HW-2

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$\mathbf{Q}\mathbf{1}$

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As $V_{GS} = V_{DD} - V_{OH}$ and only when $V_{OH} \leq V_{DD} - V_{Th}$ could guarentee the transistor is turned on. And the maximum value is the output voltage before t = 0

$$V_{OH} = V_{DD} - V_{Th}$$

$$= V_{DD} - V_{T0} - \gamma(\sqrt{2|\phi_F|} + V_{OH} - \sqrt{2|\phi_F|})$$

$$= 1.8(V)$$
(1)

b

As informed in the question, V_{Th} is constant and is the average of its maximum and minimum, which is

$$V_{Th} = V_{T0} + \frac{1}{2}\gamma(\sqrt{2|\phi_F| + V_{OH}} + \sqrt{2|\phi_F| + V_{OH}/2}) - \gamma\sqrt{2|\phi_F|}$$

$$= 0.67(V)$$
(2)

As $V_{out} = V_{OH} \rightarrow V_{OH}/2$, $V_{DS} = V_{DD} - V_{OH} \rightarrow V_{DD} - V_{OH}/2$. Thus,

$$R_{eq} = \frac{1}{2} \left[\frac{V_{DD} - V_{OH}}{\frac{1}{2} \kappa (V_{DD} - V_{OH} - V_{Th})^2} + \frac{V_{DD} - V_{OH}/2}{\frac{1}{2} \kappa (V_{DD} - V_{OH}/2 - V_{Th})^2} \right]$$

$$= \frac{V_{DD} - V_{OH}}{\kappa (V_{DD} - V_{OH} - V_{Th})^2} + \frac{V_{DD} - V_{OH}/2}{\kappa (V_{DD} - V_{OH}/2 - V_{Th})^2}$$

$$= 6.8 \times 10^6 (\Omega)$$
(3)

 \mathbf{c}

When $t \to \infty$,

$$V_{out} = I_{DSAT}R_{SW}$$

$$= \frac{1}{2}\kappa[V_{DD} - V_{out} - V_{T0} - \gamma(\sqrt{2|\phi_F|} + V_{out} - \sqrt{2|\phi_F|})]^2 R_{SW}$$
(4)

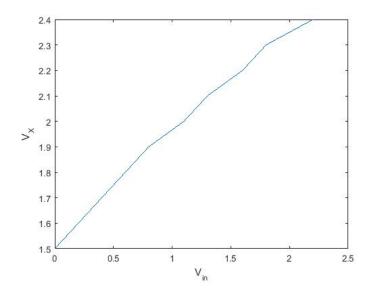


Figure 1: Q2_a

 $\mathbf{Q2}$

$$V_X = V_{DD} - I_{SD}R_1$$

= $V_{DD} + \frac{1}{2}\kappa \frac{W}{L}(V_X - V_{in} + V_{T0})^2 (1 + \lambda V_X)R_1$ (5)

 \mathbf{a}

See Figure 1.

 \mathbf{b}

$$\frac{W}{L} = 1.1\tag{6}$$

Q3

a

It is clear that $V_{X,max} = V_{DD} - V_{Th}$. And

$$V_{Th} = V_{T0} + \frac{1}{2}\gamma(\sqrt{2|\phi_F| + V_{X,max}/2} - \sqrt{2|\phi_F|})$$

$$= 0.53(V)$$
(7)

Thus, $V_{X,max} = 1.97(V)$. As well as

$$R_{eq} = \frac{1}{2} R_{eq,max}$$

$$= \frac{V_{DD} - \frac{V_{X,max}}{2}}{\kappa \frac{W}{L} (V_{DD} - V_{X,max}/2 - V_{Th})^2 [1 + \lambda (V_{DD} - V_{X,max}/2)]}$$

$$= 829.7861(\Omega)$$
(8)

Thus,

$$t_{pLH} = R_{eq}C_L ln \frac{V_{DD}}{V_{DD} - V_{out}}$$

$$= R_{eq}C_L ln \frac{2V_{DD}}{V_{DD} + V_{Th}}$$

$$= 2.0781(ns)$$
(9)

b

$$\Delta t_{pLH} = 0.69 R_{eq} C_0 W_0 = t_0$$
 (10)

 \mathbf{c}

$$t_{pHL} = 0.69RC_L = 17.25(ns)$$
 (11)

