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## How does investor confidence lead to trading? Linking investor return experiences, confidence, and investment beliefs



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#### HIGHLIGHTS

- Combines investor brokerage records and matching monthly survey measurements.
- · Examines the mechanism through which investor confidence translates into trading.
- Given same return experience, more confident investors change beliefs more strongly.
- More strongly changing beliefs of confident investors associated with more turnover.
- Compared to less confident investors, confident investors underperform substantially.

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#### ABSTRACT

Confident investors trade more than less confident investors, but why? Prior research tests the ultimate relation between investor confidence and trading, but does not empirically examine the underlying mechanism that explains why confidence leads to trading. We complement the literature by developing a conceptual framework and presenting empirical evidence on a psychologically plausible mechanism through which confidence leads to trading. Using a combination of individual investors' brokerage records and matching monthly survey data, we show that more confident investors rely more on intuitive judgments when forming beliefs about expected returns. In particular, they rely more on naïve reinforcement learning and extrapolate individual return experiences into the future more strongly. Given the same return experience, more confident investors change their beliefs more strongly, providing more reason to trade. Ultimately, confident investors have higher turnover, which hurts their performance.

#### 1. Introduction

Why do confident investors trade so much? Previous literature tests the ultimate relation between confidence and trading (e.g., Barber and Odean, 2001; Glaser and Weber, 2007; Grinblatt and Keloharju, 2009), but does not open up the black box of *how* 

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investor confidence leads to trading. Recent literature, however, points to the need to elucidate possible *mechanisms* by which greater or lesser confidence influences downstream financial behavior (see e.g., Parker et al., 2012, 387). It is important to have empirical evidence on the mechanism through which investor confidence affects trading, as such knowledge could help improve individual investor decision-making. Individual investors typically overtrade, which hurts their performance through the accumulation of transaction costs (Barber and Odean, 2000). An increasing self-responsibility for making consequential investment choices, such as managing one's personal retirement savings (see van Rooij et al., 2011), magnifies the relevance of the

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detrimental effect of trading activity on investment performance, adding to the importance of this study's research question.

Besides the lack of an empirical test of the precise role of confidence in investor belief formation and behavior, another motivation for the current study is that some of the literature's assumed mechanisms on how investor confidence relates to trading seem psychologically implausible. One standard explanation for the positive relationship between investor confidence and trading relies on a model about how investors process and interpret signals about firm fundamentals (see Odean, 1998). More confident investors are theorized to underestimate the variance of private signals, believe more strongly in their private signals, and overweight these signals when updating their beliefs. Such a model assumes that investors possess relatively advanced informationprocessing skills and look primarily for signals on assets' fundamental values. Reflecting on that assumption, Cochrane (2013, 44) states that "[m]odels in which an informed trader possesses a 'signal' about the value of a liquidating dividend just don't describe the vast majority of trading. [...] [M]ost [...] traders [...] look at patterns of prices, volumes, and past trading activity, not 'information' or opinion[s] about firm fundamentals". It is unlikely that the average individual investor possesses private information about the fundamental value of assets (Coval et al., 2005; Kaniel et al., 2008; Seasholes and Shu, 2010; Døskeland and Hvide, 2011). Moreover, individual investors primarily do not look at fundamental information, but instead try to interpret past price patterns (Cohen et al., 2002; Barberis et al., 2013), consistent with naïve reinforcement learning for expected returns (Kaustia and Knüpfer, 2008; Choi et al., 2009; Greenwood and Shleifer, 2014) as well as asset prices and returns in equilibrium (Barberis et al., 2015).

We contribute to the literature on the role of confidence in individual investor belief formation and trading behavior, in two ways. First, we develop a conceptual framework which proposes a psychologically plausible mechanism through which confidence leads to trading. Second, we empirically test this mechanism in a sample of actual individual investors. In so doing, we differ from previous literature, which merely assumes rather than empirically tests the mechanism through which investor confidence translates into more trading. Responding to Cochrane's (2013) critique that current models of investor confidence and trading rely on implausible assumptions, we incorporate in our framework signals that are easy for individual investors to observe and process when updating their beliefs: individual past investment returns. We propose that investors - to varying degrees, depending on their confidence - extrapolate their past returns when forming expectations about future returns and subsequently trade based on those expectations. More confident investors rely more on intuitive judgments (akin to System 1 in Dual Process Theory, see e.g. Stanovich and West, 2000) when forming beliefs about expected returns. In particular, they rely more on naïve reinforcement learning and extrapolate individual return experiences into the future more strongly. That is, given the same return experience, more confident investors change their beliefs more strongly, providing more reason to trade.

To test the framework, we exploit a dataset which consists of the following two key parts. First, in collaboration with a large discount brokerage firm from the Netherlands, we commissioned a leading market research agency to develop, pretest, and program an online survey instrument to collect data on individual investors' return expectations and the confidence they have in these expectations on a monthly basis over twelve consecutive months. Second, we retrieve these investors' trading records, including

information on investment returns and turnover, and match this to their survey data on return expectations and confidence. By merging these two data sources, we obtain a panel dataset that allows us to verify the direct link between confidence and trading as documented in the prior literature, but more importantly, to study the *mechanism* linking confidence and trading, which has not been empirically examined to date.

We find empirical support for the link between confidence and trading as proposed in the framework: confident investors change their return expectations more strongly. The average change in return expectations for investors with above-average confidence is 0.2 units higher (on a 1–7 point Likert scale) than for investors with below-average confidence. Importantly, these higher changes in return expectations translate into economically significant effects on trading and performance. Investors with above-average confidence have 8.6 percentage-points higher monthly turnover than those with below-average confidence. Investors with above-average confidence underperform investors with below-average confidence by 88 basis points per month.

#### 2. Conceptual framework and hypotheses

Our conceptual framework connects individual investor experiences, confidence, beliefs, and trading behavior Fig. 1. Investor experiences comprise individual-level past returns. In the framework, investors form beliefs about future returns based on their return experiences. When doing so, they extrapolate recent return experiences, relying on naïve reinforcement learning. Updates in beliefs drive trading. Confidence enters the framework at the stage of belief formation: investors' confidence level interacts with their interpretation of return experiences, in that confidence stimulates the reliance on naïve reinforcement learning when updating beliefs

The conceptual framework extends previous work on individual investor belief formation and behavior by including an "experience-confidence-belief" intermediate link. In particular, Dominitz and Manski (2011) and Greenwood and Shleifer (2014) document that individuals' return expectations depend positively on experienced returns. Consistent with naïve reinforcement learning, individuals extrapolate recent experiences into future expectations: good (bad) past returns lead them to form optimistic (pessimistic) expectations about future returns.

In our framework, investor confidence refers to the notion of confidence, as described in Kahneman (2011, 212, 217) "Confidence is a feeling, which reflects the coherence of the information and the cognitive ease of processing it. [...] [D]eclarations of high confidence mainly tell you that an individual has constructed a coherent story in his mind [...]. [...] Our understanding of cognitive ease and associative coherence locates subjective confidence firmly in System 1". More confident investors' reliance on Dual Process Theory's System 1 is associated with decision-making based on quick and intuitive shortcuts (System 2 is associated with slower and more effortful conscious reasoning).<sup>2</sup> Individuals who base their judgments primarily on intuition (System 1) have high confidence in those judgments (Simmons and Nelson, 2006) and use more cognitive shortcuts and heuristics than individuals who do not base their judgments primarily on intuition (Stanovich and West, 2000; Evans, 2008). In particular, such individuals rely more on naïve reinforcement learning (Alós-Ferrer and Hügelschäfer, 2012).<sup>3</sup> Accordingly, we hypothesize that more confident investors

<sup>&</sup>lt;sup>1</sup> Related, Graham et al. (2009) assume that more confident investors are more willing to act on their personal beliefs.

<sup>&</sup>lt;sup>2</sup> Stanovich and West (2000) and Evans (2008) discuss Dual Process Theory in

 $<sup>^3</sup>$  Section 5.2 provides evidence that investor confidence indeed relates to reliance on intuition.

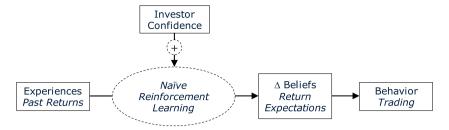


Fig. 1. Conceptual framework.

rely more on naïve reinforcement learning when updating return expectations than their less confident counterparts (Hypothesis 1). Given the same past return experience, more confident investors will thus update their return expectations by larger magnitudes than their less confident counterparts: investor confidence will be positively related to the magnitude of updates in investor return expectations (Hypothesis 2). Updates in investor return expectations change investor demand for risky assets, that is, create reason to trade and thus result in more trading (Hypothesis 3). Jointly, Hypotheses 1–3 imply that more confident investors trade more as they have more reason to trade, since given the same return experience, they change their beliefs more strongly than their less confident counterparts.

