

## Part 1: Translation (Moving Objects)

### Theory

Translation moves an object from one position to another by adding translation factors to coordinates.

- $\text{New X} = \text{Old X} + T_x$
- $\text{New Y} = \text{Old Y} + T_y$

### Example 1.1: Translating a Single Triangle

```
from OpenGL.GL import *
from OpenGL.GLUT import *
from OpenGL.GLU import *

# Original triangle vertices
triangle_vertices = [
    [200, 200],
    [300, 200],
    [250, 300]
]

# Translation values
tx = 100 # Move 100 pixels right
ty = 50  # Move 50 pixels up

def draw_triangle(vertices):
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
glBegin(GL_TRIANGLES)

# glBegin(GL_LINES)

# glVertex2f(200, 200)

# glVertex2f(300, 200)

# glVertex2f(250, 300)

# glVertex2f(200, 200)

# glVertex2f(300, 200)

# glVertex2f(250, 300)

for vertex in vertices:

    glVertex2f(vertex[0], vertex[1])

glEnd()

def translate_point(x, y, tx, ty):

    return [x + tx, y + ty]

def translate_shape(vertices, tx, ty):

    translated = []

    for vertex in vertices:

        new_point = translate_point(vertex[0], vertex[1], tx, ty)

        translated.append(new_point)

    return translated

def iterate():

    glViewport(0, 0, 500, 500)

    glMatrixMode(GL_PROJECTION)
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
glLoadIdentity()

glOrtho(0.0, 500, 0.0, 500, 0.0, 1.0)

glMatrixMode(GL_MODELVIEW)

glLoadIdentity()

def showScreen():

    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT)

    glLoadIdentity()

    iterate()

    # Draw original triangle in yellow

    glColor3f(1.0, 1.0, 0.0)

    draw_triangle(triangle_vertices)

    # Translate and draw new triangle in red

    glColor3f(1.0, 0.0, 0.0)

    translated_triangle = translate_shape(triangle_vertices, tx, ty)

    # draw_triangle(translated_triangle)

    glutSwapBuffers()

glutInit()

glutInitDisplayMode(GLUT_RGBA)

glutInitWindowSize(500, 500)

glutInitWindowPosition(0, 0)

wind = glutCreateWindow(b"Translation Example")
```

```
glutDisplayFunc(showScreen)

glutMainLoop()
```

### Example 1.2: Animated Translation

```
from OpenGL.GL import *

from OpenGL.GLUT import *

from OpenGL.GLU import *


triangle_vertices = [

    [50, 200],

    [150, 200],

    [100, 300]

]


# Animation variables

tx = 0

ty = 0

direction = 1 # 1 for right, -1 for left


def draw_triangle(vertices):

    glBegin(GL_TRIANGLES)

    for vertex in vertices:

        glVertex2f(vertex[0], vertex[1])

    glEnd()
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
def translate_shape(vertices, tx, ty):  
  
    translated = []  
  
    for vertex in vertices:  
  
        translated.append([vertex[0] + tx, vertex[1] + ty])  
  
    return translated  
  
def iterate():  
  
    glViewport(0, 0, 500, 500)  
  
    glMatrixMode(GL_PROJECTION)  
  
    glLoadIdentity()  
  
    glOrtho(0.0, 500, 0.0, 500, 0.0, 10.0)  
  
    glMatrixMode(GL_MODELVIEW)  
  
    glLoadIdentity()  
  
def animate(value):  
  
    global tx, ty, direction  
  
    # Move the triangle  
  
    tx += direction * 2  
  
    ty += direction * 2  
  
    # Reverse direction at boundaries  
  
    if tx > 300 or tx < 0:  
  
        direction *= -1  
  
    if ty > 300 or ty < 0:
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
        direction *= -1

    glutPostRedisplay()

    glutTimerFunc(16, animate, 3)  # ~60 FPS

def showScreen():

    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT)

    glLoadIdentity()

    iterate()

    glColor3f(0.0, 1.0, 1.0)

    translated_triangle = translate_shape(triangle_vertices, tx, ty)

    draw_triangle(translated_triangle)

    glutSwapBuffers()

glutInit()

glutInitDisplayMode(GLUT_RGBA | GLUT_DOUBLE)

glutInitWindowSize(500, 500)

glutInitWindowPosition(0, 0)

wind = glutCreateWindow(b"Animated Translation")

glutDisplayFunc(showScreen)

glutTimerFunc(0, animate, 0)

glutMainLoop()
```

## Part 2: Rotation (Spinning Objects)

### Theory

Rotation rotates an object around a pivot point by an angle  $\theta$  (theta).

