# Visualizing the PCA transformation

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#### Dimension reduction

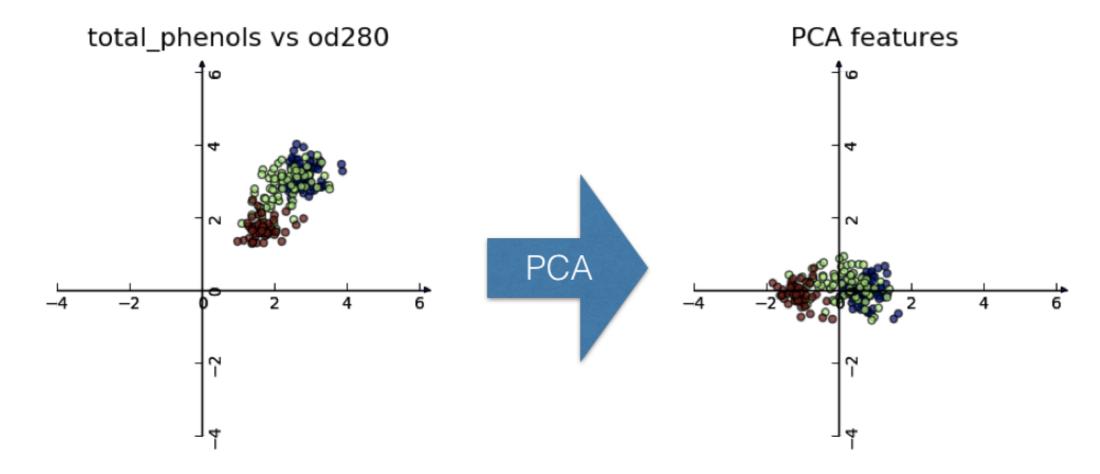
- More efficient storage and computation
- Remove less-informative "noise" features
- ... which cause problems for prediction tasks, e.g. classification, regression

## **Principal Component Analysis**

- PCA = "Principal Component Analysis"
- Fundamental dimension reduction technique
- First step "decorrelation" (considered here)
- Second step reduces dimension (considered later)

## PCA aligns data with axes

- Rotates data samples to be aligned with axes
- Shifts data samples so they have mean 0
- No information is lost



## PCA follows the fit/transform pattern

- PCA is a scikit-learn component like KMeans or StandardScaler
- fit() learns the transformation from given data
- transform() applies the learned transformation
- transform() can also be applied to new data

## Using scikit-learn PCA

samples = array of two features ( total\_phenols & od280 )

```
[[ 2.8
       3.92]
 [ 2.05 1.6 ]]
from sklearn.decomposition import PCA
model = PCA()
model.fit(samples)
PCA(copy=True, ...)
transformed = model.transform(samples)
```

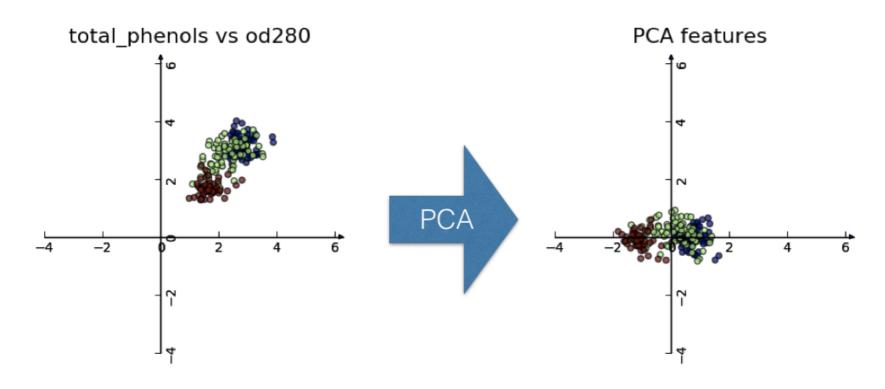


#### **PCA** features

- Rows of transformed correspond to samples
- Columns of transformed are the "PCA features"
- Row gives PCA feature values of corresponding sample

