

MIEEC

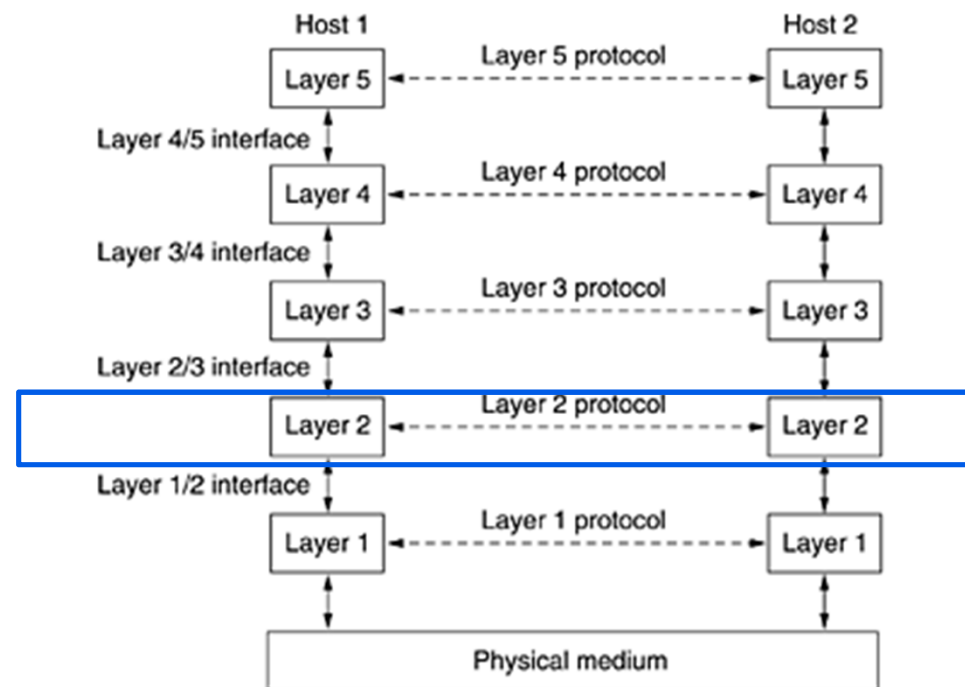
# Computer Networks

Lecture note 4

The data link layer



## ***Data link***



# Functions and services

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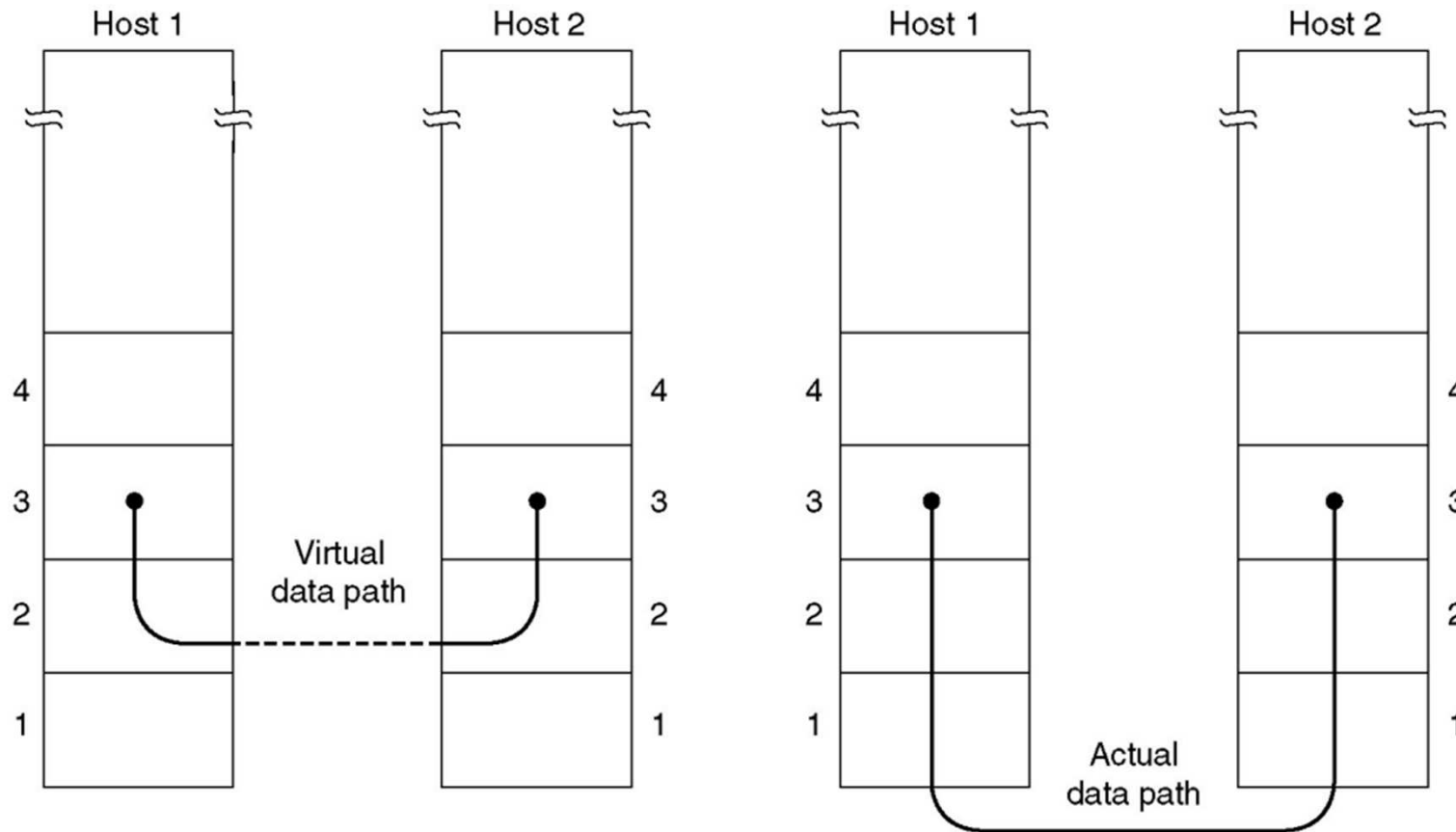
## Main functions:

- Service interface to upper layer (network)
- Dealing with transmission errors
- Regulating data flow

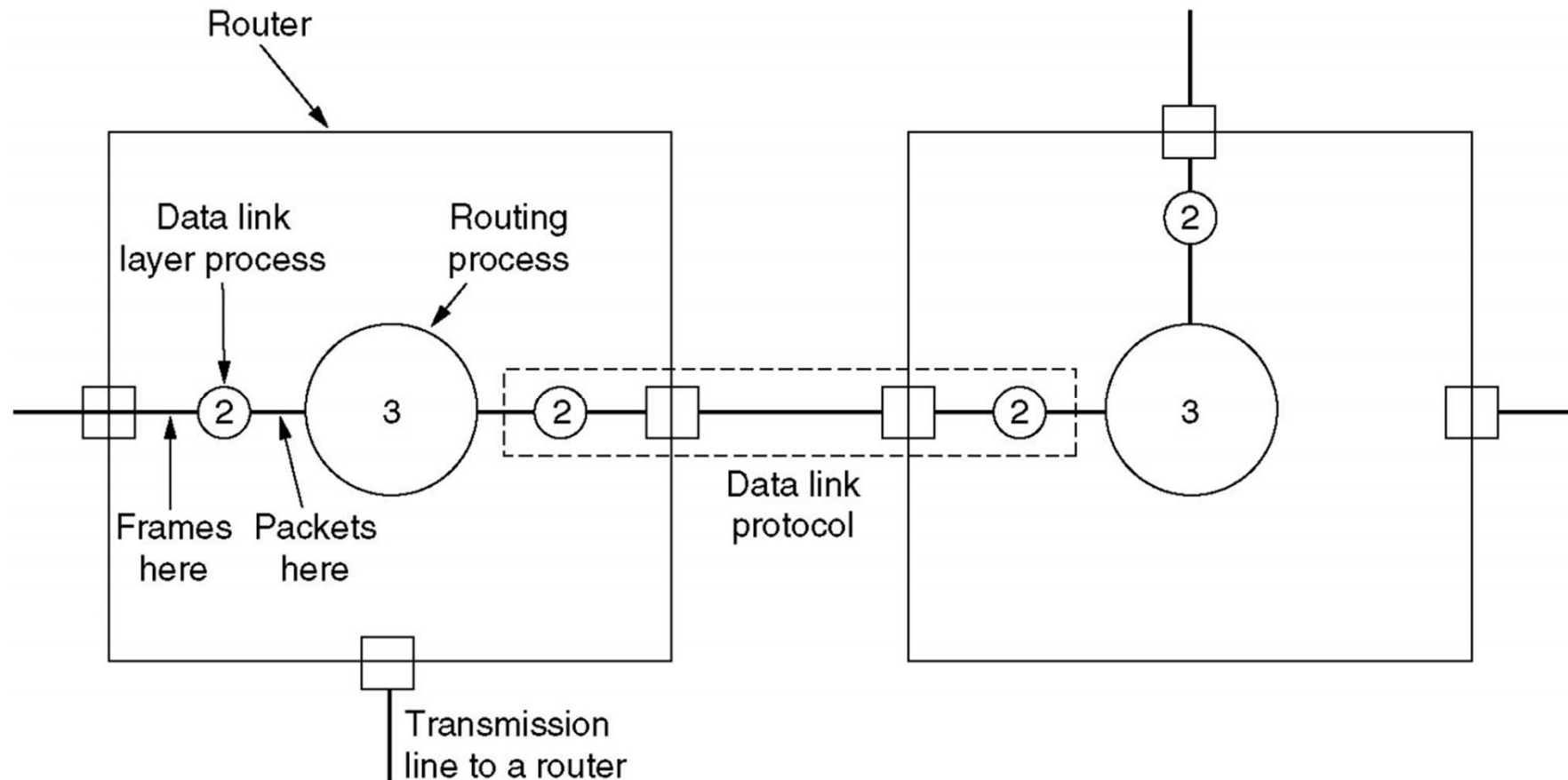
## Services provided:

