Telescoping Jet Substructure

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We introduce a novel jet substructure method which exploits the variation of observables with respect to a sampling of phase-space boundaries quantified by the variability. We apply this technique to identify boosted W boson and top quark jets using telescoping subjets which utilizes information coming from subjet topology and that coming from subjet substructure. We find excellent performance of the variability, in particular its robustness against finite detector resolution. The extension to telescoping jet grooming and other telescoping jet substructure observables is also straightforward. This method provides a new direction in heavy particle tagging and suggests a systematic approach to the decomposition of jet substructure.

The Large Hadron Collider (LHC) has begun to probe 55 physics above the electroweak scale, where the momenta 56 of massive Standard Model particles are much larger than 57 their invariant masses, resulting in hadronic decays of 58 jets with prong-like substructures. Many jet substructure 59 variables have been designed [1–3] and combined using 60 multivariate techniques [4-7] to identify such jets and 61 increase the sensitivity to beyond the Standard Model 62 The ability to reconstruct the jet features 63 accurately is obscured by the presence of additional 64 proton-proton interactions, i.e. pileup, as well as the 65 underlying event of the hard collision, both of which 66 cause additional radiation to fall within the catchment 67 area of the jet. Often, this radiation is removed through a 68 grooming procedure, e.g. pruning [8] or trimming [9]. Jet 69 substructure observables and grooming procedures target 70 certain intuitive features of the radiation properties and 71 often have tuneable parameters. For example, the prun- 72 ing parameters $z_{\rm cut}$ and $D_{\rm cut}$ control the softness and $_{73}$ noncollinearity of a discarded particle. Conventionally, 74 one makes a single choice of parameters deemed optimal 75 by some metric. However, such a choice may neglect the 76 full information the entire observable class contains.

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Recently, Q-jets [10] introduced non-determinism in jet $_{79}$ clustering. The procedure probes each jet multiple times $_{79}$ and quantifies differences among pruned jets using the $_{80}$ mass volatility. Later, telescoping jets [11] probed the radiation pattern surrounding the dominant energy flow with multiple angular resolutions $\{R_i\}$ and extracted the full information contained in jets at all angular scales. In this Letter, we apply telescoping jets to analyze a set 81 of commonly used jet observables and grooming proce- 82 dures. We demonstrate the feasibility of this method as 83 applied to the identification of hadronically decaying W^{84} bosons and top quarks, utilizing the variability of each 85 observable induced by the variation of its parameters.

In hadronic boosted two-body resonance decays, such 87 as that from a W boson, the resonance mass M intro- 88

duces a two-prong structure in the jet at an angular scale $\Theta \approx 2M/p_T$ between the two prongs, where p_T is the transverse momentum of the heavy particle. On the other hand, QCD jets initiated by isolated quarks and gluons do not have such a distinct scale. However, when examining jets with masses near $M \pm \Delta m$, QCD jets are also two-prong-like but "fuzzier" when $\Delta m \gg \Gamma$, where Γ is the natural width of the resonance. Besides this nontrivial subjet topology, the strong interaction dictates the formation of subjets with subjet substructures and subjet superstructures [12] which are sensitive to the partonic origins of subjets.

In the case of boosted top quarks, the top mass (M_t) and the W mass (M_W) are similar. Therefore $\Theta_t \approx 2M_t/p_T^t$ and $\Theta_W \approx 2M_W/p_T^W$ are comparable. This results in the generic three-prong structure in the hadronic top decay $t \to W + b \to q_1 + q_2 + b$. However, when examining jets with a mass near $M_t \pm \Delta m$ the selected QCD jets are, again, two-prong-like, so observables which distinguish three-prong jets from two-prong jets will help discriminate QCD jets from true top quark jets.