#### PCA features are not correlated

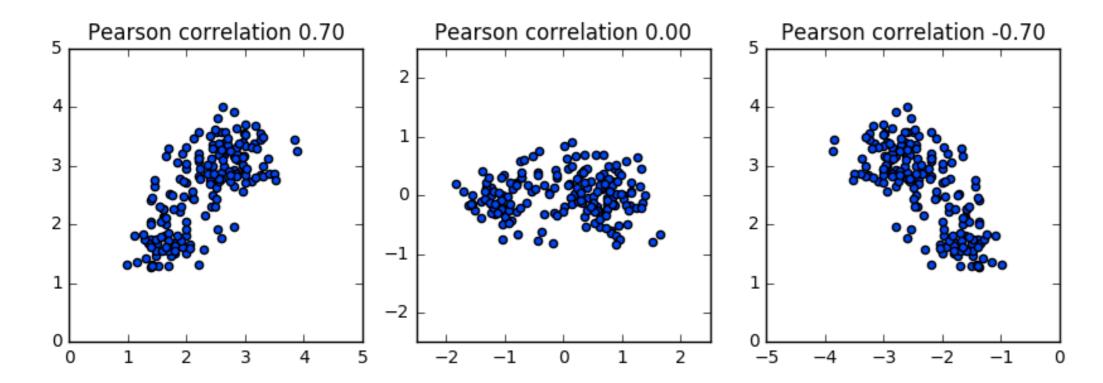
- Features of dataset are often correlated, e.g. total\_phenols and od280
- PCA aligns the data with axes
- Resulting PCA features are not linearly correlated ("decorrelation")





#### Pearson correlation

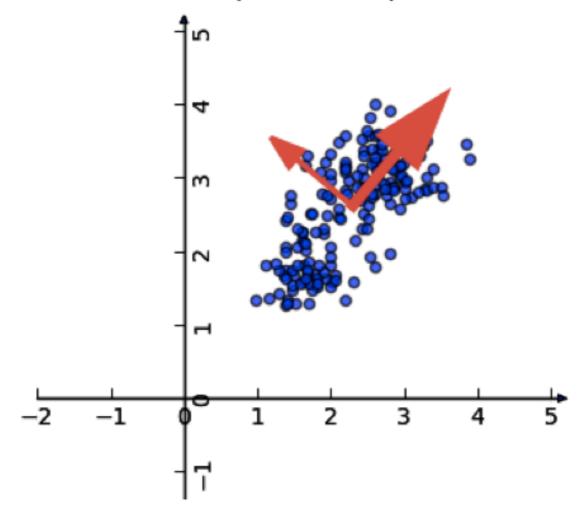
- Measures linear correlation of features
- Value between -1 and 1
- Value of 0 means no linear correlation



## Principal components

- "Principal components" = directions of variance
- PCA aligns principal components with the axes

#### The Principal Components



## Principal components

- Available as components\_ attribute of PCA object
- Each row defines displacement from mean

```
print(model.components_)
```

# Let's practice!

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## Intrinsic dimension

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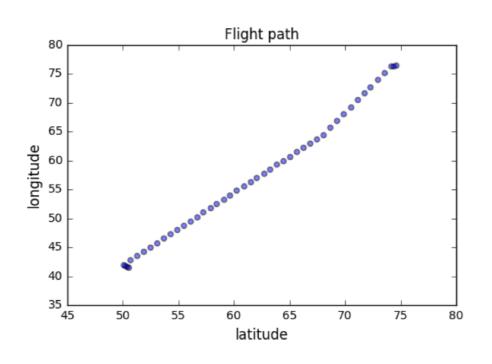
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## Intrinsic dimension of a flight path

- 2 features: longitude and latitude at points along a flight path
- Dataset appears to be 2dimensional
- But can approximate using one feature: displacement along flight path
- Is intrinsically 1-dimensional

```
latitude longitude
50.529 41.513
50.360 41.672
50.196 41.835
```



