

Clipping

- **Any procedure that identifies those portions of a picture that are either inside or outside of a specified region**

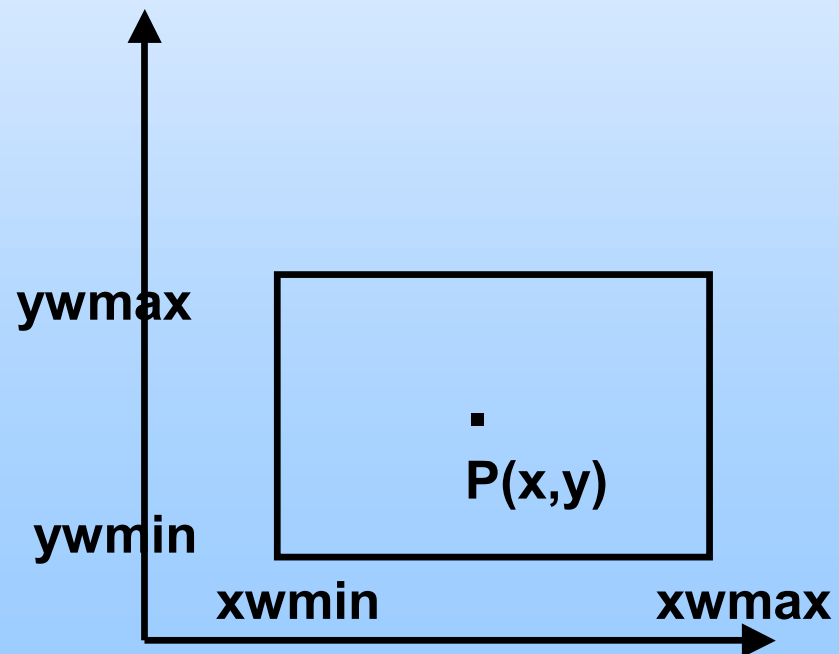
- **Point clipping**
- **Line clipping**
- **Area clipping or polygon clipping**
- **Curve clipping**
- **Text clipping**

Point clipping

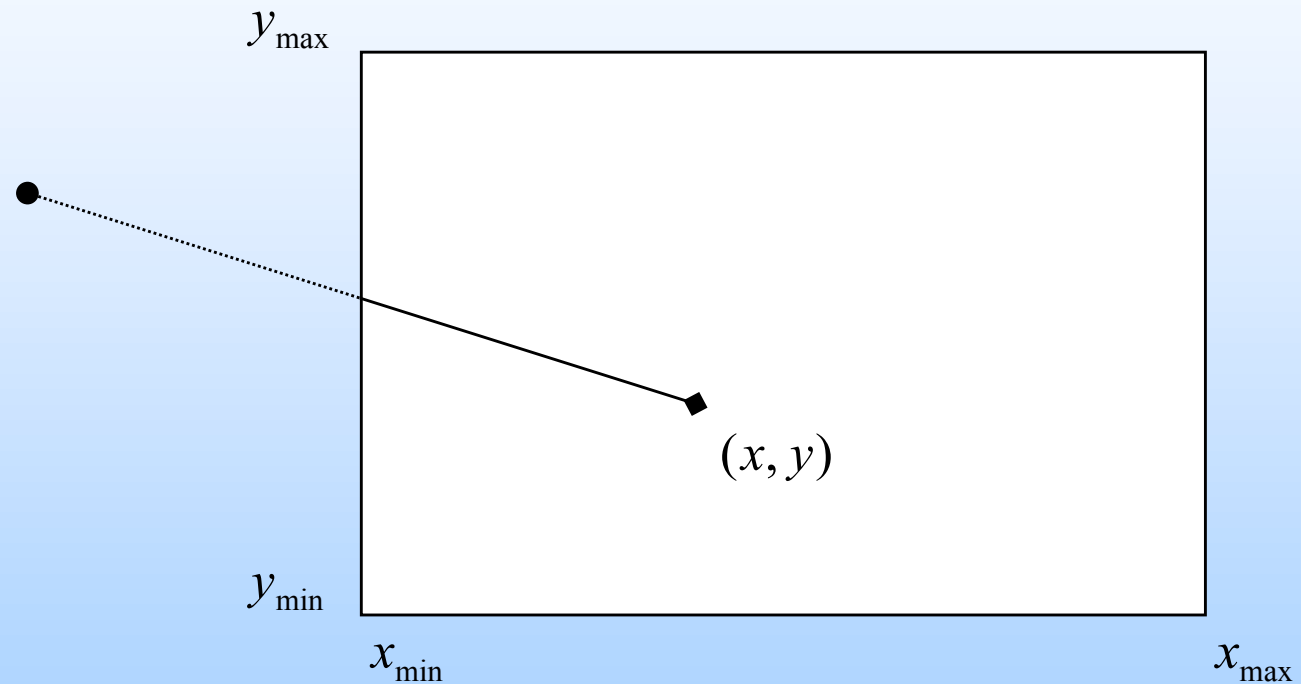
- In a rectangular clip window save a point $P = (x, y)$ for display if

