

Self-Check 9

Answer the following questions to check your understanding of your material. Expect the same kind of questions to show up on your tests.

1. Definitions and Short Answers - functions

1. What is the equivalent **lambda expression** that computes the same as the following named function?

a.

```
def Double(n):  
    return n + n  
lambda n: n+n
```

b.

```
def Bigger(a, b):  
    return a if a > b else b
```

```
lambda a, b: a if a > b else b
```

2. What lambda expression can you pass to a list's sort method's optional **key plug-in function** if you want to sort a list of strings **by string length**? For example

```
>>> L = ['an', 'apple', 'a', 'day', 'keeps', 'the', 'doctor', 'away']  
>>> L.sort(key=lambda     )  
>>> L  
['a', 'an', 'day', 'the', 'away', 'apple', 'keeps', 'doctor']
```

which orders the strings from shortest to the longest. Fill in the yellow blank above.

```
lambda x: len(x)
```

3. If you want to sort a list of strings **primarily by length** and **secondarily alphabetically** (case-sensitive), what lambda would you pass to the key parameter of the list's sort method? Fill in the yellow blank below.

```
>>> L = ['a', 'glass', 'of', 'water', 'is', 'empty', 'or', 'full']  
>>> L.sort(key=lambda     )  
>>> L  
['a', 'is', 'of', 'or', 'full', 'empty', 'glass', 'water']
```

```
lambda x: (len(x), x)
```

4. Which of the following can properly sort a list of month names by month order, and why or why not? Assuming the following global symbols have been defined.

```
L = ['Apr', 'May', 'Nov', 'Mar', 'Jan', 'Feb', 'Oct', 'Jun', 'Jul', 'Aug', 'Sep', 'Dec']
```

ML = ['Jan', 'Feb', 'Mar', 'Apr', 'May', 'Jun', 'Jul', 'Aug', 'Sep', 'Oct', 'Nov', 'Dec']

MD = {'Jan':1, 'Feb':2, 'Mar':3, 'Apr':4, 'May':5, 'Jun':6, 'Jul':7, 'Aug':8, 'Sep':9, 'Oct':10, 'Nov':11, 'Dec':12}

- a. `L.sort(key=ML)` `TypeError: 'list' object is not callable`
 - b. `L.sort(key=MD)` `TypeError: 'dict' object is not callable`
 - c. `L.sort(key=lambda x: ML[x])`
`TypeError: list indices must be integers or slices, not str`
 - d. `L.sort(key=lambda x: MD[x])` `Correct`
 - e. `L.sort(key=lambda x: ML.index(x))` `Correct`
 - f. `L.sort(key=lambda x: MD.index(x))`
`AttributeError: 'dict' object has no attribute 'index'`
5. If `chr(97)` evaluates to 'a', then what is the value of
`list(map(chr, [97, 98, 99, 100, 101]))`
?
['a', 'b', 'c', 'd', 'e']
6. What is the value of
`list(map(max, [1, 7, 2, 8], [5, 6, 3, 0]))`
?
[5, 7, 3, 8], because it is equivalent to
[max(1, 5), max(7, 6), max(2, 3), max(8, 0)]
7. How do you use the built-in function `zip` to convert lists [1, 7, 2, 8] and [5, 6, 3, 0] into a list of tuples, as in
`[(1, 5), (7, 6), (2, 3), (8, 0)]`
?
`zip([1, 7, 2, 8], [5, 6, 3, 0])`
8. How to you write the equivalent **list-comprehension** version of
`list(map(max, [1, 7, 2, 8], [5, 6, 3, 0]))`
?
`[max(*t) for t in zip([1, 7, 2, 8], [5, 6, 3, 0])]`
9. Suppose you want to do
`list(map(lambda x, y: x+y, [1, 7, 2, 8], [5, 6, 3, 0]))`
but **replace** the lambda expression (underlined above) with **an existing function** that does the same.
What can you use instead?
(Hint: **import** from the **operator** module)
`import operator`

`list(map(operator.add, [1, 7, 2, 8], [5, 6, 3, 0]))`
10. If you want to read and print lines from a file but skip all blank lines using the following code template

```

1 fh = open('myfile')
2 for line in filter(lambda __, fh.readlines()):
3     print(line, end=") # no need to print extra newline
4 fh.close()

```

What should you put as the lambda expression above? Note that a blank line consists of a single newline character.

