

FutureMapping: The Computational Structure of Spatial AI Systems

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Abstract

*We discuss and predict the evolution of Simultaneous Localisation and Mapping (SLAM) into a general **geometric and semantic** ‘Spatial AI’ perception capability for intelligent embodied devices. A big gap remains between the visual perception performance that devices such as augmented reality eyewear or consumer robots will require and what is possible within the constraints imposed by real products. Co-design of algorithms, processors and sensors will be needed. We explore the **computational structure** of current and future Spatial AI algorithms and consider this within the landscape of ongoing hardware developments.*

1. Introduction

While the usually stated goal of computer vision is to report ‘what’ is ‘where’ in an image in a general way, *Spatial AI* is the **online** problem where vision is to be used, usually alongside other sensors, as part of the Artificial Intelligence (AI) which permits an embodied device to interact usefully with its environment. This device must operate in real-time, in a context, and with goals. It may be what we would classically think of as a robot, a fully autonomous artificial agent; or it could be a device like an AR headset designed to be used by a human to augment their capabilities. As recently clarified by Markoff [31], either autonomous AI as in a robot or an ‘Intelligence Augmentation’ (IA) system such as AR have very similar requirements in terms of Spatial AI.

So the goal of a Spatial AI system is not abstract scene understanding, but **continuously** to capture the right information, and to build the right representations, to enable real-time interpretation and action. The design of such a system will be framed at one end by task requirements on its performance, and at the other end by constraints imposed by the setting of the device in which it is to be used.

Let us consider the example of a mass market household robot product of the future, which is set the tasks of monitoring, cleaning and tidying a set of rooms. Its task requirements will include the ability to check whether fur-

niture and objects have moved or changed; to clean surfaces and know when they are clean; to recognise, move and manipulate objects; and to deal promptly and respectfully with humans by moving out of the way or assisting them. Meanwhile, its Spatial AI system, comprising one or more cameras, supporting sensors, processors and algorithms, will be constrained by factors including the price, aesthetics, size, safety, and power usage, which must fit within the range of a consumer product.

As a second example, this time from the IA domain, we imagine a future augmented reality system which should provide its wearer with a robust spatial memory of all of the places, objects and people they have encountered, enabling things such as easily finding lost objects, and the placing of virtual notes or other annotations on any world entity. To achieve wide adoption, the device should have the size, weight and form factor of a standard pair of spectacles (65g), and operate all day without needing a battery charge (<1W power usage).

There is currently a big gap between what such powerful Spatial AI systems need to do in useful applications, and what can be achieved with current technology under real world constraints. There is much promising research on the algorithms and technology needed, but **robust performance** is still difficult even when expensive, bulky sensors and unlimited computing resources are available. The gap between reality and desired performance becomes much more significant still when the constraints on real products are taken into account. In particular, the size, cost and power requirements of the computer processors currently enabling advanced robot vision are very far from fitting the constraints imposed by these applications we envisage.

The PAMELA project from the Universities of Manchester, Edinburgh and Imperial College has opened up research in this area by taking a broad look at the interaction of Spatial AI algorithms and the increasingly heterogeneous processors they must run on, producing pioneering work such as the SLAMBench framework [38, 4]. As the project nears its end, in this paper we take a long view of Spatial AI research, make some analysis of the key computational structure of these problems, and taking account of ongoing

trends in processor technology make some predictions for the future of this field.

2. SLAM, Spatial AI and Machine Learning

The research area of visual SLAM (Simultaneous Localisation and Mapping) in robotics and computer vision has long been concerned with real-time, incremental estimation of the shape and structure of the scene around a robot, and the robot's position within it. The level of scene representation that has been possible in real-time SLAM has gradually improved, from sparse features (e.g. [8]) to dense (e.g. [42]) maps and now increasingly semantic labels [33, 54].

Commercial SLAM provider SLAMcore Ltd. [1] refers to sparse localisation, dense mapping and semantic labelling as Levels 1, 2 and 3 capabilities respectively. These are ongoing steps along SLAM's evolution towards spatial perception. Observing the steady and consistent progress of SLAM over more than 20 years, we have become confident that the operation of current and foreseeable SLAM systems is the best guide we have for the algorithmic structure of future Spatial AI.

Spatial AI will be fundamental enabling technology for a the next generation of smart robots, mobile devices and other products that we can't yet imagine; a new layer of technology that could eventually be pervasive. In the recent technical report from leading UC Berkeley researchers on systems challenges for AI [51], it is argued that devices which can act intelligently in their environments via continual learning must be capable of Simulated Reality (SR) which can "faithfully simulate the real-world environment, as the environment changes continually and unexpectedly, and run faster than real time". Judea Pearl, recently discussing efficient situated learning and the need to reason about causation [43], argues that "what humans possessed that other species lacked was a mental representation, a blue-print of their environment which they could manipulate at will to imagine alternative hypothetical environments for planning and learning". Both of these describe exactly what we envision as the end-goal of SLAM's ongoing evolution into Spatial AI.

Most Spatial AI systems will have multiple applications, not all predictable at the time of design. We therefore make the following hypothesis: *When a device must operate for an extended period of time, carry out a wide variety of tasks (not all of which are necessarily known at design time), and communicate with other entities including humans, its Spatial AI system should build a general and persistent scene representation which is close to metric 3D geometry, at least locally, and is human understandable.* To be clear, this definition leaves a lot of space for many choices about scene representation, with both learned and designed elements, but rules out algorithms which make use of very specific task-focused representations.

Our second hypothesis is that: *The usefulness of a Spatial AI system for a wide range of tasks is well represented by a relatively small number of performance measures.* That is to say that whether the system is to be used to guide the autonomous flight of a delivery drone in a tight space, or a household robot to tidy a room, or to enable an augmented reality display to add synthetic objects to a scene, then even though these applications certainly have different requirements and constraints, the suitability of a Spatial AI system for each can be specified by a the specification of a small number of performance parameters. The obvious parameters describe aspects like global device localisation accuracy and update latency, but we believe that there are other metrics which will be more meaningful for applications, like distance to surface contact prediction accuracy, object identification accuracy or tracking robustness. We will discuss performance metrics further in Section 9.

For the purposes of the rest of this paper, we will therefore call such a module which incrementally builds and maintains a generally useful, close to metric scene representation, in real-time and from primarily visual input, and with quantifiable performance metrics, a *Spatial AI system*.

2.1. Machine Learning

In recent years, Machine Learning (ML) has increasingly come to the fore in AI, and overcome human-designed approaches in many problems. In machine learning, the parameters of a black box computational unit which transforms inputs to outputs are learned by adjusting them on the basis of training data, with the aim of optimising its performance either when compared to explicit labels provided by an external source (supervised learning), or more indirectly by judging performance against high level task goals over a period of time (reinforcement learning). Machine Learning contrasts with *estimation methods* where the computational unit to achieve an AI task is explicitly hand-designed with nameable variables, modules, algorithms and other structures.

Computer vision has proved to be a very successful domain for the application of ML. As is well known, Deep Learning approaches mainly based on Convolutional Neural Networks (CNNs) have become the dominant approach to achieving state of the art results in many vision problems, such as image classification or segmentation.

More recently, deep learning has started to show promising results on problems in vision-guided robotics (e.g. [13]). In these approaches, a deep network which processes the raw pixels of incoming images is trained 'end to end' by supervision from a non-learned system (e.g. [21]), or via reinforcement based on the the achievement of discrete tasks such as object placement or local navigation. These networks learn directly to output motor control signals based on visual input, and therefore any internal representation

they need (such as the shape of the environment, and the robot's position within it) are represented within the network itself as required to achieve the task, in an implicit form which is not accessible beyond the task at hand.

In general Spatial AI problems, there has so far been less success in machine learning methods which incrementally improve a world representation over time from multiple measurements. Such learning requires a computational unit which has memory and captures its own internal representation over time. A Recurrent Neural Network (RNN) is the fundamental concept of a network whose activations and outputs depend not just 'single shot' on the current input data but also on internal states which are the outcome of previous inputs. There are many related ideas and also efforts to interface deep networks with explicit memory blocks.

In Spatial AI, training an RNN or similar to produce useful output sequentially from a real-time stream of input data requires it to capture within its internal state a persistent set of concepts which must closely relate to the shape and qualities of the environment around the device. We have certainly seen some success with methods aiming to do this, such as the work of Wen *et al.* [55] on estimating incremental visual odometry from video using an RNN whose training was via a supervised known pose signal.

