HW-2

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$\mathbf{Q}\mathbf{1}$

a

As $V_{GS} = V_{DD} - V_{OH}$ and only when $V_{OH} \leq V_{DD} - V_{Th}$ could guarentee the transistor is turned on. And the maximum value is the output voltage before t = 0

$$V_{OH} = V_{DD} - V_{Th}$$

$$= V_{DD} - V_{T0} - \gamma(\sqrt{2|\phi_F| + V_{OH}} - \sqrt{2|\phi_F|})$$

$$-$$
(1)

 \mathbf{c}

When $t \to \infty$,

$$V_{out} = I_{DSAT}R_{SW}$$

$$= \frac{1}{2}\kappa[V_{DD} - V_{out} - V_{T0} - \gamma(\sqrt{2|\phi_F|} + V_{out} - \sqrt{2|\phi_F|})]^2 R_{SW}$$
(2)
$$= \frac{1}{2}\kappa[V_{DD} - V_{out} - V_{T0} - \gamma(\sqrt{2|\phi_F|} + V_{out} - \sqrt{2|\phi_F|})]^2 R_{SW}$$

b

As informed in the question, V_{Th} is constant and is the average of its maximum and minimum, which is

$$V_{Th} = V_{T0} + \frac{1}{2}\gamma(\sqrt{2|\phi_F| + V_{OH}} + \sqrt{2|\phi_F| + V_{OH}/2}) - \gamma\sqrt{2|\phi_F|}$$

$$= (3)$$

As $V_{out} = V_{OH} \rightarrow V_{OH}/2$, $V_{DS} = V_{DD} - V_{OH} \rightarrow V_{DD} - V_{OH}/2$. Thus,

$$R_{eq} = \frac{1}{2} \left[\frac{V_{DD} - V_{OH}}{\frac{1}{2} \kappa (V_{DD} - V_{OH} - V_{Th})^2} + \frac{V_{DD} - V_{OH}/2}{\frac{1}{2} \kappa (V_{DD} - V_{OH}/2 - V_{Th})^2} \right]$$

$$= \frac{V_{DD} - V_{OH}}{\kappa (V_{DD} - V_{OH} - V_{Th})^2} + \frac{V_{DD} - V_{OH}/2}{\kappa (V_{DD} - V_{OH}/2 - V_{Th})^2}$$

$$= \frac{V_{DD} - V_{OH}}{\kappa (V_{DD} - V_{OH}/2 - V_{Th})^2}$$
(4)

 $\mathbf{Q2}$

$$V_X = V_{DD} - I_{SD}R_1$$

$$= V_{DD} + \frac{1}{2}\kappa \frac{W}{L}(V_X - V_{in} + V_{T0})^2 (1 + \lambda V_X)R_1$$
(5)

 \mathbf{a}

b

$$\frac{W}{L} = 3.24\tag{6}$$

 $\mathbf{Q3}$

 \mathbf{a}

$$t_{pLH} = R_{eq}C_{L}ln\frac{V_{DD}}{V_{DD} - V_{out}}$$

$$= R_{eq}C_{L}ln\frac{2V_{DD}}{V_{DD} + V_{Tn}}$$

$$= \frac{3V_{DD}R_{eq}C_{L}}{2\kappa\frac{W}{L}(V_{DD} - V_{Tn})^{2}}(1 - \frac{5}{6}\lambda V_{DD})ln\frac{2V_{DD}}{V_{DD} + V_{Tn}}$$

$$= \frac{3V_{DD}R_{eq}C_{L}}{2\kappa\frac{W}{L}(V_{DD} - V_{Tn})^{2}}(1 - \frac{5}{6}\lambda V_{DD})ln\frac{2V_{DD}}{V_{DD} + V_{Tn}}$$

 \mathbf{b}

$$\Delta t_{pLH} = 0.69 R_{eq} C_0 W_0$$

$$= t_0 \tag{8}$$

 \mathbf{c}

$$t_{pHL} = 0.69RC_L$$

= 1.735 × 10⁻⁶(s) (9)

