

## Year 2 - CY2019 Allocation Renewal

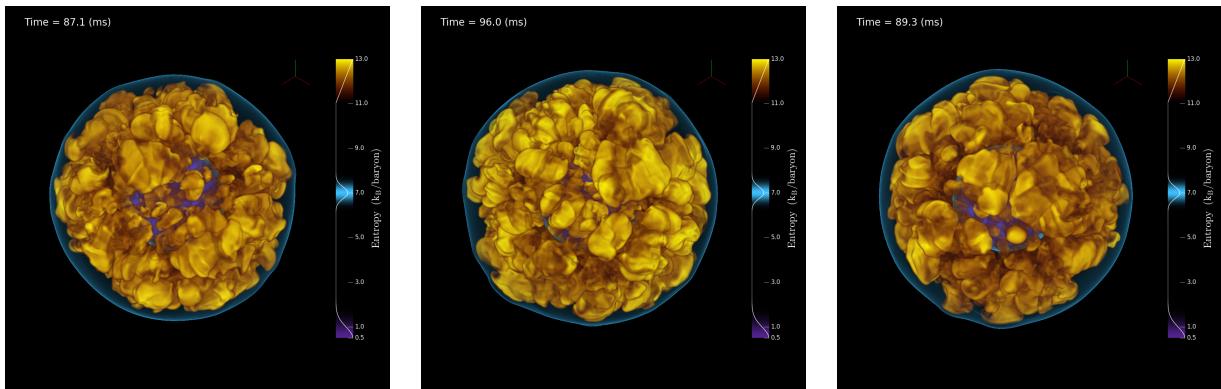
### Achievements in Year 1

#### 1 Progress on Year 1 Milestones

##### 1.1 3D simulations of magnetorotational core-collapse supernovae

One of the key objectives for Year 1 of our INCITE project was to execute a parameter study of magnetorotational core-collapse supernova (CCSN) simulations using high-fidelity neutrino transport and magnetohydrodynamics (MHD) as implemented in our Spark-M1 application, built in the FLASH simulation framework (Fryxell et al., 2000; Dubey et al., 2009). Spark-M1 utilizes the new Spark high-order MHD solver (Couch, 2017), the M1 two-moment explicit neutrino transport method (Shibata & Taniguchi, 2011; O’Connor, 2015; O’Connor & Couch, 2018b), an accurate and efficient multipole gravity solver (Couch, 2013) including the general relativistic monopole correction (Marek et al., 2006), an approximate 21-isotope nuclear network for accurately tracking the composition at low densities (Couch & Ott, 2015), and the FLASH framework for adaptive mesh refinement (AMR), I/O, and runtime management. The methods and physics included in Spark-M1 make it one of the most high-fidelity and high-performance CCSN simulation tools in the world.

The Spark MHD solver (Couch, 2018) implements the cell-centered method of generalized Lagrangian multipliers (GLM; Dedner et al., 2002; Mignone et al., 2010) to control the growth of the divergence of the magnetic field. The GLM-MHD scheme employs hyperbolic advection and parabolic damping of divergence errors in order to avoid expensive elliptic divergence cleaning (e.g., Jiang & Wu, 1999) or complicated staggered-mesh constrained transport (e.g., Gardiner & Stone, 2005; Lee et al., 2009; Lee, 2013). Spark implements the GLM-MHD scheme via a finite-volume approach using high-order primitive reconstruction, multiple Riemann solvers for flux calculation, and method-of-lines time integration using multi-stage strong stability preserving (SSP) low-storage Runge-Kutta (RK) integrators of second- and third-order (e.g., Gottlieb & Shu, 1998). For realistic, non-Gamma-law equations of state, Spark avoids the approach of Colella & Glaz (1985) used in other FLASH solvers and adopts the volumetric internal energy,  $\rho e$ , as an auxiliary thermodynamic primitive variable instead, as in Almgren et al. (2010). We have



**Figure 1:** Volume renderings of entropy from three of the 3D magnetorotational CCSN simulations that we are currently running on *Mira* as part of this INCITE project. Shown are cases with magnetic fields (left), magnetic fields and rotation (middle), and no magnetic fields but fast rotation (right). All of these simulations are currently at around 100 ms post-bounce and are on-going.

found this approach to be generally more robust but either method should be technically equivalent (e.g., [Zingale & Katz, 2015](#)). For our CCSN application, we use fifth-order WENO reconstruction ([Borges et al., 2008](#)), second-order time integration, and the HLLD approximate Riemann solver which includes MHD waves ([Miyoshi & Kusano, 2005](#)).