`lambda x: x != '\n'`

11. In the stack interpreter example, several versions of the interpreter are given.

The if-elif version looks like this:

```

1 def StackInterpreter():
2     L = []
3     while True:
4         line = input('command? ')
5         words = line.split()
6         if len(words) == 0:
7             pass
8         elif words[0] == 'show':
9             print(L)
10        elif words[0] == 'push':
11            L.extend(words[1:])
19        elif words[0] == 'pop':
20            print(L.pop())
21        elif words[0] == 'quit':
22            break
23        else:
24            print('unknown command')

```

How can lines 8-24 be replaced with a check for quit followed by using the command word (i.e., words[0]) to look up and execute the corresponding action? That is,

```

8'     if words[0] == 'quit':
9'         break
10'    D = {'show': ____,
11'        'push': ____,
12'        'pop': ____,
13'    }
14'    f = D.get(words[0], _____)
15'    f()

```

- a. on line 10' (i.e., revised line 10), what should go into the blank? Will it work if you fill in the blank on line 10' with `print(L)`? Why or why not?

`lambda: print(L)`

It won't work if you just put `print(L)` without `lambda` because `print(L)` is evaluated at the time of constructing the dictionary, not at the time of lookup. `print(L)` returns `None`, so `D.get('show')` gives you `None`, but `None` can't be called on line 15'.

- b. on line 11', what should go into the blank?
`lambda: L.extend(words[1:])`
 because you want the dictionary lookup on line 14' to give you a function (including `lambda`) that can be called on line 15'.
- c. on line 12', what should go into the blank? `lambda: print(L.pop())`
- d. what does the `D.get(key, altval)` method do? How would it be rewritten without calling the `.get()` method?
`D[key] if key in D else altval`
- e. what goes into the blank on line 14'?
`lambda: print('unknown command')`
- f. can lines 10'-15' be rewritten without using temporary variables `D` and `f`? How?
`{'show': _.. }.get(words[0], ...)()`

12. One alternative to `lambda` in the lookup table above is to use **inner functions**,

```

1 def StackInterpreter():
2     L = []
3     def show(): # inner function
4         print(L)
5     def push():
6         L.extend(words[1:])
7     def pop():
8         print(L.pop())
9     def unknown():
10        print('unknown command')
11    D = {'show': show, 'push': push, 'pop': pop }
12    while True:
13        line = input('command? ')
14        ...

```

- a. What are the inner functions in this code fragment?
`show()`, `push()`, `pop()`, `unknown()`
- b. Why would it be preferable to using inner functions in this case (hint: line 11)?
 makes the lookup table `D` easier to maintain and update, and potentially more expressive since `lambdas` are limited to single-line expressions whereas inner functions can be arbitrary code.
- c. How would the lookup code `D.get(words[0], _____)` be written differently from the `lambda` version? Fill in the blank.
`D.get(words[0], unknown)`

13. How can you add the documentation string (docstring) to the `StackInterpreter()` function above so that you can do `help(StackInterpreter)` in interactive mode and get the help text?

```
$ python3 -i stack.py
>>> help(StackInterpreter)
This is a stack interpreter. The commands are:
show          -- shows stack content
push item1 item2 item3 -- pushes item1,... as str on stack
pop           -- pops and displays popped data
quit          -- exit interpreter
END
>>>
加上三引號
```

14. Does *Python Style Guide* recommend using **camel case** or **snake case** for function names?
 snake case

15. What are examples of **recursive data types** in Python? Are the following data types recursive?

- a. int
- b. list
- c. tuple
- d. dict
- e. set
- f. float
- g. bool

recursive: list, tuple, dict

Not recursive: int, set (because set is mutable but members of set are not mutable), float, bool

If someone asks, str is a debatable case, because you could argue that a substring is "contained" inside the string, and python's built-in "in" operator works on substrings; but each "member" is a character that can only be single-character strings but cannot further contain other strings.

16. What is a **recursive function**?

a function that calls itself directly or indirectly to solve part of the problem.

17. What is a **base case** in a recursive function? Should all recursive functions have at least one base case? Why or why not?

a base case is a conditional path where the function returns without making a recursive call. All recursive functions should have at least one base case or else it will not terminate normally.

18. If you want to count the number of integers in a list that may contain either integers or list of integers and other lists (of integers and other lists...),

a. Can you use a loop such as follows? If not, for what cases will it fail?

```
1 def count_ints(L):
2     n = 0
3     for i in L:
```

```

4     if type(i) == int:
5         n += 1
6     return n

```

It only counts 'integer'.
'list' will not be counted.