$$xw_{\min} \leq x \leq xw_{\max}$$

$$yw_{\min} \leq y \leq yw_{\max}$$



Inside/Outside Test



$$x_{\min} \leq x \leq x_{\max}$$

$$y_{\min} \leq y \leq y_{\max}$$

Line Clipping

- Check whether the line is completely outside or inside the window boundary.
- Then perform inside outside test.
- Parametric eqn of a line with endpoints (x_1, y_1) and (x_2, y_2) is

$$x = x_1 + u (x_2 - x_1)$$

Where $u = (y - y_1) / (y_2 - y_1)$ (horizontal intersection)

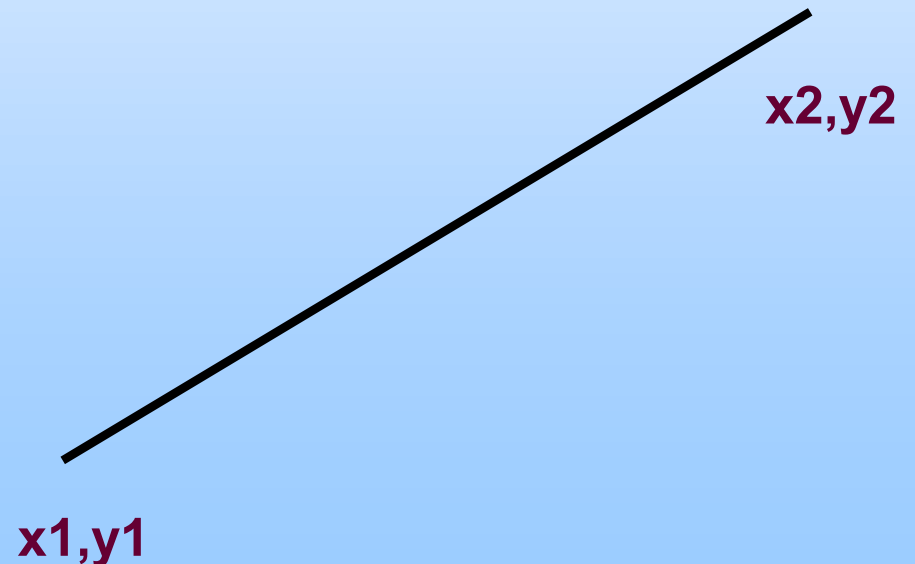
And $y = y_{\min}$ or $y = y_{\max}$

$$y = y_1 + u (y_2 - y_1)$$

$u = (x - x_1) / (x_2 - x_1)$ (vertical intersection)