#### Intrinsic dimension

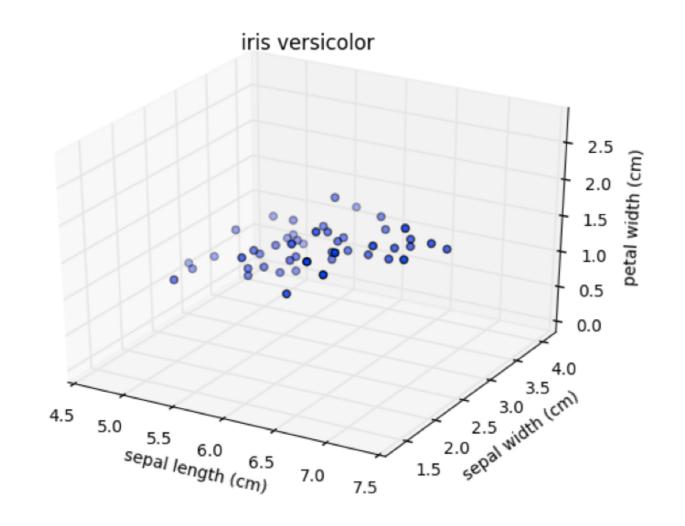
- Intrinsic dimension = number of features needed to approximate the dataset
- Essential idea behind dimension reduction
- What is the most compact representation of the samples?
- Can be detected with PCA

#### Versicolor dataset

- "versicolor", one of the iris species
- Only 3 features: sepal length, sepal width, and petal width
- Samples are points in 3D space

### Versicolor dataset has intrinsic dimension 2

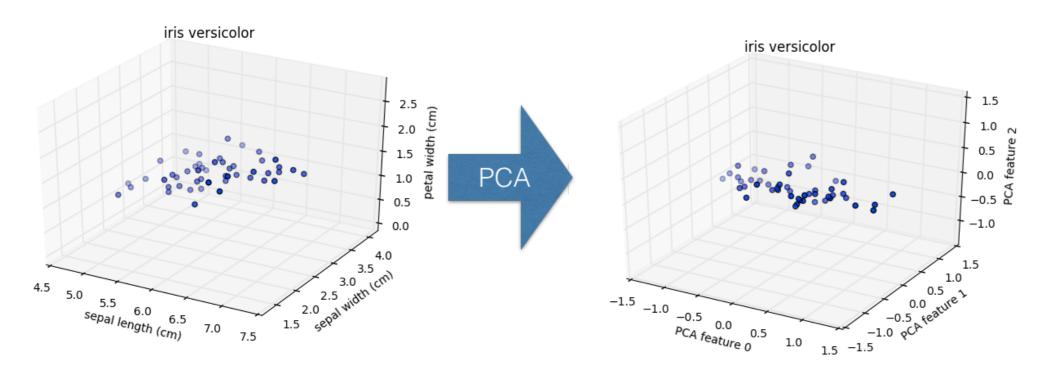
- Samples lie close to a flat 2-dimensional sheet
- So can be approximated using 2 features



#### PCA identifies intrinsic dimension

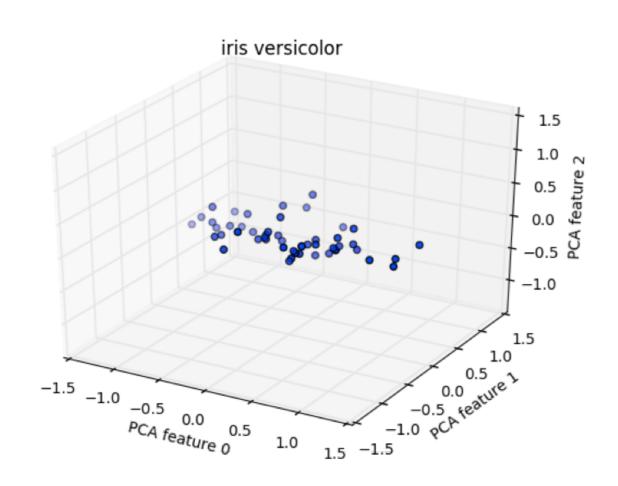
- Scatter plots work only if samples have 2 or 3 features
- PCA identifies intrinsic dimension when samples have any number of features
- Intrinsic dimension = number of PCA features with significant variance