- Unacknowledged connectionless service
- Acknowledged connectionless service
- Acknowledged connection-oriented service

# Service to the network layer

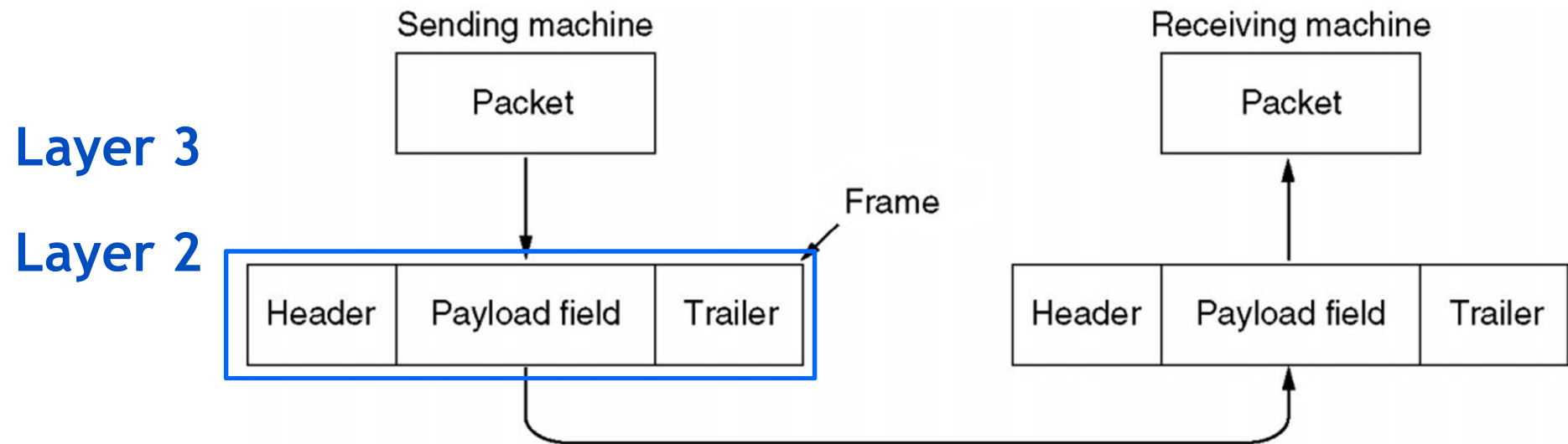


# Data link: the big picture



# Frames and packets

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# *Framing*

# TO THINK

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The data link gets a stream of 1s and 0s from the physical layer.

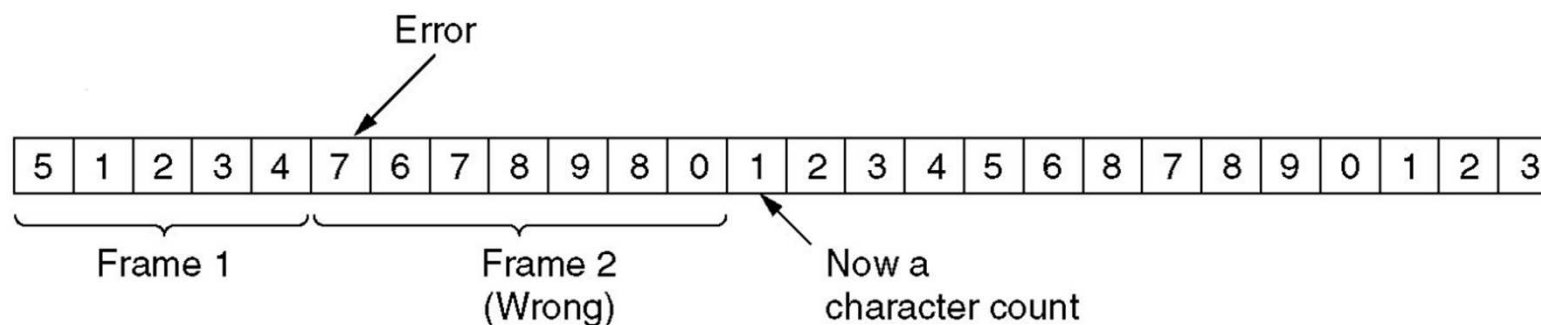
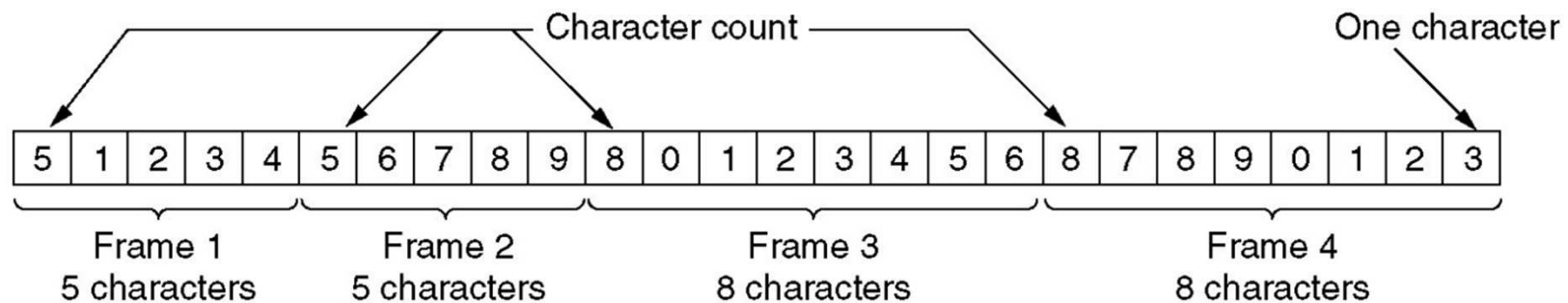
[sender] => ..00100100001011010111100101001011101000 => [receiver]

- Where does a frame start/stop?
  - Need to split a bit stream into frames



# Character counting

- Send the length of each frame



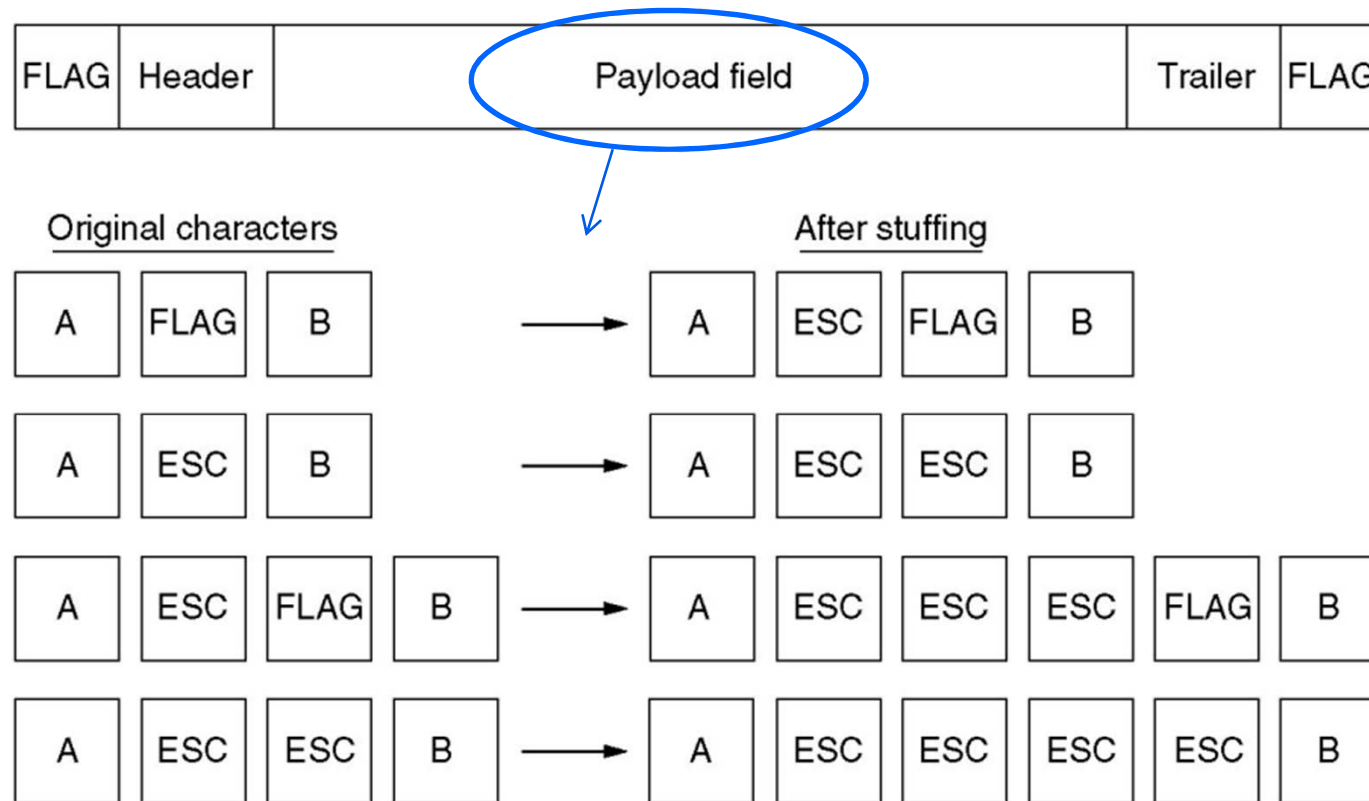
# Start/Stop Flags

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- Unique sequence as flag
  - What's the problem with flagging sequences?

