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Telescoping Jet Substructure

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We introduce a novel jet substructure calculus which exploits the variation of observables with respect to a sampling of phase-space boundaries quantified by the variability. We apply this method to identify boosted W boson and top quark jets using telescoping jet grooming and telescoping subjets, demonstrating its ability to disentangle information coming from subjet topology and that coming from subjet substructure. We find excellent performance of the variability, in particular its robustness against finite detector resolution. This method provides a new direction in heavy particle tagging and enables a more complete and systematic approach to the decomposition of jet substructure.

The Large Hadron Collider (LHC) has begun to probe physics above the electroweak scale, where the momenta of massive Standard Model particles are much larger than their invariant masses, resulting in hadronic decays of jets with prong-like substructures. Many jet substructure variables have been designed [1–3] and combined using multivariate techniques [4–7] to identify such jets and increase the sensitivity to beyond the Standard Model physics. However, the ability to reconstruct the features of such jets accurately is obscured by the presence of additional proton-proton interactions, i.e. pileup, as well as the underlying event of the hard collision, both of which cause additional radiation to fall within the catchment area of the jet. Often, this radiation is removed through a grooming procedure, e.g. pruning [8] or trimming [9]. Jet substructure observables and grooming procedures target certain intuitive features of the radiation properties and often have tuneable parameters. For example, in the pruning algorithm, the $z_{\rm cut}$ and $D_{\rm cut}$ parameters control the softness and noncollinearity of a discarded particle. Conventionally, one makes a single choice of parameters deemed optimal by some metric. However, such a choice may neglect the full information the entire observable class contains.

Recently, Q-jets [10] introduced non-determinism in jet clustering. The procedure probes each jet multiple times and quantifies differences among pruned jets using the mass volatility. Later, telescoping jets [11] probed the radiation pattern surrounding the dominant energy flow with multiple angular resolutions $\{R_i\}$ and extracted the full information contained in jets at all angular scales. In this Letter, we apply telescoping jets to analyze a set of commonly used jet observables and grooming procedures. We demonstrate the feasibility of this method as applied to the identification of hadronically decaying W bosons and top quarks. The mass volatility in Q-jets is promoted to the variability of each observable induced by the variation of its parameters.

In hadronic boosted two-body resonance decays, such as that from a W boson, the resonance mass M introduces a two-prong structure in the jet at an angular scale $\Theta \approx 2M/p_T$ between the two prongs, where p_T is the transverse momentum of the heavy particle. On the other hand, QCD jets initiated by isolated quarks and gluons do not have such a distinct scale. However, when examining jets with masses near $M \pm \Delta m$, QCD jets are also two-prong-like but with a more distended radiation pattern when $\Delta m \gg \Gamma$, where Γ is the natural width of the resonance. Besides this nontrivial *subjet topology*, the strong interaction dictates the formation of subjets with *subjet substructures* and *subjet superstructures* [12] which are sensitive to the partonic origins of subjets.

In the case of boosted top quarks, the top mass (M_t) and the W mass (M_W) are not hierarchically separated. Therefore $\Theta_t \approx 2M_t/p_T^t$ and $\Theta_W \approx 2M_W/p_T^W$ can be comparable. This results in the generic three-prong structure in the hadronic top decay $t \to W + b \to q_1 + q_2 + b$. However, when examining jets with a mass near $M_t \pm \Delta m$ the selected QCD jets are, again, two-prong-like, so observables which distinguish three-prong jets from two-prong jets will help discriminate QCD jets from true top quark jets.

Given an arbitrary jet observable $\mathcal{O}$ with a parameter a, the variation of the observable with respect to the sampling of parameters $\{a_i\}$ within $(a_{\rm min}, a_{\rm max})$, or the *variability*, is quantified by the coefficient of variation $v^a_{\mathcal{O}}$ defined as the ratio of the standard deviation and the mean of $\{\mathcal{O}_{a_i}\}$,

$$v^a_{\mathcal{O}} = \frac{\sigma(\mathcal{O}_{a_i})}{\langle \mathcal{O}_{a_i} \rangle} \, . \tag{1}$$

Variations with respect to multiple varied parameters can be studied using the variability matrix. Much like the first derivative in calculus, the variability $v^a_{\mathcal{O}}$ measures the change of the observable $\mathcal{O}$ with respect to the change of the phase-space boundary set by the parameter a. Instead of combining observables with different parameters in a multivariate analysis, the variability can give a trend of the observable variation which itself can be used as a distinguishing feature to classify jets.