- New X =  $(X - X_c) * \cos(\theta) - (Y - Y_c) * \sin(\theta) + X_c$
- New Y =  $(X - X_c) * \sin(\theta) + (Y - Y_c) * \cos(\theta) + Y_c$

Where  $(X_c, Y_c)$  is the center of rotation.

### Example 2.1: Rotating a Triangle by 45 Degrees

```
from OpenGL.GL import *
from OpenGL.GLUT import *
from OpenGL.GLU import *
import math

triangle_vertices = [
    [250, 200],
    [300, 200],
    [275, 250]
]

def draw_triangle(vertices):
    glBegin(GL_TRIANGLES)
    for vertex in vertices:
        glVertex2f(vertex[0], vertex[1])
    glEnd()

def rotate_point(x, y, cx, cy, angle_deg):
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
# Convert angle to radians

angle_rad = math.radians(angle_deg)


# Translate point to origin

temp_x = x - cx

temp_y = y - cy


# Apply rotation

rotated_x = temp_x * math.cos(angle_rad) - temp_y *
math.sin(angle_rad)

rotated_y = temp_x * math.sin(angle_rad) + temp_y *
math.cos(angle_rad)


# Translate back

new_x = rotated_x + cx

new_y = rotated_y + cy


return [new_x, new_y]


def rotate_shape(vertices, cx, cy, angle):

    rotated = []

    for vertex in vertices:

        new_point = rotate_point(vertex[0], vertex[1], cx, cy, angle)

        rotated.append(new_point)

    return rotated


def calculate_center(vertices):
```



## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
cx = sum(v[0] for v in vertices) / len(vertices)

cy = sum(v[1] for v in vertices) / len(vertices)

return cx, cy


def iterate():

    glViewport(0, 0, 500, 500)

    glMatrixMode(GL_PROJECTION)

    glLoadIdentity()

    glOrtho(0.0, 500, 0.0, 500, 0.0, 1.0)

    glMatrixMode(GL_MODELVIEW)

    glLoadIdentity()


def showScreen():

    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT)

    glLoadIdentity()

    iterate()

    # Calculate center of triangle

    cx, cy = calculate_center(triangle_vertices)

    cx = cy = 0 # Rotate around origin (0,0)

    # Draw original triangle in yellow

    glColor3f(1.0, 1.0, 0.0)

    draw_triangle(triangle_vertices)

    # Rotate by 45 degrees and draw in red

    glColor3f(1.0, 0.0, 0.0)
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
rotated_triangle = rotate_shape(triangle_vertices, cx, cy, 45)

draw_triangle(rotated_triangle)

glutSwapBuffers()

glutInit()
glutInitDisplayMode(GLUT_RGBA)
glutInitWindowSize(500, 500)
glutInitWindowPosition(0, 0)
wind = glutCreateWindow(b"Rotation Example")
glutDisplayFunc(showScreen)
glutMainLoop()
```

### Example 2.2: Continuously Rotating Triangle

```
from OpenGL.GL import *
from OpenGL.GLUT import *
from OpenGL.GLU import *
import math

triangle_vertices = [
    [250, 200],
    [300, 200],
    [275, 250]
]
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
# Animation variable

angle = 0

def draw_triangle(vertices):

    glBegin(GL_TRIANGLES)

    for vertex in vertices:

        glVertex2f(vertex[0], vertex[1])

    glEnd()

def rotate_point(x, y, cx, cy, angle_deg):

    angle_rad = math.radians(angle_deg)

    temp_x = x - cx

    temp_y = y - cy

    rotated_x = temp_x * math.cos(angle_rad) - temp_y *
math.sin(angle_rad)

    rotated_y = temp_x * math.sin(angle_rad) + temp_y *
math.cos(angle_rad)

    return [rotated_x + cx, rotated_y + cy]

def rotate_shape(vertices, cx, cy, angle):

    rotated = []

    for vertex in vertices:

        new_point = rotate_point(vertex[0], vertex[1], cx, cy, angle)

        rotated.append(new_point)

    return rotated

def calculate_center(vertices):
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
cx = sum(v[0] for v in vertices) / len(vertices)

cy = sum(v[1] for v in vertices) / len(vertices)

return cx, cy


def iterate():

    glViewport(0, 0, 500, 500)

    glMatrixMode(GL_PROJECTION)

    glLoadIdentity()

    glOrtho(0.0, 500, 0.0, 500, 0.0, 1.0)

    glMatrixMode(GL_MODELVIEW)

    glLoadIdentity()


def animate(value):

    global angle

    angle = (angle - 5) % 360 # Increment angle and wrap at 360

    glutPostRedisplay()

    glutTimerFunc(16, animate, 0)


def showScreen():