# Flagging and stuffing: Byte stream

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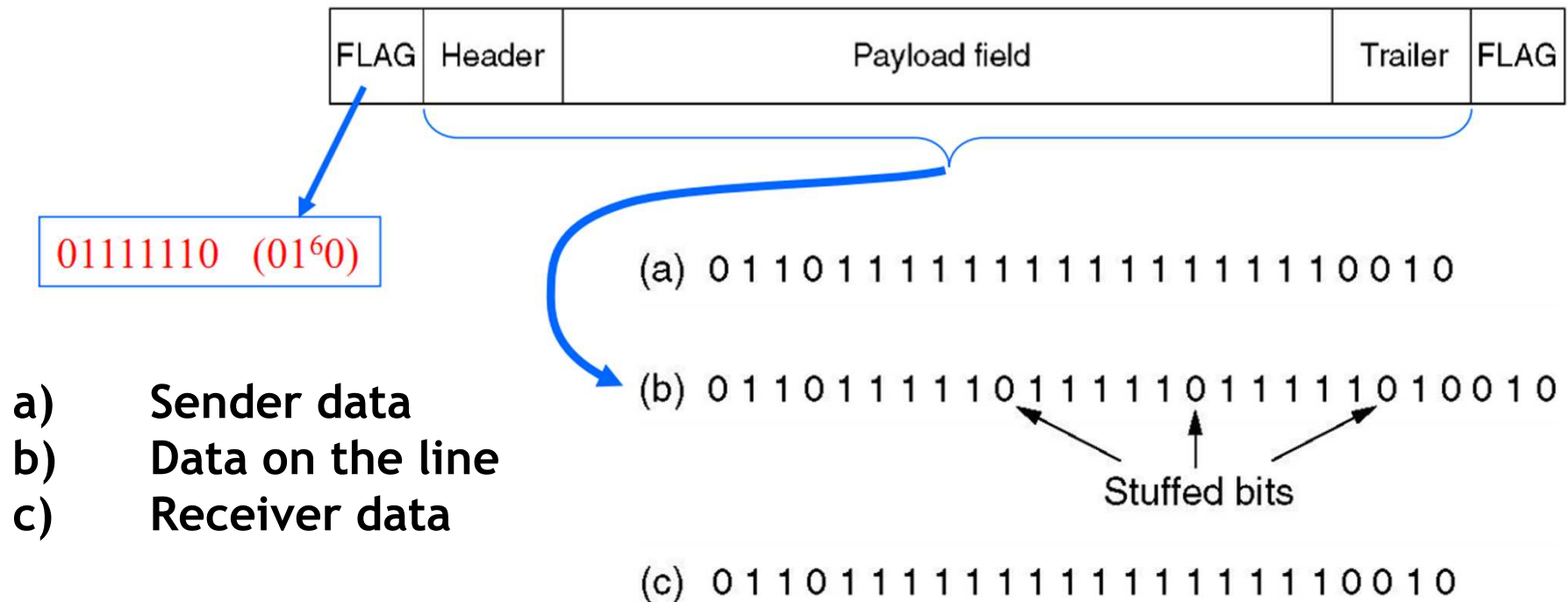


# Flagging and stuffing

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- How do you know where a byte starts?

# Flagging and stuffing: Bit stream



a) => b)

1<sup>5</sup> => 1<sup>50</sup>

b) => c)

1<sup>50</sup> => 1<sup>5</sup>

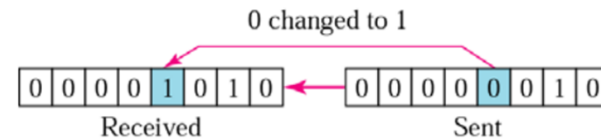
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# *Error detection*

# Types of errors

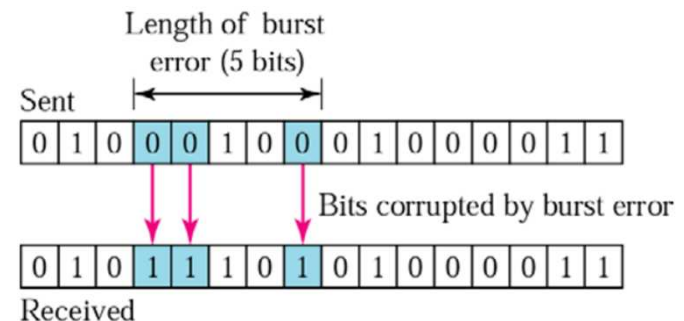
## Simple (individual) errors

- Random
- Independent from errors in other (previous) bits



## Errors in bursts

- Random
- Not independent
- Burst: period with higher probability of error
- Burst length:  $[\# \text{ last bit}] - [\# \text{ first bit}] + 1$



# TO THINK

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What's the math expression for:

- Probability frame has no errors
- Probability frame has errors

Assume

- $p$  - bit error probability (Bit Error Ratio, BER)
- $n$  - frame length
- Independent errors



# TO THINK

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Assume

- $p$  - bit error probability, BER
- $n$  - frame length
- Independent errors

Student A explains to student B why

$$P(\text{frame has no errors}) = (1 - p)^n = (1 - BER)^n$$

Student B explains to student A why

$$\begin{aligned} P(\text{frame has errors}) &= 1 - (1 - p)^n = FER \\ &= 1 - (1 - BER)^n \end{aligned}$$

# Error counting

Assume

- $p$  - bit error probability, BER
- $n$  - frame length
- Independent errors

- How many errors?

- $P(\text{frame has *one or more* errors}) = 1 - (1 - p)^n = FER$

- $P(\text{frame has } i \text{ errors})$

- $i = 0 \Rightarrow P = (1 - p)^n$

- $i = 1 \Rightarrow P = \binom{n}{1} p(1 - p)^{n-1}$

- $i \Rightarrow P = \binom{n}{i} p^i (1 - p)^{n-i}$

Good wired channel

- $p = 10^{-7}$
- $n = 10^4$  (Ethernet frame)
- $p(FER) = 1 - (1 - 10^{-7})^{10^4} \sim 10^{-3}$

Wireless channel

- $p = 10^{-3}$
- $n = 10^4$  (Ethernet frame)
- $p(FER) = 1 - (1 - 10^{-3})^{10^4} \sim 1$

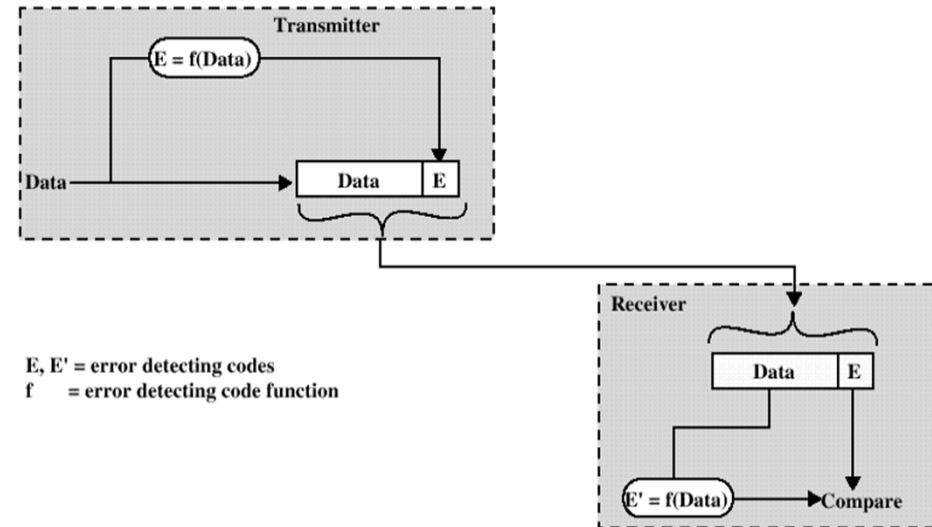
# Error detection techniques - effectiveness

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- Minimum number **d** of bit errors detected in a block of  $n$  bits
  - If fewer than  $d$  errors, errors are detected
  - Maximum distance of code
- Maximum burst length of errors detected **B**

# Error detection techniques - redundancy

- $k \Rightarrow k + r$ 
  - $k$  data bits
  - $r$  redundancy bits
- Check for errors
  - Using  $r$  and  $k$
  - If error, ask to retransmit
- Techniques
  - Parity check
  - Cyclic Redundancy Check, CRC



# Simple parity check

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- Add 1 parity bit every k data bits
  - k+1 bits on the line
- Set parity bit to 1 or 0 to satisfy:
  - Total number of bits with value “1” is even
    - even parity
  - Total number of bits with value “1” is odd
    - odd parity
- 11101**0** 10101**1** 00101**0**
  - Odd or even?

# Simple parity check

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- Allows detection of
  - Simple errors
  - Any odd number of errors in a k+1 block
- What goes by undetected?
  - Even number of errors
  - $P(\text{undetected}) = \sum_{\text{even } i} \binom{n}{i} p^i (1-p)^{n-i}$
- Used in character-oriented protocols

Assume

- p - bit error probability, BER
- n - frame length
- Independent errors

# Bi-dimensional parity

- Blocks represented as rows in a matrix
- One parity bit per
  - Row
  - Column
- Can detect the exact location of single error or multiple even errors in single row/column
- Errors in rectangle configuration are undetectable
  - Minimum code distance  $d=4$

1	0	0	1	0	1	0	1
0	1	1	1	0	1	0	0
1	1	1	0	0	0	1	0
1	0	0	0	1	1	1	0
0	0	1	1	0	0	1	1
Vertical checks							0

Horizontal checks

1	0	0	1	0	1	0	1
0	1	1	1	0	1	0	0
1	1	1	0	0	0	1	0
1	0	0	0	1	1	1	0
0	0	1	1	0	0	1	1
Vertical checks							0

# Internet (IP) Checksum

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- Note: not layer 2!
- IP Checksum
  - Easily implementable in software
  - 1's complement sum of 16 bit words
  - **d**=2
- 1's complement sum
  - Mod-2 addition with carry-out
  - Carry-out bit is added to least significant bit
  - Take 1's complement

	1010011
	<u>0110110</u>
carry-out ①	0001001
Carry wrap-around	<u>0000001</u>
	0001010
One's complement = 1110101	



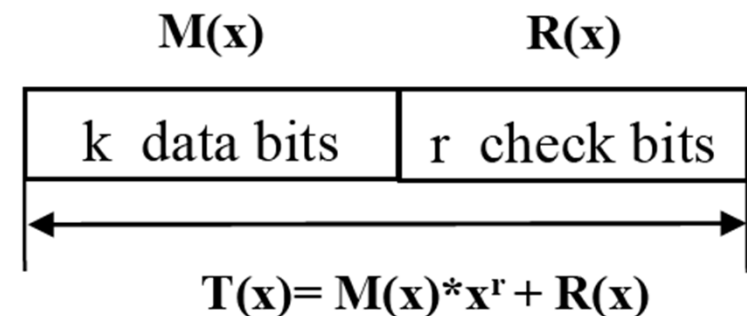
# Cyclic redundancy check CRC

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- Represent bit string as polynomial

$$- 1101001 \Rightarrow x^6 + x^5 + x^3 + 1$$

- $T(x)$  : transmitted bits
- $M(x)$  : message bits
- $R(x)$  : check bits



- Goal: take  $T(x)$  and assess presence of errors
- $G(x)$  : generator polynomial