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With $\beta_n=\beta_p$, and $|\gamma_n|=|\gamma_p|$ with $|\lambda_n|=|\lambda_p|$ from the table coming with questions. $\frac{t_{pLH,n}}{t_{pLH,p}}$ becomes,

$$\frac{t_{pLH,n}}{t_{pLH,p}} = \frac{R_{eq,n}}{R_{eq,p}} \frac{ln \frac{2V_{DD}}{V_{DD} + V_{Tn}}}{ln \frac{2V_{DD}}{V_{DD} + V_{Tp,0}}}
= \frac{(V_{DD} + V_{Tn})(V_{DD} - V_{Tp,0})^2 [1 + \frac{1}{2}\lambda_p(V_{DD} + V_{Tp,0})] ln \frac{2V_{DD}}{V_{DD} + V_{Tn}}}{(V_{DD} + V_{Tp,0})(V_{DD} - V_{Tn})^2 [1 + \frac{1}{2}\lambda_n(V_{DD} + V_{Tn})] ln \frac{2V_{DD}}{V_{DD} + V_{Tn}}}
= 1.3001$$
(12)

Which means, using PMOS will make it a bit faster.

Q4

As how to use HSPICE is not taught, and therefore no tutorial was given. And this is the first time ever I've such a program, which means there is no way I could know how to use it before hand. I can only use what I can see from netlist figures.

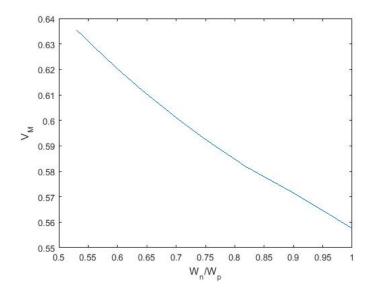


Figure 2: Q4_a

\mathbf{a}

$$\begin{array}{c|cccc} \text{For } V_M = 0.5 V_{DD}, \ \frac{W_n}{W_p} = \frac{90}{127.50575} \approx \frac{90}{127.5}. \\ 90/90 & 0.5576 \\ 90/100 & 0.5715 \\ 90/110 & 0.5819 \\ 90/120 & 0.5925 \\ 90/127.5 & 0.6 \\ 90/140 & 0.6116 \\ 90/150 & 0.6202 \\ 90/160 & 0.6283 \\ 90/170 & 0.6357 \\ \end{array}$$

\mathbf{b}

See Figure 3. For high-to-low delay equals low-to-high delay, $\frac{W_n}{W_p} = \frac{90}{135.75}$.

\mathbf{c}

See Figure 4.

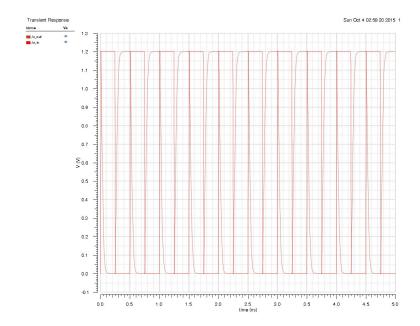


Figure 3: Q4_b

$D_{input(ps)}$	$\mathrm{t}_{ ext{-}}\mathrm{pHL}(\mathrm{ps})$	$t_pLH(ps)$
0.1	27	27
50	32	27
100	39	27
150	44	27
200	48	27
500	65	27

Quite clear that high-to-low delay is positively related with input rise time. And in fact it is still a fuction of input.

\mathbf{d}

Except for high-to-low delay increased to 67ps, I saw no suspicious things. And here is my paramiters:

PMOS	L	$50\mathrm{nm}$
	W	$542.8\mathrm{nm}$
NMOS	L	$50\mathrm{nm}$
	W	$90\mathrm{nm}$
$V_{-}dd$		1.2V
V_{-in}	rise time	$200 \mathrm{ps}$
	fall time	10 ps
	pulse width	235 ps
	period	880 ps
	voltage 1	0V
	voltage 2	1.2V
Cap		5 fF

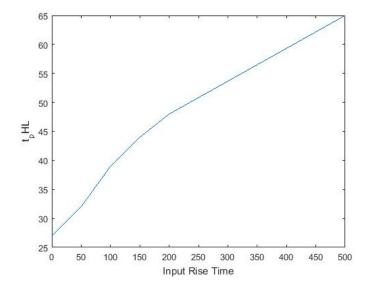


Figure 4: Q4_c

 \mathbf{e}

For what I got, it is the same as the result from part (b). And have no conflict with part(c).

$$\frac{t_{pHL}}{t_{pLH}} = \frac{R_n}{R_p}$$

$$= \frac{I_{DSAT,p}(1 - \frac{7}{9}\lambda_n V_{DD})}{I_{DSAT,N}(1 - \frac{7}{9}\lambda_p V_{DD})}$$

$$= \frac{\kappa_p W_p (V_{DD} - V_{T0})^2 (1 - \frac{7}{9}\lambda_n V_{DD})}{\kappa_n W_n (V_{DD} - V_{Tn})^2 (1 - \frac{7}{9}\lambda_p V_{DD})}$$
(13)

Thus the ratio has nothing to do with input rise/fall time. But, of course, signal frequency become too high, output will go wild.