I pledye any bonor-that I have alived by the Seever George Server and Server - Sur

(5135 Problem Ser 3

This freet is healid because it there exists an element in not A such that it'd (c,1) & R, then by the proof, (c,c) toes not recessorily exist in R, and R does not meet the reflexive relation definition that states for all elements a in A, (a,a) much be in the relation. Here, because C is in the set by that Method relation, R is not reflexive by this proof.

2 P: Yx (x \in A \rightarrow (x,x) \in R) ? Definion of reflexive solutions. S: Yx (x \in A \rightarrow (x,x) \in S)

a because Rland S are reflexive, they both unit contain for all elemones X in set A (xix) ER. (4 they both contain those relations, then the mon of Rand S) contains these relations, therefore R (1) S is reflexible.

As street above, R and S contain for all x inset A the relation (x,x). Because floor News are in both sets it follows that the intersection will also have (x,x) for all x in set A. Toverton, the intersection of R and S , salso reflective.

IX ... X+H - FILX X+K (KL) (C)

Then the read the property was placed to be a transfer to the service of the serv

Letined as all elevere Mi Are universalised not MS, and Wx (x,x) ES,

Then Yx (x,x) & S. Therefore, Si is artifettexive, and the Merseption

RNS nould revar all reflexive relations with R because \$ 15 and reflexive.

Therefore, RNS 05 antipotherore, and R-S is and reflexive.

do (a,c) ESOR ←> 36 (ab) ER) N(b,c) ES) Yx (x,x) € SOR => 36 ((x,6)ERN (b,xES)) let 6=x. \(\frac{1}{2}\times (\times_1\times) \in SOR G \(\times \left((\times_1\times) \in R \Lambda (\times_1\times) \in S)\) Vx (x,x) eseR E TAT Yx (x,x) ESOR - T Because the risht-tide is true of fellow that the (x,x) ESOR, Therefore SOR is reflexive. . Texted . + P. by the Letholici of publices: Ha Yb ((9,6) ER (6, a) ER-1) By definition of R. Yx (Coet) -> (Cxxxxxx) A Let a bex : Ux (Cxx) ER + Cxx) ER +) Because both Rand RT gre over set A, and (x,x) FR dorall x, -1. re 3 suggests that (xx) ER for all x, thretire R-1 vs reflere.

3A. i. [0] R is the set of all runners distrible by ? [1] R is the set of all numbers with renainder I was divided by ?

11: 14 E [6]R 11: .75 E [5]R 10. 7, for all presible renables when divided by 7. V. Us, the same amber common have Enodufferent remainders when divided by 7.

11. Because (a) = [b], we can substitute for either on the NoH site to habe [a] N[a] + Ø. This is true of there is aif loast are elevent in [a]. Because the phoblem states "Let a and b be my tho channers in set A," we look that Ea] + Ø. Therefore, [a] n(a] + Ø, prowing (a) = (b) -> [a] n(b) + Ø.

(a) 1 (b) + & inplies that [a] and [b] share a

Comon clevery let this clement be element x, where x E [a] and

X E [b]. Thus, by defeation of embalance class in 3.B.i., this implies

that (a,x) ER and (b,x) ER, by the symmetric dimensal

early lare relations, (b,x) ER (x, b) ER. By transactivity of

equivalence relations, (b,x) ER (x,b) ER (x,b) ER. This,

[a] 1 (b) + & -> (a,b) ER.