Note that by incorporating the stylized fact that individual investors extrapolate past returns, the framework can predict under certain conditions correlated behavior of investors. Thus, one may wonder how the market can clear from a general equilibrium perspective. In Section 4.3, we provide a discussion and empirical evidence regarding these issues. In general, the framework can be consistent with general equilibrium if there is heterogeneity in individual return experiences, or if other investor types (e.g., institutions) are present in the market to absorb individual investor demand and supply. For example, Barberis et al. (2015) develop a CAPM for an economy where traders extrapolate past returns, which they label "X-CAPM". The authors find that already the presence of a small share of 5% of rational traders that do not extrapolate past returns is sufficient for an equilibrium to exist (see Barberis et al., 2015).

#### 3. Data

In the analyses of this paper, we exploit a dataset matching brokerage records with monthly survey data for 1376 clients of the largest discount broker in the Netherlands from April 2008 through March 2009. The sample period corresponds to a relatively volatile stock-market period. Accordingly, there is substantial variation in individual investors' portfolio returns and return expectations, which is beneficial for testing the predictions of our framework. One may be concerned, however, about unobserved factors that could impact both the survey measures and the return variable, such as monthly variation in market returns during the sample period and the according swings in market sentiment. To alleviate such concerns and control for such unobserved factors, we include month fixed effects in our panel regressions (see Section 4.1 for details on our empirical setup). As the investors in our sample do not receive investment advice from the broker, the transactions and survey responses reflect their own decisions and opinions.

#### 3.1. Brokerage records

We have brokerage records of investors who completed at least one survey during the sample period. Apart from transaction information, the records contain information on investors' portfolio balances, demographics, and their six-digit postal code. Using data from Statistics Netherlands, we use this postal code to assign income and residential house value to investors. Dutch postal codes cover only small geographical areas (at maximum one street). Thus, the postal code level information that we retrieve from Statistics Netherlands provides a relatively close proxy for individuals' income and home value. Table 1 defines all variables. Table 2 provides descriptive statistics of all brokerage accounts available, and those for the subset of accounts of clients who completed the survey in each particular month of the sample period.

A comparison with samples of discount brokerage clients used in other studies of individual investor behavior in the United States (Barber and Odean, 2000, 2001) shows that this study's sample is similar in terms of age and gender, portfolio size, and turnover. Moreover, according to a report on Dutch retail investors by Millward-Brown (2006), the account values comprise the major share of investors' total self-managed wealth. As capital gains are not taxed in the Netherlands, tax-loss-selling plays no role for the investors in the sample.

#### 3.2. Survey data

#### 3.2.1. Survey design and data collection

In collaboration with the discount brokerage firm, we commissioned a market research agency to develop, pretest, and program an online survey instrument to collect detailed data on individual investors' return expectations and the confidence investors have in these expectations. In early April 2008, the market research agency invited via email 20,000 randomly selected clients to become part of a panel that would receive a survey at the end of each month between April 2008 and March 2009. In October 2008, we sent a reminder email to these same 20,000 clients to maintain a sufficient panel size. The first survey of April 2008 was completed by 787 clients. The corresponding response rate of 3.9% (= 787/20,000) is comparable to that of similar investor surveys (cf. Dorn and Sengmueller, 2009). Over the entire sample period from April 2008 to March 2009, 1376 clients completed the survey at least once. Of these clients, 67% completed the survey at least 3 times, 31% completed it at least 6 times, 9% completed it at least 9 times, and 3% completed it 12 times. Overall, 1045 clients completed the survey for two consecutive months at least once, allowing us to identify updates in return expectations based on 3955 month-investor observations. A potential concern is that the monthly variation in response rate (Table 2, Panel B) could be non-random or that variation in response timing could affect the results. Robustness checks in Section 5.3 suggest that both concerns are not relevant in our data.

In the survey, we measure investors' return expectations and confidence therein. We also measure investors' risk perceptions and risk tolerance (as control variables). That is, we measure investors' beliefs (return expectations and risk perceptions), confidence in beliefs (regarding return expectations), and preferences (risk tolerance) for each upcoming month (Table 3). We use qualitative measures, which are easier to understand than quantitative measures and have greater explanatory power for decision-making (Wärneryd, 1996; Kapteyn and Teppa, 2011).

**Table 1** Variable definitions.

Variable	Definition
Gender	Indicator variable taking the value 0 for male investors and 1 for female investors.
Age	Age of the investor in years as of April 2008.
Account tenure	Account tenure of the investor in years as of April 2008.
Income	Annual disposable income in 2007 (equals gross income minus taxes, social-security contributions, and health insurance premiums paid). Assigned to each investor based on his or her 6-digit postal code. This postal code is unique for each street in the Netherlands. Data source is the average net income per 6-digit postal code from Statistics Netherlands (Central Bureau of Statistics).
Portfolio value	Value of the investment assets in an investor's account at the end of the month.
Fraction of account invested	Portfolio value at the end of the month divided by total account value ( = portfolio value + cash)
House value	Value of the house in 2008. Assigned to each investor based on his or her 6-digit postal code. This postal code is unique for each street in the Netherlands. Data source is the average residential house value per 6-digit postal code from Statistics Netherlands (Central Bureau of Statistics).
Derivatives	Indicator variable taking the value 1 if an investor traded an option or futures contract at least once during a particular month; 0 otherwise.
Traded	Indicator variable taking the value 1 if an investor traded in a particular month; 0 otherwise.
Turnover	Average of the absolute values of all purchases and sales in a particular month, divided by the average of the portfolio values at the beginning and end of a particular month.
Return	Monthly investor return given by the product of the daily relative changes in the value of his or her portfolio after transaction costs and adjusting for portfolio in- and outflows. For example, a monthly return of 10% takes the value 0.1 in the data.
Std(Return)	Investor-specific standard deviation of daily portfolio returns in a particular month (in monthly terms).
Return expectation	Reflects how optimistic a respondent is about his or her investment portfolio and its returns in the upcoming month. Details on the survey questions are given in Table 3.
Risk tolerance	Reflects a respondent's general predisposition toward financial risk. Details on the survey questions are given in Table 3.
Risk perception	Reflects a respondent's interpretation of how risky the stock market will be in the upcoming month. Details on the survey questions are given in Table 3.
Confidence	Reflects a respondent's confidence about the response to the return expectation question. Details on the survey questions are given in Table 3.

Because of data availability, the data retrieved from Statistics Netherlands refer to different years, that is, to 2007 for income and to 2008 for house value.

#### 3.2.2. Beliefs and preferences

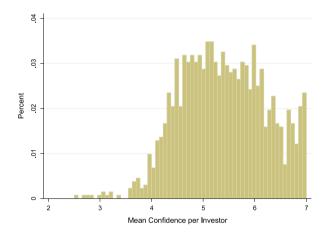
Return expectations depict investors' optimism about the returns of their investments. Risk perceptions gauge investors' interpretations of the riskiness of their investments. Risk tolerance reflects investors' predisposition (like or dislike) toward financial risk. To ensure that we measure investors' beliefs and preferences reliably, we use multiple items (i.e., survey questions) per variable, include these items in the survey in a random order, and mix regular- and reverse-scored items (Netemeyer et al., 2003). After rescaling reverse-scored items, we compute the final survey measures by averaging their respective item scores. Such measures perform at least as well as those using "optimally" weighted factor scores, but have the benefit of providing a readily interpretable absolute modal meaning (Dillon and McDonald, 2001).

To examine each variable's reliability, we calculate Cronbach's alpha (Cronbach, 1951). Cronbach's alpha indicates the degree of interrelatedness among a set of items (i.e., survey questions) that measure a particular variable (e.g., return expectations). For a variable to be called reliable, Cronbach's alpha should be above 0.7 (Hair et al., 1998). Our measurements are reliable, as Cronbach's alpha ranges between 0.71 and 0.89 for the beliefs and preferences variables. The individual items within each survey measure thus pick up similar information.