We consider a variety of telescoping applications. We focus on the variability of the jet mass with respect to varying the parameters which determine the jet constituents contributing to the jet mass. The sampling of the telescoping parameters is uniform within the range $(a_{\min}, a_{\max})$.

Telescoping subjets: N subjets are reconstructed exclusively around dominant energy flows within a jet. A similar method using the leading subjets in a reclustered jet was explored in [13]. We choose the subjet axes as the N-subjettiness axes [14] with $\beta = 1$ and build subjets around them with radius R_T [15–18]. Particles are assigned to the nearest axis according to the distance ΔR_{ij} between the axis $\hat{n}_i$ and particle p_j,

$$\text{subjet}_i = \{p_j \mid \Delta R_{ij} < R_T \text{ and } \Delta R_{ij} < \Delta R_{kj}\ ,\ \forall k \neq i\}, \tag{2}$$

where k is the index of the other axes $\hat{n}_k$. The variability v_N of the invariant masses of the sum of N subjets is reconstructed with the telescoping parameter $a = R_T \in (0.1, 1.0) \times R$. Note that $a_{\max}$ is chosen to be the jet radius R to scan through the entire catchment area of the jet. On the other extreme, the dominant energy features will be lost if a is too small, so $a_{\min}$ is chosen as $0.1 \times R$. We focus only on $N = 2$ and 3 in W and $N = 2$, 3, and 4 in top tagging, but N could be extended further for more exotic boosted topologies.

Telescoping pruning: we fix $z_{\text{cut}} = 0.1$ and construct v_{prun}, the variability of the pruned jet mass with the telescoping parameter $a \in (0.1, 2.0)$ in $D_{\text{cut}} = a\ 2m_{\text{jet}}/p_{T_{\text{jet}}}$.

Telescoping trimming: we construct v_{trim}, the variability of the trimmed jet mass with the telescoping parameter $a = f_{\text{cut}} \in (0.0, 0.1)$.

Besides variabilities, useful angular observables, which encode information about subjet topology, and mass observables, which reveal the presence of specific decay products, can be obtained seamlessly from the telescoping subjet algorithm. For instance, in W tagging with $N = 2$, subjet topology is affected by the jet mass cut, but W and QCD jets can still have significantly different distributions for the angle θ_2 between the two dominant energy flows. For top tagging with $N = 3$, we consider the minimal angle $\theta_{\min}$ among the subjet axes. For QCD jets, this angle is expected to be small while for top jets it will be distributed away from zero. Also, we attempt to identify the W inside the top jet [19, 20] by considering m_{W2}, the invariant mass of two of the three exclusive voronoi regions closest to the W mass, and its variability $v_{m_{W2}}$ by scanning within those two regions.

The study is performed using samples generated from Monte Carlo simulations of proton-proton collisions at $\sqrt{s} = 13$ TeV using Pythia8 [21]. Particles are clustered into jets with FastJet 3 [22] using the anti-k_T algorithm [23] with $R = 1.0$ and are required to be central with a pseudorapidity $|\eta| < 1.2$. We consider two kinematic regimes where the jet p_T is either between 350 GeV and 500 GeV or 800 GeV and 1 TeV. Signal W boson and top quark jets are generated using decays of heavy Kaluza-Klein gravitons with invariant masses at 1 or 2 TeV for the two p_T bins in $gg \to G^* \to W^+W^-$ or $t\bar{t} \to$ hadrons. Background QCD jets are generated from the Standard Model dijet process. To study the impact of finite detector resolution, we compare the results with the particles clustered in pseudo-calorimeter (η, ϕ) cells of size 0.1×0.1, with each cell momentum constructed with zero mass and direction from the primary vertex. Finally, in the case of telescoping subjets, jets are groomed using the trimming algorithm with $R_{\text{sub}} = 0.3$ and $f_{\text{cut}} = 0.05$ to remove the effects of pileup **BUT WE DON'T ADD IN PILE-UP SO IS THERE ANOTHER WAY TO WORD THIS?**. A selection on the trimmed jet mass is made between 70 GeV and 90 GeV for W tagging and between 160 GeV and 190 GeV for top tagging.