# CRC - Generator Polynomial

- $G(x)$

- $r+1$  bits long

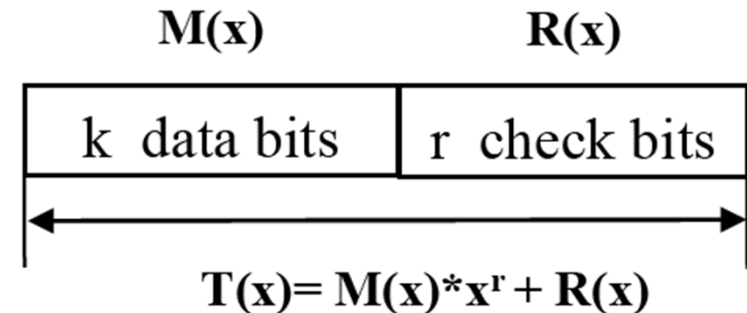
- Find  $R(x)$  such that

- $T(x) = M(x) x^r + R(x) = A G(x)$

- This means that

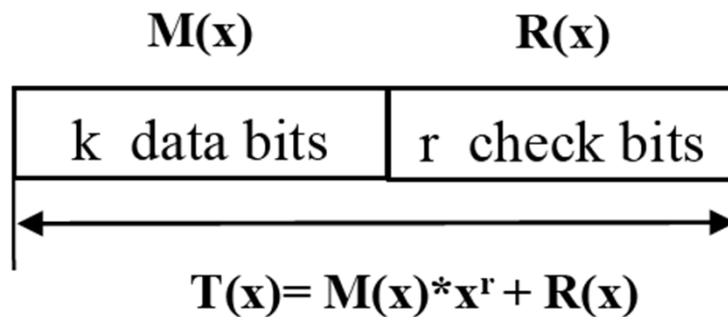
- $M(x) x^r = A G(x) + R(x)$  (mod-2 arithmetic)

- $R(x) = \text{remainder of } M(x) x^r / AG(x)$



# CRC - checking at the receiver

- Divide  $T(x)$  by  $G(x)$ 
  - If remainder is zero  $\Rightarrow$  no errors
  - Errors if remainder non zero



$T'(x)$										$G(x)$				
1	1	0	1	0	1	0	1	1	1	1	0	0	1	
1	0	0	1							1	1	0	0	1
0	1	0	0	0										
	1	0	0	1										
	0	0	0	1	1									
		0	0	0	0									
		0	0	1	1	0								
			0	0	0	0								
			0	1	1	0	1							
				1	0	0	1							
				0	1	0	0	1						
					1	0	0	1						
						0	0	0						
							0	0	0					

0 0 0

R(x)

# CRC - Generating R(x)

- $R(x) = \text{remainder of } M(x)x^r / AG(x)$

- Example

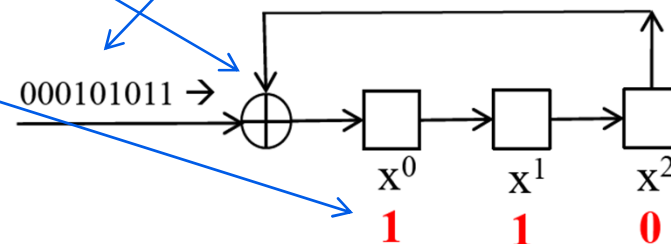
- $r = 3, x^r = x^3; G(x) = x^3 + 1$  (**1001**)
- $M(x) = x^5 + x^4 + x^2 + 1$  (**110101**)
- $M(x)x^3 =$   
 $x^8 + x^7 + x^5 + x^3$  (**110101**)
- $R(x) = x + 1$
- $T(x) = M(x)x^3 + x + 1$   
 $= x^8 + x^7 + x^5 + x^3 + x + 1$   
 $= 1101011$

$M(x) * x^3$								$G(x)$			
1	1	0	1	0	1	0	0	1	0	0	1
1	0	0	1					1	1	0	0
0	1	0	0	0							
1	0	0	1								
0	0	0	1	1							
0	0	0	0								
0	0	1	1	0							
0	0	0	0								
0	1	1	0	0							
1	0	0	1								
0	1	0	1	0							
1	0	0	1								
0	0	1	1								

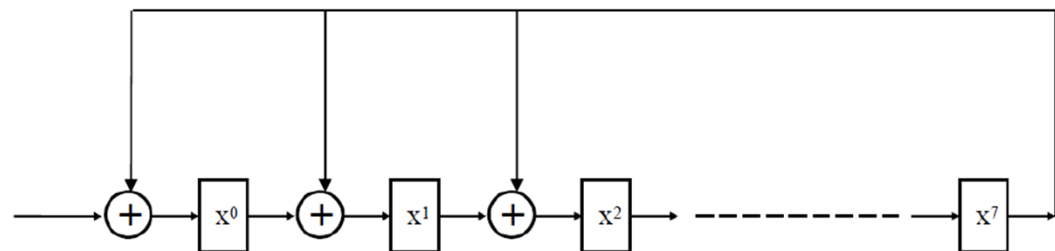
**R(x)**

# CRC - Generating R(x): hardware, shift registers

- $G(x) = x^3 + 1$
- $M(x) x^3 = x^8 + x^7 + x^5 + x^3$  (110101000)
- $R(x) = x + 1$  (011)



- $G(x) = x^8 + x^2 + x + 1$



# CRC - Performance

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- For  $r$  check bits CRC can detect:
  - All patterns of 1,2, or 3 errors ( $d > 3$ )
  - All bursts of errors of  $r$  or fewer bits
  - All errors consisting of an odd number of inverted bits
- ITU-16:  $r=16$ ,  $G(x)=$ 
  - $x^{16} + x^{12} + x^5 + 1$  (1000100000100001)
- ITU-32:  $r=32$ ,  $G(x)=$ 
$$x^{32} + x^{26} + x^{23} + x^{22} + x^{16} + x^{12} + x^{11} + x^{10} + x^8 + x^7 + x^5 + x^4 + x^2 + x^1 + 1$$

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# *Automatic Repeat Request (ARQ)*

# Motivation

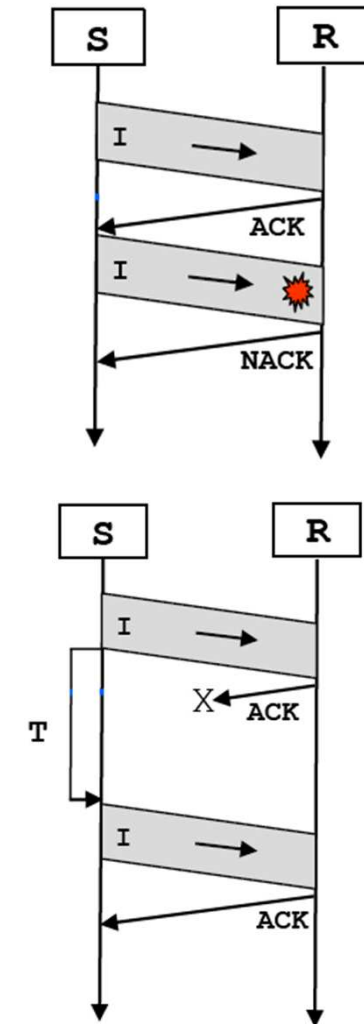
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- When errors are detected in a frame
- Receiver asks for retransmission
- ARQ
  - Automatic retransmission of:
    - Packets with errors
    - Missing packets
- Stop and wait
- Go back N
- Selective repeat



# Stop and Wait ARQ

- Sender: sends frame (DATA)
  - Waits for acknowledgement
- Receiver: receives frame
  - If no errors in frame: send ACK
  - If errors: send NACK
- Sender:
  - receives ACK => transmit new frame
  - receives NACK => retransmit frame
- If frame, ACK, NACK is lost?
  - Timeout T