- b. Can you use a loop such as follows? If not, for what cases will it fail?

```

1 def count_ints(L):
2     n = 0
3     for i in L:
4         if type(i) == int:
5             n += 1
6         elif type(i) == list:
7             for j in i:
8                 n += 1
9     return n

```

if a list in list
it will not be counted.

- c. Fill in the code below for counting recursively. You may assume types of elements are either int or list. Note that this version of the code is slightly differently from the slide.

```

1 def count_ints(L):
2     if ____: # base case #type(L) == int
3         return 1
4     else:
5         n = 0
6         for i in L:
7             n += ____ #count_ints(i)
8         return n

```

- d. Rewrite lines 5-8 above to eliminate the for loop and replace it with a combination of `sum()` and `map()`.

`return sum(map(count_ints, L))`

19. Recursion can also replace a loop. Rewrite the `count_int` by converting the loop into a recursive call with its own base case (i.e., loop's terminating condition) and another recursive case for "the rest of the loop".

```

1 def rec_count(L):
2     if type(L) == int: # first base case
3         return ____ # 1
4     if ____: # L = []
5         return ____ # 0
6     return rec_count(____) + rec_count(____)
7     # one recursive call for current element, and

```

```
8 # 2nd recursive call for "the rest of the loop"
  # rec_count(L[0]) + rec_count(L[1:])
```

20. Explain what the following functions do in terms of what the parameters are (if any) and what the return value is.

- a. `os.getcwd()`
get current working directory path (string)
- b. `os.listdir(d)`
get list of names of files and directories in directory d
- c. `os.path.isdir(d)`
check if d (string) is a directory

21. To count files recursively, consider the following version of code

```
1 def count_files(p = '.'):
2     import os
3     if ____: # p is the name of a file, not a directory
4         return 1
5     dir_content = ____ # get list of names (files & dir)
6     return sum(____) # sum recursive count of content
```

- a. What does `'.'` mean as the default value of parameter `p`?
current working directory.
- b. How do you call a function from `os` module to check if a path `p` is a **file** rather than a **directory** ("folder")? Fill in the blank on line 3.
`not os.path.isdir(p)`
- c. If `p` a **path** is a directory, how do you obtain a **list of names** (of files and directories) in `p`? Fill in the blank on line 5.
`os.listdir(p)`
- d. How do you recursively count each path of the list so that the counts can be summed? Fill in the blank on line 6.
`map(count_files, dir_content)`

22. In the recursive-find example,

- a. calling
`M = [1, 2, [3, [4, 23]]]`
`rec_find(M, 23)`
results in the tuple value `(2, 1, 1)`. What does it mean?
the value 23 can be found in the list `M = [1, 2, [3, [4, 23]], 5, 6]` at `M[2][1][1]`.
- b. Calling
`rec_find(43, 43)`
results in `True`. What does it mean?
有在43找到43

- c. What would be the result of calling

```
rec_find([1, 2, 3], [1, 2, 3])
```

? **True**

- d. What would be the result of calling

```
rec_find([[1, 2, 3]], [1, 2, 3])
```

? **(0,)**

23. The source code for the recursive-find function looks like this:

```
1 def rec_find(L, val):
2     if type(L) in {list, tuple}: # look inside L
3         for i, v in enumerate(L):
4             p = rec_find(v, val) # recursively find item
5             if p == True: # L[i] == val, so we return (i,)
6                 return (i,)
7             if p != False: # L[i] recursively found val,
8                 return (i,)+p # prepend i to its path p
9     return L == val # L not seq or for-loop didn't find
```

- a. What is the **condition of the base case** in this recursive function?

type(L) is neither list nor tuple

- b. Is line 9 executed only if `type(L)` is **not in {list, tuple}**? Or can it be executed even if `type(L)` is either **list** or **tuple**? If so, describe how line 9 can still be reached after executing lines 3-8?

yes, line 9 can be executed even if type(L) is either list or tuple. This is because if for-loop runs to its completion without an early return on line 6 or line 8, then it falls through and executes line 9. This means val hasn't matched any member of L recursively.

- c. Can line 9 compare only two ints, or can it be comparing two tuples or two lists?

- d. Line 5 tests

```
5 if p == True:
```

but why can't it be replaced with

```
5 if p:
```

?

because if p evaluates to true even if p is not == True. The return value can also be a non-empty tuple containing the indices of the matched items. This case catches the case returned by line 9, which is a match at the last (innermost) index, hence return (i,).