However, a group of methods which seems very promising aims to impose structure on what is learned by a network. Gupta *et al.* [16] presented a method for local navigation which forces a deep network to learn about a robot's environment in a manner which tends towards a metric grid by presenting it with metric spatial transformations based on the robot's known motion in 2D. Zhou *et al.* [59] have excitingly shown how networks to estimate incremental camera motion and scene depth can be trained in a coupled manner from unlabelled video data, using photoconsistency via the geometric warping between textured depth frames as self-supervision.

These are learning architectures which use the designer's knowledge of the structure of the underlying estimation problem to increase what can be gained from training data, and can be seen as hybrids between pure black box learning and hand-built estimation. Another key paper in this area introduced the idea of Spatial Transformer Networks [20], as generalised in Handa *et al.*'s gvn [17]. Why should a neural network have to use some of its capacity to learn a well understood and modelled concept like 3D geometry? Instead it can focus its learning on the harder to capture factors such as correspondence of surfaces under varying lighting.

These insights support our first hypothesis that future Spatial AI systems will have recognisable and general mapping capability which builds a close to metric 3D model. This 'SLAM' element may either be embedded within a specially architected neural network, or be more explicitly

separated from machine learning in another module which stores and updates map properties using standard estimation methods (as in SemanticFusion [33] for instance). In both cases, there should be an identifiable region of memory which contains a representation of space with some recognisable geometric structure.

Besides utility, such AI systems will have the additional advantage of using representations that can be communicated to and understood by humans, and therefore in principle controlled.

2.2. Closed Loop SLAM

As a sensor platform carrying at least one camera and other sensors moves through the world, its motion either under active control or provided by another agent, the essential algorithmic ways that a Spatial AI system of any variety works can be summarised as follows:

1. Starting from and continuing to make use of prior knowledge of the type of scene it is working in, the system uses data from its sensors to incrementally build and refine a persistent world model which captures abstracted geometric, appearance and semantic information about its environment. It also models and incrementally estimates the state of the moving camera platform relative to the world. The amount of data stored to represent a region of space of a certain size will have a maximum bound so that if the sensor spends a long time in one region the size of the representation does not grow arbitrarily.
2. As new image data is captured from the moving camera, it is compared with the current world model. With low latency, the system must decide which new data is not important and which can be used to update the model's persistent estimates. The task of matching up sensor data to the relevant parts of the model is called *data association*.
3. The model update is often considered as consisting of *tracking*, which is getting new estimates of the sensor platform's position/state, and *map update* where the scene model is improved and expanded. This division is however somewhat arbitrary.

The key computational quality of this approach is its *closed loop* nature, where the world model is persistent and incrementally updated, representing in an abstracted form all of the useful data which has been acquired to date, and is used in the real-time loop for data association and tracking. This is in contrast with vision systems which perform incremental estimation (such as visual odometry, where camera motion is estimated from frame to frame but long term data structures are not retained), or which can only achieve

global consistency with off-line, after the event batch computation. That is not to say that in a closed loop Spatial AI system every computation should happen at a fixed rate, but more importantly that it should be available when needed to allow real-time operation of the whole system to continue without pauses.

Closed loop SLAM has generally been enabled by probabilistic estimation, the fundamental approach building models which summarise past data in a form which acknowledges uncertainty and allows new data to be correctly weighted and fused. In sparse feature-based SLAM, probabilistic fusion is implemented via tools such as the Extended Kalman Filter (as in [8]) or incremental non-linear optimisation (as in [28]).

Sparse feature maps are useful as landmark sets for position estimation, but do not provide much information about the scene around a camera, and progress has more recently been towards systems aiming to do better, via dense mapping and now semantic mapping. Ultimately, if a scene model is fully *generative* then it can be used to make complete predictions about sensor data. This is important because then in principle *every* piece of sensor data can be compared with the model prediction to uncover what is previously unseen or changed in the scene. In simple terms, for a system and to recognise something which is unusual, it must keep up to date a full predictive model of what is normal.

The latest real-time SLAM systems are hybrids, combining estimation of tracking and dense surface shape with learned components for labelling and recognition (e.g. SemanticFusion [33]). As mentioned earlier, other learned components are now looking promising for other elements of a full system such as VO and depth estimation (e.g. Zhou *et al.* [59]). We foresee these components coming together in an increasingly tight and interlinked fashion, helping and feeding into each other. While SemanticFusion currently uses geometric SLAM and CNN-based labelling as essentially separate modules which are fused into a final labelled map output, systems coming in the near future will be closely integrated in a tight loop which will surely give much better performance. For instance, a CNN for labelling which takes as input not just a new live image frame but also the current set of label distributions reprojected from the 3D map should be much better, and ideas like this are starting to be proven [58].

One clear goal is to create a SLAM system which can as far as possible understand a scene directly and efficiently at the level of recognised objects and entities (as in the prototype system SLAM++ [49]), reserving bottom-up reconstruction and labelling for unfamiliar elements. Whether the components making up such a system are designed or learned may not have a big impact on the overall computational structure.

Our main aim in the rest of this paper is therefore to analyse the computational structure of Spatial AI systems, while avoiding pinning down specifics where this is difficult, and to make some predictions and tentative design choices about their implementation going forward. A crucial element of this is that Spatial AI is fundamentally an embodied, real-time problem. We believe strongly that the design of the algorithms and data structures required should take place in a tightly integrated manner with that of the physical processors and sensors which together form a whole system. In the next section we will therefore consider the relevant landscape in processor and sensor design.

3. The Future Landscape of Processor and Sensor Hardware

SLAM research was for many years conducted in the era when single core CPU processors could reliably be counted on to double in clock speed, and therefore serial processor capability, every 1–2 years. In recent years this has stopped being true. The strict definition of Moore’s Law, describing the rate of doubling of transistor density in integrated circuits, has continued to hold well into the current era. What has changed is that this can no longer be proportionally translated into serial CPU performance, due to the breakdown of another less well known rule of thumb called Dennard Scaling, which states that as transistors get smaller their power density stays constant. When transistors are reduced down to today’s nanometre sizes, not so far from the size of the atoms they are made from, they leak current and heat up. This ‘power wall’ limits the clock speed at which they can reasonably be run without overheating uncontrollably to something around 4GHz.

Processor designers must therefore increasingly look towards alternative means than simply faster clocks to improve computation performance. The processor landscape is becoming much more complex, parallel and specialised, as described well in Sutter’s online article ‘Welcome to the Jungle’ [53]. Processor design is becoming more varied and complex even in ‘cloud’ data centres. Pressure to move away from CPUs is even stronger in embedded applications like Spatial AI, because here power usage is a critical issue, and parallel, heterogeneous, specialised processors seem to be the only route to achieving the computational performance Spatial AI needs within power restrictions which will fit real products. So while current embedded vision systems, e.g. for drones, often use CPU only implementations of SLAM algorithms (rather than requiring GPUs), we believe that this is not the right approach for the longer term. While current desktop GPUs are certainly power-hungry, Spatial AI must eventually embrace parallelism and heterogeneity in computation, and accept that this will be the dominant paradigm going forward for practical systems.

Mainstream geometrical computer vision started to take advantage of parallel processing in the form of GPUs nearly 10 years ago (e.g. [45]), and in Spatial AI this led to breakthroughs in dense SLAM [42, 41]. The SIMT (Single Instruction, Multiple Threads) parallelism that GPUs provide is well suited to elements of real-time vision where the same operation needs to be applied to every element of a regular array in image or map space. Concurrently, GPUs were central to the emergence of deep learning in computer vision [27], by providing the computational resource to enable neural networks of sufficient scale to be trained to finally prove their worth in significant tasks such as image classification.

The move from CPUs to GPUs as the main processing workhorse for computer vision is only the beginning of how processing technology is going to evolve. We foresee a future where an embedded Spatial AI system will have a heterogeneous, multi-element, specialised architecture, where low power operation must be achieved together with high performance. A standard SoC (system-on-chip) for embedded vision ten years from now, which might be used in a personal mobile device, drone or AR headset, will be likely to still have elements which are similar in design to today's CPUs and GPUs, due to their flexibility and the huge amount of useful software they can run. However, it is also likely to have a number of specialised processors optimised for low power real-time vision.

The key to efficient processing which is both fast and consumes little power is *to divide computation between a large number of relatively low clock-rate or otherwise simple cores, and to minimise the movement of data between them*. A CPU pulls and pushes small pieces of data one by one from and to a separate main memory store as it performs computation, with local caching of regularly used data the only mechanism for reducing the flow. Programming for a single CPU is straightforward, because any type of algorithm can be broken down into sequential steps with access to a single central memory store, but the piece by piece flow of data to and from central memory has a huge power cost.