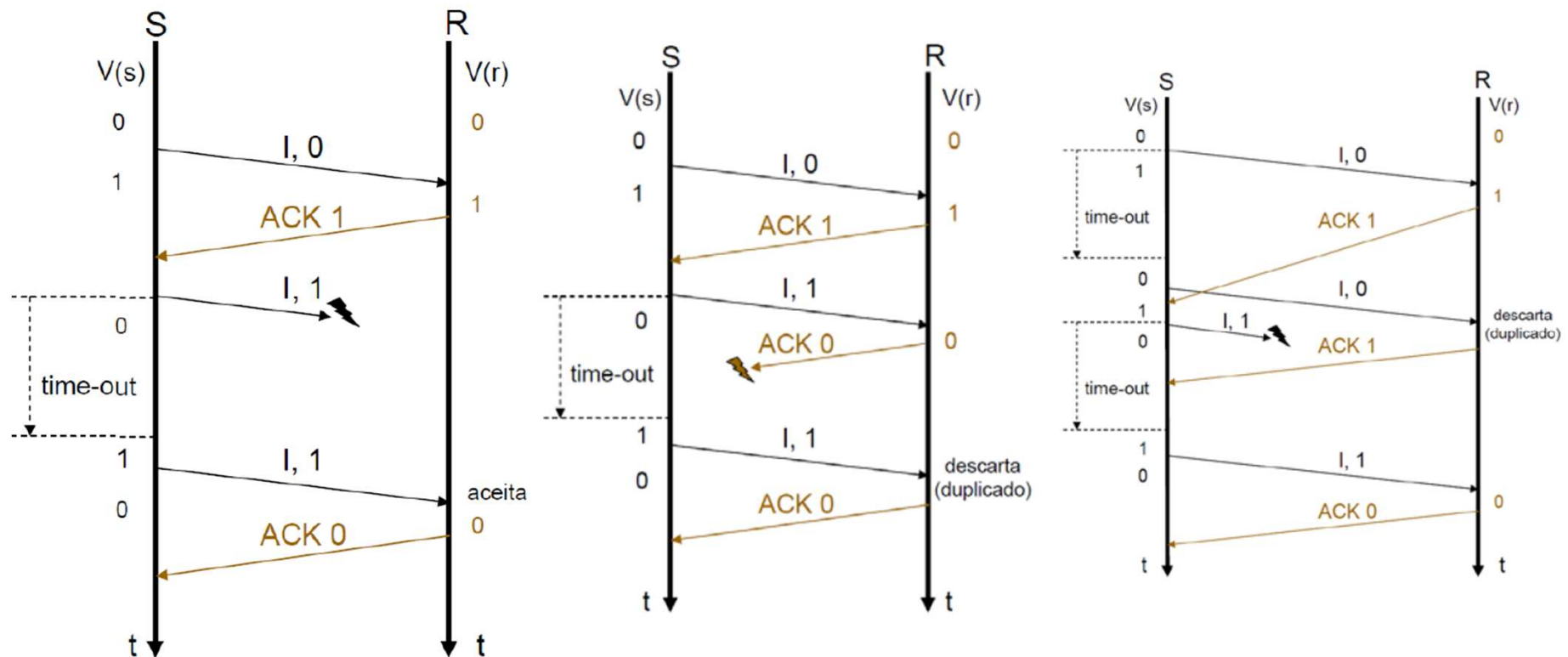


# Sequence numbers

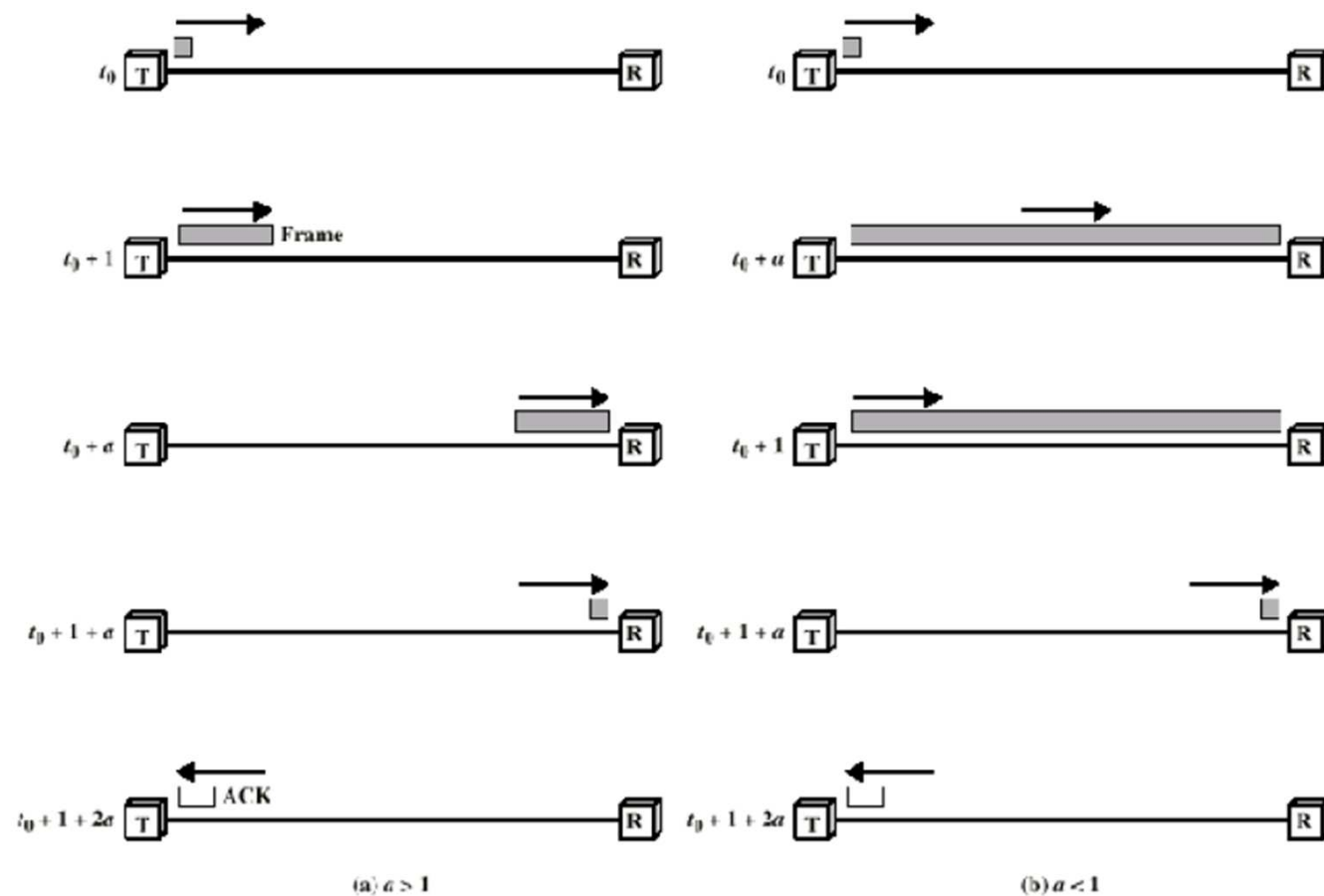
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- Problems
  - Receiver: is this a new frame or retransmission?
  - Sender: which frame is ACKed / NACKed?
- Solution: sequence numbers
  - Frames numbered
  - ACK numbered
    - ACK(i) means receiver is waiting for frame i
  - No NACK required
  - Module 2 sequence numbers

# Examples



# Efficiency



Stop-and-Wait Link Utilization (transmission time = 1; propagation time =  $a$ )

# Efficiency

- Propagation and transmission

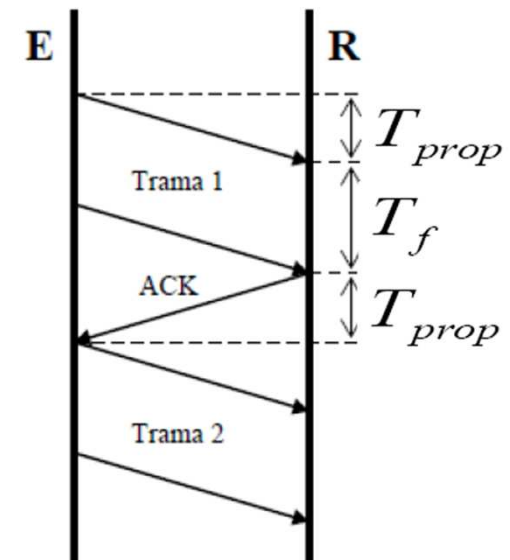
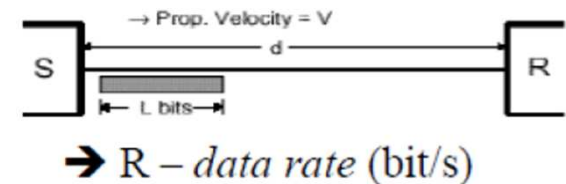
- $T_{prop} = \tau = \frac{d}{V}$

- $T_f = \frac{L}{R}$

- Efficiency

- $a = \frac{T_{prop}}{T_f}$

- $S = \frac{T_f}{T_{prop} + T_f + T_{prop}} = \frac{1}{1 + 2a}$



# Efficiency examples

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- WAN ATM

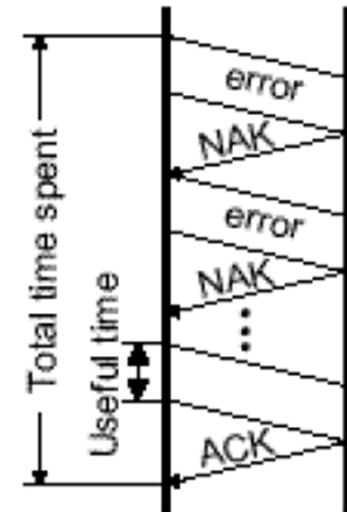
- $L = 424 \text{ bit}$ ;  $R = 155.52 \text{ Mbit/s}$ ;  $T_f = 2.7 \mu\text{s}$
- $d = 1000 \text{ km}$ ; fiber optics  $5 \mu\text{s/km} \Rightarrow T_{\text{prop}} = 5 \mu\text{s}$
- $a = 1852$ ,  $S = 0.0003$

- LAN

- $L = 1000 \text{ bit}$ ,  $R = 10 \text{ Mbit/s}$ ,  $T_f = 100 \mu\text{s}$
- $d = 0.1 \sim 10 \text{ km}$ ; coax  $4 \mu\text{s/km} \Rightarrow T_{\text{prop}} = 0.4 \sim 40 \mu\text{s}$
- $a = 0.004 \sim 0.4$ ;  $S = 0.55 \sim 0.99$

# Efficiency with errors

- $P_e = \text{FER}$
- $P(A=k)$ 
  - Probability of k attempts required for successful transmission
  - $P(A = k) = p_e^{k-1}(1 - p_e)$
- $E(A)$ 
  - Expected number of attempts
  - $E(A) = \sum_{k=1}^{+\infty} kP(A = k) = \frac{1}{1-p_e}$
- Efficiency
  - $S = \frac{T_f}{E(A)(T_f + 2T_{prop})} = \frac{1}{E(A)(1+2a)} = \frac{1-p_e}{1+2a}$



# TO THINK

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Assume sender and receiver are far apart

- Why is efficiency smaller?
- How can the efficiency be improved?