To examine the complementarity of the information contained in the telescoping subjet variables, subsets of them are inputs for Boosted Decision Trees (BDTs) implemented in TMVA [24]. For top tagging we also consider the ratio v_{42} between v_4 and v_2,

$$v_{42} = \frac{v_4}{v_2}\ . \tag{3}$$

Shown in Figure 1 are the distributions of v_2, v_4, and v_{42} for top and QCD jets. We find that top jets have a broader v_2 distribution and a narrower v_4 distribution. The large variation of the jet mass when telescoping around the two subjet axes is caused by the transition of the W from being partially reconstructed to fully reconstructed. **IS THIS COMMENT STILL AS VALID OR SHOULD IT BE PHRASED DIFFERENTLY:** There is not an intrinsic mass scale dictating the third hard emission for QCD jets. On the other hand, the three prongs inside top jets are quark-initiated subjets, whereas the subjets in QCD jets can have gluonic origins. Quark subjets are narrower than gluon subjets; therefore v_3 of top jets is statistically smaller. v_{42} has almost the same performance as the BDT with input $\{v_2, v_4\}$, suggesting that v_{42} may be the optimal way of combining the two variabilities. **ADD IN THING ABOUT TOPS HAVING A SEMI-HARD EMISSION FOR v_4.**

An interesting feature of v_{42} is that it cuts off naturally at 1, most clearly seen in QCD jets. Crucially, $v_4 \leq v_2$. **THIS NO LONGER HOLDS:** [The two-prong structure in QCD jets implies that v_2 and v_4 collect almost the same information. The third energy flow axis can not be displaced far from the two axes determined at $N = 2$. Hence, little new information is collected by constructing a third subjet and the distribution of v_{32} for QCD jets peaks at 1.] **THERE IS NO LONGER A PEAK.**

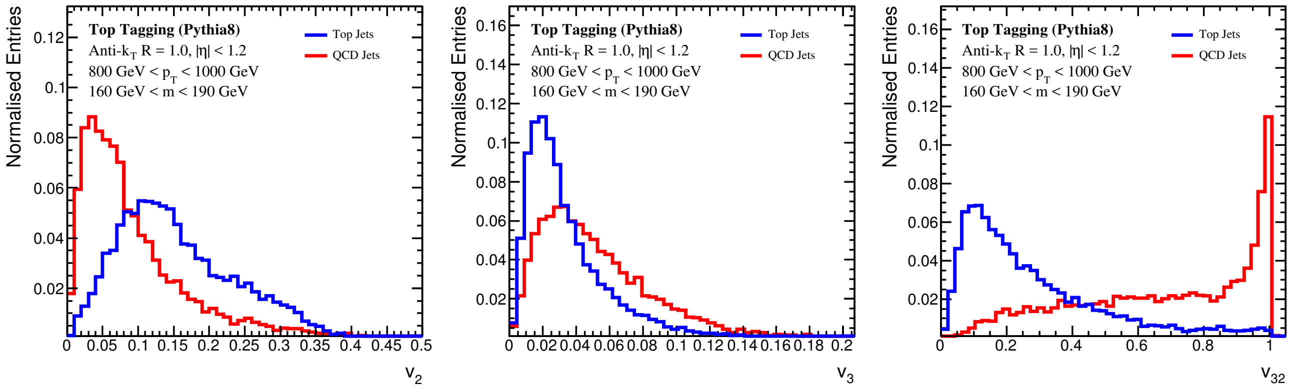

FIG. 1. The distributions of the variabilities v_2 (left panel) and v_4 (middle panel), as well as their ratio v_{42} (right panel) for top and QCD jets with 800 GeV $< p_T <$ 1 TeV and 160 GeV $< m <$ 190 GeV using the truth-particle information.