More efficient processor designs aim to keep processing and the data operated on close together, and to limit the transmission of intermediate results. The ideal way to achieve this is a close match between the design of a processor/storage architecture and the algorithm it must run. A GPU certainly has large advantages over a CPU for many computer vision processing tasks, but in the end a GPU is a processor designed originally for computer graphics rather than vision and AI. Its SIMT architecture can efficiently run algorithms where the same operation is carried out simultaneously on many different data elements. In a full Spatial AI system, there are still many aspects which do not fit well with this, and a joint CPU/GPU architecture is currently needed with substantial data transfer between the two.

While it is relatively accessible to design custom 'accelerator' processors which could implement certain specific low-level algorithms with high efficiency (see for instance the OpenVX project from the Khronos Group), there has been relatively little work until recently on thinking about the whole computational structure of whole close loop embedded systems like Spatial AI. It is certainly true now that low power vision is seen as an increasingly important aim in industry, and custom processors to achieve this have been developed such as Movidius' Myriad series. These processors combine low power CPU-like, DSP-like and custom elements in a complete package. The 'HPU' custom-designed by Microsoft for their Hololens AR headset is rather similar in design, and the recently announced second version will include additional custom hardware support for neural networks.

If we try to look further ahead, we can conceive of processor designs which offer the possibility of a much closer match between architecture and algorithms. Highly relevant to our aims are major efforts which are now taking place on new ways of doing large-scale processing by being made up from large numbers of independent and relatively low-spec cores with the emphasis on communication. SpiNNaker [15] is a major research project from the University of Manchester which aims to build machines to emulate biological brains. It has produced a prototype machine made up from boards which each have hundreds of ARM cores, and with up to a million cores in total. With the rather different commercial aim of providing an important new type of processor for AI, Graphcore is a UK company developing 'IPU' processors which comprise thousands of highly interconnected cores on a single chip.

Both of these projects are primarily being designed with efficient implementation of neural networks in mind, in the case of both SpiNNaker and Graphcore with the belief that the important matter is the overall topology of a large number of cores, each performing different operations but highly and efficiently inter-connected in a graph configuration adapted to the use case. These designs have not taken strong decisions about the type of processing carried out at each core, or the type of messages they can exchange, with the desire to leave these matters to the choice of future programmers. This is as opposed to more explicitly neuromorphic architectures aiming to implement particular models of the operation of biological brains, such as IBM's Truenorth project.

Such architectures are not yet close to ready for embedded vision, but seem to offer great long term potential for the design of Spatial AI systems where the graph structure of the algorithms and memory stores we use can be matched to the implementation on the processor in a custom and potentially highly efficient way. We will consider this in more detail later on.

But we also believe that we should go further than thinking of mapping Spatial AI to a single processor, even when it has an internal graph architecture. A more general concept of a graph applies to communication to cameras and other sensors, actuators and other outputs, and potentially entirely off-board computing resources in the cloud.

A particularly important consideration is the real-time data flow between the one or more camera sensors in a Spatial AI system and the main processing resource where map storage and processing occurs. Video data is huge and expensive to transmit. However, it is highly redundant, both temporally and spatially: nearby pixels in both space and time tend to have similar values.

The concept of a camera is today becoming increasingly broad with ongoing innovation by sensor designers, and for our purposes we consider any device which essentially captures an array of light measurements to be a visual sensor. Most are passive in that they record and measure the ambient light which reaches them from their surroundings, while another large class of cameras emit their own light in a more or less controlled fashion. In Spatial AI, many types of camera have been used, with the most common being passive monocular and stereo camera rigs, and depth cameras based on structured light or time of flight concepts. Every camera design represents a choice in terms of the quality of information it provides (measured in such ways as spatial and temporal resolution and dynamic range), and the constraints it places on the system it is used in such as size and power usage. In previous work [18] we studied some of the trade-offs possible between performance and computational cost in the Spatial AI sub-problem of real-time tracking.

One type of visual sensor which is particularly promising for Spatial AI is known as the event camera. This is a sensor which instead of capturing a sequence of full image frames as a standard video camera does, only records and transmits changes in intensity. The output of the sensor is a stream of ‘events’ from the independently sensitive analogue pixels, each with pixel coordinates and an accurate timestamp. The principle is that the event stream encodes the content of video at a much lower bit-rate, while offering advantages in time temporal and intensity sensitivity, and it has recently been demonstrated (e.g. [23]) that SLAM algorithms can be formulated which estimate camera motion, scene intensity and depth from only the event stream.

The event camera is surely only the starting point for coming rapid changes in image sensor technology, where low power computer vision will be an increasingly important driver. We can expect a full generalisation of the concept of the event camera to sensors which perform significant processing of intensity data as part of the sensing process itself, and will communicate with a main processor in a bidirectional manner in an abstracted form which is very different from sensing raw video streams.

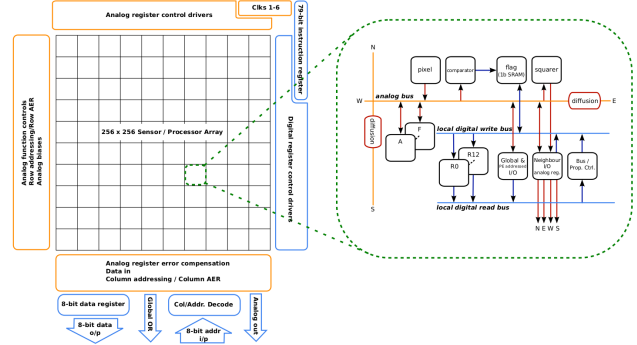


Figure 1. The SCAMP5 architecture for integrated visual sensing and processing (Figure taken from Martel and Dudek [32], and reproduced courtesy of the authors.)

One significant ongoing academic project in this space is the SCAMP series of vision chips with in-plane processing from the University of Manchester (see [32] for an introduction), and Figure 1 taken from that paper. The SCAMP5 chip runs at 1.2W and has an image resolution of 256×256 , with each pixel controlled by and processable by per-pixel processing. Using analog current-mode circuits, summation, subtraction, division, squaring, and communication of values with neighbouring pixels can be achieved extremely rapidly and efficiently to permit a significant level of real-time vision processing completely on-chip. Ultra-low power operation can alternatively already be achieved in applications where low update rates are sufficient.

As we will discuss later on, the range of vision processing which could eventually be performed by such an image plane processor is still to be fully discovered. The obvious use is in front-end pre-processing such as feature detection or local motion tracking. We believe that the longer term potential is that while a central processor will be required for full model-based Spatial AI, close-to-sensor processing can interact fully with this via two-way low communication, with the main aim of reducing the bit-rate needed between the sensor and main processor and therefore the communication power requirements.

Finally, when considering the evolution of the computing resources for Spatial AI, we should never forget that, cloud computing resources will continue to expand in capacity and reduce in cost. All future Spatial AI systems will likely be cloud-connected most of the time, and from their point of view the processing and memory resources of the cloud can be assumed to be close to infinite and free. What is not free is communication between an embedded device and the cloud, which can be expensive in power terms, particularly if high bandwidth data such as video is transmitted. The other important consideration is the time delay, typically of significant fractions of a second, in sending data to the cloud for processing.

The long term potential for cloud-connected Spatial AI is clearly enormous. The vision of Richard Newcombe, Director of Research Science at Oculus, is that all of these devices should communicate and collaborate to build and maintain shared a ‘machine perception map’ of the whole world. The master map will be stored in the cloud, and individual devices will interact with parts of it as needed. A shared map can be much more complete and detailed than that build by any individual device, due to both sensor coverage and the computing resources which can be put into it. A particularly interesting point is that the Spatial AI work which each individual device needs to do in this setup can in theory be much reduced. Having estimated its location within the global map, it would not need to densely map or semantically label its surrounding if other devices had already done that job and their maps could simply be projected into its field of view. It would only need to be alert for changes, and in turn play its part in returning updates.

4. High Level Design

We now turn more specifically to a design for the architecture of a Spatial AI device. Despite the clear potential for cloud-connected shared mapping, here we choose to focus purely on a single device which needs to operate in a space with only on-board resources, because this is the most generally capable setup which could be useful in any application and not require additional infrastructure.

