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## 5. The Perceptron Algorithm

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## The Perceptron Algorithm

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All right.  
We defined earlier, training error  
for any classifier as a fraction of  
training samples  
that are misclassified--  
so in terms of whether or not the  
classifier  
applied to their training example,  
whether it disagrees with a given label

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## Perceptron Concept Questions 1

0/1 point (graded)

Remember that the Perceptron Algorithm (without offset) is stated as the following:

**Perceptron** $\left(\{(x^{(i)}, y^{(i)}), i = 1, \dots, n\}, T\right)$ :

```
initialize  $\theta = 0$ (vector);
for  $t = 1, \dots, T$  do
  for  $i = 1, \dots, n$  do
    if  $y^{(i)} (\theta \cdot x^{(i)}) \leq 0$  then
      update  $\theta = \theta + y^{(i)} x^{(i)}$ 
```

What does the Perceptron algorithm take as inputs among the following? Choose all those apply.

☒ Training set

☐ T - the number of times the algorithm iterates through the whole training set

☐ Test set

☒  $\theta$

☐  $\theta_0$

✗

## Perceptron Update 1

1/1 point (graded)

Now consider the Perceptron algorithm with Offset. Whenever there is a "mistake" (or equivalently, whenever  $y^{(i)} (\theta \cdot x^{(i)} + \theta_0) \leq 0$  i.e. when the label  $y^i$  and  $h(x)$  do not match), perceptron updates

$$\theta \text{ with } \theta + y^{(i)} x^{(i)}$$

and

$$\theta_0 \text{ with } \theta_0 + y^{(i)}.$$

More formally, the Perceptron Algorithm with Offset is defined as follows:

**Perceptron**  $\left( \{ (x^{(i)}, y^{(i)}), i = 1, \dots, n \}, T \right) :$   
 initialize  $\theta = 0$ (vector);  $\theta_0 = 0$ (scalar)  
 for  $t = 1, \dots, T$  do  
   for  $i = 1, \dots, n$  do  
     if  $y^{(i)} (\theta \cdot x^{(i)} + \theta_0) \leq 0$  then  
       update  $\theta = \theta + y^{(i)} x^{(i)}$   
       update  $\theta_0 = \theta_0 + y^{(i)}$

In the next set of problems, we will try to understand why such an update is a reasonable one.

When a mistake is spotted, do the updated values of  $\theta$  and  $\theta_0$  provide a better prediction? In other words, is

$$y^{(i)} ((\theta + y^{(i)} x^{(i)}) \cdot x^{(i)} + \theta_0 + y^{(i)})$$

always greater than or equal to

$$y^{(i)} (\theta \cdot x^{(i)} + \theta_0)$$

☐ Yes, because  $\theta + y^{(i)} x^{(i)}$  is always larger than  $\theta$

☒ Yes, because  $(y^{(i)})^2 \|x^{(i)}\|^2 + (y^{(i)})^2 \geq 0$

☐ No, because  $(y^{(i)})^2 \|x^{(i)}\|^2 - (y^{(i)})^2 \leq 0$

☐ No, because  $\theta + y^{(i)} x^{(i)}$  is always larger than  $\theta$



## Perceptron Update 2

0 points possible (ungraded)

For a given example  $i$ , we defined the training error as 1 if  $y^{(i)} (\theta \cdot x^{(i)} + \theta_0) \leq 0$ , and 0 otherwise:

$$\varepsilon_i(\theta, \theta_0) = \mathbb{I}[y^{(i)} (\theta \cdot x^{(i)} + \theta_0) \leq 0]$$

Say we have a linear classifier given by  $\theta, \theta_0$ . After the perceptron update using example  $i$ , the training error  $\varepsilon_i(\theta, \theta_0)$  for that example can (select all those apply):

☐ Increase

☒ Stay the same

☒ Decrease



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You have used 1 of 2 attempts

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[in this question inputs of the algorithm to start must first initialize value of parameters theta to start algorithm ?? i can't able to begin...](#)
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[0:35 "primitive vectors" -> "parameter vectors"](#)