And $x = x_{\min}$ or $x = x_{\max}$

Where $0 < u < 1$



Clipping Algorithms

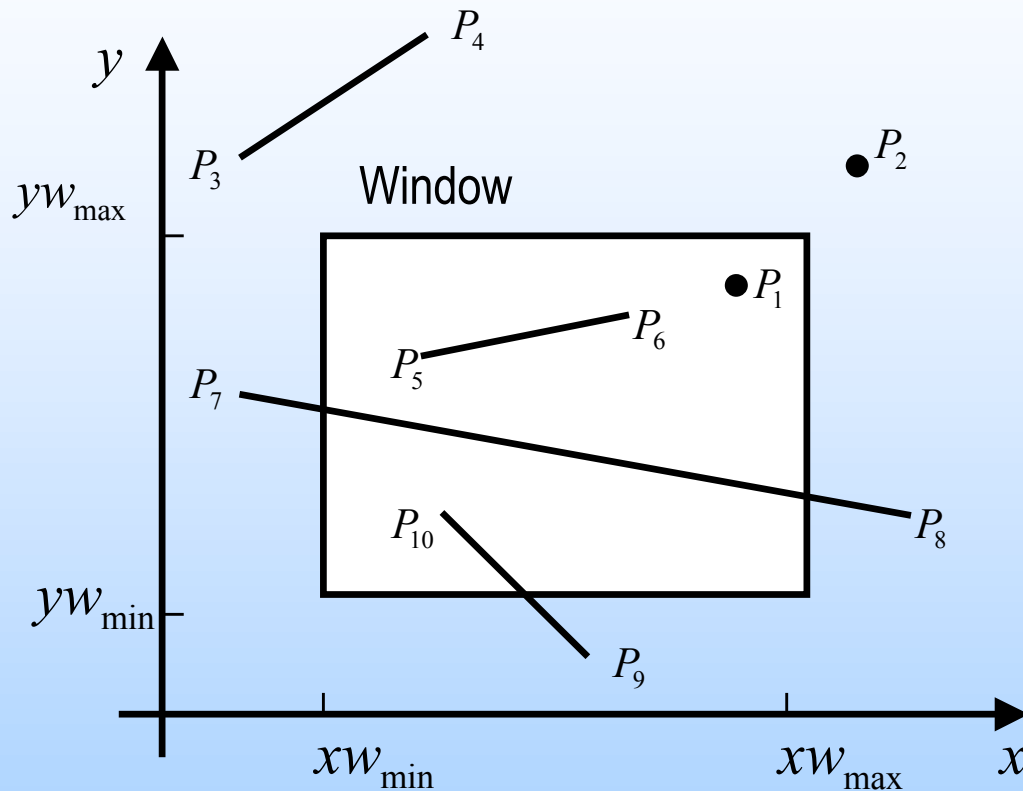
Line Clipping:

- Cohen-Sutherland (encoding) -Oldest and most commonly used
- Nicholl-Lee-Nicholl (encoding) (more efficient)
- Liang-Barsky (parametric)- More efficient than Cohen-Sutherland