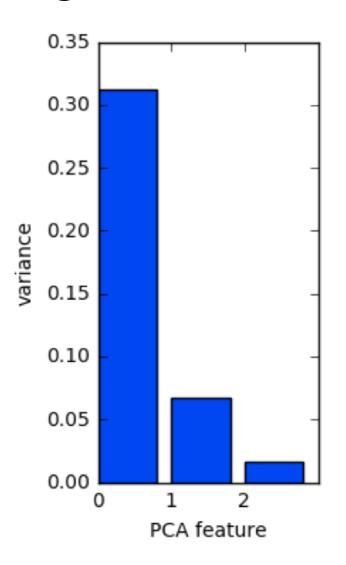
## PCA of the versicolor samples





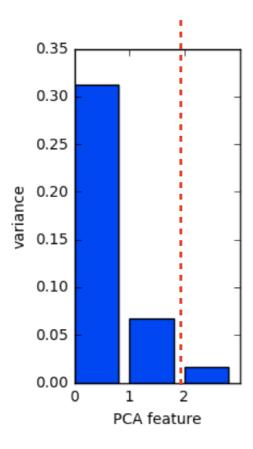
## PCA features are ordered by variance descending





#### Variance and intrinsic dimension

- Intrinsic dimension is number of PCA features with significant variance
- In our example: the first two PCA features
- So intrinsic dimension is 2



## Plotting the variances of PCA features

samples = array of versicolor samples

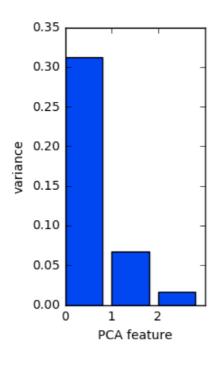
```
import matplotlib.pyplot as plt
from sklearn.decomposition import PCA
pca = PCA()
pca.fit(samples)
```

```
PCA(copy=True, ...)
```

```
features = range(pca.n_components_)
```

## Plotting the variances of PCA features

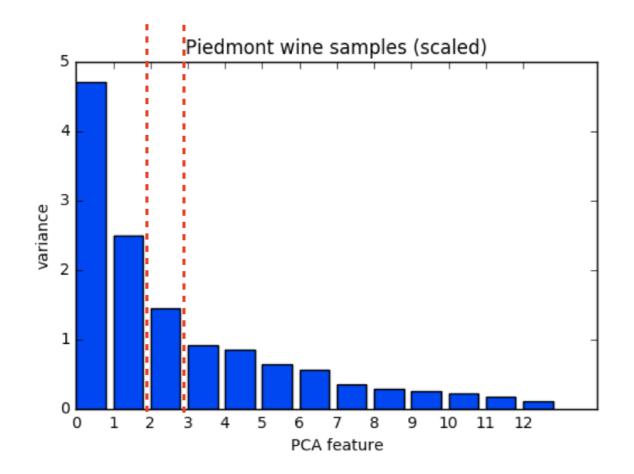
```
plt.bar(features, pca.explained_variance_)
plt.xticks(features)
plt.ylabel('variance')
plt.xlabel('PCA feature')
plt.show()
```





## Intrinsic dimension can be ambiguous

- Intrinsic dimension is an idealization
- ... there is not always one correct answer!
- Piedmont wines: could argue for 2, or for 3, or more



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# Dimension reduction with PCA