Neutrino transport in Spark-M1 is carried out using the M1 two-moment explicit approach described in [O'Connor \(2015\)](#); [O'Connor & Couch \(2018b,a\)](#). The M1 scheme solves the first two angular moments of the Boltzmann equation for neutrinos and utilizes an analytic closure for the higher-order moments. The neutrino fluxes, both in real space and in energy space, are computed explicitly as a hyperbolic system resulting in favorable performance and scaling properties (at the cost of time step sizes limited by the speed of light) while the matter-radiation source terms are computed implicitly. This implicit solve is completely local and requires solving only a 4x4 matrix. Our M1 solver is fully velocity-dependent, except in the calculation of the explicit flux terms, which is done to  $\mathcal{O}(v/c)$ . We currently do not include inelastic neutrino scattering in the multidimensional version of our transport solver although inelastic neutrino electron scattering is included in the 1D implementation in GR1D ([O'Connor, 2015](#)). We plan to implement and include inelastic scattering in our 3D simulations in Years 2 and 3 of this project.

The two-moment M1 approach is inherently more accurate than zeroth-moment only approaches such as flux-limited diffusion (e.g., [Bruenn et al., 2013](#); [Dolence et al., 2015](#); [Lentz et al., 2015](#)). M1 does not require a flux-limiter-based closure for the radiation fluxes as they are solved for directly. Furthermore, the analytic closure we currently use for the moments beyond the first is simple and straightforward yet shows encouraging agreement with 1D Boltzmann and Monte Carlo neutrino transport calculations ([O'Connor, 2015](#); [Murchikova et al., 2017](#)). As compared with flux-limited diffusion, M1 does not suffer from the inability to capture “shadows” inherent to FLD schemes. A known limitation of M1 is cases in which distinct beams of radiation intersect, causing radiation “shocks.” The M1 solution in such cases becomes highly diffuse at the intersection. This is a problem in, e.g., radiation hydrodynamic calculations of accretion disks. For CCSNe, however, the radiation field is highly forward peaked and cases in which distinct beams of radiation might cross are essentially non-existent. Hence, M1 is *ideally* suited for the CCSN problem due to its accuracy (for the specific problem) and efficiency. In addition, the severe limitation of time steps determined by the speed of light is not so drastic in CCSNe since the explicit time step is already just a factor of a few larger than this thanks to the enormous sound speeds in the proto-neutron star (PNS). Another significant advantage of M1 is that it is a fully multidimensional transport scheme, i.e., the solution at a given grid point is dependent on the fluxes from every direction around that point. This is distinct from the often-adopted “ray-by-ray” approximation (e.g., [Bruenn et al., 2013, 2016](#); [Müller et al., 2012](#); [Hanke et al., 2013](#); [Melson et al., 2015](#); [Lentz et al., 2015](#)) in which the transport problem is solved only along discrete radial rays. The advantages of M1 for neutrino transport in CCSNe have not gone unnoticed and a number of groups are now exploring or adopting this approach ([Just et al., 2015](#); [Kuroda et al., 2016](#); [Skinner et al., 2016](#); [Roberts et al., 2016](#)).

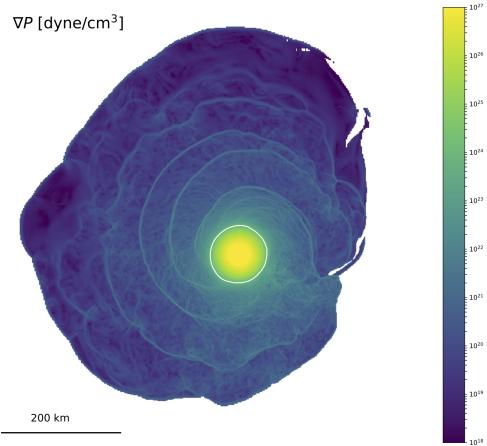
In our FLASH CCSN application we have assumed that the composition of the matter throughout the entire computational domain is determined by nuclear statistical equilibrium (NSE). This common approximation (e.g., [Burrows et al., 2007](#); [Ott et al., 2008](#); [Dolence et al., 2015](#); [Skinner et al., 2016](#); [Roberts et al., 2016](#); [Kuroda et al., 2016](#)) is appropriate at high densities and temperatures where the nuclear reaction rates are sufficiently fast to establish equilibrium essentially instantly but becomes increasingly incorrect at low densities such as those in the silicon and