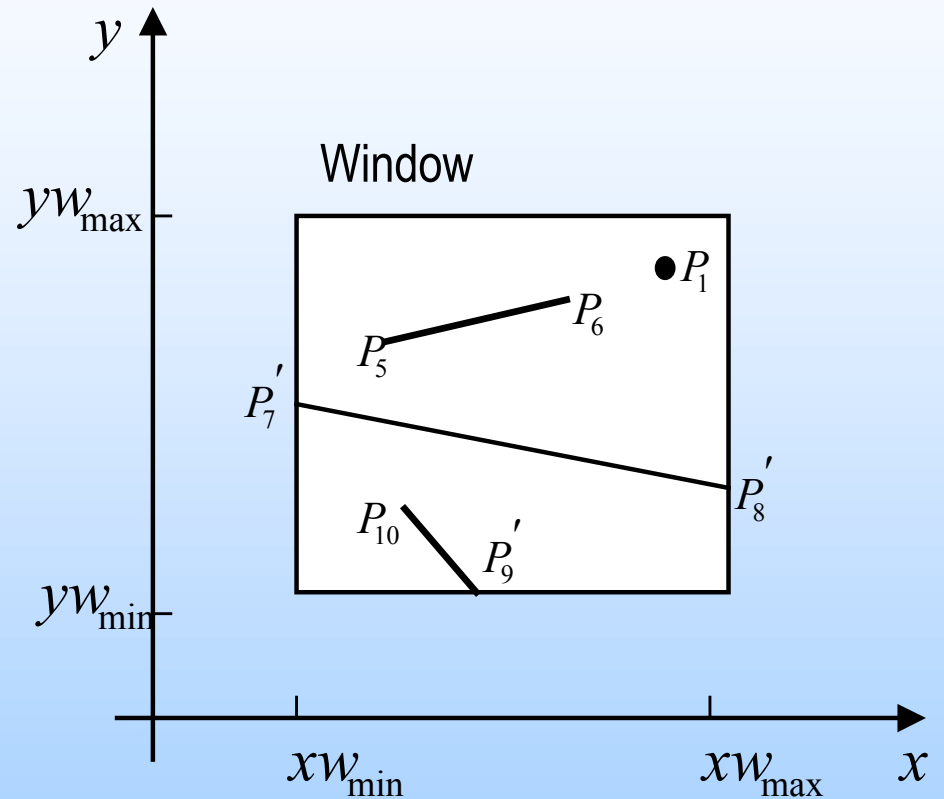
Polygon Clipping:

- Sutherland-Hodgeman (divide and conquer strategy)
- Weiler-Atherton (modified for concave polygons)

Line Clipping



(a) Before Clipping



(b) After Clipping

$$x_{\min} \leq x \leq x_{\max}$$

$$y_{\min} \leq y \leq y_{\max}$$

Sutherland and Cohen 2D Clipping Algorithm

Basic Idea

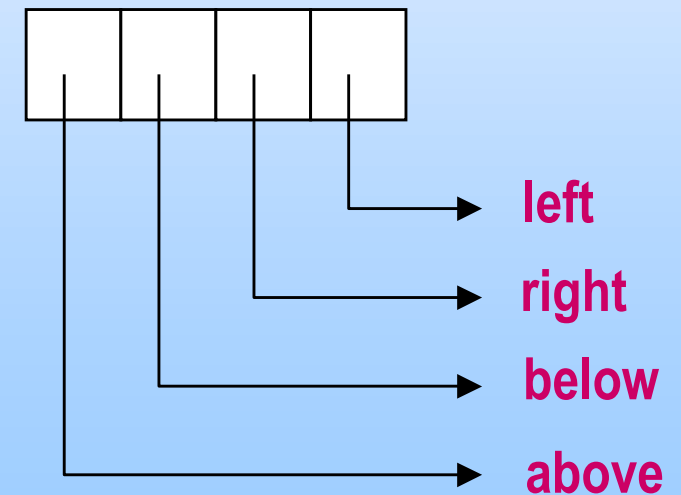
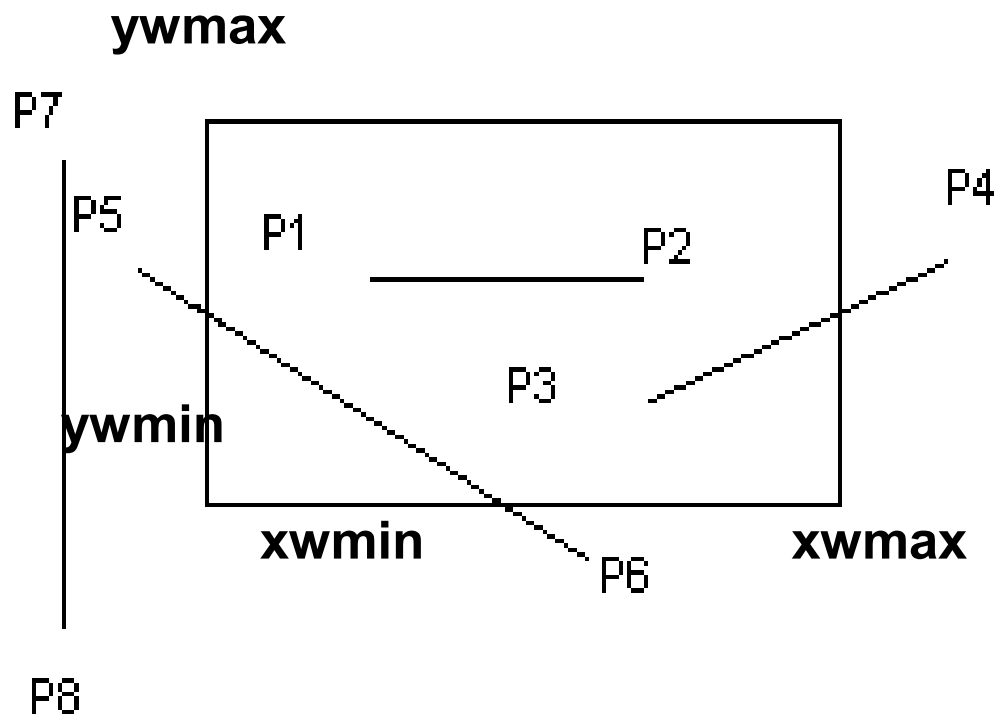
- **Encode the line endpoints**
- **Successively divide the line segments so that they are completely contained in the window or completely lies outside window**
- **Division occurs at the boundary of window**