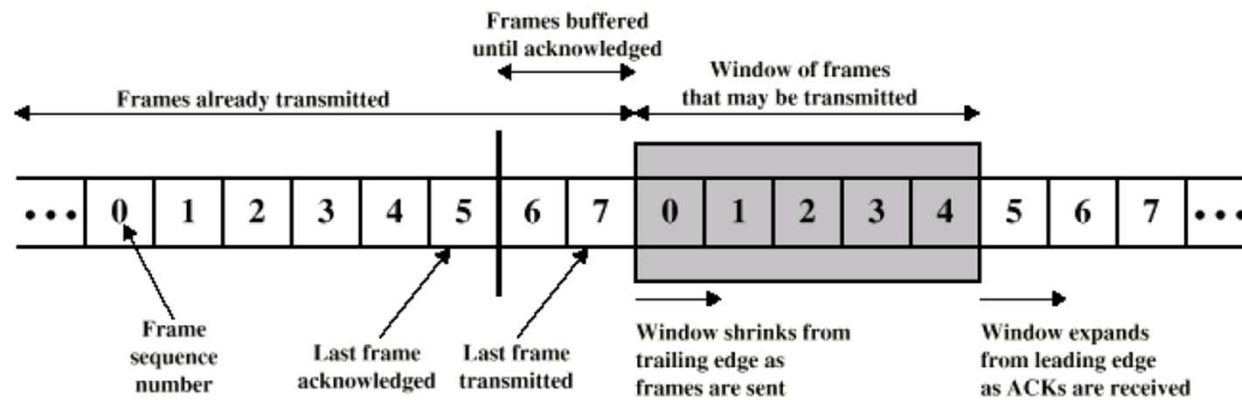


# Go back N ARQ (AKA Sliding window)

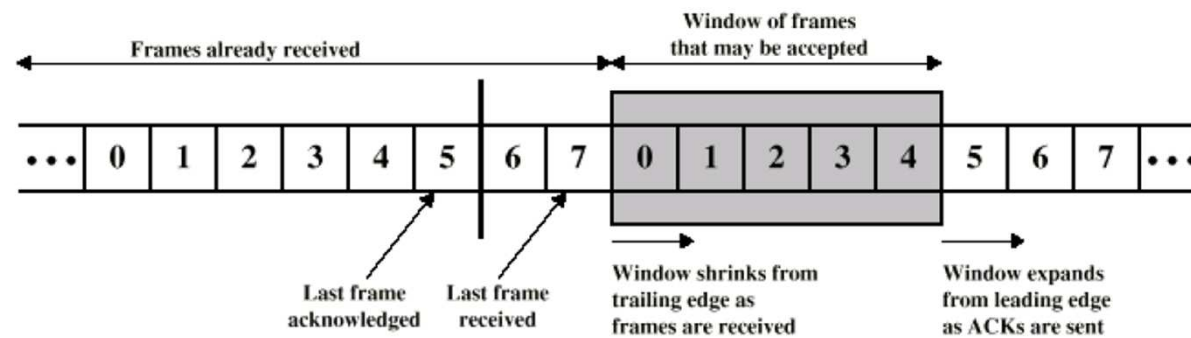
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- Stop and wait inefficient when
  - $T_{\text{prop}} > T_f$  ( $a > 1$ )
  - Single frame per RTT
- Go back N
  - new packets sent before confirmation of previous packets
  - sliding window
    - range of packets that can be sent
    - window slides with acknowledgements

# Sliding window model

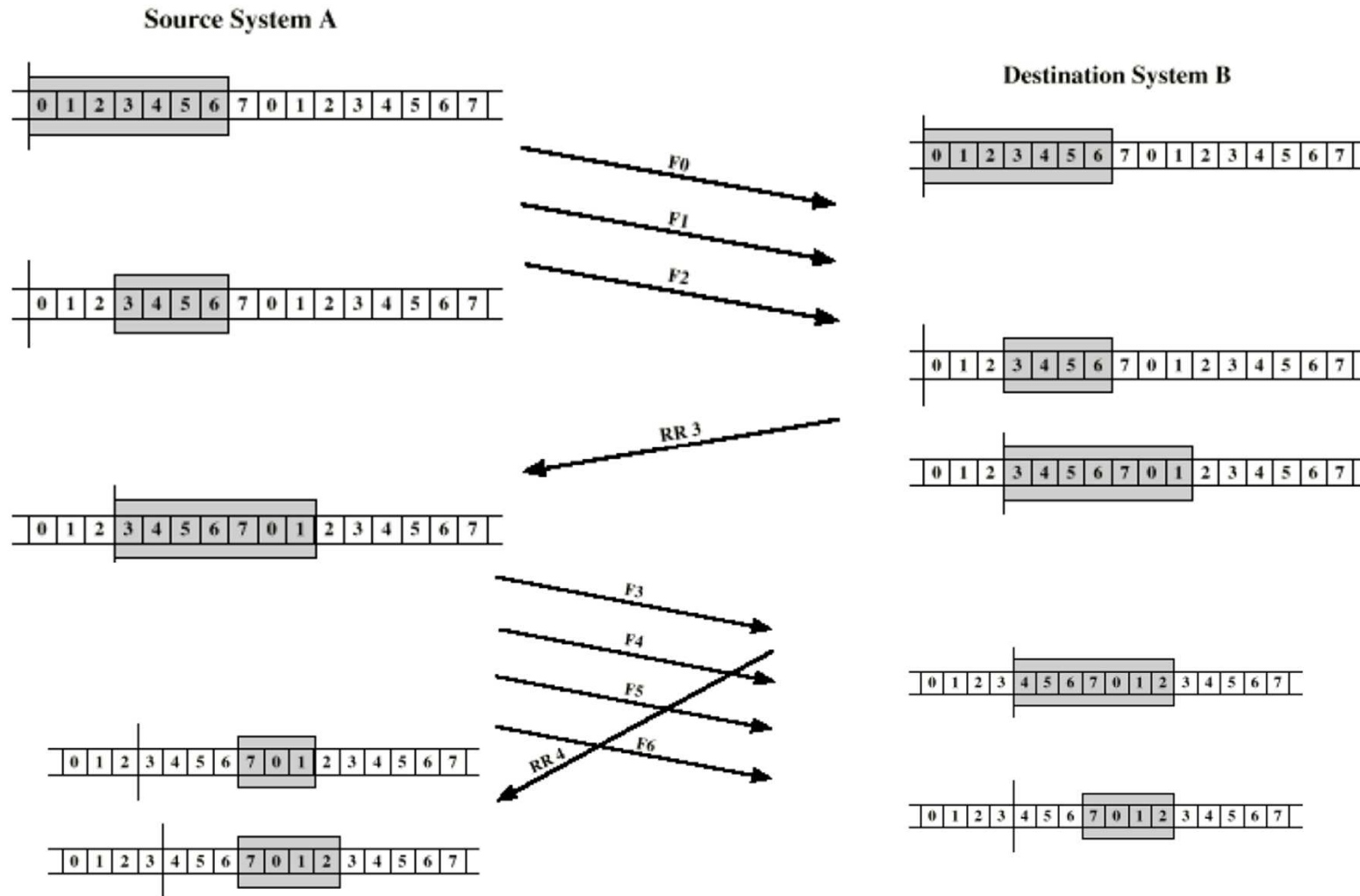


(a) Sender's perspective



(b) Receiver's perspective

# Example



# Go back N basic behavior

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- Sender
  - May send up to  $W$  frames without RR (ack)
  - Frames  $I(k)$  are numbered sequentially
  - Cannot send  $I(k+W)$  until reception of  $RR(k)$
- Receiver
  - Does not accept frames out of sequence
  - Sends  $RR(k)$  indicating
    - All packets up to  $k-1$  have been received
    - The next expected frame is  $k$

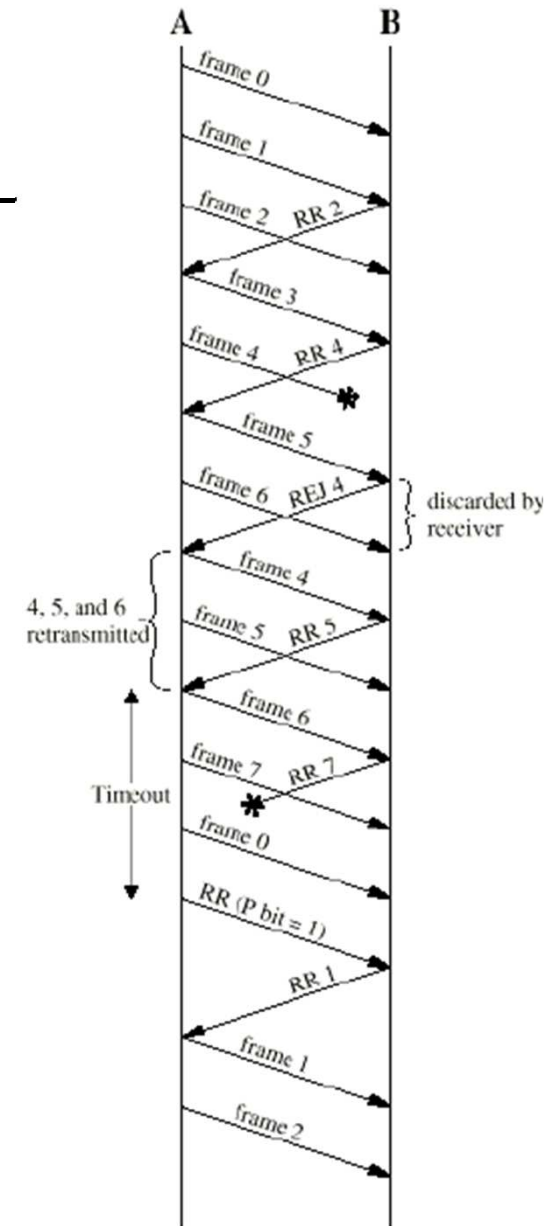
# Go back N ARQ

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- Sequence numbers
  - Module  $M$  ( $0..M-1$ )
  - $n$  bits to represent in header
  - $2^k-1$  maximum window
- Extensions to basic behavior
  - Piggy backing for bidirectional flows
  - RR sent in data packets of opposite direction