oxygen shells surrounding the collapsing iron core. Critically, correctly predicting the explosion energy or nucleosynthetic products such as radioactive nickel can be severely impacted by the inappropriate assumption of NSE (Bruenn et al., 2016). Bruenn et al. (2016) advocate the use of an approximate nuclear network in regions that are not in NSE, while other groups (e.g., Müller et al., 2012; Melson et al., 2015) use a “flashing” approach rather than a full network calculation. We have recently implemented a method for transitioning to a nuclear network and appropriate EOS at low densities. Our new approach blends the pressures between the high- and low-density EOS’s to prevent spurious pressure discontinuities and uses an auxiliary variable to track whether a zone is entering or exiting NSE, allowing us to appropriately set the composition in the transition region.

So far in 2018, we have made good progress in executing a parameter study of magnetorotational CCSN simulations. Figure 1 shows volume renderings of entropy from three of the five high-resolution 3D simulations we are running on *Mira* and *Theta*. We opted to use the  $15-M_{\odot}$  progenitor from Heger et al. (2005) in order to facilitate a direct comparison to the recent results of Summa et al. (2018). We are executing five different cases for this one progenitor: (1) non-rotating, non-magnetic; (2) rotating, non-magnetic; (3) non-rotating, magnetic; (4) rotating, magnetic; and (5) rapidly rotating, non-magnetic. For rotating cases, we take the rotation profile directly from the progenitor model that was evolved with rotation and magnetic fields and prescriptions for angular momentum transport (Heger et al., 2005). For the rapidly-rotating case, we simply multiply the angular speed of the profile by two, making the rate of rotation similar to one of the models explored by Summa et al. (2018). The magnetic field is initialized with a quasi-poloidal field geometry with the peak strength set to match the field strength of the original progenitor model, about  $10^8$  G. The peak angular speed of this model is about  $0.2 \text{ rad s}^{-1}$  ( $0.4 \text{ rad s}^{-1}$  for the “rapidly” rotating case).

This is, in fact, not very rapid rotation or field strength and so in these models we do not expect to see dramatic, magnetorotationally-dominated dynamics. Rather, we aim to explore the impact of plausibly typical rotation rates and field strengths on the CCSN mechanism.

The 3D magnetorotational CCSN simulations are on-going and we fully expect to reach our target final simulation times by the end of Year 1. Already, we are seeing an impact of rotation and, to a lesser extent, magnetic fields. We are already seeing that the rotating cases are closer to explosion. The presence of magnetic fields is, so far, having little impact on the gross dynamics of the simulations, but for these initial field strengths it will take a longer period of evolution to build of substantial field strengths. The magnetic fields, even if weak, may still have an impact on the behavior of the turbulence in the gain region and the PNS. This is an aspect of our simulations that we will analyze in detail once the simulations have reached later times. We will also look for the presence of a



**Figure 2:** Equatorial slice plot of the gradient of pressure from a 3D magnetorotational CCSN simulation run as part of our previous INCITE project. The development of a non-axisymmetric rotational instability in the PNS leads to the generation of strong spiral pressures waves. The gravitational wave emission is also significantly amplified.

non-axisymmetric rotational instability in the

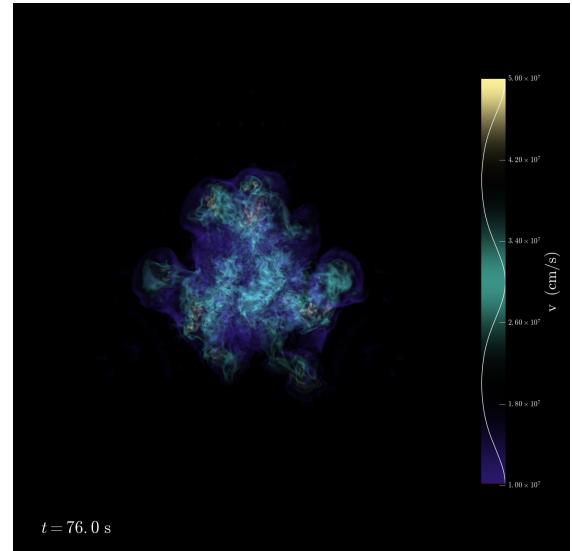
In work based on simulations ran as part of our previous INCITE allocation, we have identified the emergence of such an instability for magnetic and rotating initial conditions. This instability can generate strong pressure waves that transport energy to the gain region, and also leads to very loud gravitational wave signals. An image of the strong pressure waves is shown in Figure 2.