Region Code Setting

- **Calculate the difference between endpoint coordinates and clipping boundaries.**
- **Use the resultant sign bit of each difference calculation to set corresponding region.**

- **Bit 1** sign bit of $x - xw_{\min}$
 - **Bit 2** sign bit of $xw_{\max} - x$
 - **Bit 3** sign bit of $y - yw_{\min}$
 - **Bit 4** sign bit of $yw_{\max} - y$
- OR**
- if($x < xw_{\min}$) then **Bit 1**
 - if($x > xw_{\max}$) then **Bit 2**
 - if($y < yw_{\min}$) then **Bit 3**
 - if($y > yw_{\max}$) then **Bit 4**

1001	1000	1010
0001	0000	0010
0101	0100	0110

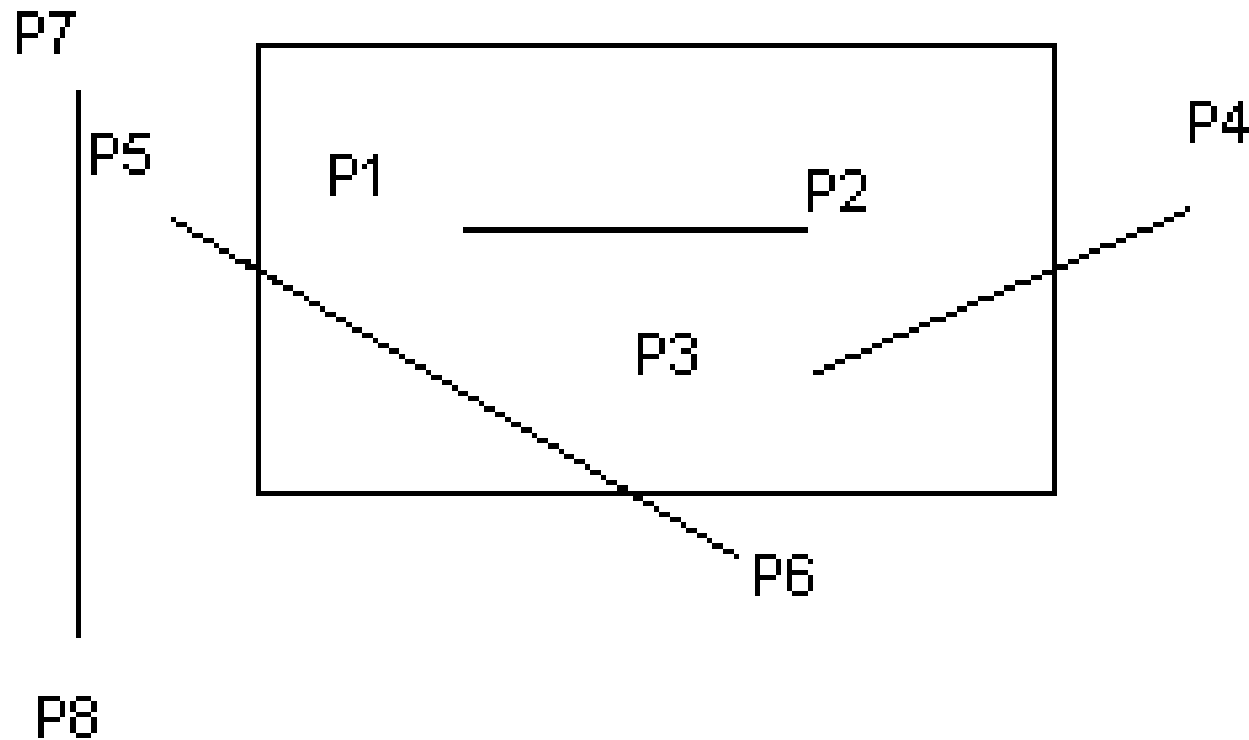


Bit 1- left

Bit 2- right

Bit 3- below

Bit 4 - Above



P1,P2 - 0000

P3 - 0000

P4 - 0010

P5 - 0001

P6 - 0100

P7 - 0001

P8 - 0101

- **After setting the region code determine whether the lines are**
 - **Completely inside the clip window.**
 - **Completely outside the clip window.**
 - **Intersecting with the window boundaries.**

- **Completely Inside**
 - Region code 0000 for both the endpoints.
 - Accept the line
- **Completely outside**
 - Lines have 1 in the same bit position.
 - Reject the line.

Method to test for total clipping

- Perform logical **AND** operation with the region code.
- If the result is not 0000 line is completely outside the clipping region.
- Lines that are not completely outside or inside a clip window are checked for intersection with the window boundary.