# Go back N under errors

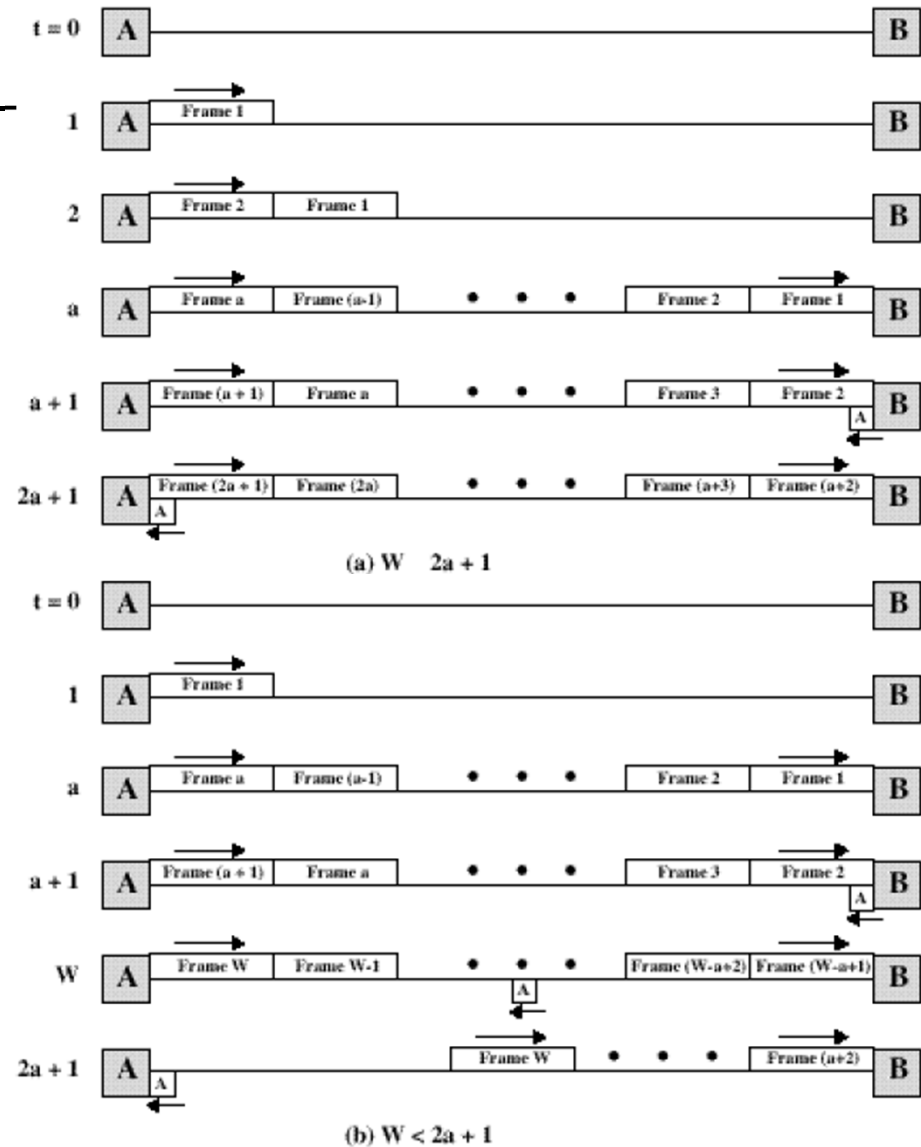
- Discards frames with errors
- Frame out of sequence
  - 1<sup>st</sup>: receiver sends REJ(k)
    - k is next in-sequence frame expected
  - Following: discard, no REJ
- Sender receives REJ(k)
  - Retransmits frames k, k+1, ...
  - Continues with sliding window
- Upon sender timeout
  - Requests receiver to send RR



# Efficiency

- If  $W \geq 1 + 2a$
- $\Rightarrow S = 1$

- If  $W < 1 + 2a$ :
- $\Rightarrow S = W / (1 + 2a)$



# Selective reject ARQ

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- Also uses sliding window
- Receiver
  - accepts out-of-sequence frames
  - Confirms negatively missing frames (SREJ)
  - Confirms blocks of frames with RR
- Sender retransmits only SREJ frames
- Suitable for large  $W$
- Maximum window size is  $W = \frac{M}{2} = 2^{k-1}$



# Efficiency under errors

- $p_e = \text{FER}$

- Go back N

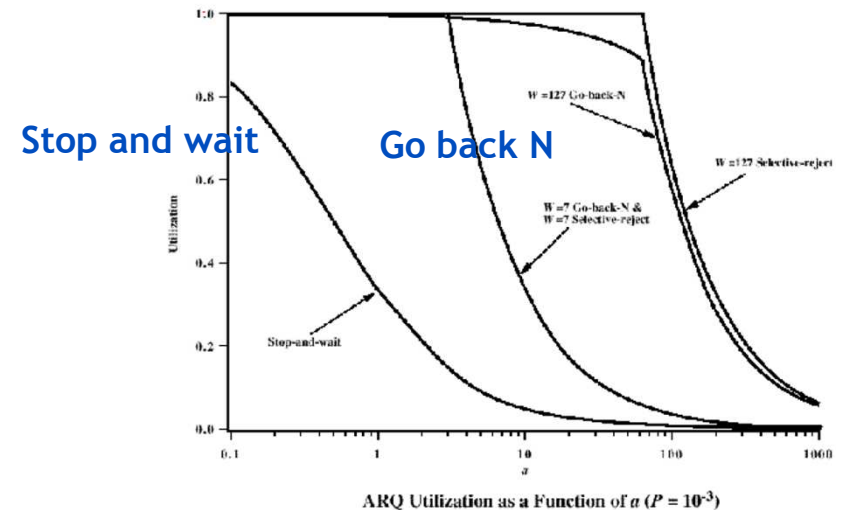
$$- S = \frac{(1-p_e)}{1+2ap_e}, W \geq 1 + 2a$$

$$- S = \frac{W(1-p_e)}{(1+2a)(1-p_e+Wp_e)}, W < 1 + 2a$$

- Selective reject

$$- S = (1 - p_e), W \geq 1 + 2a$$

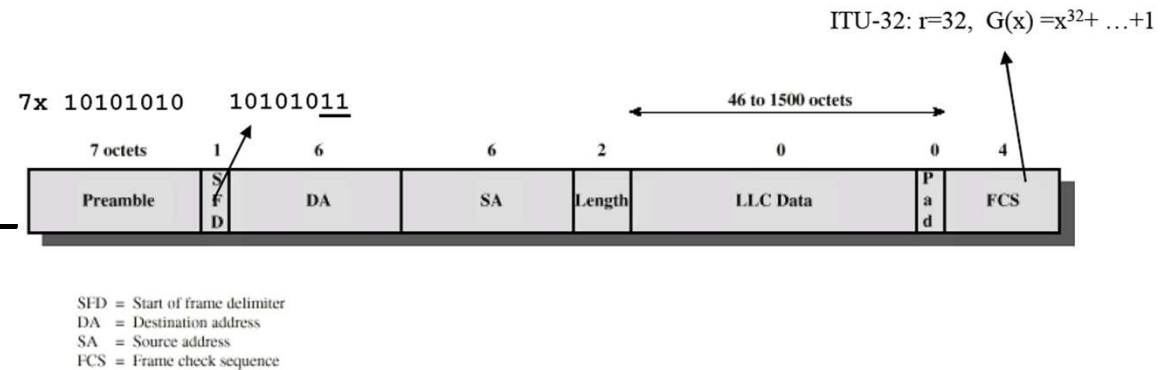
$$- S = \frac{W(1-p_e)}{(1+2a)}, W < 1 + 2a$$



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# *Framing, error detection, and ARQ in common networks*

# Ethernet



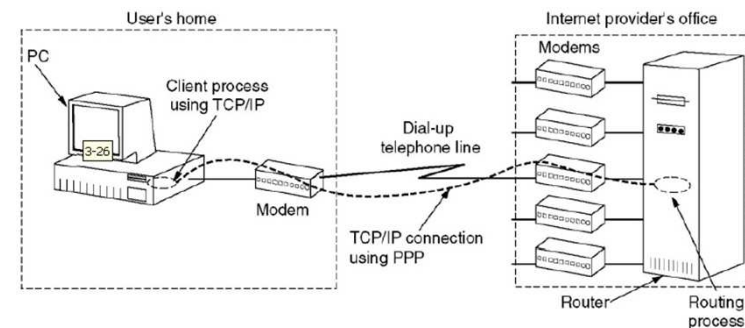
- Framing
  - Preamble + start frame delimiter
  - End of frame: end of Manchester transitions
- Error detection
  - Frame check sequence, CRC ITU-32
- No ARQ
  - Very low BER, low FER
  - Strong CRC, discards frames with errors

# PPP, Point-to-Point protocol

- Framing
  - Flags 0x7E, ESC 0x7D

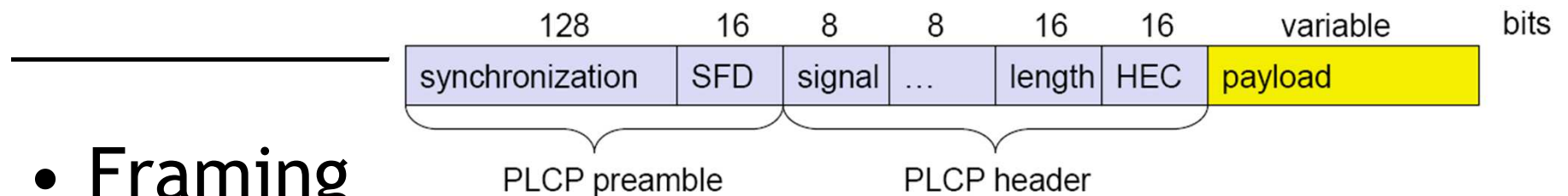
Bytes	1	1	1	1 or 2	Variable	2 or 4	1
	Flag	Address	Control	Protocol	Payload	Checksum	Flag
	01111110	11111111	00000011				01111110