Given an arbitrary jet observable \mathcal{O} with a parameter a, the variation of the observable with respect to the sampling of parameters $\{a_i\}$ within (a_{\min}, a_{\max}) is quantified by the coefficient of variation $v_{\mathcal{O}}$ defined as the ratio of the standard deviation $\sigma(\mathcal{O})$ and the mean $\langle \mathcal{O} \rangle$ of $\{\mathcal{O}_{a_i}\}$,

$$v_{\mathcal{O}} = \frac{\sigma(\mathcal{O})}{\langle \mathcal{O} \rangle} \ . \tag{1}$$

The $v_{\mathcal{O}}$ observable is referred to as the variability. Analogous to the first derivative in calculus, the variability $v_{\mathcal{O}}$ measures the change of the observable \mathcal{O} with respect to the change of the phase-space boundary set by the parameter a. Instead of combining observables with different parameters in a multivariate analysis, the variability can give a trend of the observable variation which itself can be used as a distinguishing feature to classify jets.

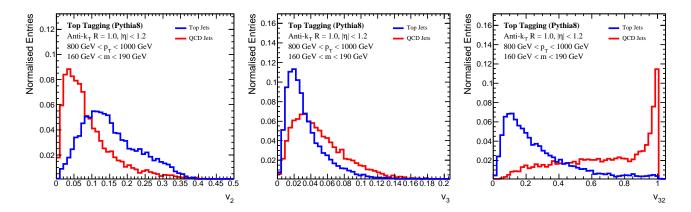


FIG. 1. The distributions of the variabilities v_2 (left panel) and v_3 (middle panel), as well as their ratio v_{32} (right panel) for top and QCD jets with 800 GeV $< p_T < 1$ TeV and 160 GeV < m < 190 GeV using the truth-particle information.

We focus on the variability of the jet mass with re-126 spect to varying the parameters which determine the jet127 constituents contributing to the jet mass. The sampling 128 of the telescoping parameters is chosen to be uniform₁₂₉ within the range (a_{\min}, a_{\max}) . We outline the procedure₁₃₀ of telescoping subjets: N subjets are reconstructed exclusively around dominant energy flows within a jet. A_{132} similar method using the leading subjets in a reclustered₁₃₃ jet was explored in [13]. We groom the jets using the $_{\mbox{\tiny 134}}$ trimming algorithm with $R_{\rm sub}=0.3$ and $f_{\rm cut}=0.05_{_{135}}$ to remove underlying event contaminations. Although 136 we do not include pileup in our studies, using groomed $_{{\scriptscriptstyle 137}}^{-}$ jet constituents can also mitigate the pileup effect. We $_{\scriptscriptstyle{138}}$ choose the subjet axes as the N-subjettiness axes $[14]_{139}$ with $\beta = 1$ and build subjets around them with radius₁₄₀ R_T within the voronoi regions [15–18]. Particles are $_{141}$ assigned to the nearest axis according to the distance $_{_{142}}$ ΔR_{ij} between the axis \hat{n}_i and particle p_i ,

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subjet_i =
$$\{p_j \mid \Delta R_{ij} < R_T \text{ and } \Delta R_{ij} < \Delta R_{kj}, \forall k \neq i\}$$
, (2)¹⁴⁵

where k is the index of the other axes \hat{n}_k . The variability¹⁴⁶ v_N (the shorthand notation of v_{m_N}) of the invariant¹⁴⁷ masses of the sum of N subjets is reconstructed with the¹⁴⁸ telescoping parameter $a=R_T\in(0.1,1.0)\times R$. Note that¹⁴⁹ a_{\max} is chosen to be the jet radius R to scan through the¹⁵⁰ entire catchment area of the jet. On the other extreme,¹⁵¹ the dominant energy features will be lost if a is too small,¹⁵² so a_{\min} is chosen as $0.1\times R$. We focus on N=2 and 3_{153} in W and N=2, 3, and 4 in top tagging, but N could¹⁵⁴ be extended further for more exotic boosted topologies. ¹⁵⁵