    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT)

    glLoadIdentity()

    iterate()

    cx, cy = calculate_center(triangle_vertices)

    cx = cy = 0

    glColor3f(0.0, 1.0, 0.0)
```

```
rotated_triangle = rotate_shape(triangle_vertices, cx, cy, angle)

draw_triangle(rotated_triangle)

glutSwapBuffers()

glutInit()
glutInitDisplayMode(GLUT_RGBA | GLUT_DOUBLE)
glutInitWindowSize(500, 500)
glutInitWindowPosition(0, 0)
wind = glutCreateWindow(b"Continuous Rotation")
glutDisplayFunc(showScreen)
glutTimerFunc(0, animate, 0)
glutMainLoop()
```

## Part 3: Scaling (Resizing Objects)

### Theory

Scaling changes the size of an object relative to a fixed point.

- New X = (X - Xc) \* Sx + Xc
- New Y = (Y - Yc) \* Sy + Yc

Where Sx and Sy are scaling factors (1.0 = no change, >1 = enlarge, <1 = shrink).

### Example 3.1: Scaling a Rectangle

```
from OpenGL.GL import *

from OpenGL.GLUT import *

from OpenGL.GLU import *
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
rectangle_vertices = [  
    [200, 200],  
    [300, 200],  
    [300, 300],  
    [200, 300]  
]  
  
def draw_rectangle(vertices):  
    glBegin(GL_QUADS)  
    for vertex in vertices:  
        glVertex2f(vertex[0], vertex[1])  
    glEnd()  
  
def scale_point(x, y, cx, cy, sx, sy):  
    # Translate to origin  
    temp_x = x - cx  
    temp_y = y - cy  
  
    # Apply scaling  
    scaled_x = temp_x * sx  
    scaled_y = temp_y * sy  
  
    # Translate back  
    new_x = scaled_x + cx  
    new_y = scaled_y + cy
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
    return [new_x, new_y]

def scale_shape(vertices, cx, cy, sx, sy):
    scaled = []

    for vertex in vertices:
        new_point = scale_point(vertex[0], vertex[1], cx, cy, sx, sy)
        scaled.append(new_point)

    return scaled

def calculate_center(vertices):
    cx = sum(v[0] for v in vertices) / len(vertices)
    cy = sum(v[1] for v in vertices) / len(vertices)
    return cx, cy

def iterate():
    glViewport(0, 0, 500, 500)

    glMatrixMode(GL_PROJECTION)

    glLoadIdentity()

    glOrtho(0.0, 500, 0.0, 500, 0.0, 1.0)

    glMatrixMode(GL_MODELVIEW)

    glLoadIdentity()

def showScreen():
    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT)

    glLoadIdentity()
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
iterate()

cx, cy = calculate_center(rectangle_vertices)

# Original rectangle in yellow
glColor3f(1.0, 1.0, 0.0)
draw_rectangle(rectangle_vertices)

# Scaled up (1.5x) in green
glColor3f(0.0, 1.0, 0.0)
scaled_up = scale_shape(rectangle_vertices, cx, cy, 1.5, 1.5)
draw_rectangle(scaled_up)

# Scaled down (0.5x) in red
glColor3f(1.0, 0.0, 0.0)
scaled_down = scale_shape(rectangle_vertices, cx, cy, 0.5, 0.5)
draw_rectangle(scaled_down)

glutSwapBuffers()

glutInit()
glutInitDisplayMode(GLUT_RGBA)
glutInitWindowSize(500, 500)
glutInitWindowPosition(0, 0)
wind = glutCreateWindow(b"Scaling Example")
glutDisplayFunc(showScreen)
```



```
glutMainLoop()
```

### Example 3.2: Pulsating (Breathing) Animation

```
from OpenGL.GL import *
from OpenGL.GLUT import *
from OpenGL.GLU import *
import math

rectangle_vertices = [
    [200, 200],
    [300, 200],
    [300, 300],
    [200, 300]
]

