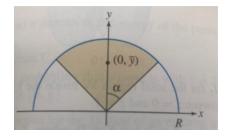
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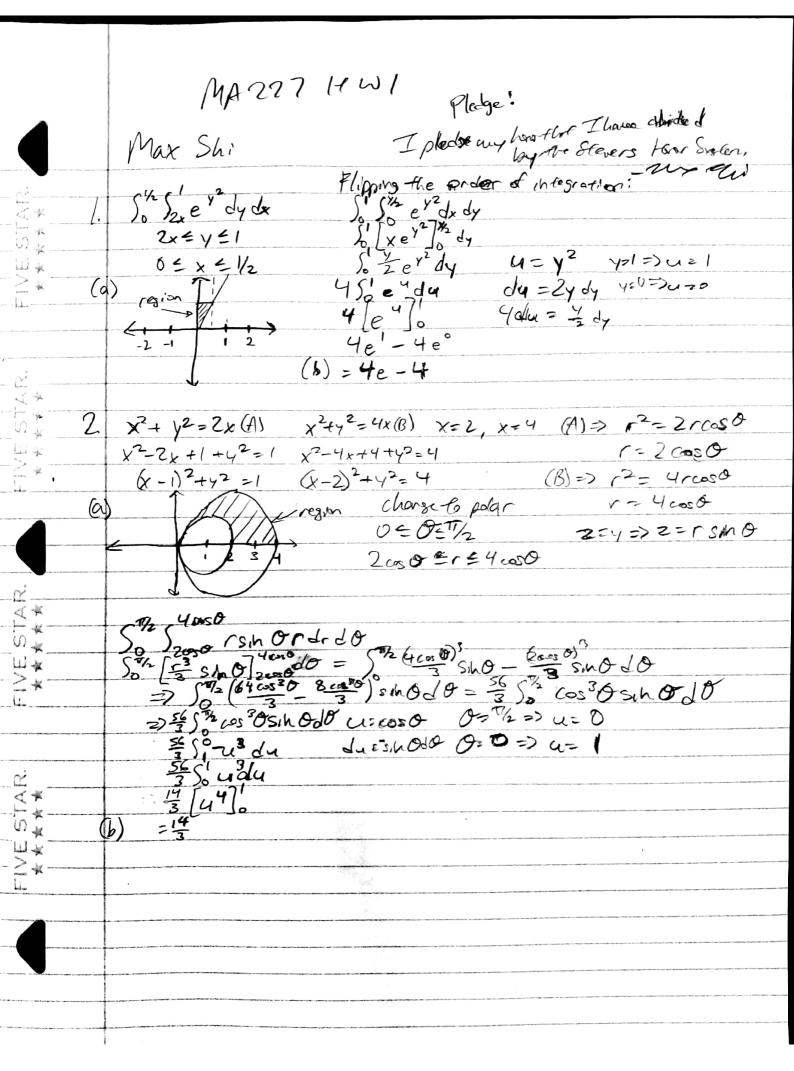
Pledge and Sign:

A high quality scan of the solutions in pdf format is to be uploaded to Canvas before the deadline. You need to pledge and sign on the cover page of your solutions. You may use this page as the cover page.

Legibility, organization of the solution, and clearly stated reasoning where appropriate are all important. Points will be deducted for sloppy work or insufficient explanations.

- 1. Given the iterated integral $\int_0^{1/2} \int_{2x}^1 e^{y^2} dy dx$:
 - (a) [3 pts.] Draw the region of integration.
 - (b) [7 pts.] Evaluate the integral.
- **2.** Consider the region D in the xy-plane bounded by the upper semi-circles of $x^2 + y^2 = 2x$ and $x^2 + y^2 = 4x$, and the piece of the x-axis between x = 2 and x = 4.
 - (a) [3 pts.] Sketch the region D.
 - (b) [7 pts.] Find the volume of the solid which lies below the plane z=y and above the region D, described above.
- 3. [10 pts.] Consider the lamina L which occupies the shaded region in the figure below. The blue curve is the circle $x^2+y^2=R^2$. L has mass density $\rho(x,y)=\sqrt{x^2+y^2}$ kg/m² at a point (x,y). Show that the y-coordinate, \bar{y} , of the center of mass of L is given by: $\bar{y}=\left(\frac{3R}{4}\right)\left(\frac{\sin\alpha}{\alpha}\right)$. Recall that $\cos\left(\frac{\pi}{2}-\alpha\right)=\sin\alpha$.





3. $\int_{7/2-4}^{7/2+4} \int_{0}^{R} P(x,y) r dr d\theta \qquad M_{W} = \int_{7/2-4}^{7/2+4} \int_{0}^{R} r^{2}(r \sin \theta) dr d\theta$ $P(x,y) = \int_{0}^{7/2+4} P(r \cos \theta) dr d\theta \qquad (7/2+4) \int_{0}^{7/2+4} P(r \cos$ 572 - Sor3shododo M2 Sand SR = 1 M2 Sand So 12 drdo 572-0 [47 0 SINOSO Signad By sh'odo 5 to 10 10 STA 3 40 1 - (05 0) T/2 - X R3[0]7/2 d R3 [1]+4- +4) = (3(2d) Ry (-cos(72+d)+.cos(=-d))

Ry (-cos(=-(-d))+cos(=-d))

Applying cos(=-d)=sind

Ry (-sin(-d)+sind)

Ry (2sind)

(sond) $\frac{1}{y} = \frac{M_{\star}}{M}$ $\frac{1}{y} = \frac{R^{4}}{2} \left(\sinh \theta \right) \cdot \frac{3}{R^{3}2} \alpha$ Y=3RY sind