#### 3.2.3. Confidence

We measure investor confidence similar to Gamble et al. (2015) by asking after each of the five questions for return expectations: "How confident are you about this answer?" (Table 3). Thus, for each investor we receive five responses for confidence per month. The final confidence measure is calculated by averaging the responses to these five confidence questions. On average, investors are relatively confident about their return expectations, as the mean (median) confidence is 5.44 (5.38) and above the scale midpoint of 4. We find substantial cross-sectional variation in confidence (Fig. 2). Within investors, confidence is stable over time (see Section 5.2 for details). Fig. 3 shows how return expectations and confidence vary over time.

Graphically, there appears to be a negative co-movement between return expectations and confidence. Statistically, however, there is



**Fig. 2.** Distribution of mean investor confidence. Mean confidence is the mean calculated over all observations per investor (time-series mean). Confidence is measured on a 7-point Likert scale (see Table 3). A small value indicates low confidence, whereas a large value indicates high confidence.

no correlation between these two measures (Pearson correlation coefficient =-0.010, p-value =0.427). Thus, the confidence measure does not simply pick up return-expectation information nor is driven by return experiences (see robustness checks in Section 5.2). Instead, investors (to varying degrees) express confidence in *both* optimistic and pessimistic return expectations. Likewise, there is no correlation between confidence and risk perception (Pearson correlation coefficient =-0.002, p-value =0.831) and only a very marginal correlation with risk tolerance (Pearson correlation coefficient =-0.032, p-value =0.015).

Consistent with Barber and Odean (2001) and Grinblatt and Keloharju (2009), we find a direct effect of confidence in that more confident investors have higher turnover. Investors with above-average confidence have 8.6 percentage-points higher monthly turnover than those with below-average confidence (*p*-value = 0.054), while investors in the highest confidence quartile have 10.3 percentage-points higher monthly turnover than other investors (*p*-value = 0.049).

**Table 2**Descriptive statistics.

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Panel A: All brokerage ac	counts												
Month Investors	N	Apr-08 1376	May-08 1376	Jun-08 1376	Jul-08 1376	Aug-08 1376	Sep-08 1376	Oct-08 1376	Nov-08 1376	Dec-08 1376	Jan-09 1376	Feb-09 1376	Mar-09
Gender	Mean	0.08	0.08	0.08	0.08	0.08	0.08	0.08	0.08	0.08	0.08	0.08	0.08
Age	Mean	50.56	50.56	50.56	50.56	50.56	50.56	50.56	50.56	50.56	50.56	50.56	50.56
	std	13.57	13.57	13.57	13.57	13.57	13.57	13.57	13.57	13.57	13.57	13.57	13.57
Account tenure	Mean	4.07	4.07	4.07	4.07	4.07	4.07	4.07	4.07	4.07	4.07	4.07	4.07
	std	2.77	2.77	2.77	2.77	2.77	2.77	2.77	2.77	2.77	2.77	2.77	2.77
Income €	Mean	20,242	20,242	20,242	20,242	20,242	20,242	20,242	20,242	20,242	20,242	20,242	20,242
	std	4314	4314	4314	4314	4314	4314	4314	4314	4314	4314	4314	4314
Portfolio value €	Mean	52,854	52,695	44,872	42,840	45,963	37,688	31,127	30,100	30,679	29,564	26,514	27,875
	std	156,058	156,096	134,883	127,338	135,203	117,935	101,325	104,663	105,279	99,322	91,598	92,307
Fraction of account Inv.	Mean	0.68	0.67	0.63	0.64	0.65	0.63	0.63	0.64	0.64	0.64	0.64	0.65
	std	0.31	0.31	0.32	0.32	0.32	0.32	0.33	0.33	0.33	0.33	0.34	0.33
House value €	Mean	278,982	278,982	278,982	278,982	278,982	278,982	278,982	278,982	278,982	278,982	278,982	278,983
	std	112,278	112,278	112,278	112,278	112,278	112,278	112,278	112,278	112,278	112,278	112,278	112,278
Derivatives	Mean	0.22	0.20	0.21	0.21	0.19	0.22	0.25	0.18	0.16	0.17	0.17	0.18
Traded	Mean	0.46	0.47	0.48	0.47	0.41	0.51	0.63	0.42	0.37	0.41	0.40	0.42
Turnover (traders)	Mean	0.55	0.46	0.42	0.60	0.46	0.62	0.99	0.73	0.61	0.80	0.67	0.78
	std	1.53	1.22	1.12	1.85	1.41	1.87	3.63	1.82	1.82	2.77	2.49	2.46
Return	Mean std	0.03 0.16	0.00 0.13	-0.17 0.19	-0.10 0.19	0.05 0.17	-0.24 0.19	-0.23 0.33	-0.12 0.19	-0.04 0.20	0.00 0.19	-0.16 0.18	-0.01 0.19
Std(Return)	Mean	0.14	0.13	0.18	0.23	0.18	0.31	0.53	0.36	0.26	0.27	0.23	0.30
	std	0.25	0.23	0.29	0.33	0.28	0.36	0.42	0.37	0.32	0.32	0.32	0.35
Panel B: Survey responde	ents												
Month	N	Apr-08	May-08	Jun-08	Jul-08	Aug-08	Sep-08	Oct-08	Nov-08	Dec-08	Jan-09	Feb-09	Mar-09
Investors		787	701	605	557	520	491	650	402	330	312	272	291
Gender	Mean	0.07	0.08	0.08	0.08	0.08	0.08	0.09	0.08	0.08	0.08	0.09	0.09
Age	Mean	50.55	51.22	51.50	51.83	52.79	52.60	51.50	52.31	52.65	52.64	53.83	53.25
	std	13.51	13.55	13.43	13.57	12.90	13.05	13.29	13.25	12.88	12.86	12.62	12.67
Account tenure	Mean	3.93	3.98	4.09	3.98	4.11	4.08	4.26	4.35	4.34	4.45	4.53	4.38
	std	2.76	2.79	2.77	2.78	2.77	2.76	2.78	2.73	2.75	2.74	2.68	2.71
Income €	Mean	20,181	20,088	20,109	19,978	20,085	20,002	20,147	19,892	19,859	20,046	20,034	20,028
	std	4285	3956	4240	3729	3835	4153	4197	3808	3543	3897	3844	3860
Portfolio value €	Mean	54,446	54,264	45,411	45,509	49,557	39,707	29,490	33,660	30,169	30,693	27,444	27,229
	std	143,872	144,617	128,455	128,159	124,176	105,507	100,216	118,529	66,600	66,198	53,089	55,039
Fraction of account Inv.	Mean	0.69	0.68	0.63	0.63	0.65	0.63	0.64	0.64	0.65	0.63	0.65	0.67
	std	0.30	0.30	0.32	0.32	0.31	0.32	0.32	0.32	0.33	0.33	0.32	0.33
House value €	Mean	276,690	272,969	272,038	273,559	274,221	274,736	277,543	272,429	272,020	273,443	277,193	273,03
	std	110,125	102,015	109,290	101,943	101,006	110,771	112,864	104,787	98,530	99,506	108,672	100,57
Derivatives	Mean	0.24	0.23	0.25	0.25	0.23	0.24	0.26	0.19	0.20	0.24	0.22	0.20
Traded	Mean	0.52	0.54	0.55	0.52	0.46	0.54	0.64	0.46	0.42	0.48	0.49	0.45
Turnover (traders)	Mean	0.65	0.43	0.49	0.57	0.36	0.50	1.10	0.86	0.47	0.56	0.70	1.00
	std	1.82	1.13	1.41	1.61	0.91	1.08	4.68	2.23	1.51	1.07	2.08	3.91
Return	Mean std	0.03 0.17	0.00 0.12	-0.18 0.18	-0.10 0.18	0.05 0.20	-0.25 0.18	-0.22 0.34	-0.12 0.19	-0.04 0.16	0.00 0.20	-0.17 0.20	-0.01 0.21
Std(Return)	Mean	0.15	0.13	0.18	0.23	0.18	0.31	0.53	0.37	0.26	0.28	0.25	0.32
	std	0.29	0.22	0.29	0.34	0.30	0.38	0.43	0.39	0.32	0.31	0.38	0.43
Return expectation	Mean	4.28	4.18	3.57	3.78	4.09	3.45	3.37	3.59	3.72	3.97	3.53	4.16
	std	0.94	0.92	0.96	0.97	1.00	1.06	1.04	1.10	0.99	1.09	1.17	1.06
Risk perception	Mean	4.49	4.44	5.00	4.15	3.97	4.45	4.27	4.26	4.24	4.18	4.44	4.24
	std	1.63	1.58	1.93	1.13	1.15	1.17	1.31	1.28	1.24	1.22	1.32	1.20
Risk tolerance	Mean	3.91	3.93	3.58	3.77	3.85	3.56	3.67	3.70	3.79	3.74	3.73	3.86
	std	1.19	1.11	1.25	1.19	1.18	1.30	1.33	1.26	1.18	1.20	1.28	1.14
Confidence	Mean	5.31	5.35	5.45	5.48	5.40	5.58	5.62	5.48	5.42	5.32	5.51	5.38
	std	0.96	0.96	0.94	0.99	1.07	1.00	0.97	1.04	1.03	1.06	0.98	1.04

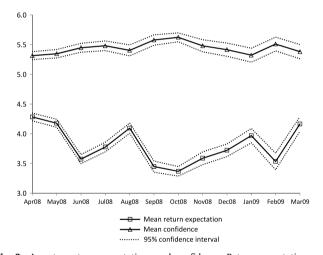
This table presents monthly summary statistics for the brokerage account data. Panel A refers to all investors for whom brokerage records are available. This sample includes investors who participated at least once in the survey during the sample period, and who were not excluded by the sample-selection restrictions defined in Section 3. The monthly summary statistics presented in Panel B refer to the subset of investors who responded to the survey in each respective month. Variables are defined in Table 1. Turnover statistics refer to the subset of investors that traded in a particular month.