# Animation variables
scale_factor = 1.0
scale_direction = 1

def draw_rectangle(vertices):
    glBegin(GL_QUADS)
    for vertex in vertices:
        glVertex2f(vertex[0], vertex[1])
    glEnd()
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
def scale_point(x, y, cx, cy, sx, sy):  
    temp_x = x - cx  
    temp_y = y - cy  
    scaled_x = temp_x * sx  
    scaled_y = temp_y * sy  
    return [scaled_x + cx, scaled_y + cy]  
  
def scale_shape(vertices, cx, cy, sx, sy):  
    scaled = []  
    for vertex in vertices:  
        new_point = scale_point(vertex[0], vertex[1], cx, cy, sx, sy)  
        scaled.append(new_point)  
    return scaled  
  
def calculate_center(vertices):  
    cx = sum(v[0] for v in vertices) / len(vertices)  
    cy = sum(v[1] for v in vertices) / len(vertices)  
    return cx, cy  
  
def iterate():  
    glViewport(0, 0, 500, 500)  
    glMatrixMode(GL_PROJECTION)  
    glLoadIdentity()  
    glOrtho(0.0, 500, 0.0, 500, 0.0, 1.0)  
    glMatrixMode(GL_MODELVIEW)
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
glLoadIdentity()

def animate(value):

    global scale_factor, scale_direction

    scale_factor += scale_direction * (0.01)

    # Reverse direction at boundaries
    if scale_factor > 1.5 or scale_factor < 0.5:
        scale_direction *= -1

    glutPostRedisplay()

    glutTimerFunc(16, animate, 0)

def showScreen():

    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT)

    glLoadIdentity()

    iterate()

    cx, cy = calculate_center(rectangle_vertices)

    glColor3f(1.0, 0.0, 1.0)

    scaled_rect = scale_shape(rectangle_vertices, cx, cy, scale_factor,
scale_factor)

    draw_rectangle(scaled_rect)

    glutSwapBuffers()
```

```
glutInit()  
  
glutInitDisplayMode(GLUT_RGBA | GLUT_DOUBLE)  
  
glutInitWindowSize(500, 500)  
  
glutInitWindowPosition(0, 0)  
  
wind = glutCreateWindow(b"Pulsating Animation")  
  
glutDisplayFunc(showScreen)  
  
glutTimerFunc(0, animate, 0)  
  
glutMainLoop()
```

## Part 4: Combined Transformations

### Example 4.1: Rotating and Translating Circle

```
from OpenGL.GL import *  
  
from OpenGL.GLUT import *  
  
from OpenGL.GLU import *  
  
import math  
  
# Animation variables  
  
angle = 0  
  
orbit_angle = 0  
  
def draw_point(x, y):  
    glPointSize(2)  
  
    glBegin(GL_POINTS)  
  
    glVertex2f(x, y)  
  
    glEnd()
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
def draw_circle_points(x, y, cx, cy):  
    draw_point(x + cx, y + cy)  
    draw_point(y + cx, x + cy)  
    draw_point(y + cx, -x + cy)  
    draw_point(x + cx, -y + cy)  
    draw_point(-x + cx, -y + cy)  
    draw_point(-y + cx, -x + cy)  
    draw_point(-y + cx, x + cy)  
    draw_point(-x + cx, y + cy)  
  
def draw_circle(radius, cx, cy):  
    d = 1 - radius  
    x = 0  
    y = radius  
  
    draw_circle_points(x, y, cx, cy)  
  
    while x < y:  
        if d < 0:  
            d = d + 2 * x + 3  
        else:  
            d = d + 2 * x - 2 * y + 5  
            y -= 1  
        x += 1  
        draw_circle_points(x, y, cx, cy)
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
def rotate_point(x, y, cx, cy, angle_deg):  
    angle_rad = math.radians(angle_deg)  
    temp_x = x - cx  
    temp_y = y - cy  
    rotated_x = temp_x * math.cos(angle_rad) - temp_y *  
math.sin(angle_rad)  
    rotated_y = temp_x * math.sin(angle_rad) + temp_y *  
math.cos(angle_rad)  
    return rotated_x + cx, rotated_y + cy  
  
def iterate():  
    glViewport(0, 0, 500, 500)  
    glMatrixMode(GL_PROJECTION)  
    glLoadIdentity()  
    glOrtho(0.0, 500, 0.0, 500, 0.0, 1.0)  
    glMatrixMode(GL_MODELVIEW)  
    glLoadIdentity()  
  
def animate(value):  
    global orbit_angle  
    orbit_angle = (orbit_angle - 2) % 360  
    glutPostRedisplay()  
    glutTimerFunc(16, animate, 0)  
  
def showScreen():  
    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT)
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
glLoadIdentity()

iterate()