The first thing to consider in the design of our hypothetical future Spatial AI system is what it will be required to do:

1. Our system will comprise one or more cameras, and supporting sensors such as an IMU, closely integrated with a processing architecture in a small, low power package which is embedded in a mobile entity such as a robot or AR system. While much can be achieved in SLAM and vision with a single camera as the only sensor, it is clear that most practical applications will observe their surroundings with multiple cameras and support this with other appropriate sensors. For instance, a future household robot is likely to have navigation cameras which are centrally located on its body and specialised extra cameras, perhaps mounted on its wrists to aid manipulation.
2. In real-time, the system must maintain and update a world model, with geometric and semantic information, and estimate its position within that model, from primarily or only measurements from its on-board sensors.
3. The system should provide a wide variety of task-useful information about ‘what’ is ‘where’ in the scene. Ideally, it will provide a full semantic level

model of the identities, positions, shapes and motion of all of the objects and other entities in the surroundings.

4. The representation of the world model will be close to metric, at least locally, to enable rapid reasoning about arbitrary predictions and measurements of interest to an AI or IA system.
5. It will probably retain a maximum quality representation of geometry and semantics only in a focused manner; most obviously for the part of the scene currently observed and relevant for near-future interaction. The rest of the model will be stored at a hierarchy of residual quality levels, which can be rapidly upgraded when revisited.
6. The system will be generally alert, in the sense that every incoming piece of visual data is checked against a forward predictive scene model: for tracking, and for detecting changes in the environment and independent motion. The system will be able to respond to changes in its environment.

The next element of our high level thinking is to identify the core ways that we can achieve all of this with high performance but low power requirements.

We believe that the key to efficient processing in Spatial AI is to identify the graphs of computation and data movement in the algorithms required, and as far as possible to make use of or design processing hardware which has the same properties, with the particular goal of minimising data movement around the architecture. We need to identify the following things: What is stored where? What is processed where? What is transmitted where, and when?

We will not attempt here to draw strong parallels with neuroscience, but clearly there is much scope for relating the ideas and designs we discuss here in artificial Spatial AI systems with the vision and spatial reasoning capabilities and structures of biological brains. The human brain apparently achieves high performance, fully ‘embedded’ semantic and geometric vision using less than 10 Watts of power, and certainly its structures have properties which mirror some of the concepts we discuss. We will leave it to other authors to analyse the relationships further; this is mostly due to our lack of expertise in neuroscience, but also partly due to a belief that while artificial vision systems clearly still have a great deal to learn from biology, they need not be designed to replicate the performance or structure of brains. We consider the Spatial AI computation problem purely from the engineering point of view, with the goal of achieving the performance we need for applications while minimising resources. It should surely not be surprising that some aspects of our solutions should mimic

those discovered by biological evolution, while in other respects we might find quite different methods due to two contrasts: firstly between the incremental ‘has to work all of the time’ design route of evolution and the increased freedom we have in AI design; and secondly between the wetware and hardware available as a computational substrate.

5. Graphs in SLAM

SLAM and the wider Spatial AI problem have some immediately apparent graph structures built into them. We will here aim to identify and discuss these.

5.1. Geometrical Graphs

There are well known graphs which emerge naturally from the geometry of cameras and 3D spaces and the data which represents these.

5.1.1 Image Graph

First, there is the regular, usually rectangular geometry of the pixels which make up the image sensor of a camera. While each of these pixels is normally independently sensitive to light intensity, many vision algorithms make use of the fact that the output of nearby pixels tends to be strongly correlated. This is because nearby pixels often observe parts of the same scene objects and structures. Most commonly, a regular graph in which each pixel is connected to its four (up, down, left, right) neighbours is used as the basis for smoothing operations in many early vision problems such as dense matching or optical flow estimation (e.g. [44]).

The regular graph structure of images is also taken advantage of by the early convolutional layers of CNNs for all kinds of computer vision tasks. Here the multiple levels of convolutions also acknowledge the typical hierarchical nature of local regularity in image data.

5.1.2 Map Graph

The other clear geometrical graph present in Spatial AI problems is in the maps or models which are built and maintained of an environment by SLAM systems. This graph structure has been recognized and made use of by many important SLAM methods (e.g. [22, 26, 49, 12, 35]).

As a camera moves through and observes the world, a SLAM algorithm detects, tracks and inserts into its map features which are extracted from the image data. (Note that we use the word ‘feature’ here in a general sense to mean some abstraction of a scene entity, and that we are not confining our thinking to sparse point-like landmarks.) Each feature in the scene has a region of camera positions from which it is measurable. A feature will not be measurable if it is outside of the camera’s field of view; if it is occluded; or for other reasons such that its distance from the camera

or angle of observation are very different from when it was first observed.

This means that as the camera moves through a scene, features become observable in variable overlapping patterns. As measurements are made of the currently visible features, estimates of their locations are improved, and the measurements are also used to estimate the camera’s motion. The estimates of the locations of features which are observed at the same time become strongly correlated with each other via the uncertain camera state. Features which are ‘nearby’ in terms of the amount of camera motion between observing them are still correlated but somewhat less strongly; and features which are ‘distant’ in that a lot of motion (and SLAM based on intermediate features) happens between their observation are only weakly correlated.

The probabilistic joint density over feature locations which is the output of SLAM algorithms can be efficiently represented by a graph where ‘nearby’ features are joined by strong edges, and ‘distant’ ones by weak edges. A threshold can be chosen on the accuracy of probabilistic representation which leads to the cutting of weaker edges, and therefore a sparse graph where only ‘nearby’ features are joined.

One way to do SLAM is not to explicitly estimate the state of scene features, but instead to construct a map of a subset of the historical poses that the moving camera has been in, and to keep the scene map implicit. This is usually called pose graph SLAM, and within this kind of map the graph structure is obvious because we join together poses between which we have been able to get sensor correspondence. Poses which are consecutive in time are joined; and poses where we are able to detect a revisit after a longer period of time are also joined (this is called a loop closure). Whether the graph is of historic poses, or of scene features, its structure is very similar, in that it connects either ‘nearby’ poses or the features measured from those poses, and there is not a fundamental difference between the two approaches.

A property of a passive camera which is different from other sensors is that it has effectively infinite range. It can see objects which are very close in exquisite detail; but also observe objects which are extremely far away. Visual maps will consist of all of these things, and this is why we have not been precise so far with the concepts of ‘nearby’ and ‘distant’. The locality in visual maps is not a matter of simple metric distance. Remembering that what is important is how feature position estimates become correlated due to camera motion and measurements, a SLAM graph will have a multi-scale character, such that elements measured from a close camera (the different objects on a table) may form a significant interconnected chunk of a graph, while another similar chunk contains much more separated elements seen from farther away (a group of buildings on the other side of

the city).

This leads us to conclude that *the most likely representation for Spatial AI is to represent 3D space by a graph of features, which are linked in multi-scale patterns relating to camera motion and together are able of generating dense scene predictions.*

Chli and Davison [5] investigated an automatic way to discover the hierarchical graph structure of a feature-based map by analysing correlations purely in measurement space, and it is clear that relating such a structure quite closely to a co-visibility keyframe graph gives a similar result. However, this work was based on standard point features. We have not yet discovered a suitable feature representation which describes both local appearance and geometry in such a way that a relatively sparse feature set can provide a dense scene prediction. We believe that learned features arising from ongoing geometric deep learning research will provide the path towards this.

Some very promising recent work which we believe is heading in the right direction Bloesch *et al.*'s CodeSLAM [3]. This method uses an image-conditioned autoencoder to discover an optimisable code with a small number of parameters which describes the dense depth map at a keyframe. In SLAM, camera poses and these depth codes can be jointly optimised to estimate dense scene shape which is represented by relatively few parameters. In this method, the scene geometry is still locked to keyframes, but we believe that the next step is to discover learned codes which can efficiently represent both appearance and 3D shape, and to make these the elements of a graph SLAM system.

5.1.3 Image/Model Correspondence

Let us go a little deeper into this idea, and in particular to understand that as a camera moves through the world, the contact or *correspondence* between its image graph and its map graph will change, continuously and dynamically, in a way which can be very rapid but is not random. What does this mean for the computational structures we should use in Spatial AI?

Fundamentally, in a SLAM process we cannot pre-compute the shape of the map that will be built, because it depends on the motion of the camera. However, perhaps we can have a generic structure which is representative of many types of motion, ready to be filled when needed as a space is explored. What is important in graph maps, from a computational point of view, is *topology*: which things are connected to which others, and in which patterns. Maps with hierarchical topologies in regular space such as multi-scale occupancy grids or heightmaps have been developed (e.g. [57, 60]), and these enable efficient mapping in systems where localisation can be separated and assumed to

be good. In general visual SLAM, the graph needs a flexible structure, which is multiscale but can also be adapted at loop closure, and there are still good questions about how to design the ideal container. Experiments could be performed with current dense SLAM systems to determine the typical patterns of correlation between surface elements in various applications.

