

Problem 1:**(a)**-MergeSort or Heapsort: $O(n \log n)$ -Max priority queue using get max and percolate down operation k times:

Call build heap is $O(n)$, then call get max and percolate down so the result is $O(n + k \log k)$.

(b)

Select k th largest number using rand-select is $O(n)$, then sort the k largest numbers is $O(k \log k)$. So, our algorithm takes $O(n + k \log k)$.

I would definitely use max-priority queue or order statistics algorithm since their best asymptotic worst-case running time is better than either mergesort or heapsort.

Problem 2:**a)**

-If a string is shorter than another and there is no character in the index, consider its value as the smallest.

-Change the base, $b = \text{"a-z"}$

-Compare each index according to the ascii table such as; a: 97 and z: 122 at the ascii table, when we compare 'a' and 'z' value of 'z' is greater than 'a'.

Then following is same as radix sort for integers;

----> do the following for each letter i where i varies from the far right to left.

----> Sort input array according to the i th letter.

b)

"VEYSEL", "EGE", "SELIN", "YASIN" } 0th step

"EGE", "VEYSEL", "SELIN", "YASIN"} 1st step----->Notice that "SELIN" comes before "YASIN"

"VEYSEL", "EGE", "SELIN", "YASIN"} 2nd step

"EGE", "SELIN", "VEYSEL", "YASIN"} 3rd step

"EGE", "YASIN", "SELIN", "VEYSEL"} 4th step

“EGE”, “VEYSEL”, “SELIN”, “YASIN”} 5h step

“EGE”, “SELIN”, “YASIN”, “VEYSEL”} 6h step

c)

At (b) we can observe that number of steps = length of the longest word. (Let's say k: length of the longest word in the list)

Our base is “a-z” which is 26. (difference between letter “z” and “a” in the alphabet)

Number of elements is n.

So, the complexity is $O(k \cdot (n + 26))$