

Q. $\int_0^2 \int_1^2 \int_0^{yz} xyz \, dx \, dy \, dz$

$$= \int_0^2 \int_1^2 \left[\int_0^{yz} \frac{x^2}{2} (yz) \, dx \right] dz \, dy$$

$$= \frac{1}{2} \int_0^2 \int_1^2 \left[\frac{x^2}{2} (yz) \right]_0^{yz} dz \, dy$$

$$= \frac{1}{2} \int_0^2 \int_1^2 \left[(yz) [(yz)^2] \right] dz \, dy$$

$$= \frac{1}{2} \int_0^2 \left[\int_1^2 (y^3 z^3) \right] dz \, dy$$

$$= \frac{1}{2} \int_0^2 \left[\int_1^2 (y^3) \cdot \frac{z^4}{4} \right] dz \, dy$$

$$= \frac{1}{4 \times 2} \int_0^2 \left[(y^3) (z^4) \right]_1^2 dy$$

$$= \frac{1}{8} \int_0^2 \left[(y^3) (2^4 - 1^4) \right] dy$$

$$= \frac{1}{8} \int_0^2 \left[(y^3) (15) \right] dy$$

$$= \frac{1}{8} \int_0^2 y^3 (24 - 14) dy$$

$$= \frac{1}{8} \int_0^2 y^3 (16 - 1) dy$$

$$= \frac{1}{8} \int_0^2 y^3 (15) dy$$

$$= \frac{15}{8} \int_0^2 y^3 dy$$

$$= \frac{15}{8} \left[\frac{y^4}{4} \right]_0^2 dy$$

$$= \frac{15}{8 \times 4} \left[y^4 \right]_0^2$$

$$= \frac{15}{8 \times 4} (2^4 - 2^0)$$

$$= \frac{15 \times (16 - 1)}{32}$$

$$= \frac{15 \times 15}{32}$$