5.2. Computation Graph

The other key type of graph which we can easily identify in Spatial AI problems is in the computation which takes place in a SLAM system's real-time loop.

We make a hypothesis that the core computation graph for the tightest real-time loop of future SLAM systems will have many elements which are familiar with today's systems. Specifically the Dense SLAM paradigm introduced by Newcombe *et al.* [39, 41, 42] is at the centre of this in our view, because this approach aims to model the world in dense, generative detail such that every new pixel of data from a camera can be compared against a model-based prediction. This allows systems which are generally 'aware', since as they continually model the state of the world in front of the camera, they can detect when something is out of place with respect to this model, and therefore dense SLAM systems are now being developed which are moving beyond static scenes to reconstruct and track dynamic scenes [40, 47]. Dense SLAM systems can also make the best possible use of scene priors, which will increasingly come from learning rather than being hand-designed.

Following some of these arguments, Newcombe *et al.*'s KinectFusion algorithm [41] was chosen as the basis for the first version of the SLAMBench framework [38] which aimed to provide a forward looking benchmark for the computational properties of SLAM systems. Since KinectFusion, dense SLAM has been augmented with semantic labelling in systems like SemanticFusion [33], which uses the surfel-based and loop closure-capable ElasticFusion [56] as its dense SLAM basis. As well as being used for SLAM, incoming image and depth frames are fed to a CNN which has been pre-trained for per-pixel semantic labelling into thirteen classes typical of domestic scenes, such as wall, floor, table, chair or bed. The output for each pixel is a distribution over possible labels, and these are then projected onto the 3D SLAM map, where each surfel maintains and updates a label probability distribution via Bayesian fusion.

As we discussed before, a goal of this line of research is to get to a general SLAM system which has the ability to identify and estimate the locations of all of the objects in a scene, in the style demonstrated in a prototype way by SLAM++ [49] which made efficient maps directly at the level of objects in precise 3D poses, but could only deal with a small number of specific object types. How can we get back to this 'object-oriented SLAM' capability in the much

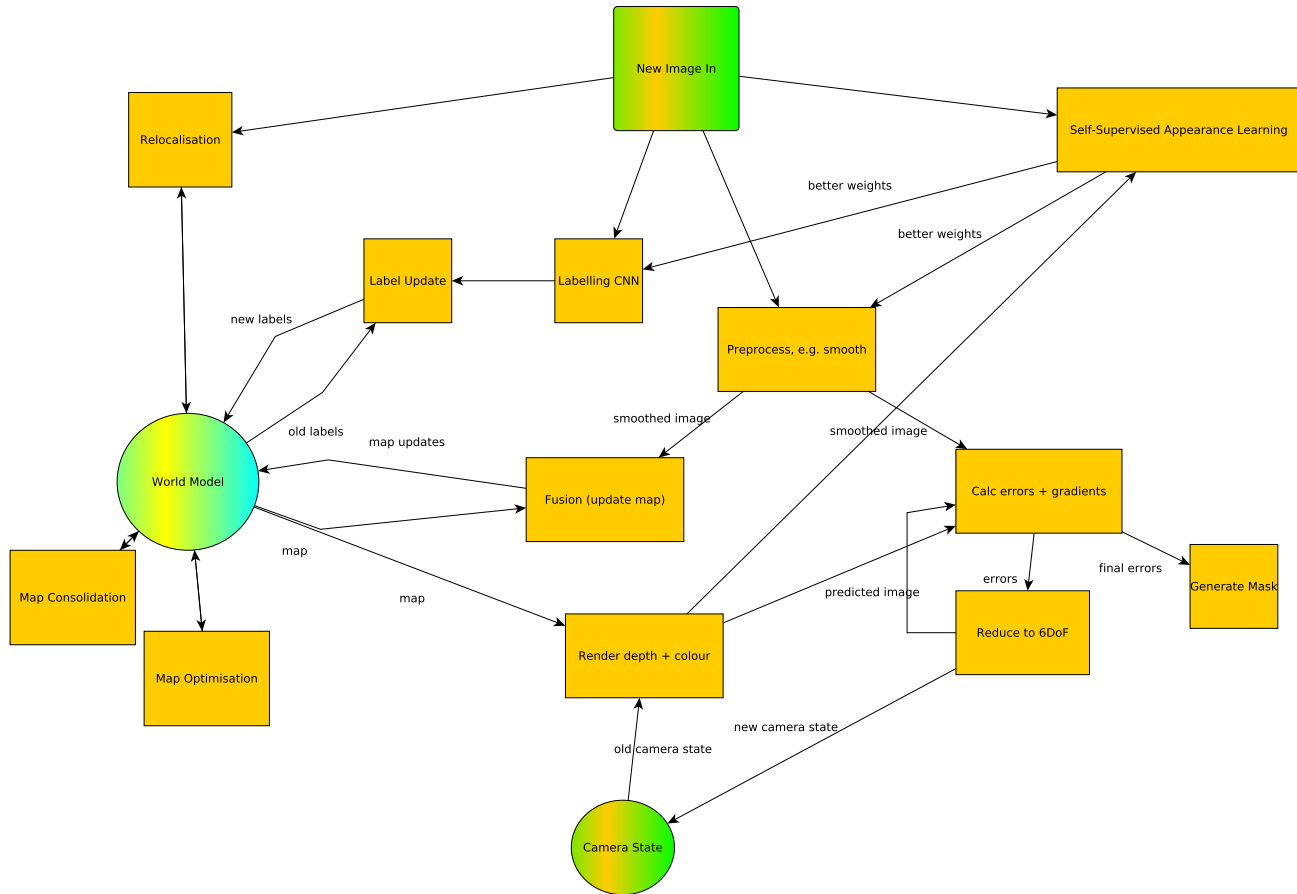


Figure 2. Some elements of the Spatial AI real-time computation graph.

more general sense, where a wide range of object classes of varying style and details could be dealt with? As discussed before, SLAM maps of the future will probably be represented as multi-scale graphs of learned features which describe geometry, appearance and semantics. Some of these features will represent immediately recognised whole objects as in SLAM++. Others will represent generic semantic elements or geometric parts (planes, corners, legs, lids?) which are part of objects either already known or yet to be discovered. Others may approach surfels or other standard dense geometric elements in representing the geometry and appearance of pieces whose semantic identity is not yet known, or does not need to be known.

Recognition, and unsupervised learning, will operate on these feature maps to cluster, label and segment them. The machine learning methods which do this job will themselves improve by self-supervision during the SLAM process, taking advantage of dense SLAM's properties as a 'correspondence engine' [50].

From a starting point of the algorithmic analysis of the KinectFusion algorithm in SLAMBench [38], we make an

attempt at drawing a computation graph for a generally capable future Spatial AI system in Figure 2.

Most computation relates to the *world model*, which is a persistent, continuously changing and improving data store where the system's generative representation of the important elements of the scene is held; and the input *camera data stream*. Some of the main computational elements are:

- Empirical labelling of images to features (e.g. via a CNN).
- Rendering: getting a dense prediction from the world map to image space.
- Tracking: aligning a prediction with new image data, including finding outliers and detecting independent movement.
- Fusion: fusing updated geometry and labels back into the map.
- Map consolidation: fusing elements into objects, or imposing smoothing, regularisation.

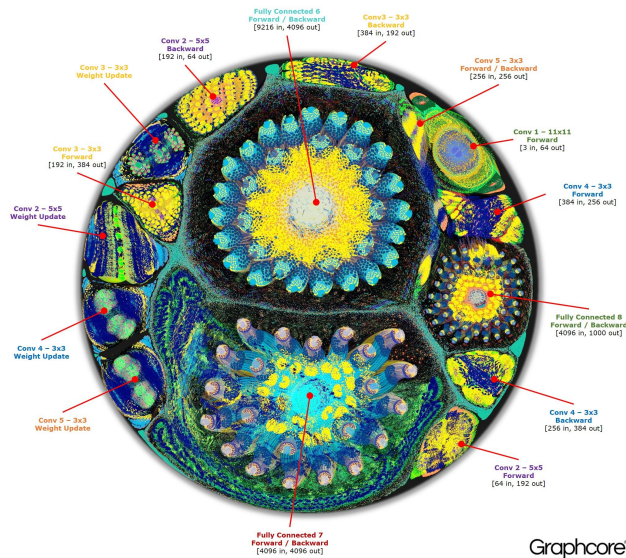


Figure 3. Graphcore’s Poplar graph compiler turns the specification of an algorithm from a framework such as TensorFlow into a definition of the computation graph which is suitable for efficient distributed deployment on their IPU graph processor. This is a visualisation of the result for the AlexNet image classification CNN, supporting both training and run-time operation, where the spatial configuration and colouring indicates close connectivity of the different processing modules required. Image courtesy of Graphcore.