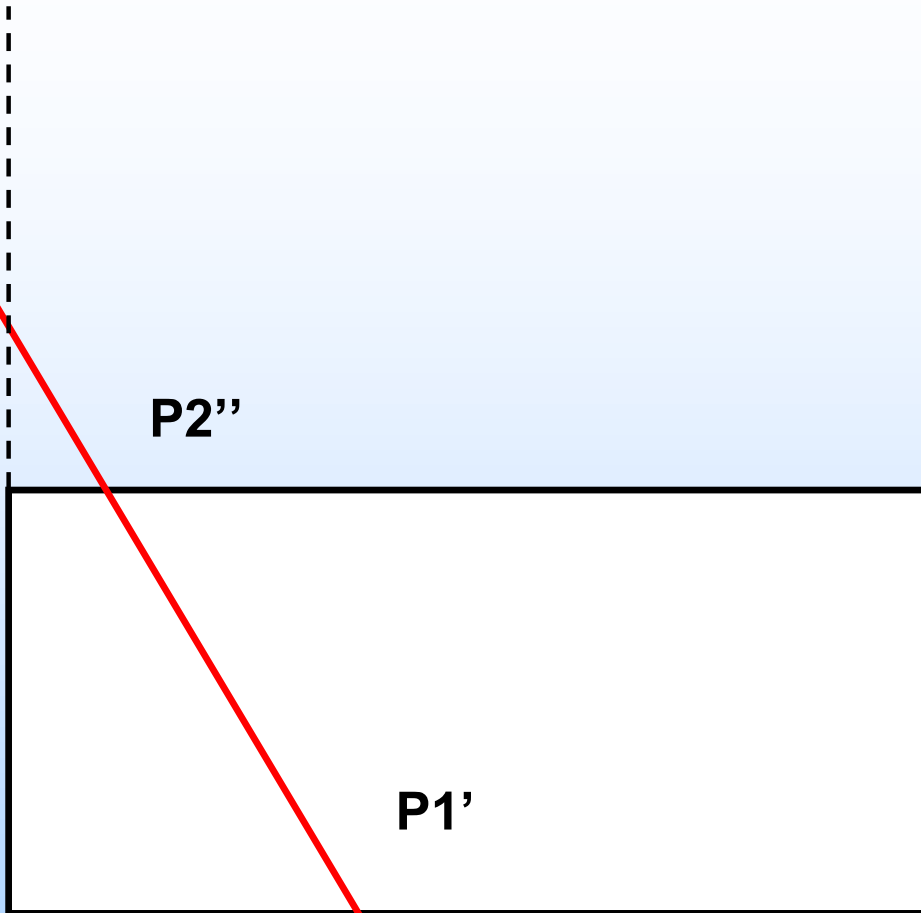
P2

P2'

P2''

P1'