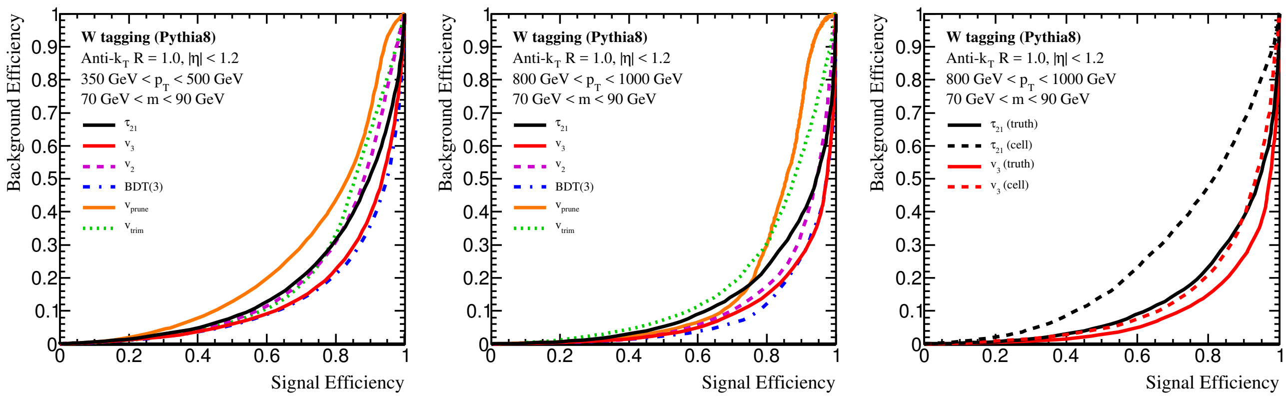

FIG. 2. The W tagging ROC curves of the variabilities v_2, v_3, $v_{\rm trim}$, and $v_{\rm prun}$; the BDT combinations of three telescoping subjets variables $\{v_2, v_3, \theta_2\}$; and the two-prong tagger $\tau_{21} = \tau_2/\tau_1$ in the $(300\ {\rm GeV}, 500\ {\rm GeV})$ jet p_T bin (left panel) and the $(800\ {\rm GeV}, 1\ {\rm TeV})$ bin (middle panel). Right panel: ROC curves of v_3 and τ_{21} in the $(800\ {\rm GeV}, 1\ {\rm TeV})$ jet p_T bin. Solid curves correspond to the ones with the truth-particle information, and the dashed curves are the ones using the pseudo-calorimeter cell particle information.

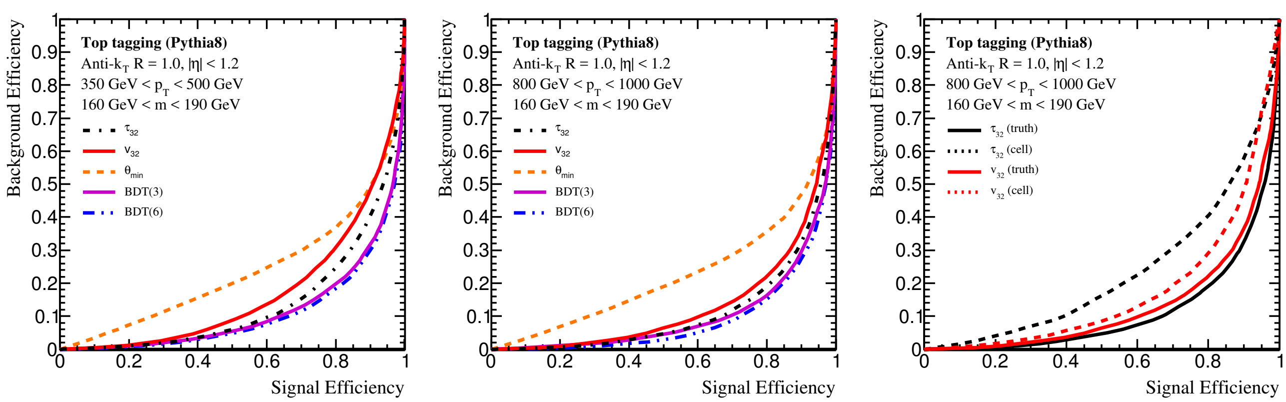

FIG. 3. The top tagging ROC curves of the variability ratio v_{42}, the minimal angle among three subjets $\theta_{\rm min}$, the BDT combinations of three and six telescoping subjets variables $\{m_{W2}, v_2, v_3\}$ and $\{\theta_2, \theta_{\rm min}, m_{W2}, v_2, v_3, v_{m_{W2}}\}$, and the three-prong tagger $\tau_{32} = \tau_3/\tau_2$ in the $(300\ {\rm GeV}, 500\ {\rm GeV})$ jet p_T bin (left panel) and the $(800\ {\rm GeV}, 1\ {\rm TeV})$ bin (middle panel). Right panel: ROC curves of v_{42} and τ_{32} in the $(800\ {\rm GeV}, 1\ {\rm TeV})$ jet p_T bin. Solid curves correspond to the ones with the truth-particle information, and the dashed curves are the ones using the pseudo-calorimeter cell particle information.