These simulations are currently running in the Capability queue on *Mira*. One simulation is running on *Theta*.

### 1.2 3D Simulations of CCSN Progenitors

One of the most remarkable and exciting results of recent 3D simulations of the CCSN mechanism is the discovery that realistic non-spherical structure in the progenitor star can have a dramatic impact (Couch & Ott, 2013; Couch et al., 2015; Couch & Ott, 2015; Müller & Janka, 2015; Müller et al., 2017; O’Connor & Couch, 2018a). The breaking of spherical symmetry is manifest in the turbulent convection driven by nuclear burning in the cores of massive stars. As a massive star nears collapse, strongly convective burning in the Si and O shells surrounding the iron core can reach speeds of nearly  $1000 \text{ km s}^{-1}$  and is characteristically very large in spatial scale (Arnett & Meakin, 2011; Couch & Ott, 2015; Müller et al., 2016). These convective perturbations will reach the stalled shock shortly after core bounce and can aid neutrino-driven explosions by either enhancing the strength of post-shock turbulence (Couch et al., 2015) or causing large scale “forced shock deformations” (Müller et al., 2017), or both. These results serve to remind us that CCSN mechanism simulations are initial value problems and that the details of our initial conditions matter tremendously! Our work inaugurated the era of detailed investigation into the impact of 3D progenitor structure on the CCSN mechanism (Couch & Ott, 2013, 2015). As part of this INCITE project we are advancing the investigation into 3D progenitor structure substantially. Specifically, we will simulate 3D progenitors including rotation and magnetic fields.

A key milestone for Year 1 is to carry out new, high-fidelity 3D simulations of the final minutes of stellar evolution to the point of iron core collapse. For these simulations we will use the Spark MHD solver (Couch, 2018) and include rotation and magnetic fields *for the first time ever* in a 3D CCSN progenitor simulation. We are using 1D massive star evolution models constructed using MESA (Paxton et al., 2011, 2013, 2015), initialized in 3D approximately five minutes prior to core collapse. We plan to run two, full-3D progenitor simulations in Year 1: one non-rotating, non-magnetic case and one rotating, magnetic case. In the original proposal, we planned four 3D progenitor simulations in Year 1. Our test simulations executed in octant geometry have shown that the expense of the simulations increases significantly as the stars approach collapse. This is due to more vigorous nuclear burning in the core, increasing the expense of the nuclear network solve. Therefore, in order to ensure that we can simulate sufficiently long time



**Figure 3:** 3D progenitor simulation run in octant geometry as a forerunner of our planned Year 1 production simulations. Shown is the magnitude of the velocity. Peak convective speeds reach over  $500 \text{ km/s}$  prior to core collapse.

scales, we have opted to begin with just two simulations.

To this point in Year 1, we have made substantial gains in improving our simulation approach for 3D CCSN progenitors. We have improved the OpenMP threading of our nuclear network code. We have improved the efficiency of the empirical load balancing approach our progenitor application uses. We have tested several approaches to the initial mapping of the 1D progenitor model to the 3D domain and have improved our approach to stabilize the initial conditions. We have implemented new, modern reaction rates for electron captures and for key carbon reactions. And, importantly, we have run a test 3D progenitor simulation in octant geometry all the way to core instability and collapse.

We are now ready to begin our 3D progenitor production simulations on *Mira*. For the rotating, magnetic progenitor we are using a MESA model constructed using the magnetic field production and angular momentum transport model of [Spruit \(2002\)](#), as implemented for stellar evolution by [Heger et al. \(2005\)](#); [Paxton et al. \(2015\)](#). This model yields a realistic rotation profile and an estimate for the *strength* of the magnetic field as a function of radius in the star. There is very limited information about the 3D geometry of the field. To address this, we are initializing the field in a random, divergenceless fashion with a typical strength matching the 1D MESA model estimate. We will then allow the field to relax to a quasi-steady-state configuration. This transition should occur on the rotational and convective time scale, both of which are about 30 s. We will simulate roughly 3 to 5 minutes of evolution up to core collapse.