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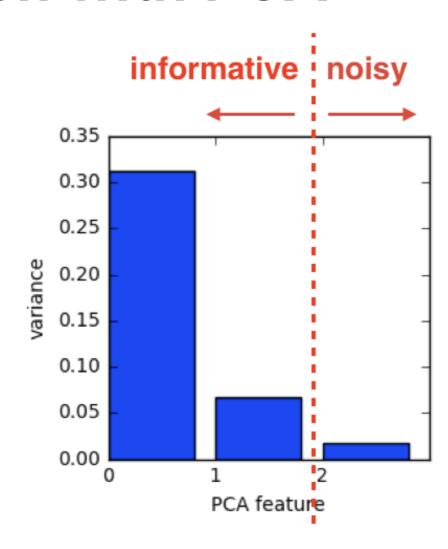


#### Dimension reduction

- Represents same data, using less features
- Important part of machine-learning pipelines
- Can be performed using PCA

#### Dimension reduction with PCA

- PCA features are in decreasing order of variance
- Assumes the low variance features are "noise"
- ... and high variance features are informative



#### Dimension reduction with PCA

- Specify how many features to keep
- E.g. PCA(n\_components=2)
- Keeps the first 2 PCA features
- Intrinsic dimension is a good choice

#### Dimension reduction of iris dataset

- samples = array of iris measurements (4 features)
- species = list of iris species numbers

```
from sklearn.decomposition import PCA
pca = PCA(n_components=2)
pca.fit(samples)
```

#### PCA(copy=True, ...)

```
transformed = pca.transform(samples)
print(transformed.shape)
```

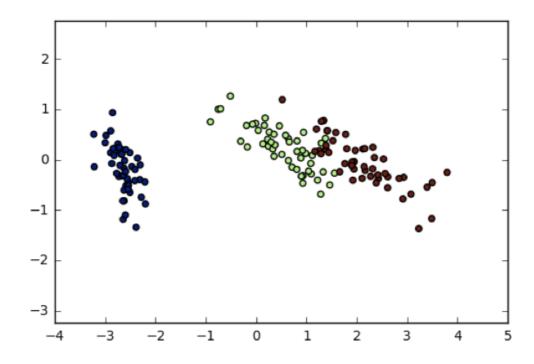
```
(150, 2)
```



### Iris dataset in 2 dimensions

- PCA has reduced the dimension to 2
- Retained the 2 PCA features with highest variance
- Important information preserved: species remain distinct

```
import matplotlib.pyplot as plt
xs = transformed[:,0]
ys = transformed[:,1]
plt.scatter(xs, ys, c=species)
plt.show()
```

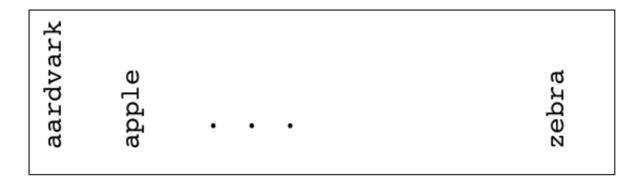


#### Dimension reduction with PCA

- Discards low variance PCA features
- Assumes the high variance features are informative
- Assumption typically holds in practice (e.g. for iris)

## Word frequency arrays

- Rows represent documents, columns represent words
- Entries measure presence of each word in each document
- ... measure using "tf-idf" (more later)



document0
document1
.

```
0, 0.1, ... 0.

word frequencies ("tf-idf")
```

## Sparse arrays and csr\_matrix

- "Sparse": most entries are zero
- Can use scipy.sparse.csr\_matrix instead of NumPy array
- csr\_matrix remembers only the non-zero entries (saves space!)

```
aardvark
apple
.
```

document0
document1
.

```
0, 0.1, ... 0.

word frequencies ("tf-idf")
```

## TruncatedSVD and csr\_matrix

- scikit-learn PCA doesn't support csr\_matrix
- Use scikit-learn TruncatedSVD instead
- Performs same transformation

```
from sklearn.decomposition import TruncatedSVD
model = TruncatedSVD(n_components=3)
model.fit(documents) # documents is csr_matrix
TruncatedSVD(algorithm='randomized', ...)
transformed = model.transform(documents)
```



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