**Table 3** Survey questions.

Survey variable	Answer categories
Return expectation (1 = low/pessimistic, 7 = high/optimistic)	
Next month, I expect my investments to do less well than desired.	1 (totally agree)-7 (totally disagree)
For the next month, I have a positive feeling about my financial future.a	1 (totally agree)-7 (totally disagree)
Next month, my investments will have a worse performance than those of most other investors.	1 (totally agree)-7 (totally disagree)
Next month, it is unlikely that my investment behavior will lead to positive returns.	1 (totally agree)-7 (totally disagree)
For the next month, the future of my investment portfolio looks good. <sup>a</sup>	1 (totally agree)-7 (totally disagree)
Risk tolerance ( $1 = low risk tolerance, 7 = high risk tolerance$ )	
Next month, I prefer certainty over uncertainty when investing.	1 (totally agree)-7 (totally disagree)
Next month, I avoid risks when investing.	1 (totally agree)-7 (totally disagree)
lext month, I do not like to take financial risks.	1 (totally agree)-7 (totally disagree)
Next month, I do not like to "play it safe" when investing. <sup>a</sup>	1 (totally agree)-7 (totally disagree)
Risk perception ( $1 = low$ perceived risk, $7 = high$ perceived risk)	
consider investing to be very risky next month. <sup>a</sup>	1 (totally agree)-7 (totally disagree)
consider investing to be safe next month.	1 (totally agree)-7 (totally disagree)
consider investing to be dangerous next month. <sup>a</sup>	1 (totally agree)-7 (totally disagree)
consider investing to have little risk next month.	1 (totally agree)-7 (totally disagree)
Confidence ( $1 = low confidence, 7 = high confidence$ )	
How confident are you about this answer?b	1 (not confident at all)-7 (very confident

This table presents the questions used in this study's 12 monthly surveys. A 7-point Likert scale is used to record investors' response to each question. Each survey variable (return expectation, risk tolerance, risk perception, confidence) is calculated as the equally weighted average of the respective survey questions.

- Denotes a reverse-scored question.
- <sup>b</sup> Indicates that this question is asked five times, that is, after each return expectation question.



**Fig. 3.** Investor return expectations and confidence. Return expectations and confidence are measured on a 7-point Likert scale (see Table 3). A small value indicates low return expectations or confidence, whereas a large value indicates high return expectations or confidence.

#### 4. Empirical tests

## 4.1. Confident investors rely more strongly on naïve reinforcement learning

We test whether more confident investors rely more on naïve reinforcement learning. That is, we examine whether compared to less confident investors, more confident investors extrapolate return experiences more strongly when updating their return expectations (Hypothesis 1). We run panel regressions with the change in return expectations from the end of the previous month to the end of the current month (baseline specification) or levels of return expectations as the dependent variable. We include investors' portfolio returns during the current month (calculated as the product of the daily relative changes in the value of their portfolio, taking into account transaction costs and adjusting for portfolio in- and outflows) to capture return experiences and continuous interactions of these returns with investor confidence at the end of the previous month (alternatively per investor average confidence), as explanatory variables. Regarding investor time-invariant effects, we include gender, age, account tenure, income, average portfolio value, <sup>4</sup> and house value. These variables are related to investor sophistication and experience, which drive individual investor behavior (Barber and Odean, 2001; Dhar and Zhu, 2006; Korniotis and Kumar, 2011) and could also affect the updating of their beliefs. Bauer et al. (2009) find that investors who trade derivatives score higher on a survey question measuring whether they invest as a hobby compared to investors who do not trade derivatives. Therefore, we include an indicator of derivatives trading (Derivatives) as a time-variant control capturing potential alternative trading motivations, such as entertainment. We include month fixed effects to control for unobserved factors that could impact both the survey measures and return variable (such as monthly variation in market returns). By including these controls, we measure the distinct effects of individual return experiences and confidence on investor return expectations (see Table 4). In the first and second columns of Table 4, we document returnexperience-based naïve reinforcement learning. In particular, the positive coefficient on experienced returns indicates that investors extrapolate individual return experiences when updating their return expectations. In the third column, which is the baseline specification, we extend model (1) by including confidence at the end of the previous month, and an interaction of that variable with returns, as independent variables. The third column provides supporting evidence for Hypothesis 1: the interaction term of confidence and returns is positive and significant. More confident investors thus extrapolate recent return experiences more strongly when forming their return expectations.<sup>5</sup>

<sup>&</sup>lt;sup>4</sup> We include the average of the portfolio value instead of the time-variant monthly portfolio value, because the monthly value is highly correlated with investors' returns. Instead of using the per-postal-code assigned income and residential house value control variables, we alternatively estimate model specifications with three-digit postal-code fixed effects and two-way clustered standard errors (investor and postal code). Results are consistent with the current specification. Thus, unobserved location-specific factors other than income and house value (such as overall wealth, education, or information) do not explain our results.

 $<sup>^5</sup>$  The coefficient for past return is insignificant in this specification, but the three coefficients for past return, confidence, and the interaction term of both these variables are jointly significant at the 1% level (p-value = 0.000). The coefficient for past return is negative in this specification. Thus, investors with very low levels of confidence (below 2.89) would actually depict a reversed extrapolation bias. Only 0.73% of observations are below this threshold, and thus such a reversed extrapolation bias has little empirical relevance.

**Table 4**Impact of past return and confidence on changes in return expectation.

Dependent variable	$\Delta$ return $\epsilon$	expectation	Return e	expectation	$\Delta$ return e (Baseline S	expectation Spec.)	$\Delta$ return $\epsilon$	expectation	Return ex	pectation
	(1)		(2)		(3)		(4)		(5)	
	Coef.	Std. err.	Coef	Std. err.	Coef	Std. err.	Coef.	Std. err.	Coef.	Std. err.
Return	0.423	0.086***	0.411	0.078***	-0.461	0.432	-0.503	0.479	0.321	0.370
Confidence $t-1$					0.032	0.014**			-0.021	0.022
Return $*$ Confidence $t-1$					0.159	0.075**			0.041	0.067
Avg. Confidence							-0.001	0.014		
Return * Avg. Confidence							0.166	0.086*		
Gender	0.054	0.039			0.053	0.040	0.060	0.040		
Age	0.000	0.001			0.000	0.001	0.001	0.001		
Account tenure	-0.002	0.003			-0.002	0.003	-0.002	0.003		
ln(Income)	0.025	0.088			0.026	0.088	0.020	0.088		
In(Avg. portfolio value)	-0.003	0.006			-0.003	0.006	-0.003	0.006		
ln(House value)	0.013	0.045			0.012	0.045	0.014	0.045		
Derivatives	0.049	0.036	0.148	0.050***	0.052	0.036	0.049	0.036	0.136	0.057**
Constant	-0.650	0.586	3.643	0.068***	-0.067	0.590	0.151	0.601	3.837	0.156***
Time fixed effects		YES		YES	,	YES		YES	Y	ES
Individual fixed effects		NO		YES		NO		NO	Y	ES
N observations	;	3955		5918	3	955	3955		39	)55
N investors		1045		1376	1	045	1045		1045	
$R^2$	(	0.164		0.198	0	.165	0	.165	0.200	

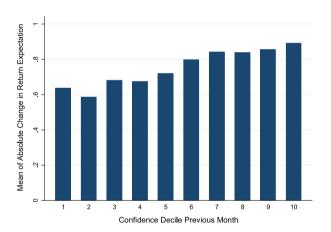
This table presents the results from regressions of changes (columns 1, 3, 4) in investor return expectations (= Return Expectation<sub>t</sub> - Return Expectation<sub>t-1</sub>) or levels (columns 2, 5) of return expectations (= Return Expectation<sub>t</sub>) on past investor returns, interactions of past returns with past confidence (columns 3, 5) or with per investor average confidence (column 4), and a set of control variables. That is, we regress the end of the month update of return expectations in t on the respective return experience during that month t. The columns show results of linear panel models. The number of individual investors included in the regression (1045) is smaller than the sample available for analysis (1376) because not all investors responded to the survey for two consecutive months (columns 1, 3, 4, 5). Standard errors are clustered on the investor level. Variables are defined in Table 1.