Byte stuffing

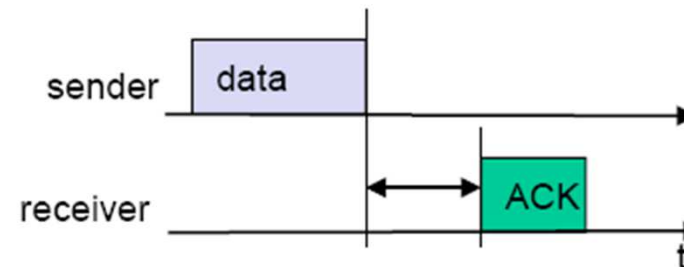


- Error detection negotiable
- No ARQ

# Wireless LAN



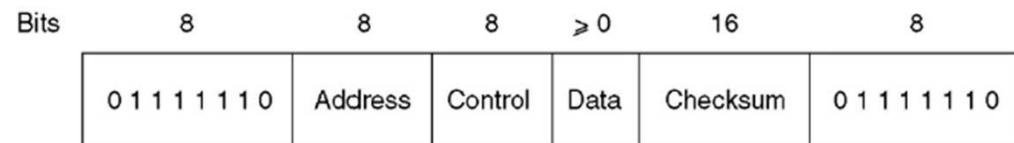
- Framing
  - 1010101010... synchronization
  - Start frame delimiter
  - Length
- Header error check
  - ITU-16 CRC
- ARQ
  - Modified Stop and Wait



# High-Level Data Link Control

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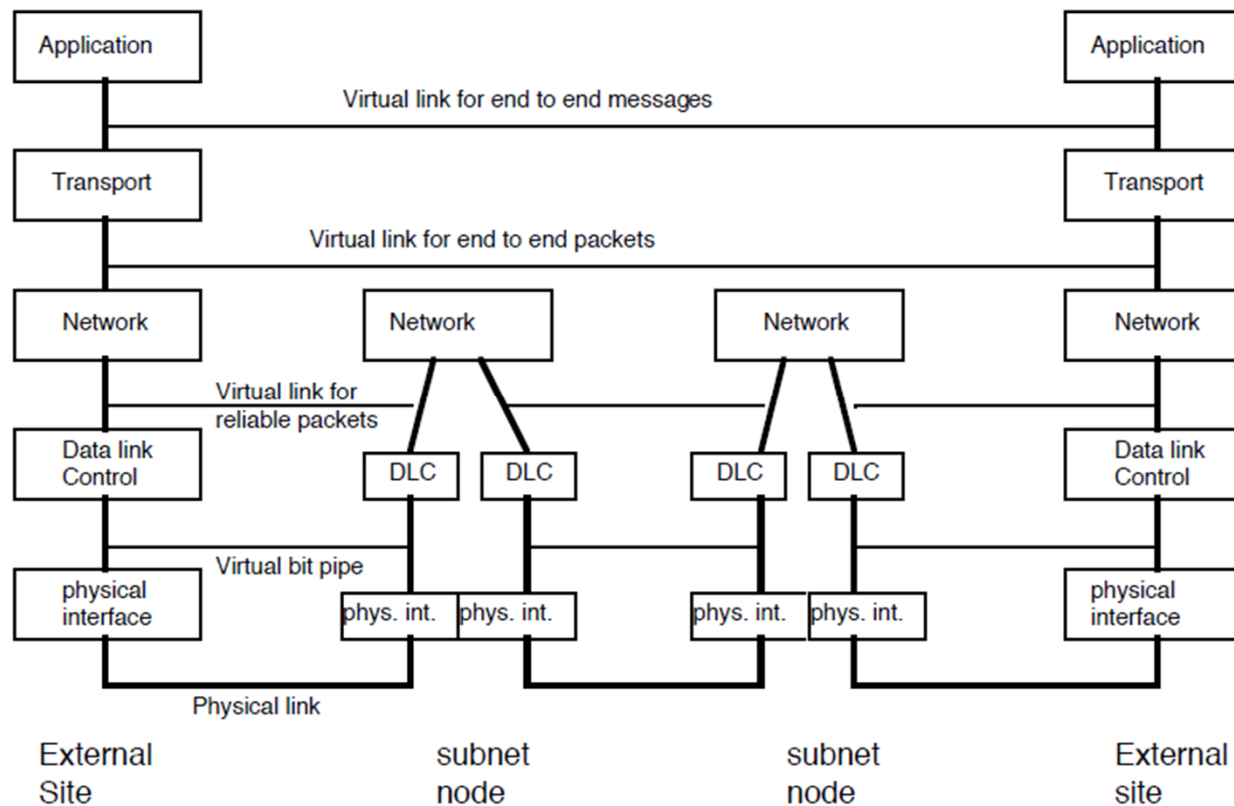
- HDLC, bit oriented
- Framing
  - Flags
  - Bit stuffing
- Error detection
  - ITU-16 CRC
- ARQ
  - Selective reject
- Basis for GSM/GPRS/UMTS, ...



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# *Reliability in the protocol stack*

# Reliability in the protocol stack



FEC, ARQ

ARQ

ARQ

FEC

Forward Error Correction, channel coding

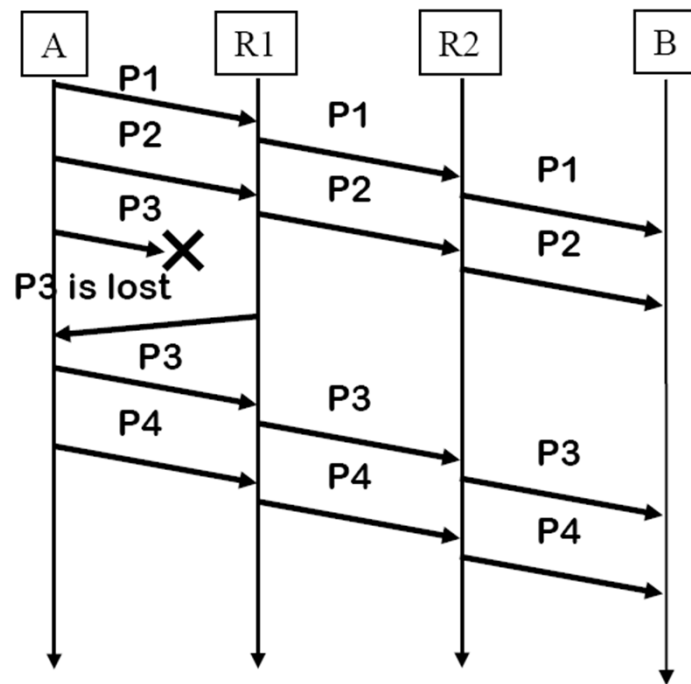


# BER and FER

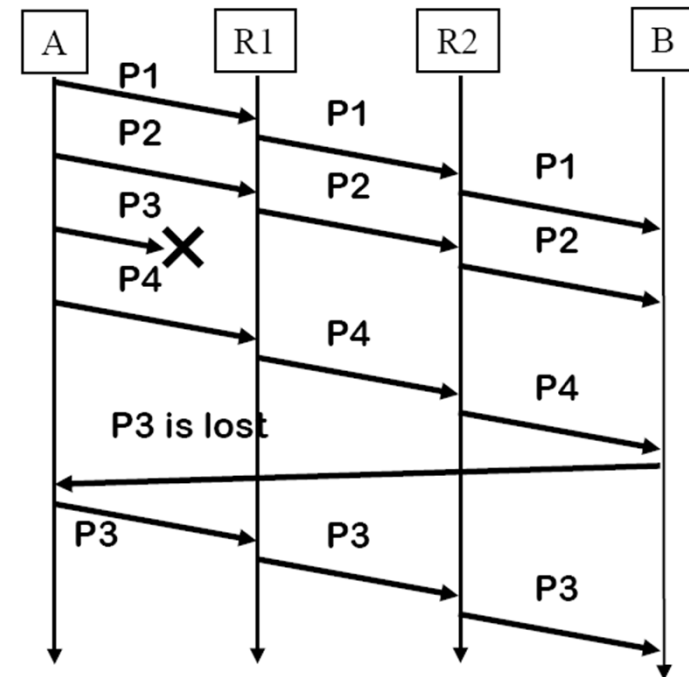
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- Layer 2 service either:
  - Delivers packets without errors
  - Discards packets
- Layer 2 transforms bit errors into frame errors, BER => FER
- ARQ solutions for FER
- Two strategies
  - Link-by-link ARQ
  - End-to-end ARQ

# Link-by-link vs. End-to-end ARQ



Link-by-link



End-to-end

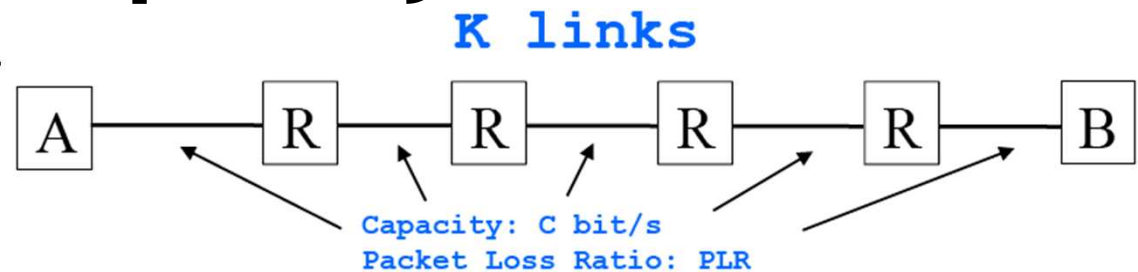
# TO THINK

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Link-by-link vs. End-to-end ARQ

- Which provides lower delay?
- Which provides higher bitrates?

# End-to-end capacity



- Assume no losses in queues
  - Packet Loss Ratio (PLR) = FER
- Link capacity =  $C \cdot (1 - \text{PLR})$
- End-to-end
  - LL ARQ,  $C_{LL} = C \cdot (1 - \text{PLR})$
  - EE ARQ,  $C_{EE} = C \cdot (1 - \text{PLR})^k$
- EE ARQ is inefficient

K	PLR	$C_{EE}$	$C_{LL}$
10	0.05	$0.6 C_{EE}$	$0.95 C_{LL}$
10	0.0001	$0.9990 C_{EE}$	$0.9999 C_{LL}$

# Complexity

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- LL ARQ is more complex
  - Requires intermediary nodes in the network to process individual flows
  - And store frames in case of retransmission request

# ARQ in TCP/IP model

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- Packet losses are repaired:
  - At the DLL on lossy channels (e.g. wireless)
  - At the end systems, transport/application

# **HOMEWORK**

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- Review slides
- Read:
  - Tanenbaum 3.1, 3.2, 3.6, 3.7
  - Bertsekas - 2.3, 2.4
- Do your Moodle homework