Ч

With $\beta_n=\beta_p$, and $|\gamma_n|=|\gamma_p|$ with $|\lambda_n|=|\lambda_p|$ from the table coming with questions. $\frac{t_{pLH,n}}{t_{pLH,p}}$ becomes,

$$\frac{t_{pLH,n}}{t_{pLH,p}} = \frac{R_{eq,n}}{R_{eq,p}} \frac{ln \frac{2V_{DD}}{V_{DD} + V_{Tn}}}{ln \frac{2V_{DD}}{V_{DD} + V_{Tp,0}}}
= \frac{(V_{DD} - V_{Tp,0})^2 (1 - \frac{5}{6}\lambda_n V_{DD}) ln \frac{2V_{DD}}{V_{DD} + V_{Tn}}}{(V_{DD} - V_{Tn})^2 (1 - \frac{5}{6}\lambda_p V_{DD}) ln \frac{2V_{DD}}{V_{DD} + V_{Tp,0}}}$$
(10)

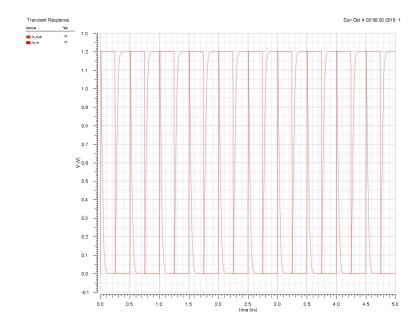


Figure 1: Q4_b

$\mathbf{Q4}$

ล

For $V_M = 0.5 V_{DD}$, $\frac{W_n}{W_p} = \frac{90}{127.50575} \approx \frac{90}{127.5}$. (((The following table need to be ploted!!!))) 90/90 0.557690/100 0.571590/110 0.581990/1200.592590/127.50.690/1400.611690/150 0.620290/160 0.628390/170 0.6357

b

For high-to-low delay equals low-to-high delay, $\frac{W_n}{W_p} = \frac{90}{135.75}$.

 $((({\it The following table need to be ploted})))$

$D_{input(ps)}$	$t_{-}pHL(ps)$	$t_{-}pLH(ps)$	
0.1	27	27	
50	32	27	
100	39	27	(((Figure here!!!)))
150	44	27	
200	48	27	
500	65	27	

Quite clear that high-to-low delay is positively related with input rise time. And in fact it is still a fuction of input.

\mathbf{d}

Except for high-to-low delay increased to 67ps, I saw no suspicious things. And here is my paramiters:

PMOS	${ m L}$	$50\mathrm{nm}$
	W	$542.8\mathrm{nm}$
NMOS	L	$50\mathrm{nm}$
	W	$90\mathrm{nm}$
$V_{-}dd$		1.2V
V_{-in}	rise time	$200 \mathrm{ps}$
	fall time	$10 \mathrm{ps}$
	pulse width	235 ps
	period	880 ps
	voltage 1	0V
	voltage 2	1.2V
Cap		5fF

 \mathbf{e}

For what I got, it is the same as the result from part (b). And have no conflict with part(c).

$$\frac{t_{pHL}}{t_{pLH}} = \frac{R_n}{R_p}$$

$$= \frac{I_{DSAT,p}(1 - \frac{7}{9}\lambda_n V_{DD})}{I_{DSAT,N}(1 - \frac{7}{9}\lambda_p V_{DD})}$$

$$= \frac{\kappa_p W_p (V_{DD} - V_{T0})^2 (1 - \frac{7}{9}\lambda_n V_{DD})}{\kappa_n W_n (V_{DD} - V_{Tn})^2 (1 - \frac{7}{9}\lambda_p V_{DD})}$$
(11)

Thus the ratio has nothing to do with input rise/fall time. But, ofcourse, signal frequency become too high, output will go wild.