In the case where there is a third, semi-hard emission, the emission is captured by all telescoping subjets at $N = 3$ and does not induce the observable variation and so $v_4 < v_2$. In general, for larger N, more particles are captured by-default and so the variability is expected to decrease ($v_{N+M} \leq v_N$, where $M \geq 0$).

The performances of the observables are illustrated by receiver operating characteristic (ROC) curves, plotting the background efficiency as a function of the signal efficiency, where a lower curve indicates a better tagging performance. Shown in Figure 2 are the ROC curves of v_2, v_3, $v_{\rm trim}$, $v_{\rm prun}$, the BDT combinations of the telescoping subjet variables $\{v_2, v_3, \theta_2\}$, and the two-prong tagger $\tau_{21} = \tau_2/\tau_1$ in W tagging. The left and middle panels correspond respectively to two jet p_T regions of $(350\ \text{GeV}, 500\ \text{GeV})$ and $(800\ \text{GeV}, 1\ \text{TeV})$. Overall, the tagging performance increases at higher p_T, demonstrating the general advantage of applying telescoping deconstruction to the boosted regime. We find excellent performance of v_3 and its qualitatively different feature compared to τ_{21}. In the right panel, we compare the tagging performance using truth particles and pseudo-calorimeter clusters, which degrade information about structures smaller than the cell size. We find that v_3 is much more robust against this smearing, especially at high p_T. The v_3 observable utilizes the W isolation and probes the rapid depletion of radiation around the W at larger angles in the boosted regime. This is the manifestation of the fact that the W carries zero color charge which affects the color structure of the subjets. The time dilation that occurs before W hadronically decays can also create a huge difference from QCD jets in the jet formation process. On the other hand, the fact that v_3 performs better than v_2 hints at the significance of a third hard emission in W and QCD jets; v_3 disentangles that effect in the quantification of the W isolation. Neither $v_{\rm prun}$ nor $v_{\rm trim}$ are as effective as v_2 or v_3 in the boosted regime. However, they demonstrate the generality of the telescoping algorithm and may have improved performance with further optimizations conducted on the choices of ranges for the grooming parameters.

Shown in Figure 3 are the ROC curves for top tagging performance including v_{42}, $\theta_{\rm min}$, the BDT combinations of telescoping subjets variables $\{v_2, v_3, m_{W2}\}$ and $\{\theta_2, \theta_{\rm min}, m_{W2}, v_2, v_3, v_{m_{W2}}\}$, and the three-prong tagger $\tau_{32} = \tau_3/\tau_2$. Again, the left and middle panels correspond to the two kinematic regimes $p_T \in (350\ \text{GeV}, 500\ \text{GeV})$ and $p_T \in (800\ \text{GeV}, 1\ \text{TeV})$, and we note tagging performance increases at higher p_T. In the right panel, the ROC curves plot both truth-particle and pseudo-calorimeter information. We find the excellent performance of v_{42} and its robustness against smearing, especially at high p_T where the performance of the more conventionally used τ_{32} observable degrades dramatically. This indicates the qualitatively different features of v_{42} and a three-prong tagger. We also find the usefulness of including m_{W2} in the minimal BDT combination which significantly increases the tagging performance. It is clear that the intrinsic mass scale M_W within the top jet is a unique feature distinguishing itself from the QCD background. One may also start to see the W isolation within the top jet in the boosted regime.

To conclude, we introduce a qualitatively new jet substructure calculus using variability to quantify the change of observables with respect to a sampling of the phase-space boundaries in the observable definition. This method is general and can be used to analyze arbitrary classes of jet substructure observables and grooming procedures. In this context of W and top tagging, we find excellent performance, especially in the case of telescoping subjets, quantified by v_3 in W tagging and v_{42} in top tagging. Furthermore, their robustness is found to be significantly better than more widely used N-prong taggers such as N-subjetiness via a comparison of the performance between reconstruction from using truth particles and from a pseudo-calorimeter.

The new physics messages we learn include the emergence of the isolation of W jets at high p_T, which is a dominant feature over their two-prong structure. This is true for all other heavy, color-singlet Standard Model particles including the Z and the Higgs boson. The top jet also has features beyond the three-prong structure which can be exploited to increase tagging performance. The telescoping subjets provides a systematic framework within which one can construct qualitatively new jet substructure observables. This paves the road toward complete and systematic jet studies using telescoping deconstruction [25].

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