

HW-2

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Q1

a

As $V_{GS} = V_{DD} - V_{OH}$ and only when $V_{OH} \leq V_{DD} - V_{Th}$ could guarantee the transistor is turned on. And the maximum value is the output voltage before $t = 0$.

$$\begin{aligned} V_{OH} &= V_{DD} - V_{Th} \\ &= V_{DD} - V_{T0} - \gamma(\sqrt{2|\phi_F| + V_{OH}} - \sqrt{2|\phi_F|}) \end{aligned} \quad (1)$$

Therefore,

$$2|\phi_F| + V_{OH} + \gamma(\sqrt{2|\phi_F| + V_{OH}}) - (V_{DD} - V_{T0} + \sqrt{2|\phi_F|} + 2|\phi_F|) = 0 \quad (2)$$

So,

$$\sqrt{2|\phi_F| + V_{OH}} = -\frac{\gamma}{2} + \sqrt{\frac{\gamma^2}{4} + V_{DD} - V_{T0} + \gamma\sqrt{2|\phi_F|} + 2|\phi_F|} \quad (3)$$

Then, finally:

$$\begin{aligned} V_{OH} &= \frac{\gamma^2}{2} + V_{DD} - V_{T0} + \gamma\sqrt{2|\phi_F|} \\ &\quad - \gamma\sqrt{\frac{\gamma^2}{4} + V_{DD} - V_{T0} + \gamma\sqrt{2|\phi_F|} + 2|\phi_F|} \\ &= V_{DD} - 0.4 \times \sqrt{V_{DD} + 0.52} - 0.04(V) \end{aligned} \quad (4)$$

c

When $t \rightarrow \infty$,

$$\begin{aligned} V_{out} &= I_{DSAT} R_{SW} \\ &= \frac{1}{2} \kappa \frac{W}{L} [V_{DD} - V_{out} - V_{T0} - \gamma(\sqrt{2|\phi_F| + V_{out}} - \sqrt{2|\phi_F|})]^2 R_{SW} \\ &= \end{aligned} \quad (5)$$

b

As informed in the question, V_{Th} is constant and is the average of its maximum and minimum, which is

$$V_{Th} = V_{T0} + \frac{1}{2}\gamma(\sqrt{2|\phi_F| + V_{OH}} + \sqrt{2|\phi_F| + V_{out}}) - \gamma\sqrt{2|\phi_F|} \quad (6)$$

As $V_{out} = V_{OH} \rightarrow V_{OH}/2$, $V_{DS} = V_{DD} - V_{OH} \rightarrow V_{DD} - V_{OH}/2$. Thus,

$$\begin{aligned} R_{eq} &= \frac{1}{2} \left[\frac{V_{DD} - V_{OH}}{\frac{1}{2}\kappa(V_{DD} - V_{OH} - V_{Th})^2} + \frac{V_{DD} - V_{OH}/2}{\frac{1}{2}\kappa(V_{DD} - V_{OH}/2 - V_{Th})^2} \right] \\ &= \frac{V_{DD} - V_{OH}}{\kappa(V_{DD} - V_{OH} - V_{Th})^2} + \frac{V_{DD} - V_{OH}/2}{\kappa(V_{DD} - V_{OH}/2 - V_{Th})^2} \end{aligned} \quad (7)$$

Q2

$$\begin{aligned} V_X &= V_{DD} - I_{SD}R_1 \\ &= V_{DD} + \frac{1}{2}\kappa\frac{W}{L}(V_X - V_{in} + V_{Th})^2[1 + \lambda(V_X - V_{in})]R_1 \end{aligned} \quad (8)$$

a

b

$$\begin{aligned} 1.5(V) &= 2.5(V) - 0.5 \times (-30)^{-6}(A/V^2) \times \frac{W}{L} \times (1.5(V) - 0.4(V))^2 \\ &\times (1 - 0.1(V^{-1}) \times a.5(V)) \times 20 \times 10^3(\Omega) \end{aligned} \quad (9)$$

Thus,

$$\frac{W}{L} = 3.24 \quad (10)$$

Q3

a

$$\begin{aligned} t_{tLH} &= 0.69R_{eq}C_L \\ &= \end{aligned} \quad (11)$$

b

$$\begin{aligned} \Delta t_{pLH} &= 0.69R_{eq}C_0W_0 \\ &= \end{aligned} \quad (12)$$

c

$$\begin{aligned} t_{pHL} &= 0.69RC_L \\ &= \end{aligned} \quad (13)$$

d