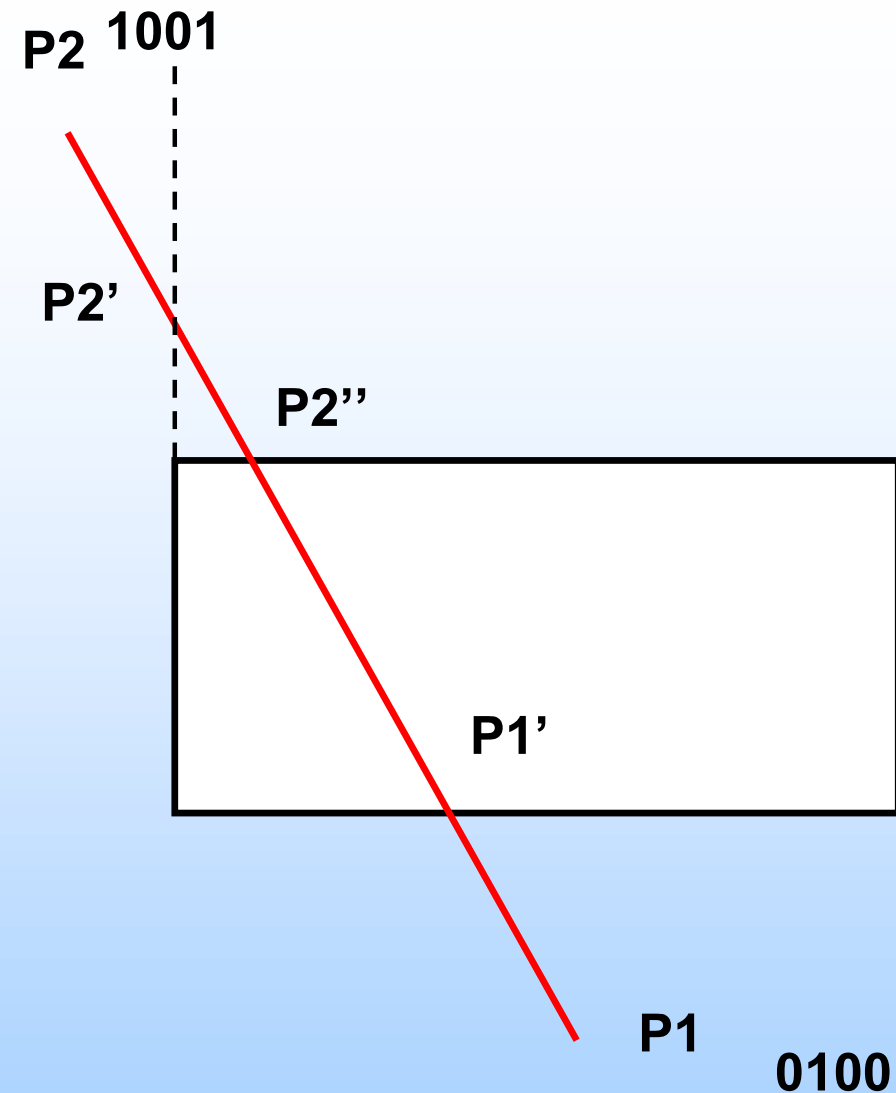
P1



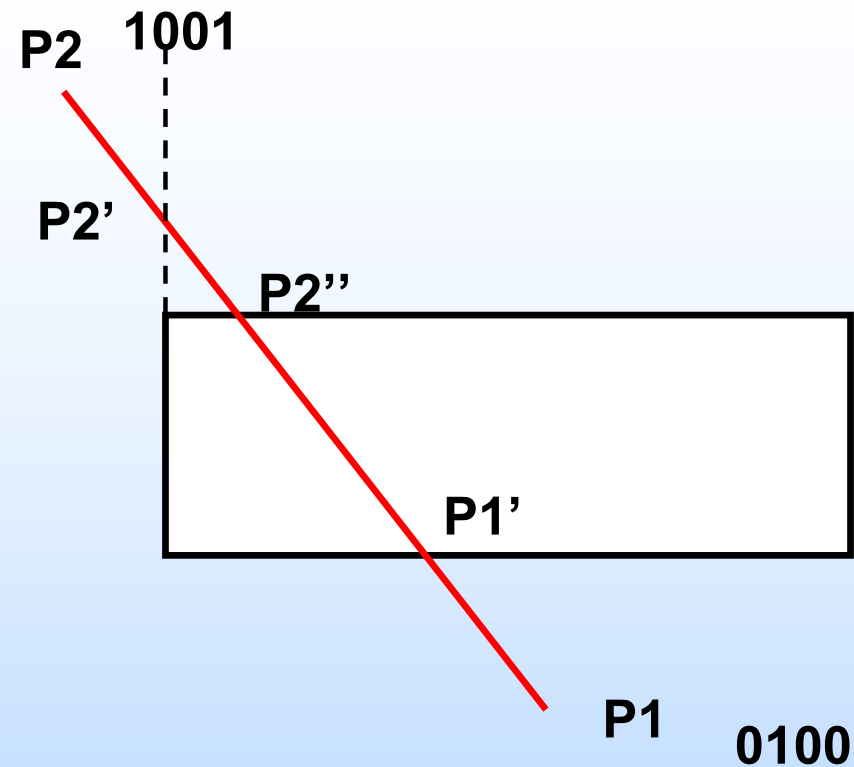
Steps

- Lines may or may not cross the window interior.
- Start from an outside end point and check with the clipping boundary to determine how much of the line can be discarded.
- The remaining part of the line is checked against other boundaries & continue until either the line is totally discarded or a section is found inside the window.
- Check line end points against clipping boundaries in the order
 - Left, Right, Bottom, top

- Check P1 against left, right & bottom boundary.
- Find intersection point P1' with bottom boundary and discard line section from P1 to P1'.
- Line reduced to P1' P2.



- Check P2 against the boundaries.
- P2 to the left of the window. **1001**
- Intersection point P2' is calculated.
- P2' above the window.
- Final intersection calculation leads to p2''.
- Line from P1' to P2'' s saved



- Intersection points with a boundary is calculated using slope intercept form
- Intersections with a vertical boundary:
 $y = y_1 + m(x - x_1)$ (x is either xmin or xmax)
- Intersections with a horizontal boundary:
 $x = x_1 + (y - y_1)/m$ (y is either ymin or ymax)

Continue until a trivial accept or a trivial reject.

Cohen-Sutherland Line-Clipping

- Will do unnecessary clipping.
- Not the most efficient.
- Clipping and testing are done in fixed order.
- Efficient when most of the lines to be clipped are either rejected or accepted (not so many subdivisions).
- Easy to program.
- Parametric clipping are more efficient.