- \* Denote statistical significance at the 10% level.
- \*\* Denote statistical significance at the 5% level.
- \*\*\* Denote statistical significance at the 1% level.

The fourth column shows that the results do not differ substantially if we relate changes in beliefs alternatively to per investor sample-period average confidence. This result is consistent with a robustness check reported in Section 5.2 which shows that confidence, being related to a certain type of decision maker who relies more on intuition (Dual Process Theory's System 1), is stable within investors. Finally, the fifth column documents that when, alternatively, we regress levels of beliefs on investor confidence in an individual fixed-effects model, the confidence and confidence return interaction terms are no longer significant. That is, the very small (if any) time variation in investor confidence in the sample (see Section 5.2) does not drive our results.

## 4.2. Confident investors change their return expectations more strongly

Next, we analyze the link between investor confidence and magnitudes of changes in beliefs. That is, we test Hypothesis 2, according to which more confident investors change their beliefs more strongly. In this section we focus on the absolute value of changes in return expectations, as both positive and negative updates in return expectations provide reason for trading (see Section 4.3). Fig. 4 plots the average of the absolute values of the changes in return expectations against previous month's confidence deciles. This figure suggests that investor confidence is positively related to the absolute magnitude of updates in beliefs. We test the significance of the relation of confidence and the absolute magnitudes of updates of return expectation (=  $ABS[Return\ Expectation_{t} - ReturnExpectation_{t-1}])$  using panel regressions with the explanatory variables as in Section 4.1 We estimate the direct impact of investor confidence on absolute magnitude of changes in beliefs. That is, we model the effect



**Fig. 4.** Mean of absolute changes in return expectations per confidence decile in previous month. This figure shows the mean absolute change of investor return expectations (= mean of ABS[Return Expectation $_t$  — Return Expectation $_{t-1}$ ]) per decile of the distribution of confidence of the previous month. Return expectation and confidence are measured on a 7-point Likert scale (see Table 3). A small value indicates low return expectation or confidence, whereas a large value indicates high return expectation or confidence.

of investor confidence on changes in beliefs, irrespective of the direction of these changes in beliefs.

The first column of Table 5 shows that investor confidence is positively and significantly related to the magnitudes by which investors update their return expectations. We find support for Hypothesis 2: more confident investors change their beliefs more strongly. When controlling for the standard deviation of returns in investors' portfolios (see second column in Table 5), the effect of confidence on the magnitudes of updates in return expectations remains significant. Thus, higher magnitudes of updates by confident investors are not driven merely by more volatile return experiences (see the related robustness check in Section 5.3). Finally, in the third column, we use the log of absolute magnitudes

 $<sup>^{\</sup>rm 6}\,$  This also holds for the analyses testing Hypotheses 2 and 3.

**Table 5**Impact of confidence on absolute changes in return expectations.

Dependent variable	ABS[∆ return e	expectation]	ABS[∆ return e	expectation]	$ln(ABS[\Delta returexpectation])$	n
	(1)		(2)		(3)	
	Coef.	Std. err.	Coef.	Std. err.	Coef.	Std. err.
Return	-0.006	0.067	0.044	0.065	0.175	0.113
Confidence $t-1$	0.092	0.012***	0.092	0.012***	0.119	0.021***
Std(Return)			0.058	0.049	0.081	0.078
Gender	-0.033	0.040	-0.032	0.040	-0.013	0.071
Age	0.002	0.001**	0.002	0.001**	0.002	0.002
Account tenure	-0.005	0.005	-0.005	0.005	-0.006	0.008
In(Income)	0.051	0.119	0.048	0.119	-0.183	0.194
In(Avg. portfolio value)	0.011	0.008	0.013	0.008	0.004	0.013
In(House value)	-0.008	0.057	-0.008	0.057	0.075	0.099
Derivatives	0.034	0.034	0.027	0.035	0.055	0.058
Constant	-0.370	0.804	-0.377	0.803	-0.700	1.250
Time fixed effects		YES		YES	Y	ES
N observations		3955		3955	39	55
N investors		1045		1045	10	45
$R^2$		0.046		0.047	0.0	30

This table presents the results from regressions of absolute value (columns 1, 2) or the log of the absolute value (column 3) of changes in investor return expectations (= ABS[Return Expectation $_t$  – Return Expectation $_{t-1}$ ]) on past confidence and a set of control variables. The columns show results of linear panel models. The number of individual investors included in the regression (1045) is smaller than the sample available for analysis (1376), because not all investors responded to the survey for two consecutive months. Standard errors are clustered on the investor level. Variables are defined in Table 1.

of updates of return expectations as an alternative dependent variable, to account for skewness in the dependent variable that is introduced through the absolute-value transformation, yielding results that are consistent with those reported before. Past returns are no longer significant in all three specifications, as they impact directional changes in return expectations that average out through the absolute-value transformation.

## 4.3. Investors who change their return expectations more strongly trade more

Finally, we test whether investors who change their beliefs more strongly also trade more (Hypothesis 3). First, we test the foundation for Hypothesis (3), which is a positive relation between expected returns and demand for risky assets. Then, we test Hypothesis (3) by regressing investors' trading activity (Turnover) on the updates in their return expectations.

We regress the fraction of an investor's total account value (portfolio value + cash) invested in risky assets at the end of a particular month t on investor return expectations at the beginning of the month (Return Expectation $_{t-1}$ ) in a model with month and individual fixed effects. That is, we test whether the time variation in expected returns explains subsequent changes in demand for risky assets proxied by movements within an account from cash to the investment portfolio. As time-varying control variables, we include the portfolio return of the current month (controlling for the passive effect of portfolio returns on the composition of the account value), investor risk perception and risk tolerance at the beginning of the month, and an indicator of derivatives trading. Results in Table 6 confirm that higher return expectations increase investor demand for risky assets.

Next, we regress the turnover of investors that traded in a particular month (=  $Turnover_t$ ) on the lagged absolute

**Table 6**Impact of past return expectations on risky asset demand.

Dependent variable	Fraction of accou	ınt invested
	Coef.	Std. err.
Return	0.073	0.029**
Return expectation $t-1$	0.014	0.006**
Risk tolerance $t-1$	-0.002	0.004
Risk perception $t-1$	-0.004	0.003
Derivatives	0.027	0.013**
Constant	0.519	0.155***
Time fixed effects	Y	ES
Individual fixed effects	Y	ES
N observations	39	55
N investors	10	45
$R^2$	0.0	38

This table presents the results from regressions of the fraction of an investor's account value invested ( = Portfolio Value/(Portfolio Value + Cash)) at the end of a particular month on return expectations at the beginning of the month ( $= Return \ Expectation_{t-1})$ , and a set of control variables. The column shows results of a linear panel model. The number of individual investors included in the regression (1045) is smaller than the sample available for analysis (1376) because not all investors responded to the survey for two consecutive months (columns 1, 3, 4, 5). Standard errors are clustered on the investor level. Variables are defined in Table 1.

changes in return expectations (= ABS[Return Expectation $_{t-1}$  - Return Expectation $_{t-2}$ ]) and a set of control variables. That is, we examine the link between investors' trading activity in a particular month and the magnitude of the absolute value of the update in their return expectations over the preceding month.

The results in the first column of Table 7 support Hypothesis 3: investors who change their beliefs (return expectations) more strongly have higher turnover in the subsequent period. Larger changes in beliefs provide more reason to trade. This result also holds when we control for investors' risk tolerance and risk perception (second column), ruling out the possibility that the effect of confidence on trading would not work through more confident investors' stronger updates in beliefs, but instead would work through their risk tolerance and risk perception, which might relate to confidence and intuitive judgments (Dorn and Huberman, 2005; Butler et al., 2013). Using either log turnover (accounting for

<sup>\*</sup> Denote statistical significance at the 10% level.