- Relocalisation/loop closure detection: detecting self similarity in the map.
- Map consistency optimisation, for instance after confirming a loop closure.
- Self-supervised learning of correspondence information from the running system.

In the following sections we will think about where these data and computational elements might operate in future architectures.

6. Main Map Processing; Representation, Prediction and Update

We explained that in the overall architecture of our Spatial AI computation system, the long term key to efficient performance is to match up the natural graph structures of our algorithms to the configuration of physical hardware. As we have seen, this reasoning leads to the use of ‘close to the sensor’ processing such as in-plane image processing, and the attempt to minimise data transfer from sensors and towards actuators or other outputs using principles such as events.

However, we still believe that the bulk of computation in an embedded Spatial AI system is best carried out by a relatively centralised processing resource. The key reason for

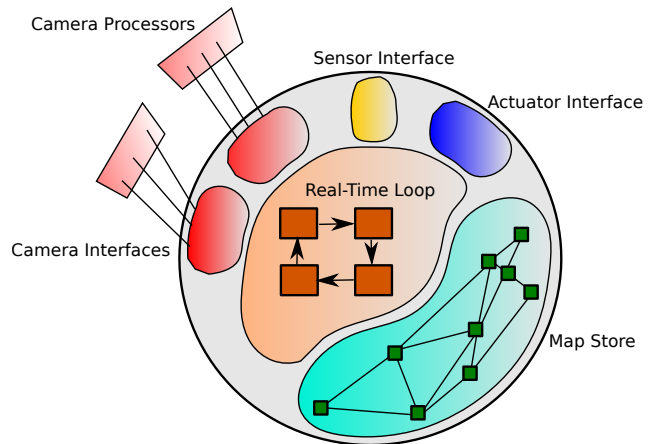


Figure 4. Spatial AI brain: an imagining of how the representation and processing graph structures of a general Spatial AI system might map to a graph processor. The key elements we identify are the real-time processing loop, the graph-based map store, and blocks which interface with sensors and output actuators. Note that we envision additional ‘close to the sensor’ processing built into visual sensors, aiming to reduce the data bandwidth (eventually in two directions) between the main processor and cameras, which will generally be located some distance away.

this is the essential and ever-present role of an incrementally built and used *world model* representing the system’s knowledge of its state and that of its environment. Every new piece of data from possibly multiple cameras and sensors is ultimately compared with this model, and either used to update it or discarded if the data is not relevant to device’s short or long-term goals.

What we are anticipating for this central processing resource is however far from the model of a CPU and RAM-like memory store. A CPU can access any contents of its RAM with a similar cost, but in Spatial AI there is much more structure present, as we saw in Section 5, both in the locality of the data representing knowledge of the world (5.1), and in the organisation of the computation workload involved in incorporating new data (5.2).

The graph structures of processing and storage should be built into the design of the central world model computation unit, which should combine storage and processing in a fully integrated way. There are already significant efforts on new ways to design architectures which are explicitly and flexibly graphlike.

To focus on one processor architecture currently under development, Graphcore’s IPU or graph processor is designed to efficiently carry out AI workloads which are well modelled as operations on sparse graphs, and in particular when all of the required storage is itself also held *within* the same graph rather than in an external memory store. An IPU chip has a large number of independent cores (in the thousands), each of which can run its own arbitrary program and

has its own local memory store, and then a powerful communication substrate such that the cores can efficiently send messages between themselves. When a program is to be run on the IPU, it is first compiled into a suitable form by analysis of the patterns of computation and communication it requires. A suitable graph topology of optimised locations of operations, data, and channels of communication is generated.

Graphcore have so far concentrated on how the IPU can be used to implement deep neural networks, both at training time and runtime. Figure 3 is a visualisation of the graph structure identified by their graph compiler Poplar from the TensorFlow definition of a standard CNN for image classification. Starting from a neuron's elemental computations of multiplying activations by weights, adding them together and passing the result through a non-linearity, they build up a processing graph which defines how these computations are joined together by data inputs and outputs. When this very detailed graph is visualised at increasing scale, with a view which 'zooms out', clusters of highly interlinked operations are apparent and these are concentrated and coloured in the visualisation, and the whole graph is mapped to a disc. The result is appealingly 'brain-like', with the various layers of the network shown as blocks of different sizes with their own internal structure visible. It is important to note that this computational structure represents the operations of both training the CNN and using it for runtime operation.

Graphcore believe that the IPU will already have performance benefits for executing well known deep neural networks compared to GPUs, and their initial product offering will be an accelerator card for machine learning in the cloud. However, their vision is greater than this, and they say that the advantages of an IPU will become greater and greater as the complexity of models increases. According to CEO Nigel Toon: 'the end game is deep, wide reinforcement learning, or more simply, building networks that improve with use', thinking towards recurrent, self-training structure with memory and constant input and output of data. Clearly this is very well aligned with the vision we have for the future of SLAM and Spatial AI, where we imagine systems with a complex pattern of designed and learned modules, communicating in real-time with input sensors and output actuators, and learning and improving their internal representations continuously.

In Figure 4 we have made a first attempt at drawing a 'Spatial AI brain' model which is somehow analogous to Graphcore's visualisations. The disc contains the modules we anticipate running inside the main processor. One of the two main areas is the map store, which is where the current world model is stored. This has an internal graph structure relating to the geometry of the world. It will also contain significant internal processing capability to operate locally

on the data in the model, and we will discuss the role of this shortly. The second main area is the real-time loop, which is where the main real-time computation connecting the input image stream to the world model is carried out. This has a processing graph structure and must support large real-time data flows and parallel computation on image/map structures so is designed to optimise this.

The main processor also has additional modules. There are camera interfaces, the job of each of which is to model and predict the data arriving at the sensor to which it is connected. This will then be connected to the camera itself, which the physical design of a robot or other device may force to be relatively far from the main processor. The connection may be serial or along multiple parallel lines.

We then imagine that each camera will have its own 'close-to-sensor' processing capability built in, separated from the main processor by a data link. The goal of modelling the input within the main processor is to minimise actual data transfer to the close-to-sensor processors. It could be that the close-to-sensor processor performs purely image-driven computation, in a manner similar to the SCAMP project, and delivers an abstracted representation to the main processor. Or, there could be bi-directional data transmission between the camera and main processor. By sending model predictions to the close-to-sensor processors, they know what is already available in the main processor and should report only differences. This is a generalisation of the event camera concept. An event camera reports only changes in intensity, whereas a future optimally efficient camera should report places where the received data is *different from what was predicted*. We will discuss close-to-sensor processing further in Section 7.

6.1. Map Store

There is a large degree of choice possible in the representation of a 3D scene, but as explained in Section 5.1.2, we envision maps which consist of graphs of learned features, which are linked in multi-scale patterns relating to camera motion. These features must represent geometry as well as appearance, such that they can be used to render a dense predicted view of the scene from a novel viewpoint. It may be that they do not need to represent full photometric appearance, and that a somewhat abstracted view is sufficient as long as it captures geometric detail.

Within the main processor, a major area will be devoted to storing this map, in a manner which is distributed around potentially a large number of individual cores which are strongly connected in a topology to mirror the map graph topology. In SLAM, of course the map is defined and grown dynamically, so the graph within the processor must either be able to change dynamically as well, or must be initially defined with a large unused capacity which is filled as SLAM progresses.

Importantly, a significant portion of the processing associated with large scale SLAM can be built directly into this graph. This is mainly the sort of ‘maintenance’ processing via which the map optimises and refines itself; including:

- Feature clustering; object segmentation and identification.
- Loop closure detection.
- Loop closure optimisation.
- Map regularisation (smoothing).
- Unsupervised clustering to discover new semantic categories.

With time, data and processing, a map which starts off as dense geometry and low level features can be refined towards an efficient object level map. Some of these operations will run with very high parallelism, as each part of the map is refined on its local core(s), while other operations such as loop closure detection and optimisation will require message passing around large parts of the graph. Still, importantly, they can take place in a manner which is internal to the map store itself.

