cover losses.

## 3.4 OTC markets

As said before in the report, in these markets there is no exchange. Thus, credit risk has always characterized them. If one of the parties in a contract goes bankrupt when the outstanding transactions for the other one are positive, it is most likely that the other party will suffer a loss.

To reduce credit risk in these markets, some ideas from exchange-traded markets are being used.

### 3.4.1 Central Counterparties

CCPs have the same role as Clearing Houses in OTC markets. likely, members of CCPs must provide initial and variation margins, and they contribute to a guaranty fund.

Once an OTC derivative transaction has been agreed between two parties A and B, it can be presented to a CCP. If the CCP accepts the transaction, it becomes the counterparty to both A and B. It agrees to two obligations:

- Buy the asset from B at time  $t$  for price  $p$
- Sell the asset to A at time  $t$  for price  $p$

Taking the credit risk of both parties.

As in the previous case, both parties should provide initial margins and daily variation margins. Also, if they are not members of the CCP, they can act through a CCP member and their relation would be similar to the one between a trader and a broker in the case of a Clearing House.

After the 2007-8 crisis, it is required that most standard OTC transactions between financial institutions are handled by CCPs.

### 3.4.2 Bilateral Cleaning

OTC transactions that are not cleared through CCPs are cleared bilaterally. A and B usually enter into a master agreement covering all their trades. (The most common agreement is an *International Swaps and Derivatives Association (ISDA) Master Agreement*). This agreement usually includes an annex (credit support annex or CSA), requiring A, B, or both, to provide collateral. The collateral is similar to the margin required by exchange clearing houses or CCPs from their members.

Collateral agreements in CSAs usually require transactions to be valued each day. If the transactions between A and B increase in value to A by  $x$ , then B has to provide collateral worth  $x$  to A, and vice-versa. Obviously, collateral significantly reduces credit risk.

[This will be further discussed in ?? when discussing credit risk].

One should expect a different kind of situation if CCPs are not present, since every actor in the market has a direct relation with each other. On the other hand, if we allow just one CCP in the market, the situation is similar to a [star network](#).

### **3.4.3 Futures and OTC Trades**

Regardless of how transactions are cleared, initial margin when provided in the form of cash usually earns interest. The daily variation margin provided by a clearing house member for futures contracts does not earn interest. This is because the variation margin constitutes the daily settlement. Transactions in the OTC market, whether cleared through CCPs or cleared bilaterally, are usually not settled daily. For this reason, the daily variation margin that is provided by the member of a CCP or, as a result of a CSA, earns interest when it is in the form of cash. Securities can be often be used to satisfy margin/collateral requirements.<sup>6</sup> The market value of the securities is reduced by a certain amount to determine their value for margin purposes. This reduction is known as a haircut.

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## **3.5 Market Quotes**

## **3.6 Delivery**

## **3.7 Types of traders & orders**

## **3.8 Regulation**

## **3.9 Accounting and Taxation**

## **3.10 Forward vs Futures**

## 4 Hedging with futures

WIP

## 5 Pricing of Forward and Futures

### 5.1 Types of Rate

## Part III

# Options