<sup>\*\*</sup> Denote statistical significance at the 5% level.

<sup>\*\*\*</sup> Denote statistical significance at the 1% level.

<sup>&</sup>lt;sup>7</sup> Because of limitations of the portfolio data, we do not have a breakdown of assets within a portfolio available. We cannot rule out that some portfolio positions are, similar to cash, invested risk-free. However, the asset classification available for investors' transactions indicates that potentially risk-free investments (bonds) make up only 1.6% of total trading volume. That is, investor' portfolios most likely include primarily risky assets.

<sup>\*</sup> Denote statistical significance at the 10% level.

<sup>\*\*</sup> Denote statistical significance at the 5% level.

<sup>\*\*\*</sup> Denote statistical significance at the 1% level.

**Table 7**Impact of absolute changes in return expectations on trading

Dependent variable	Turnover (1)		Turnover (2)		ln(Turnove (3)	r)	ln(Number (4)	of trades)
	Coef.	Std. err.	Coef.	Std. err.	Coef.	Std. err.	Coef.	Std. err.
Return $t-1$	-0.006	0.097	-0.007	0.098	0.020	0.142	0.010	0.073
ABS[ $\Delta$ return expectation] $t-1$	0.071	0.028**	0.071	0.028**	0.188	0.070***	0.085	0.049*
Risk tolerance $t-1$			0.030	0.024	0.056	0.050	0.051	$0.029^{*}$
Risk perception $t-1$			0.033	0.017*	0.056	0.040	-0.008	0.023
Gender	-0.083	0.065	-0.074	0.064	-0.139	0.232	0.126	0.160
Age	0.001	0.003	0.002	0.003	0.004	0.005	0.008	0.003
Account tenure	0.009	0.009	0.008	0.009	0.005	0.024	-0.013	0.015
ln(Income)	0.223	0.242	0.203	0.240	0.672	0.684	0.431	0.455
ln(Avg. portfolio value)	-0.083	0.023***	-0.084	0.022***	-0.222	0.043***	0.072	0.028**
ln(House value)	-0.238	0.139*	-0.226	0.139	-0.622	0.352*	-0.383	$0.229^{*}$
Derivatives	0.052	0.048	0.060	0.048	-0.059	0.149	0.710	0.103
Constant	1.547	1.501	1.337	1.455	-0.236	4.024	0.549	2.649
Time fixed effects		YES		YES		YES	Y	ES
N observations		1369		1369		1369	13	69
N investors		523		523		523	523	
$R^2$		0.083		0.089		0.112	0.1	82

This table presents the results from regressions of turnover (columns 1, 2), the log of turnover (column 3), or the log of the number of transactions (column 4) in a particular month t on the lagged absolute value of changes in investor return expectations (= ABS[Return Expectation $_{t-1}$  - Return Expectation $_{t-2}$ ]) and a set of control variables. The columns show results of linear panel models. The number of individual investors included in the regression (523) is smaller than in the previous regressions (1045), because the sample refers to investors that traded in a particular month and because the use of lagged absolute changes in return expectation reduces the panel length. Standard errors are clustered on the investor level. Variables are defined in Table 1.

- \* Denote statistical significance at the 10% level.
- \*\* Denote statistical significance at the 5% level.
- \*\*\* Denote statistical significance at the 1% level.

the skewness of this variable) or the log number of transactions as an alternative dependent variable provides consistent evidence (third and fourth columns).

Finally, Table 8 presents information on the heterogeneity in investors' return experiences, changes in return expectations, and absolute changes in return expectations. Table 8 shows that within the cross-section of investors in each month, there is substantial variation in the magnitude of returns, the sign of returns achieved (positive vs. negative), the magnitude and direction of changes in return expectations, and the magnitude of absolute changes in return expectations. That is, next to changes in beliefs as one precondition of trading, we observe a second precondition for trading: there is heterogeneity in the magnitude and direction of changes in beliefs. That is, there are differences in beliefs and changes in those differences. Accordingly, investors with reason to trade will be able to find a trading counterpart. Moreover, even if the changes in beliefs (and thus behavior) of different individual investors might be correlated (as they form expectations based on potentially correlated past returns), institutional traders can absorb individual investor demand and supply (Cohen et al., 2002). Likewise, firms tend to issue equity when stock markets perform well (Baker and Wurgler, 2000, 2009), thereby absorbing correlated demand from individual investors.

#### 5. Robustness checks

#### 5.1. Rationality of reliance on naïve reinforcement learning

Our conceptual framework links investors' return expectation formation to confidence, in that more confident investors rely more on naïve reinforcement learning and thus extrapolate recent return experiences more strongly than less confident investors. A relevant question in this regard is whether extrapolating recent return experiences when forming return expectations is rational in the sense that it is associated with achieving higher returns. In line with previous studies (e.g., Welch and Goyal, 2008), the returngenerating process in our sample does not exhibit predictability

or momentum, and return expectations do not contain information on investors' skills or subsequent performance. Investor confidence, however, might contain information related to superior trading skills, so that it could be rational for more confident investors to extrapolate recent return experiences more strongly compared to less confident investors. To examine this possibility, in the following we regress investor returns on past return expectations, past confidence, and an interaction term for past return expectations with investor confidence.

Table 9 shows that neither past return expectations alone (first column), nor investor confidence and its interaction with return expectations (second column) are significantly related to investor returns. That is, investor confidence is not correlated with superior skills. If we exclude from the model variables that are related to investor confidence, that is, return expectations (related to confidence when forming beliefs) and trading indicators (related to confidence as confidence triggers trades through changing beliefs), investor confidence has a significantly negative effect on investor returns (third column). That is, through the belief formationtrading channel, high levels of confidence have a negative impact on investor returns. The negative impact of investor confidence on returns is economically relevant. The difference in means of the monthly returns between investors with above-average confidence and below-average confidence (without controlling for any investor characteristics) is 88 basis points (p-value = 0.012). To conclude, it is not rational for more confident investors to extrapolate recent return experiences to the future more strongly. If anything, these investors' more strongly changing beliefs hurt their performance through higher turnover. Evaluating alternative performance measures (i.e., Sharpe Ratio, Jensen's Alpha) yields consistent evidence (detailed results available on request).

<sup>&</sup>lt;sup>8</sup> Controlling for investor characteristics leads to similar estimates. Based on Table 9 column (3), the coefficient for confidence is -0.007. Average confidence for the subset of investors above the overall average of 5.442 is 6.167, for investors below the overall average it is 4.751. Multiplying the confidence difference between these subgroups of 1.416 (= 6.167 - 4.751) with -0.007 gives an estimated monthly return differential of -0.0099, that is, 99 basis points.

Table 8
Heterogeneity in return experiences and changes in return expectations.

Month		Apr- 08	May- 08	Jun- 08	Jul- 08	Aug- 08	Sep- 08	Oct- 08	Nov- 08	Dec- 08	Jan- 09	Feb- 09	Mar- 09
Return	Mean	0.03	0.00	-0.18	-0.10	0.05	-0.25	-0.22	-0.12	-0.04	0.00	-0.17	-0.01
Return	std	0.17	0.12	0.18	0.18	0.20	0.18	0.34	0.19	0.16	0.20	0.20	0.21
Fraction return $\geq 0$		0.77	0.65	0.03	0.16	0.85	0.02	0.16	0.16	0.41	0.61	0.07	0.62
$\Delta$ return expectation	Mean		-0.11	-0.60	0.20	0.32	-0.65	-0.08	0.22	0.13	0.25	-0.43	0.63
$\Delta$ return expectation	sd		0.92	0.97	0.90	0.84	0.97	0.88	0.91	0.89	0.88	0.96	0.93
Fraction $\Delta$ return expectation $\geq 0$			0.47	0.23	0.56	0.67	0.23	0.38	0.61	0.50	0.60	0.31	0.72
ABS[∆ return expectation]	Mean		0.69	0.90	0.67	0.69	0.92	0.69	0.72	0.65	0.68	0.79	0.83
ABS[∆ return expectation]	sd		0.61	0.69	0.63	0.56	0.73	0.59	0.60	0.62	0.61	0.69	0.74

This table presents monthly summary statistics for investor returns, changes in return expectations, and absolute changes in return expectations. Variables are defined in Table 1.