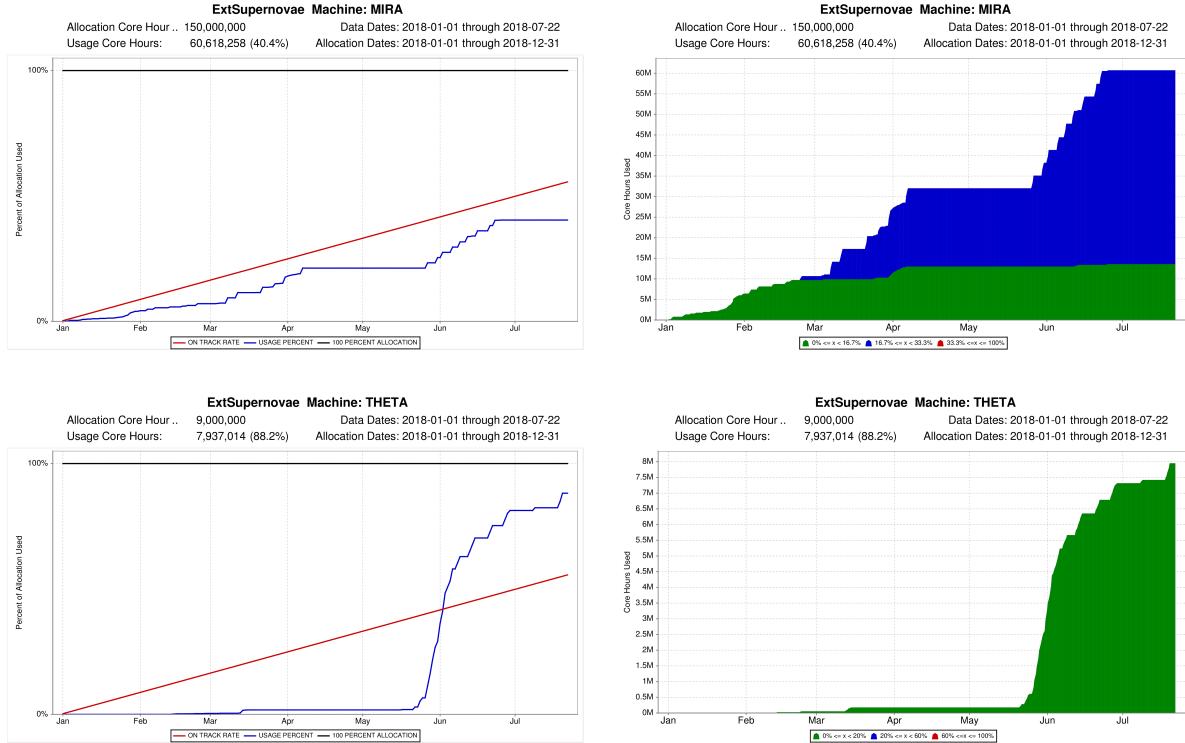
### 1.3 High-resolution Simulation of Magnetorotational Turbulence

Our final simulation milestone for Year 1 is to execute a high-resolution simulation of magnetorotational turbulence in the CCSN gain region. For this simulation, we will use the “rapidly” rotating conditions described above. We will restart the comparable fiducial resolution simulation at around 50 ms post-bounce and allow for higher resolution in the gain layer using AMR. This simulation will require many more zones than the fiducial resolution case and we expect it to, in time, be a standalone Capability-scale simulation. We are now ready to begin this simulation and will do so in the immediate future.

### 1.4 Project Usage

Thus far, we have expended 60.6M core-hours on *Mira*, 40.4% of our 2018 allocation (see Figure 4). We are slightly behind the ideal usage curve, but in Q3 we will commence production 3D progenitor simulations and the high-resolution turbulence simulation, adding a two additional capability-scale jobs to our workflow. Overall, we anticipate catching up quickly to the on-track usage curve. The vast majority of our usage on *Mira* has been at the capability level.

We have so far expended 7.9M core-hours on *Theta*, 88.2% of our 2018 allocation. At beginning of our allocation, we had technical issues with the Intel fortran compiler on *Theta* when enabling OpenMP. After a few weeks of investigation, we decided to switch to GNU fortran compiler. After that, we moved one high-resolution production simulation from *Mira* to *Theta* and tuned our application on *Theta* to continue that simulation. A weak scaling test of restarting that simulation is shown in Figure 5. Figure 5 suggests that the performance is getting worse when using more than 300 nodes on *Theta*. However, we noticed that after the maintenance on May 21, 2018, the wall-clock limit on *Theta* is limited to 6 hours with > 256 nodes and 9 hours with > 384 nodes. Since our simulations require more than 50 of restarts, this limitation made it difficult to monitor our simulation. Therefore, we have developed an automated job scheduling script



**Figure 4:** Usage of our allocation thus far in Year 1 for both *Mira* (top) and *Theta* (bottom).

to re-submit our job on Theta.