The on-chip memory of next generation graph processors like Graphcore’s IPU is fully distributed among the processing tiles, and the total capacity will initially not be huge (certainly when compared with standard off-processor RAM), and therefore there should be an emphasis on rapidly abstracting the map store towards an efficient long-term form.

Optimising the geometric estimates in a SLAM map, such that the metric map state is the most probably solution given the history of measurements obtained, is a very well known optimisation problem known as Bundle Adjustment (BA) in computer vision or graph optimisation in robotics. The sparse constraints between poses and features due to measurements lead to sparsity in the solvers needed (e.g. [25]). While BA can be interpreted in terms of matrix operations, it is also commonly posed directly as a graph algorithm [11], and is clearly well suited to implementation in a message passing manner on a graph processor.

6.2. Real-Time Loop

This other major part of the graph encompasses the core processing which operates on live data input from cameras and other sensors and connects it to the map. New images are tracked against projections from the map and fused into updated representations. This is generally massively parallel processing which is familiar from GPU-accelerated dense SLAM systems, and these functions can be defined as fixed elements in a computational graph which use a number of nodes and access a significant fraction of the

main computational resource. Functions such as segmentation and labelling of input images will also be implemented here (or possibly outside of the main processor by close-to-sensor processing).

Data from the map store is needed for *rendering*, when a predicted view of the scene is needed for tracking against new image data, and for *fusion*, when information (geometry and labels) acquired from the new data is used to update the map contents.

The most difficult issue in applying graph processing to the real-time loop is the fact that the relevant part of the graph-based map store for these operations changes continuously due to camera motion. This seems to preclude defining an efficient, fixed data path to the distributed memory where map information will be stored. Although there will be internal processing happening in the map store, this will be focused on maintenance and it does not seem appropriate to move data rapidly around the map store, for instance such that the currently observed part of the map is always available in a particular graph location.

Instead, a possible solution is to define special interface nodes which sit between the real-time loop block and the map store. These are nodes focused on communication, which are connected to the relevant components of real-time loop processing and then also to various sites in the map graph, and may have some analogue in the hippocampus of mammal brains. If the map store is organised such that it has a ‘small world’ topology, meaning that any part is joined to any other part by a small number of edge hops, then the interface nodes should be able to access (copy) any relevant map data in a small number of operations and serve them up to the real-time loop.

Each node in the map store will also have to play some part in this communication procedure, where it will sometimes be used as part of the route for copying map data backwards and forwards.

7. Processing Close to the Image Plane

A robot or other device will have one or more cameras which interface with the main processor, and we believe that the technology will develop to allow a significant amount of processing to occur either within the sensors themselves or nearby, with the key aim of reducing the amount of redundant data which flows from the cameras. A first thought is to directly attach cameras to the main processor itself, with direct parallel connections (wires) from the pixels to multiple processing nodes, and certainly this is very appealing and could be possible in some cases. However, it is likely that in most devices there are good reasons why the main processor will not be located right next to the cameras, such as heat dissipation or space. The ideal locations for cameras are unlikely to be the same as the ideal location for a main processor. In any case, most future devices are likely

to have multiple cameras which all need to interface with the same main processor and map store. Therefore some long camera to main processor connections will be needed, and this motivates additional processing in the camera itself or very nearby.

Most straightforwardly, a sensor with in-plane processing similar to SCAMP5 [32] could be used to carry out purely bottom-up processing of the input image stream; abstracting, simplifying and detecting features to reduce it to a more compact, data-rich form. Calculations such as local tracking (e.g. optical flow estimation), segmentation and simple labelling could also be performed.

Tracking using in-plane processing is an interesting problem. In plane processing is good for problems where data access can be kept very local, so estimating local image motion (optical flow), where the output is a motion vector at every pixel, is well suited. At each update, the amount of image change locally can be augmented using local regularisation where smoothness is applied based on the differences of neighbouring pixels. If we look at the parallel implementation of an algorithm like Pock’s TV-L1 optical flow [44], we see that it involves pixelwise-parallel operations, where purely parallel steps relating to the data term alternate with regularisation steps involving gradient computation, which could be achieved using message passing between adjacent neighbours. So such an algorithm is an excellent candidate for implementation on an in-plane processor.

More challenging is the tracking usually required in SLAM, where from local image changes we wish to estimate consistent global motion parameters relating to a model. This could be instantaneous camera motion estimation, where we wish to estimate the amount of global rotation for instance between one frame and the next via whole image alignment [30], or tracking against a persistent scene model as in dense SLAM [29, 39]. When dense tracking is implemented on standard processors, it involves alternation of purely parallel steps for error term computation across all pixels with reduction steps where all errors are summed and the global motion parameters are updated. The reduction step, where a global model is imposed, plays the role of regularisation, but the big difference is that the regularisation here is global rather than local.

In a modern system, such global tracking is usually best achieved by a combination of GPU and CPU, and therefore a regular (and expensive) transfer of data between the two. But we do not have this option if we wish to use in-plane processing and keep all computations and memory local. Our main option for not giving up on data locality is to give up on guaranteed global consistency of our tracking solution, but to aim to converge towards this via local message passing. Each pixel could keep its own estimate of the global motion parameters of interest, and after each

iteration share these estimates with local neighbours. We would expect that global convergence would eventually be reached, but that after a certain number of iteration that the values held by each pixel could be close enough that any single pixel could be queried for a usable estimate. Convergence would be much faster if the in-plane processor also featured some longer data-passing links between pixels, or more generally had a ‘small world’ pattern of interconnections.

Turning to the questions of labelling using local processing, this is certainly feasible but a problem with sophisticated labelling is that current in plane processor designs have very small amounts of memory, which makes it difficult to store learned convolutional masks or similar.

Future processors for bottom-up processing may move beyond operating purely in the image plane, and use a 3D stacking approach which could be well suited to implementing the layers of a CNN. Currently 3D silicon stacks are hard to manufacture, and there are particular challenges around heat dissipation and cost, but the time will surely come when extracting a feature hierarchy is a built-in capability of a computer vision camera. Work such as Czarnowski *et al.*’s **featuremetric** tracking [6] shows the wide general use this would have. We should investigate the full range of outputs that a single purely feed-forward CNN to do when trained with a multi-task learning approach.

An interesting question is whether processing close to the image plane will remain purely bottom-up, or whether two-way communication between cameras and the main processor will be worthwhile. This would enable model predictions from the world map to be delivered to the camera at some rate, and therefore for higher level processing to be carried out there such as model-based tracking of the camera’s own motion or known objects.

In the limit, if a fully model-based prediction is able to be communicated to the camera, then the camera need only return information which is *different* from the prediction. This is in some sense a limit of the way that an event camera works. An event camera outputs data if a pixel changes in brightness — which is like assuming that the default is that the camera’s view of the scene will stay the same. A general ‘model-based event camera’ will output data if something happens which differs from its prediction. These questions come down to key issues of ‘bottom-up vs. top-down’ processing, and we will consider them further in the next section.

As a final note here, any Spatial AI system must ultimately deliver a task-determined output. This could be the commands sent to robot actuators, communication to be sent to another robot or annotations and displays to be sent to a human operator in an IA setting. Just as ‘close to the sensor’ processing is efficient, there should also be a role for ‘close to the actuator’ processing, particularly because ac-

tuators or communication channels have their own types of sensing (torque feedback for actuators; perhaps eye tracking or other measures for an AR display) which need to be taken account of and fused in tight loops.

8. Attention Mechanisms, or the Return of Active Vision

The active vision paradigm [2] advocates using sensing resources, such as the directions that a camera points towards or the processing applied to its feed, in a way which is controlled depending on the task at hand and prior knowledge available. This ‘top-down’ approach contrasts with ‘bottom-up’, blanket processing of all of the data received from a camera.

In Davison’s ‘Active Search for Real-Time Vision’ the argument was made that image processing in tracking and SLAM can be greatly reduced via prediction and active search [9]. Image features need not be detected ‘bottom up’ across every frame, but their positions predicted based on a model and searched for in a focused manner. The problem with this idea was that while image processing operations can certainly be saved by prediction and active search, too much computation is required to decide *where to look*. Most successful real-time vision systems since this time have instead used a ‘brute force’ approach to low level image processing. In SLAM, this has meant either full-frame detection of simple features (e.g. FAST features [46] as in PTAM [24]), or dense whole-image tracking as (e.g. DTAM [42]). The probabilistic calculations in [9] were sequential, and in particular difficult to transfer to the parallel architectures taken advantage of by [24] or [42].