**Table 9**Impact of past return expectations and confidence on return performance.

Dependent variable	Return (1)		Return (2)		Return (3)		
	Coef.	Std. err.	Coef.	Std. err.	Coef.	Std. err.	
Return expectation $t-1$	0.003	0.003	0.012	0.017			
Confidence $t-1$			0.001	0.012	-0.007	$0.004^{*}$	
Return expectation $t - 1 * Confidence t - 1$			-0.002	0.003			
Gender	0.006	0.009	0.007	0.009	0.006	0.010	
Age	0.000	0.000	0.000	0.000	0.000	0.000	
Account tenure	0.000	0.001	0.000	0.001	0.000	0.001	
ln(Income)	0.000	0.028	-0.002	0.028	-0.009	0.029	
In(Avg. portfolio value)	0.016	0.003***	0.016	0.003***	0.017	0.003***	
In(House value)	0.010	0.016	0.010	0.016	0.012	0.017	
Derivatives	-0.079	0.013***	-0.079	0.013***	-0.099	0.013***	
Traded	-0.015	0.006**	-0.015	0.006**			
Turnover	-0.014	0.003***	-0.014	0.003***			
Constant	-0.365	0.230	-0.361	0.233	-0.296	0.238	
Time fixed effects		YES		YES	YI	ES	
N observations		3955		3955	39	55	
N investors		1045		1045	10	45	
$R^2$		0.323		0.324	0.2	95	

This table presents the results from regressions of investors' returns on past investor return expectations (column 1), continuous interactions of past returns with past confidence (column 2), past confidence (column 3), and a set of control variables. That is, we regress returns in a particular month t on the respective expectations and confidence for that month which were elicited at the end of period t-1. The columns show results of linear panel models. The number of individual investors included in the regression (1045) is smaller than the sample available for analysis (1376), because not all investors responded to the survey for two consecutive months. Standard errors are clustered on the investor level. Variables are defined in Table 1.

- \* Denote statistical significance at the 10% level.
- \*\* Denote statistical significance at the 5% level.
- \*\*\* Denote statistical significance at the 1% level.

## 5.2. Investor confidence: reliance on intuition and use of intuitive shortcuts and heuristics

In our conceptual framework, we link investor confidence with reliance on intuition and the use of intuitive shortcuts and heuristics. Our results (stronger reliance on naïve reinforcement learning by more confident investors) are consistent with such a link between confidence and reliance on intuition and heuristics, but we cannot directly test this link with the available data. Thus, in the following we perform additional robustness checks. First, to test whether investor confidence is indeed a rather general personality characteristic, we analyze whether it is relatively stable over time within a person as predicted by several studies in psychology (Stanovich and West, 2000; Evans, 2003, 2008; Alós-Ferrer and Hügelschäfer, 2012). Second, to check whether investor confidence is related to reliance on intuition and heuristics, we test whether it has a systematic relationship with other beliefs of investors that are driven by return experiences, even when investor confidence is measured in the context of return expectations. Third, we present additional evidence from a subsample of investors that in a 2006 survey was asked to indicate if they base their investment decisions primarily on intuition.

To test whether our measure of investor confidence relates to a certain type of individual (i.e., one who relies more or less on intuition in general), we first examine how the crosssectional mean of confidence changes over time. Confidence varies from month to month, but not by large amounts, and in most cases not significantly. The average of the 11 monthly absolute changes of confidence (measured on a scale from 1 to 7) is 0.1. Of the 11 changes, one is statistically significant at the 1% level (August-September 2008), two are significant at the 5% level (October-November 2008, January-February 2009), and one is significant at the 10% level (May-June 2008) (see Fig. 3). Second, we examine within-investor changes in confidence. We find a high correlation coefficient of 0.65 (p-value = 0.000) between an investor's current month's confidence and his or her previous month's confidence. Likewise, the correlations are high over longer time intervals. For example, the correlation coefficient over a six month interval is 0.53 (p-value = 0.000) and over twelve months it is 0.58 (p-value = 0.000). Also, the average crosssectional standard deviation of confidence (0.99) is larger than the average within-investor's time-series standard deviation (0.55). Sorting investors into deciles based on their confidence in the previous month and then calculating the average value of current month's confidence for each decile provides supporting evidence (see Fig. 5). That is, Fig. 5 indicates that if an investor was in a high (low) confidence decile in the previous month, he or she is also more likely to have high (low) confidence in the current month. In addition, a transition matrix (see Table 10) shows that transition probabilities are highest along the diagonal. Hence, we find evidence that our measure of investor confidence refers to a certain type of individual, as it is stable over time.

Moreover, there is no evidence that any of the small fluctuations in investor confidence are driven by past returns, that is, that high returns lead investors to learn to be overconfident (Gervais and Odean, 2001). In Table 11, we regress investor confidence on past returns. The first (no fixed-effects) and second (time fixedeffects) columns show a negative and significant relation between investor confidence and returns, while no significant effect is present in the third (changes in confidence as dependent variable) and fourth columns (levels as dependent variable including both time and individual fixed-effects). That is, confident investors generally have lower returns (because of their higher turnover, see Section 5.1), but variation in those lower returns does not change their confidence.9 This result also holds when we include an indicator variable for investors having positive returns, to test for potential asymmetry in the effect of past returns on investor confidence. That is, it is not the case that investors increase their confidence after positive returns, but not after negative returns or vice versa (column 5).

If confidence is indeed a rather general personality characteristic and related to reliance on intuition, then investors who are more confident about their return expectations, and display greater updates in those expectations, should also display greater updates in their risk perceptions. To check for this possibility, we regress the absolute changes in risk perception on past confidence with the same set of control variables as used in the returnexpectation regression in Section 4.2 We find that confidence has a significant and positive impact on the magnitude of changes for risk perceptions. The coefficient for confidence in the risk perception regression is 0.092 (p-value = 0.000) (compare to the return expectation results in Table 5, model (1)). Thus, although confidence is measured with respect to an individual's return expectation, it seems to reflect a more general personality trait, as it interacts in a consistent way with how an individual updates his or her risk perception. Note that investor confidence itself is not correlated to the risk perception measure (Pearson correlation coefficient = -0.002, p-value = 0.831). That is, investor confidence is not proxying for the perceived riskiness of investment returns.

We find further supporting evidence for a link between investor confidence and reliance on intuition using additional information from a 2006 survey with the same broker where investors were asked to indicate based on which method or information source (i.e., technical analysis, fundamental analysis, financial news, professional advice, family acquaintances, own intuition) they trade (see Hoffmann and Shefrin, 2014 for details on this survey). Matching respondents of the 2006 survey with the current survey yields a sample of 245 investors for whom we have both information on confidence and the method or information source used for forming decisions. Using this subset of the sample, we compare the fraction of investors that indicate to rely exclusively on intuition for making their decisions between investors with high and low (average) confidence. Indeed, more confident investors indicate to more often rely only on their intuition. The difference in the fraction of investors relying only on intuition between investors in the top confidence quartile and bottom confidence quartile is 6.11%. This difference, however, is not statistically significant (p-value = 0.205), potentially because of the small sample size.

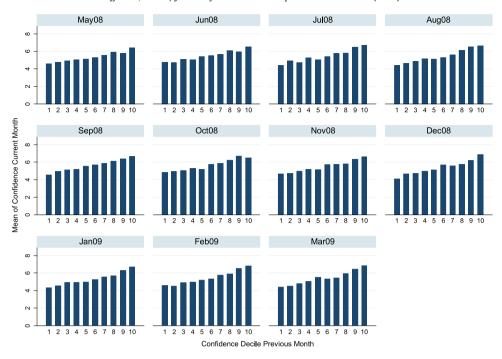
#### 5.3. Survey data quality

A general concern with survey data is that the variation in response rate could be non-random. To examine this possibility, we estimate a panel probit model where survey participation is explained by the main variables of interest, that is, investor confidence, return expectations, returns, and turnover. For confidence and return expectations, we use the sample period average per investor, because for non-participating investors, the information is not available. This regression only yields a significant coefficient (0.030) for turnover (p-value = 0.001), indicating that investors with higher turnover are more likely to participate in the survey. The economic significance of this effect, however, is small: a onestandard deviation increase of turnover from the mean increases the probability to participate in the survey by 1.45%. Nevertheless, we additionally account for potential non-random response effects in the regression model explaining turnover (Table 7) by applying an inverse-probability-weighted estimator (Robins and Rotnitzky, 1995; Wooldridge, 2002). For each of the 12 months, we estimate a logit model where the dependent variable indicates either response (1) or non-response (0) to the survey. As explanatory variables, we include confidence, return expectations, returns, and turnover. Next, the predicted probabilities of survey response are calculated. Finally, the turnover regression models are estimated again using the inverse of the predicted probabilities as sample weights. The results obtained are similar to the original specifications in terms of coefficient magnitudes, significance, and signs (detailed results available upon request). For example, the coefficient for the lagged absolute change in return expectations becomes 0.080 (p-value = 0.005) (compare Table 7, model 1). Overall, our results are thus not impacted by non-random response behav-

Another potential concern is response timing potentially affecting the results. In particular, beliefs and confidence of early versus late respondents in each month might differ because of changes in individual portfolio returns between their response days. As the majority of survey response (85%) is received within the first five days after we sent out each survey email, it is unlikely that there is a response-time pattern that could lead to a possible bias. When estimating all models excluding late respondents (more than five days response time), we obtain similar results compared to the original specifications in terms of coefficient magnitudes, significance, and signs (detailed results available upon request). That is, response timing is not a concern.

