

Max Shi

September 13, 2019

Professor Li

MA 332 Homework 2

I pledge my honor that I have abided by the Stevens Honor System.

1 (i)

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pbinom(8.25, 20, 0.4)
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[1] 0.5955987
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pbinom(8.25, 30, 0.4)
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```
[1] 0.09401122
```

```
pbinom(8.25, 50, 0.4)
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```
[1] 0.0002305229
```

```
pbinom(8.25, 100, 0.4)
```

```
[1] 5.431127e-13
```

1 (ii).

$$P(N \leq 8.25) = \Phi\left(\frac{8.25 - np}{\sqrt{np(1-p)}}\right)$$

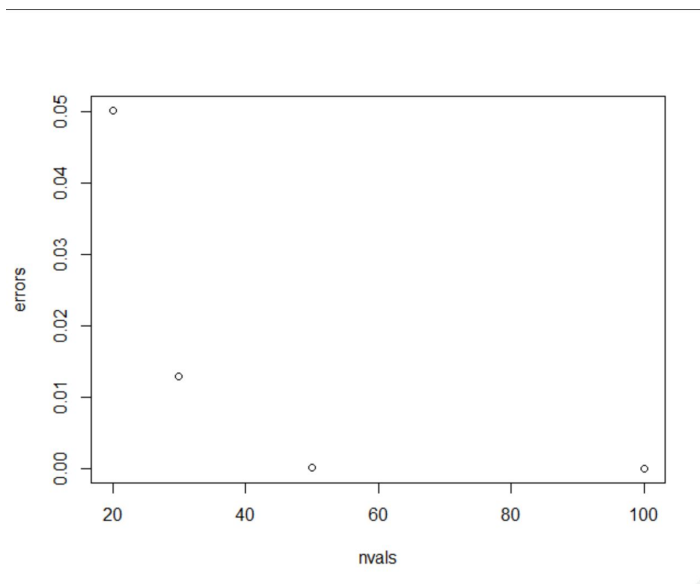
$$\text{For } n = 20, P(N \leq 8.25) = \Phi\left(\frac{8.25 - 20 \cdot 0.4}{\sqrt{20 \cdot 0.4(1-0.4)}}\right) = \Phi\left(\frac{0.25}{\sqrt{4.8}}\right) = \Phi(0.1141) = 0.5454$$

$$\text{For } n = 30, P(N \leq 8.25) = \Phi\left(\frac{8.25 - 30 \cdot 0.4}{\sqrt{30 \cdot 0.4(1-0.4)}}\right) = \Phi\left(\frac{-3.75}{\sqrt{7.2}}\right) = \Phi(-1.397) = 0.08113$$

$$\text{For } n = 50, P(N \leq 8.25) = \Phi\left(\frac{8.25 - 50 \cdot 0.4}{\sqrt{50 \cdot 0.4(1-0.4)}}\right) = \Phi\left(\frac{-11.75}{\sqrt{12}}\right) = \Phi(-3.392) = 0.000347$$

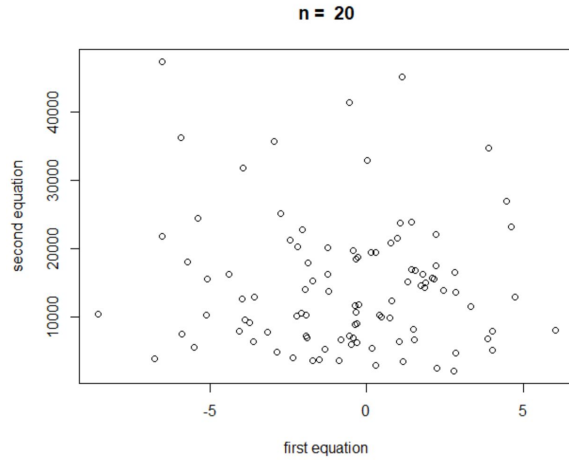
$$\text{For } n = 100, P(N \leq 8.25) = \Phi\left(\frac{8.25 - 100 \cdot 0.4}{\sqrt{100 \cdot 0.4(1-0.4)}}\right) = \Phi\left(\frac{-31.75}{\sqrt{24}}\right) = \Phi(-6.481) = 4.556 \cdot 10^{-11}$$

1 (iii).

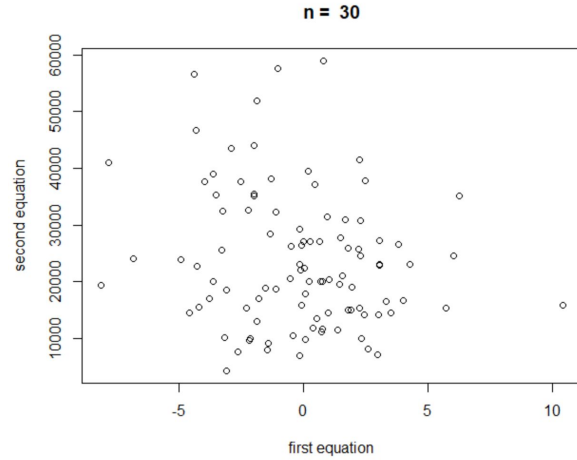


1 (iv). I perceive that as the amount of trials goes up, the Laplace theorem becomes more and more accurate toward the actual value and behavior of a binomial distribution.

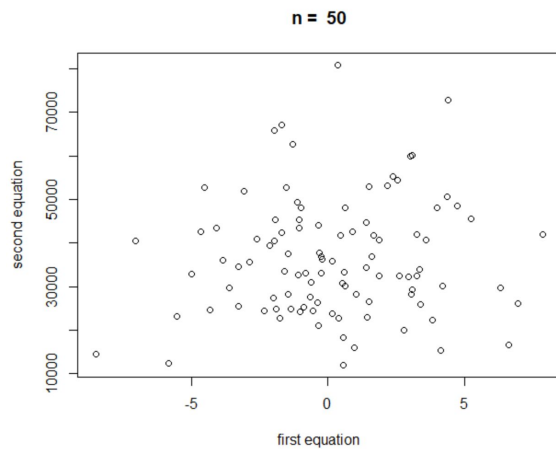
2 (i).



2(ii).



2(iii).



2(iv).

The points seem to be distributed toward the center bottom of the plot. The first equation tends to 0, or distributes close to 0, no matter what the value of  $n$  is. However, the range of the first equation decreases as  $n$  increases, and it has a tighter distribution around 0. The second equation seems to also tend toward lower numbers, however increases in range as  $n$  increases.