The generality of the telescoping algorithm allows a_{156} variety of other telescoping applications which are, how- $_{157}$ ever, beyond the scope of this Letter. For example, $_{158}$ in telescoping pruning one can fix $z_{\rm cut}$ and construct $_{159}$ $v_{\rm prun}$, the variability of the pruned jet mass with the $_{150}$ telescoping parameter a in $D_{\rm cut}=a~2m_{\rm jet}/p_{T_{\rm jet}}$. In $_{161}$ telescoping trimming, one can fix the subjet radius $R_{\rm sub}$ and construct $v_{\rm trim}$, the variability of the trimmed jet $_{163}$

mass with the telescoping parameter $a = f_{\text{cut}}$. One can also construct v_{τ_N} , the variability of the N-subjettiness with the telescoping parameter $a = \beta$ [19]. Correlations among variations with respect to multiple varied parameters can also be explored.

Besides variabilities, useful angular observables, which encode information about subjet topology, and mass observables, which reveal the presence of specific decay products, can be obtained seamlessly from the telescoping subjet algorithm. For instance, in W tagging with N=2, the subjet topology is affected by the jet mass cut, but W and QCD jets can still have significantly different distributions for the angle θ_2 between the two dominant energy flows. For top tagging with N=3, we consider the minimal angle θ_{\min} among the subjet axes. For QCD jets typically with two prongs, two of the three axes tend to be close to each other therefore θ_{\min} is expected to be small. For top jets with three prongs, this angle is distributed away from zero. Also, we attempt to identify the W inside the top jet [20, 21] by considering m_{W2} , the invariant mass of two of the three exclusive voronoi regions closest to the W mass, and the variability v_{mw_2} of the di-subjet invariant masses within those two regions.

The study is performed using samples generated from Monte Carlo simulations of proton-proton collisions at $\sqrt{s}=13$ TeV using PYTHIA8 [22]. Particles are clustered into jets with FASTJET 3 [23] using the anti- k_T algorithm [24] with R=1.0 and are required to be central with a pseudorapidity $|\eta|<1.2$. We consider two kinematic regimes where the jet p_T is either between 350 GeV and 500 GeV or 800 GeV and 1 TeV. Signal W boson and top quark jets are generated using decays of heavy Kaluza-Klein gravitons with invariant masses at 1 or 2 TeV for the two p_T bins in fully hadronic $G^* \to W^+W^-$ and $G^* \to t\bar{t}$ processes. Background QCD jets are generated from the Standard Model dijet process. To study the impact of finite detector resolution, we compare the results with the particles clustered in

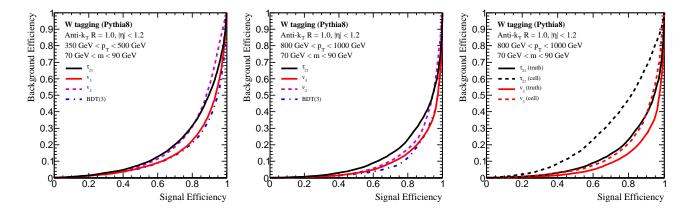


FIG. 2. The W tagging ROC curves of the variabilities v_2 and v_3 ; the BDT combinations of three telescoping subjets variables $\{v_2, v_3, \theta_2\}$; and the two-prong tagger $\tau_{21} = \tau_2/\tau_1$ in the (300 GeV, 500 GeV) jet p_T bin (left panel) and the (800 GeV, 1 TeV) bin (middle panel). Right panel: ROC curves of v_3 and τ_{21} in the (800 GeV, 1 TeV) jet p_T bin. Solid curves correspond to the ones with the truth-particle information, and the dashed curves are the ones using the pseudo-calorimeter cell particle information.

pseudo-calorimeter (η, ϕ) cells of size 0.1×0.1 , with each₁₉₇ cell momentum constructed with zero mass and direction₁₉₈ from the primary vertex. A selection on the trimmed jet₁₉₉ mass is made between 70 GeV and 90 GeV for W tagging₂₀₀ and between 160 GeV and 190 GeV for top tagging.