To measure investors' return expectations, we use survey items that have been used and cross-validated in a previous study (Hoffmann et al., 2013). In the context of the present study, however, the third survey item of the return expectation measure ("Next month, my investments will have a worse performance than those of most other investors") could raise some concerns. That is, because of the wording of this question, it could potentially pick up investor confidence in its overplacement variant (the better-than-average effect). If this is the case, our finding that updates in return expectations are related to investor confidence might be driven by regressing one confidence measure on another. To check for this possibility, we rerun the main analyses, but now exclude this survey item when calculating the measure for return expectations, as well the corresponding question for confidence when calculating the measure for investor confidence. The results of this robustness check are consistent with the main results, as reported previously: Based on these revised return expectations and confidence measures, the correlation coefficient of confidence with return expectations remains close to zero (Pearson correlation coefficient = -0.054, p-value = 0.000), and the correlation of the current month's confidence with the previous month's confidence remains high (Pearson correlation

<sup>&</sup>lt;sup>9</sup> The regression also shows that females are more confident than males. This effect is in line with the role of confidence in our framework, that is, reliance on intuition. It is also consistent with the evidence on reliance on intuition and gender differences in Butler et al. (2013).



**Fig. 5.** Mean of investor current confidence per confidence decile in previous month. This figure shows the mean confidence of investors at the end of a particular month per decile of the distribution of confidence of the previous month (cross-sectional mean). Confidence is measured on a 7-point Likert scale (see <u>Table 3</u>). A small value indicates low confidence, whereas a large value indicates high confidence.

**Table 10**One-month transition matrix across deciles of confidence distribution.

Decile $t-1$	Decile t (	Decile t (percentages)												
	1	2	3	4	5	6	7	8	9	10				
1	35.9	21.0	11.0	10.8	6.2	4.4	3.6	3.3	2.6	1.3				
2	18.6	25.0	21.0	12.2	9.0	5.9	2.9	2.7	1.9	0.8				
3	14.4	18.5	17.0	13.9	13.2	7.4	7.7	5.0	1.4	1.4				
4	6.9	12.0	17.4	18.9	14.0	12.5	8.9	5.9	1.8	1.8				
5	7.5	8.7	13.9	16.2	15.4	13.4	11.6	8.2	3.6	1.5				
6	4.2	3.2	11.0	11.7	14.9	21.1	13.9	9.7	6.2	4.0				
7	4.0	3.8	6.1	8.9	9.6	14.6	22.5	15.3	10.3	4.9				
8	1.3	3.2	4.2	5.0	7.9	11.6	20.2	20.2	17.9	8.7				
9	2.2	2.2	2.5	2.0	4.7	6.5	11.2	16.4	25.6	26.6				
10	1.7	1.2	1.7	1.7	1.7	1.9	5.5	6.9	24.9	52.9				

This table presents transition probabilities for an investor moving from a particular decile in the distribution of confidence at the end of the previous month to a decile in the corresponding distribution at the end of the current month. The confidence measure is defined in Table 1.

coefficient = 0.619, p-value = 0.000). Moreover, the coefficient of the confidence interaction term with past returns in the changes in the return-expectation regression is positive (0.196) and significant (p-value = 0.015) (compare with the original results in the third column of Table 4), the coefficient on confidence in the absolute changes in the return-expectation regression is positive (0.102) and significant (p-value = 0.000) (compare with Table 5), and the coefficient on the lagged absolute changes in return expectations in the turnover regression is positive (0.086) and significant (p-value = 0.003) (compare with Table 7).

A final potential concern with respect to the quality of the survey measures is that they are measured on a Likert scale that ranges from 1 to 7. Thus, investors that have responses at or close to the scales' upper or lower limit in a certain month might not be able to express updates in their return expectations for the next month or confidence therein appropriately. To test the robustness of the results, we exclude all observations for a particular month where return expectations or confidence values are smaller than 2 or larger than 6 in the respective previous month and estimate the models of Section 4 again on the resulting subsample. The results confirm the findings: within investors, confidence is stable over time (see Section 5.2), more confident investors rely more on naïve

reinforcement learning and exhibit larger absolute updates of their return expectations (see Section 4) (detailed results available upon request).

#### 6. Conclusion and discussion

More confident investors trade more than less confident investors, but why? Prior research tests the ultimate relation between investor confidence and trading, but does not empirically examine the underlying mechanism that explains why confidence leads to trading. We complement the literature by developing a conceptual framework and presenting empirical evidence on a psychologically plausible mechanism through which confidence leads to trading. In particular, we connect investor confidence and trading by introducing an "experience-confidence-belief" intermediate link. Investors form beliefs about future returns by extrapolating recent individual return experiences into future expectations. Confident investors rely more on such naïve reinforcement learning. That is, given the same return experience, confident investors change their beliefs more strongly, have more reason to trade than less confident investors, and thus trade more. Ultimately, confident investors' higher turnover hurts

Table 11 Impact of past returns on confidence.

Dependent variable	Confidence (1)	Confidence (1)		e	$\Delta$ confidence (3)	$\Delta$ confidence (3)		e	Confidence (5)	
	Coef.	Std. err.	Coef.	Std. err.	Coef.	Std. err.	Coef.	Std. err.	Coef.	Std. err.
Return	-0.337	0.072***	-0.198	0.089**	-0.008	0.070	-0.041	0.066	-0.037	0.073
Return > 0									-0.004	0.028
Gender	0.242	0.104**	0.239	0.104**	0.066	0.030**				
Age	0.002	0.002	0.002	0.002	0.001	0.001				
Account tenure	-0.009	0.010	-0.009	0.010	-0.002	0.003				
ln(Income)	-0.228	0.226	-0.219	0.226	0.090	0.083				
ln(Avg. portfolio value)	0.007	0.015	0.004	0.015	-0.001	0.005				
ln(House value)	0.095	0.115	0.089	0.116	-0.047	0.041				
Constant	6.326	1.489***	6.311	1.490***	-0.350	0.529	5.491	0.054***	5.492	0.054
Time fixed effects		NO		YES	,	YES	YES		YES	
Individual fixed effects		NO		NO		NO		YES	Y	ES
N observations		5918		5918	3	955	5918		5918	
N investors		1376		1376	1	.045	1376		13	76
$R^2$	(	0.012	(	0.017	0	.017	(	0.027	0.0	27

This table presents the results from regressions of confidence at the end of a particular month (columns 1, 2, 4, 5) and changes in confidence (column 3) on past investor returns and a set of control variables. The columns show results of linear panel models. The number of individual investors included in the regression in column 3 (1045) is smaller than the sample available for analysis (1376), because not all investors responded to the survey for two consecutive months. Standard errors are clustered on the investor level. Return > 0 indicates whether the return in a particular month was positive (1) or not (0). Variables are defined in Table 1.

their return performance. In particular, investors with aboveaverage confidence have 8.6 percentage-points higher monthly turnover than investors with below-average confidence. Finally, investors with above-average confidence underperform investors with below-average confidence by 88 basis points per month.

To the extent that high trading volume reduces investors' performance, our results have potential implications for developing smart defaults, frames, or nudges that might attenuate individual investors' tendency for portfolio churning. Previous literature finds that, for example, manipulating portfolio-evaluation periods or information-aggregating levels can affect investors' beliefs and behavior (see e.g., Gneezy and Potters, 1997; Gneezy et al., 2003; Beshears et al., 2011). Accordingly, especially confident investors might benefit from defaults that display their return experiences in a way such that they appear less volatile, which would potentially lead to smaller updates in their beliefs, thus giving them less reason to trade.

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<sup>\*</sup> Denote statistical significance at the 10% level.

Denote statistical significance at the 5% level.

Denote statistical significance at the 1% level.

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