Biological vision has a combination of bottom-up processing (early vision, which seems to operate in a purely bottom-up manner), and active, or top-down vision (proven by our moving heads and eyes which seek out relevant information for tasks based on model predictions). We believe that an active vision approach will return to real-time computer vision, but *at a higher level* than raw pixels. In particular, the flexibility of graph processing architectures will be much more amenable to active processing than CPU/GPU systems.

We understand very well now that entirely bottom-up processing of an image or short sequence, via a CNN for example, can achieve remarkable things such as semantic labelling, object detection, depth estimation and local motion estimation. At what level though should we interrupt this processing to bring in model-based predictions or task-dependent requirements? For instance, is it necessary to apply generic object detection processing to every image frame, when we can project previously mapped 3D objects into the newly estimated camera pose, and then apply any detection effort only to image areas so far unexplained by good object models (as shown by SLAM++ [49])? The big

question is: *What is the range of processing that we should expect a purely bottom-up algorithm to perform on input before it interacts with model-based data, predictions, and optimisation?*

The answer to this question must come back to the same kind of information gain versus computation arguments which were used in [9], but now considered more broadly. That paper studied low level feature matching in the context of a model-based prediction (such as in incremental probabilistic SLAM), and showed that the amount of image processing required to match a set of features could be much reduced by a one-by-one search strategy. Each search reduced the total model uncertainty, and therefore also the size of the search regions for the other features and the computation needed to match them. The order of search required was determined based on calculation of mutual information: the expected reduction in uncertainty for each candidate measurement. The problem with this method was that the reduction in image processing was ultimately outweighed by the extra computation needed to make the probabilistic and information theoretic calculations about what to measure next. In the end the elemental image processing computations needed to match point features are not expensive enough to make active search worthwhile, and it turns out to be better simply to detect and match all features.

But as we reach towards full scene understanding from vision in real-time, with the higher computational load required by elements such as dense reconstruction, segmentation or recognition, active choices will make sense again. Consider a simple possible bottom-up processing pipeline for semantic vision:

1. Localisation using sparse features.
2. Dense reconstruction.
3. Pixel-wise scene labelling.
4. Object instance segmentation.
5. 3D object model fitting.

In analysis, we can estimate the per-pixel computational cost of each of these elements as part of the pipeline, and assess the quality of their output. These measure should then be compared with the alternative ‘predict-update’ procedure, which could be carried out at any of the levels of output. Here we recover existing models from memory, warp them based on updates at the lower levels to make predictions for the current time-step, and then use ‘fusion’ processing on this together with the new image to update and augment the predictions into a final output. Computation should be focused on filling in not yet modelled regions, such as new parts of the scene which come into view at the edges of images or are revealed as occlusions are passed, or improving the estimates of regions where estimates have

high uncertainty, such as those seen in more detail when approached or observed in improved lighting. This ‘improvement’ will usually take the form of a probabilistic optimisation, where a weighted combination is made of model-based predictions and information from the new data.

It is important that when assessing the relative efficiency of bottom-up versus top-down vision, we take into account not just processing operations but also data transfer, and to what extent memory locality and graph-based computation can be achieved by each alternative. This will make certain possibilities in model-based prediction unattractive, such as searching large global maps or databases. The amazing advances in CNN-based vision means that we have to raise our sights when it comes to what we can expect from pure bottom-up image processing. But also, graph processing will surely permit new ways to store and retrieve model data efficiently, and will favour keeping and updating world models (such as graph SLAM maps) which have data locality.

9. Performance Metrics and Evaluation

One of the hypotheses we made at the start of this paper is that the usefulness of a Spatial AI system for a wide range of tasks is well represented by a relatively small number of performance measures which have general importance.

The most common focus in performance measurement in SLAM is on localisation accuracy, and there have been several efforts to create benchmark datasets for this (e.g. [52]). An external pose measurement from a motion capture system is considered as the ground truth against which a SLAM algorithm is compared.

We have argued that Spatial AI is about much more than pose estimation, and more recent datasets have tried to broaden the scope of what can be evaluated. Dense scene modelling is difficult to evaluate because it requires an expensive and time-consuming process such as detailed laser scanning to capture a complete model of a real scene which is accurate and complete enough to be considered ground truth. The alternative, for this and other axes of evaluation, is to generate synthetic test data using computer graphics, such as the ICL-NUIM dataset [19]. Recently this approach has been extended also to provide ground truth for semantic labelling (e.g. SceneNet RGB-D [34]), another output where it is difficult to get good ground truth for real data. It is natural to be suspicious of the value of evaluation against synthetic test data, and there are many new approaches to gathering large scale real mapping data, such as crowdsourcing (e.g. ScanNet [7]). However, synthetic data is getting better all the time and we believe will only grow in importance.

Stepping back to a bigger point, we can question the value of using benchmarks at all for Spatial AI systems. It is an often heard comment that computer vision researchers

are hooked on dataset evaluation, and that far too much effort has been spent on optimising and combining algorithms to achieve a few more percentage points on benchmarks rather than working on new ideas and techniques. SLAM, due to its real-time nature, and wide range of useful outputs and performance levels for different applications, has been particularly difficult to capture by meaningful benchmarks. I have usually felt that more can be learned about the usefulness of a visual SLAM system by playing with it for a minute or so, adaptively and qualitatively checking its behaviour via live visualisations, than from its measured performance against any benchmark available. Progress has therefore been more meaningfully represented by the progress of high quality real-time open source SLAM research systems (e.g. MonoSLAM [8, 10], PTAM [24], KinectFusion [41], LSD-SLAM [12], ORB-SLAM [36], OKVIS [28], SVO [14], ElasticFusion [56]) that people can experiment with, rather than benchmarks.

Benchmarks for SLAM have been unsatisfactory because they make assumptions about the scene type and shape, camera and other sensor choices and placement, frame-rate and resolution, etc., and focus in on certain evaluation aspects such as accuracy while downplaying other arguably more important ones such as efficiency or robustness. For instance, many papers evaluating algorithms against accuracy benchmarks make choices among the test sequences available in a dataset such as [52] and report performance only on those where they basically ‘work’.

This brings us to ask whether we should build benchmarks and aim to evaluate and compare SLAM systems at all? We still argue yes, but the focus on broadening what is meant by a benchmark for a Spatial AI system, and an acknowledgement that we should not put too much faith in what they tell us.

The SLAMBench framework released by the PAMELA research project [38] represents important initial work on looking at the performance of a whole Spatial AI system. In SLAMBench, a SLAM algorithm (specifically KinectFusion [41]) is measured in terms of both accuracy and computational cost across a range of processor platforms and using different language implementations. SLAMBench2 [4], recently released, now allows a wide range of SLAM algorithms to be compared within a unified test framework, and other work in the PAMELA project is broadening this effort in other directions. Saeedi *et al.* [48] have for instance started to address the issue of quantifying the SLAM challenge represented by the type of motion and typical scene geometry and appearance which is present in particular applications. The motion of wearable devices, ground robots and drones are all very different, and they are required to work in different environments. While SLAM on a drone is certainly challenging due to rapid motion, a small ground robot can also be a difficult case because of the low tex-

ture available in many indoor environments and its position close to the ground where there are many occlusions.

Over the longer term, we believe that benchmarking should move towards measures which have the general ability to predict performance on tasks that a Spatial AI might need to perform. This will clearly be a multi-objective set of metrics, and analysis of Pareto fronts [37] will permit choices to be made for a particular application.

A possible set of metrics includes:

- Local pose accuracy in newly explored areas (visual odometry drift rate).
- Long term metric pose repeatability in well mapped areas.
- Tracking robustness percentage.
- Relocalisation robustness percentage.
- SLAM system latency.
- Dense distance prediction accuracy at every pixel.
- Object segmentation accuracy.
- Object classification accuracy.
- AR pixel registration accuracy.
- Scene change detection accuracy.
- Power usage.
- Data movement (bits \times millimetres).

10. Conclusions

To conclude, the research area of Spatial AI and SLAM will continue to gain in importance, and evolve towards the general 3D perception capability needed for many different types of application with the full fruition of the combination of estimation and machine learning techniques. However, wide use in real applications will require this advance in capability to be accompanied by driving down the resources required, and this needs joined-up thinking about algorithms, processors and sensors. The key to efficient systems will be to identify and design for sparse graph patterns in algorithms and data storage, and to fit this as closely as possible to the new types of hardware which will soon gain in importance.

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