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To examine the complementarity of the information₂₀₂ contained in the telescoping subjet variables, subsets₂₀₃ of them are inputs for Boosted Decision Trees (BDTs)₂₀₄ implemented in TMVA [25]. For top tagging we also₂₀₅ consider the ratio v_{N2} between v_N and v_2 for N=3, 4, ₂₀₆

$$v_{N2} = \frac{v_N}{v_2} \ . \tag{3}_{208}^{207}$$

Shown in Figure 1 are the distributions of v_2 , v_3 , and 210 v_{32} for top and QCD jets. We find that top jets have a²¹¹ broader v_2 distribution and a narrower v_3 distribution. 212 The large variation of the jet mass when telescoping²¹³ around the two subjet axes is caused by the transition₂₁₄ of the W from being partially reconstructed to fully 215 There is not an intrinsic mass scale₂₁₆ reconstructed. dictating the third hard emission for QCD jets. On the217 other hand, the three prongs inside top jets are quark-218 initiated subjets, whereas the subjets in QCD jets can219 have gluonic origins. Quark subjets are narrower than 220 gluon subjets; therefore v_3 of top jets tend to be smaller.221 The v_{32} observable has almost the same performance as₂₂₂ the BDT with input $\{v_2, v_3\}$, suggesting that v_{32} may be₂₂₃ the optimal way of combining the two variabilities.

An interesting feature of v_{32} is that it cuts off naturally²²⁵ at 1, most clearly seen in QCD jets. Crucially, $v_3 \leq v_{2^{226}}$ in the collinear limit. The two-prong structure in QCD²²⁷ jets implies that v_2 and v_3 collect similar information.²²⁸ The third energy flow axis can not be displaced far from²²⁹ the two axes determined at N=2. Hence, little new²³⁰ information is collected by constructing a third subjet²³¹ and the distribution of v_{32} for QCD jets peaks at 1. In²³²

the case where there is a third, semi-hard emission, the emission is captured by all telescoping subjets at N=3 and does not induce the observable variation and so $v_3 < v_2$. In general, for larger N, more particles are captured by-default and so the variability is expected to decrease $(v_{N+1} \leq v_N)$.

The background efficiency as a function of the signal efficiency is illustrated by receiver operating characteristic (ROC) curves, where a lower curve indicates a better tagging performance. Shown in Figure 2 are the ROC curves of v_2 , v_3 , the BDT combinations of the telescoping subjet variables $\{v_2, v_3, \theta_2\}$, and the two-prong tagger $\tau_{21} = \tau_2/\tau_1$ in W tagging. The left and middle panels correspond respectively to two jet p_T regions of (350 GeV, 500 GeV) and (800 GeV, 1 TeV). Overall, the tagging performance increases at higher p_T , demonstrating the general advantage of applying telescoping jets to the boosted regime. In the right panel, we compare the tagging performance using truth particles and pseudocalorimeter clusters, which degrade information about structures smaller than the cell size. We find excellent performance of v_3 . Also, the v_3 observable is much more robust against this smearing, especially at high p_T , showing its qualitatively different feature compared to τ_{21} . The telescoping procedure in the v_3 observable utilizes the rapid depletion of radiation around the W at larger angles in the boosted regime. This "W isolation" effect is the manifestation of the fact that the W is a color singlet which affects the color structure of the subjets and the radiation pattern at large angles. The time dilation that occurs before W hadronically decays can also result in a period of time about $\mathcal{O}(1)$ fm/c [26] in which no QCD radiation is emitted, while there is no such gap in the jet formation process for QCD jets. On the other hand, the fact that v_3 performs better than v_2 hints at the significance of a third, semi-hard emission in W and