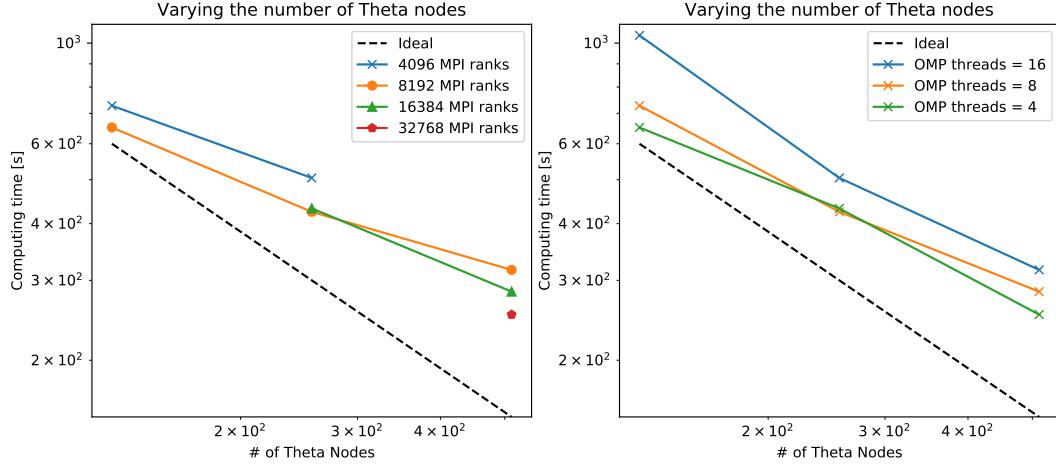
## 2 Code Development

We planned two code development milestones for Year 1: implement a “marching cubes” approach for our EOS and opacity tables and develop a simulation workflow management tool in Python. Both efforts are still underway. While developing the marching cubes capability we found that we could significantly accelerate our table interpolations by reordering some of the large arrays. This allowed for efficient vectorization by the compiler and sped up our table interpolations, both EOS and opacity, by about a factor of two. This improvement makes these aspects of our simulations relatively cheap, although the memory cost of the large tables is still high. Nevertheless, we have downgraded the priority of implementing the marching cubes approach.<sup>1</sup> We will still complete this implementation as person-power allows.

We have continued to develop workflow tools for managing our large simulations on *Mira* and *Theta*. We have implemented new bash scripts that automatically configure and submit restart jobs, which will substantially increase our queue throughput. We are incorporating these new tools into our existing Python tool chain. We have also developed Python code to automatically configure and setup simulation parameter studies and generate job submission scripts. Work on this tool continues and we will implement functionality for some limited runtime visualization and automatic data archiving in the near future.

We have also made significant progress on other code development relevant to, but not directly planned as part of, this INCITE program. In our neutrino transport, we have implemented neutrino-

<sup>1</sup>Never let optimization slow you down.



**Figure 5:** Weak scaling test on Theta. Different colors represent different combinations of MPI and OpenMP tasks.

electron inelastic scattering, an important process that we have so far only included during the 1D collapse phase of our simulations. We have also begun porting our Spark MHD solver to the DOE Exascale Computing Project (ECP)-supported AMReX framework. We are doing this within the new version of `FLASH` that is being developed as part of the DOE ECP. We anticipate moving to the AMReX version of `FLASH` in the future for our production simulations.