- e. Line 7 tests

```
7 if p != False:
```

but why isn't it redundant with line 5? Doesn't

```
p != False
```

imply


```
p == True
```

?

because `p != False` covers `p == True` as well as `p != True` but `p` is some non-empty values (in this case a tuple with indices). Since `p == True` on line 5 already returned on line 6, line 7 is like an implicit `elif`, and it consists of all those `p != True`, `p != False`, and `p` is non-empty values. That is, value returned by either line 6 or line 8 of a recursive call. By the way, the tuple `(0,)` has a true value.

24. In the code for indenting list items by their level of nesting,

```
1 def indent_list(L, level=0):
2     if L == None:
3         return
4     if type(L) in {list, tuple}:
5         for child in L:
6             indent_list(child, level+1)
7     else:
8         print(f'{" "*4*level}{L}')
9 if __name__ == '__main__':
10     L = ['F1', ['F4', 'F5', ['F8']], 'F2', 'F3', \
11         'D3', ['F6', 'F7']]
12     indent_list(L)
```

- a. By the time 'F8' is printed in the test case, how many copies of `indent_list` calls are active? What are the values of the parameters `L` and `level`?

three copies:

lowest level: (`L = ['F1', ['F4', 'F5', ['F8']], 'F2', 'F3', 'D3', ['F6', 'F7']]`, `level=0`)

next level: (`L = ['F4', 'F5', ['F8']]`, `level = 1`)

top level: (`L = ['F8']`, `level = 2`)

- b. Is line 2 ever executed when running the test case?
- c. How many times total is `indent_list(L)` called in the test case above? How can you modify the code above to print your answer?
- 13 times. could use a global and every time the function is entered increment the global

2. Programming

1. (Difficulty: ★★☆☆☆) Write a function that computes Pascal's triangle.

Col: 0 1 2 3 4 5...

Row0: 1

Row1: 1 1

```

Row2: 1 2 1
Row3: 1 3 3 1
Row4: 1 4 6 4 1
Row5: 1 5 10 10 5 1
...

```

The function should have the following call signature:

```
def pascal(row, column):
```

The function can be defined recursively as follows:

$$\text{pascal}(\text{row}, \text{col}) = \begin{cases} 1 & \text{if col} = 0 \text{ or col} = \text{row} \\ ?? & \text{if } 0 < \text{col} < \text{row} \end{cases}$$

Fill in the ?? above and write this as a recursive function. You may also check the range of the parameter values. If out of range then it should raise a `ValueError` exception.

Then, write a function `print_Pascal_triangle(n)` to print out the triangle as above. The parameter `n` indicates the number of rows.

- (Difficulty: ★★★☆☆) Generalize the recursive finding function `rec_find()` from the recursion slides #22 so that you can pass either a value to be compared for equality, or you can pass a plug-in function that defines the matching criterion. You can check if `val` parameter is a plug-in function by calling the built-in function

```
callable(val)
```

which returns `True` if `val` is a function object or a lambda expression, or returns `False` if it is a value (assumed to be `int`).

For instance, you would call the revised `rec_find` as follows:

```

>>> L = [1, -2, [3, 4], 5]
>>> rec_find(L, 3)
(2, 0)
>>> rec_find(L, lambda x: x == 3) # alternative way
(2, 0)
>>> rec_find(L, lambda x: x < 0) # finds -2 at L[1]
(1,)

```

You need to generate test cases both in terms of different `L` and `val` (as int values, lambda expressions, and the expected answers in a list (or tuple). Use a loop to invoke `rec_find` with these test values and use `assert` to check if the answer is as expected.

ANS:

```
def rec_find(L, val):
```

```

judge=callable(val)

if type(L) in {list, tuple}: # if look inside members of L
    for i, v in enumerate(L):
        p = rec_find(v, val) # recursively find each member
        if p == True:
            return (i,)
        if p != False:
            return (i,)+p
if judge == False:
    return L==val
else:
    return val(L)

```

3. (Difficulty: ★★★★★☆) Rewrite the `number_outline()` function from the recursion slides #28 so that instead of concatenating the section numbers together by '.', it lets the user specify a plug-in function that defines the format, or use the default formatting. For example,

```

L=['Intro',
  ['Motivation', 'Contributions'],
  'Related Work',
  ['By Author', 'By Subject'],
  'Technical Approach',
  ['Overview',
   ['Block Diagram', 'Schematic'],
   'Algorithm',
   ['Static', 'Dynamic'] ],
  'Conclusions']