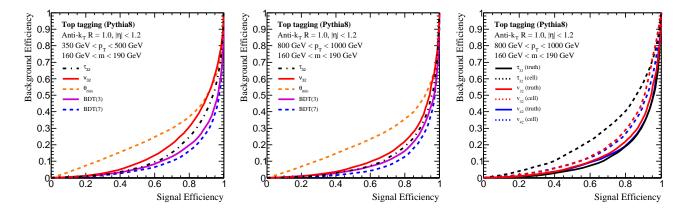


FIG. 3. The top tagging ROC curves of the variability ratio v_{32} , the minimal angle among three subjets θ_{\min} , the BDT combinations of three and seven telescoping subjets variables $\{m_{W2}, v_2, v_3\}$ and $\{\theta_2, \theta_{\min}, m_{W2}, v_2, v_3, v_4, v_{m_{W2}}\}$, and the three-prong tagger $\tau_{32} = \tau_3/\tau_2$ in the (300 GeV, 500 GeV) jet p_T bin (left panel) and the (800 GeV, 1 TeV) bin (middle panel). Right panel: ROC curves of v_{32} , v_{42} and τ_{32} in the (800 GeV, 1 TeV) jet p_T bin. Solid curves correspond to the ones with the truth-particle information, and the dashed curves are the ones using the pseudo-calorimeter cell particle information.

QCD jets. The v_3 observable disentangles such emission₂₆₉ when quantifying the isolation of W jets.

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Shown in Figure 3 are the ROC curves for top tag-271 ging performance including v_{N2} (N = 3, 4), $\theta_{\min,272}$ the BDT combinations of telescoping subjets variables₂₇₃ $\{v_2, v_3, m_{W2}\}\ \, ext{and}\ \, \{\theta_2, \theta_{\min}, m_{W2}, v_2, v_3, v_4, v_{m_{W2}}\},\ \, ext{and}_{^{274}}$ the three-prong tagger $\tau_{32} = \tau_3/\tau_2$. Again, the left and 275 middle panels correspond to the two kinematic regimes $_{\rm 276}$ $p_T \in (350 \text{ GeV}, 500 \text{ GeV}) \text{ and } p_T \in (800 \text{ GeV}, 1 \text{ TeV})_{,277}$ and we note tagging performance increases at higher p_T .278 In the right panel, the ROC curves plot both truth-279 particle and pseudo-calorimeter information. We find the280 excellent performance of v_{N2} and its robustness against₂₈₁ smearing, especially at high p_T where the performance₂₈₂ of the more conventionally used au_{32} observable degrades₂₈₃ dramatically. This indicates the qualitatively different₂₈₄ features of v_{N2} and a three-prong tagger. We also find₂₈₅ the usefulness of including m_{W2} in the minimal BDT combination which significantly increases the tagging performance. It is clear that the intrinsic mass scale²⁸⁶ M_W within the top jet is a unique feature distinguishing itself from the QCD background. Similar to the fact₂₈₇ that v_3 performs better than v_2 in W tagging, the $v_{42^{288}}$ observable has a better performance than v_{32} , suggesting₂₈₉ the significance of a fourth, semi-hard emission in top₂₉₀ jets. One would also start to see the W isolation within₂₉₁ the top jet in the boosted regime.

To conclude, we introduce a qualitatively new jet₂₉₃ substructure method using variability to quantify the₂₉₄ change of observables with respect to a sampling of the₂₉₅ phase-space boundaries in the observable definition. This₂₉₆ technique is general and can be used to analyze arbitrary₂₉₇ classes of jet substructure observables and grooming₂₉₈ procedures. In W and top tagging, we find excellent₂₉₉ performance of telescoping subjets quantified by v_3 in₃₀₀ W tagging and v_{42} in top tagging. Furthermore, their₃₀₁

robustness is found to be significantly better than more widely used N-prong taggers such as N-subjetiness via a comparison of the performance between reconstruction from using truth particles and from a pseudo-calorimeter.

The new physics messages we learn include the emergence of the isolation of W jets at high p_T , which is a dominant feature over their two-prong structure. This is true for all other heavy, color-singlet Standard Model particles including the Z and the Higgs boson. It would be promising to include such feature in their tagging strategies. The top jet also has features beyond the three-prong structure which can be exploited to increase tagging performance. The telescoping subjets provides a systematic framework within which one can construct qualitatively new jet substructure observables. This paves the road toward systematic jet studies using telescoping deconstruction.

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