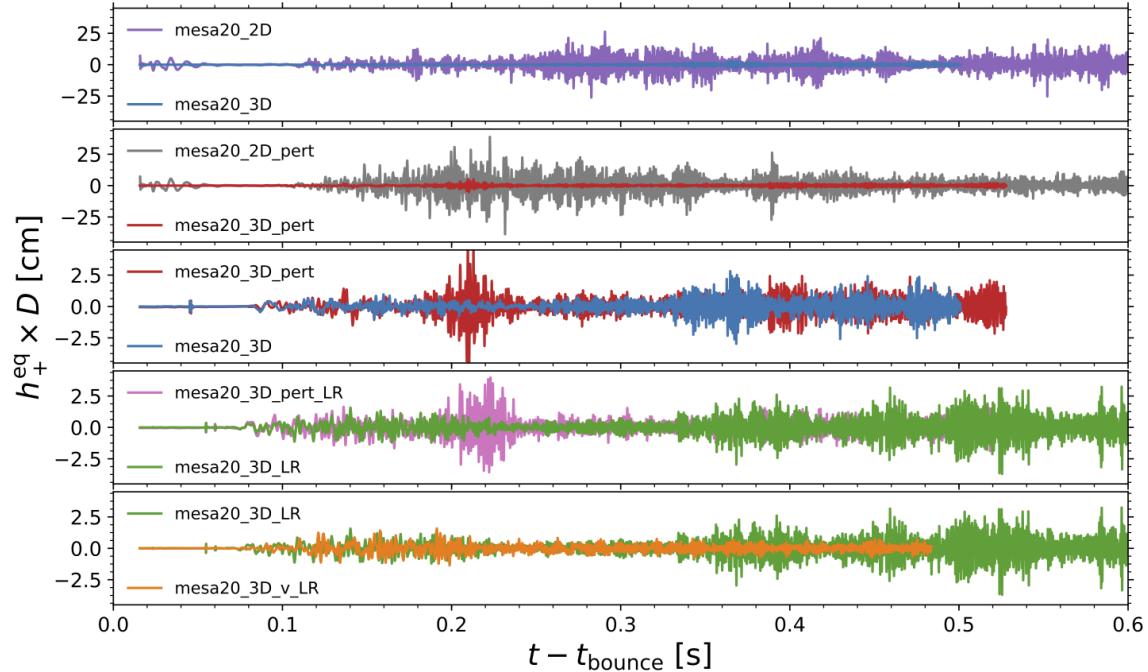
### 3 Fundamentally 3D Phenomena in CCSNe

Recently, we submitted a publication detailing results based on simulations carried out under our previous INCITE award ([O'Connor & Couch, 2018a](#)). This work includes several full 3D, high-resolution simulations using our M1 neutrino transport in `FLASH`, representing over 100 Million core-hours of work on *Mira*. In these simulations, we identify and analyze several essentially 3D aspects of CCSNe, including the presence of a new instability in the neutrino emission called the Lepton-number Emission Self-sustaining Asymmetry (LESA), first reported by ([Tamborra et al., 2014](#)). We are the first group to confirm the presence of the LESA in CCSNe and, since we use a very different transport approach, our work strongly implies this is not a numerical artifact but a real physical instability.

In [O'Connor & Couch \(2018b\)](#), we also show that the presence of the non-spherical, 3D progenitor structure has several important impacts on the CCSN mechanism. We show that convective motion in the progenitor can substantially increase the proximity to explosion. We also showed that 3D structure in the progenitor can leave a measurable imprint on the gravitational wave emission from CCSNe that could be detected by, e.g., LIGO. The gravitational wave strains from our simulations are shown in Figure 6.

### Project Plans for Year 2

We are essentially on track to achieve all of our Year 1 milestones with only minor modifications. As such, we plan to stick very close to our proposed Year 2 plan. Our goals and milestones for Year 2 of this INCITE project are detailed below.



**Figure 6:** Gravitational wave strains from the 3D simulations of O’Connor & Couch (2018b), carried out under a prior INCITE award. Our work showed for the first time that the presence of 3D structure in the progenitor star leaves a detectable imprint on the gravitational wave emission.

#### 4 Late time 3D Simulations of Magnetorotational CCSNe

In Year 2 of this project, we will carry four of the 3D simulations of magnetorotational CCSNe from Year 1 to late times, at least one second post-bounce. Long time scale simulations are crucial for accurately predicting the explosion energy, PNS mass, nucleosynthesis, etc. (Bruenn et al., 2016; Müller et al., 2017). For any simulations that fail to explode, we will attempt to simulate late enough times to capture the onset of PNS collapse to a black hole. This has the potential to elucidate the details of the formation of stellar mass black holes, such as those that have been detected by aLIGO (??). We have recently shown (?) that the GR effective potential approach can fairly accurately predict black hole formation time in 2D as compared to 1D fully GR simulations (?).

The nucleosynthetic yields from CCSN simulations are a key quantity that can be directly compared to observations and laboratory measurements of cosmic abundances. We will compute the detailed nucleosynthesis from these late-time CCSN simulations. This will be accomplished as a post-processing step using the open-source SkyNet nuclear reaction network code developed by Co-I Roberts. The input for the nuclear reaction networks will be passive tracer particle data that records thermodynamic trajectory information from our FLASH CCSN simulations. FLASH already includes a well-developed, efficient passive-particle framework that has been used extensively in the calculation of nucleosynthesis in Type Ia supernova simulations (e.g., ?). We will compute detailed abundances for elements such as radioactive nickel and titanium, two key observable quantities, and we will also examine how rotation and magnetic fields can influence the conditions for very heavy element formation and the r-process.