```

Assume you have different formatting functions defined,

```
>>> number_outline(L, my_outline_format_function)
```

```

I. Introduction
  A. Motivation
  B. Contributions
II. Related Work
  A. By Author
  B. By Subject
III. Technical Approach

```

- A. Overview
 - 1. Block Diagram
 - 2. Schematic
- B. Algorithm
 - 1. Static
 - 2. Dynamic
- IV. Conclusions

And you can plug in another function for a different format:

```
>>> number_outline(L, my_thesis_format_function)
```

```
Chapter 1. Introduction
  Section 1.1 Motivation
  Section 1.2 Contributions
Chapter 2. Related Work
  Section 2.1 By Author
  Section 2.2 By Subject
Chapter 3. Technical Approach
  Section 3.1 Overview
    3.1.1 Block Diagram
    3.1.2 Schematic
  Section 3.2 Algorithm
    3.2.1 Static
    3.2.2 Dynamic
Chapter 4. Conclusions
```

Hints:

- a. How should the parameter list for the function be revised to accommodate the plug-in function? Should it have a default value?
- b. How does your revised `number_outline()` function decide whether to use default formatting or to call the plug-in function for formatting?
- c. What parameter(s) should be passed to the plug-in function? Hint: it is best if the plug-in function just returns the formatted string instead of calling `print` directly.
- d. What adjustments are needed when `number_outline()` makes a recursive call?

```

~/self-check9

Alex@DESKTOP-EUQ8HUR ~/self-check9
$ Python -i p3.py
>>> number_outline(L, my_outline_format_function)
I. Intro
  A. Motivation
  B. Contributions
II. Related Work
  A. By Author
  B. By Subject
III. Technical Approach
  A. Overview
    1. Block Diagram
    2. Schematic
  B. Algorithm
    1. Static
    2. Dynamic
IV. Conclusions
>>>
>>> number_outline(L, my_thesis_format_function)
Chapter 1. Intro
  Section 1.1 Motivation
  Section 1.2 Contributions
Chapter 2. Related work
  Section 2.1 By Author
  Section 2.2 By Subject
Chapter 3. Technical Approach
  Section 3.1 Overview
    3.1.1 Block Diagram
    3.1.2 Schematic
  Section 3.2 Algorithm
    3.2.1 Static
    3.2.2 Dynamic
Chapter 4. Conclusions
>>>

```

```
def roman(number):
```

```

    ROMANS = (('M', 1000),
               ('CM', 900),
               ('D', 500),
               ('CD', 400),
               ('C', 100),
               ('XC', 90),
               ('L', 50),
               ('XL', 40),
               ('X', 10),
               ('IX', 9),
               ('V', 5),
               ('IV', 4),
               ('I', 1))

```

```
    result=""
```

```
    for roman,value in ROMANS:
```

```
        while number>=value:
```

```
            number-=value
```

```
            result+=roman
```

return result

ANS:

```
In [1]: L=['Intro',
['Motivation', 'Contributions'],
'Related Work',
['By Author', 'By Subject'],
'Technical Approach',
['Overview',
['Block Diagram', 'Schematic'],
'Algorithm',
['Static', 'Dynamic'] ],
'Conclusions']

In [2]: def my_thesis_format_function(prefix):
    if(len(prefix)==1):
        a = 'Chapter ' + '.'.join(map(str,prefix))+ '.'
    elif(len(prefix)==2):
        a = 'Section ' + '.'.join(map(str,prefix))
    else:
        a = '.'.join(map(str,prefix))
    return a

In [3]: def my_outline_format_function(prefix):
    if(len(prefix)==1):
        a = 'I' * int(prefix[0])
        a += '.'
        if((prefix[0])==4):
            a = 'IV.'
        return(a)
    if(len(prefix)==2):
        return(chr(ord('A')+int(prefix[1])-1)+'.')
    if(len(prefix)==3):
        return(str(prefix[2])+'.')

In [4]: def number_outline(L,key, prefix=()):
    if type(L) in {list, tuple}:
        # keep prefix[-1], extend by new dimension, starting from 1
        i = 0
        for v in L:
            if type(v) not in {list, tuple}:
                i += 1
                number_outline(v, key, prefix=prefix+(i,))
        # don't increment if v is a list/tuple
        # otherwise, indent and join the prefix together by '.'
    else:
        s = ' ' * 4*(len(prefix)-1)
        s += key(prefix)
        s += ' ' + L
        print(s)
```