Each of the four 3D simulations will require 1M node-hours on *Mira* and 10 TB of online

storage. Including 125k *Mira* node-hours for development and testing, the total request for this milestone is 4.125M *Mira* node-hours and 40 TB of online storage.

## 5 3D Simulations of Iron Core Collapse in Rotating Stars

In Year 2, we will extend the Year 1 study of iron core collapse in rotating stars to an additional initial stellar mass. We will simulate the final five minutes of stellar evolution to core collapse in 3D for a  $25-M_{\odot}$  progenitor star for both “high” and “low” core rotation rates. As in Year 1, all final models will be made publicly available. Each such simulation will require 625k node-hours on *Mira*, for a total of 1.25M node-hours for the two simulations. We request 10 TB of online storage for these simulations. We request an additional 125k node-hours for testing and development.

## 6 Capturing the Magnetorotational Instability and $\alpha$ - $\Omega$ Dynamo in the PNS

There is a very strong shear layer at the edge of the rotating PNS that is unstable to the magnetorotational instability (MRI, ?Burrows et al., 2007). The presence of convection combined with rotation in the PNS can also lead to an  $\alpha$ - $\Omega$  dynamo (?). Both mechanisms can lead to exponential amplification of magnetic fields with dramatic implications for the CCSN mechanism. Accurately capturing either process is extremely challenging computationally, requiring extremely high resolution to capture the fastest growing modes of these instabilities (?). In Year 2 of this project, we will carry out an extremely high resolution simulation of a rotating PNS in order to study the rapid growth of magnetic fields via the MRI and dynamo. This simulation will go beyond ? in a number of ways: we will use our M1 neutrino transport method rather than leakage, we will include the entire solid angle of the sphere rather than just a 90° wedge, and will simulate to later times in the aim of capturing the saturation of the magnetic fields. Using AMR, we will add two extra levels of refinement beyond our fiducial resolution only in the shear layer surrounding the PNS, between 15 km and 40 km, bringing the finest resolution elements to 163 m. This approach was piloted for capturing turbulence in the gain region during our previous INCITE project and will avoid adding additional zones in regions that are not susceptible to the instabilities of interest. This is not as high as the highest resolution used by ? but we plan to go to much longer time scales, as much as 100 ms post-bounce. This simulation will comprise about 100 million zones in 3D and require about 200,000 time steps to reach 100 ms. The expense for this simulation will be 3.75M node-hours on *Mira* and will require 40 TB of online storage. We request an additional 125k node-hours for testing and development.

## 7 MHD CCSN Simulations Using 3D Progenitors on *Theta*

In Year 2 we will use the 3D progenitor models generated in Year 1 for 3D MHD CCSN simulations on *Theta*. For these simulations, we will enhance the physical fidelity of our neutrino transport by incorporating the SciDAC TEAMS microphysics framework, if available. This planned open-source microphysics framework will incorporate the latest, state of the art neutrino interactions and cross sections that are fully self-consistent with the underlying EOS.

For these simulations we will use the rotating and non-rotating  $15-M_{\odot}$  3D progenitors produced in Year 1. We will additionally run two more 3D MHD simulations using rotating, magnetic progenitors taken from Heger et al. (2005) in order to characterize the impact of the 3D structure on magnetorotational aspects of CCSNe. For this milestone we request a total of 250k *Theta* node-hours and 20 TB of online storage to carry out four total 3D simulations. Plus an additional 31k *Theta* node-hours for development and testing, the total request for *Theta* in Y2 is 281k node-hours.

## 8 Code Development

For Year 2, we will continue to make improvements to our `Spark-M1` application. As originally proposed, we will implement the TEAMS SciDAC EOS and opacity framework. In collaboration with researchers at the University of Washington and the University of Tennessee, Co-PI Roberts is now working on the initial implementation of this framework. This effort will enhance the physical fidelity of the EOS and neutrino opacities we use in our simulations.

The second major code development effort we plan for Year 2 is the implementation of high-order, single-step methods for MHD in our CCSN application. This work is also supported by the TEAMS SciDAC collaboration. Chelsea Harris will be starting as a research associate at MSU this Fall and will be leading this effort. Our `Spark` MHD solver is written in such a way to make implementation of this new approach straight-forward. A high-order single-step method will both increase the accuracy of our simulations while also decreasing the overall communication burden. This has the potential to significantly improve our computational efficiency. We will also continue porting our various physics routines, particularly `Spark`, to the AMReX-capable version of `FLASH`.

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