# Center of screen

center_x, center_y = 250, 250

orbit_radius = 100

# Draw center circle (sun)

glColor3f(1.0, 1.0, 0.0)

draw_circle(30, center_x, center_y)

# Calculate orbiting position

orbit_x = center_x + orbit_radius

orbit_y = center_y

new_x, new_y = rotate_point(orbit_x, orbit_y, center_x, center_y,
orbit_angle)

# Draw orbiting circle (planet)

glColor3f(0.0, 0.5, 1.0)

draw_circle(15, int(new_x), int(new_y))

glutSwapBuffers()

glutInit()

glutInitDisplayMode(GLUT_RGBA | GLUT_DOUBLE)

glutInitWindowSize(500, 500)

glutInitWindowPosition(0, 0)
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
wind = glutCreateWindow(b"Orbit Animation")

glutDisplayFunc(showScreen)

glutTimerFunc(0, animate, 0)

glutMainLoop()
```

#### Example 4.2: Complex Animation - Rotating Triangle with Scaling

```
from OpenGL.GL import *

from OpenGL.GLUT import *

from OpenGL.GLU import *

import math


triangle_vertices = [

    [250, 200],

    [300, 200],

    [275, 260]

]


# Animation variables

angle = 0

scale = 1.0

scale_direction = 1


def draw_triangle(vertices):

    glBegin(GL_TRIANGLES)

    for vertex in vertices:
```



## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
    glVertex2f(vertex[0], vertex[1])

    glEnd()

def rotate_point(x, y, cx, cy, angle_deg):
    angle_rad = math.radians(angle_deg)

    temp_x = x - cx
    temp_y = y - cy

    rotated_x = temp_x * math.cos(angle_rad) - temp_y *
math.sin(angle_rad)

    rotated_y = temp_x * math.sin(angle_rad) + temp_y *
math.cos(angle_rad)

    return [rotated_x + cx, rotated_y + cy]

def scale_point(x, y, cx, cy, s):
    temp_x = x - cx
    temp_y = y - cy

    return [temp_x * s + cx, temp_y * s + cy]

def transform_shape(vertices, cx, cy, angle, scale_factor):
    transformed = []

    for vertex in vertices:
        # First rotate
        rotated = rotate_point(vertex[0], vertex[1], cx, cy, angle)

        # Then scale
        scaled = scale_point(rotated[0], rotated[1], cx, cy, scale_factor)

        transformed.append(scaled)

    return transformed
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
def calculate_center(vertices):  
    cx = sum(v[0] for v in vertices) / len(vertices)  
    cy = sum(v[1] for v in vertices) / len(vertices)  
    return cx, cy  
  
def iterate():  
    glViewport(0, 0, 500, 500)  
    glMatrixMode(GL_PROJECTION)  
    glLoadIdentity()  
    glOrtho(0.0, 500, 0.0, 500, 0.0, 1.0)  
    glMatrixMode(GL_MODELVIEW)  
    glLoadIdentity()  
  
def animate(value):  
    global angle, scale, scale_direction  
  
    angle = (angle + 3) % 360  
    scale += scale_direction * 0.01  
  
    if scale > 1.5 or scale < 0.7:  
        scale_direction *= -1  
  
    glutPostRedisplay()  
    glutTimerFunc(16, animate, 0)
```

## Department of Computer Science and Engineering

### CSE 422: Computer Graphics Lab

```
def showScreen():

    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT)

    glLoadIdentity()

    iterate()

    cx, cy = calculate_center(triangle_vertices)

    glColor3f(1.0, 0.5, 0.0)

    transformed = transform_shape(triangle_vertices, cx, cy, angle, scale)

    draw_triangle(transformed)

    glutSwapBuffers()

glutInit()

glutInitDisplayMode(GLUT_RGBA | GLUT_DOUBLE)

glutInitWindowSize(500, 500)

glutInitWindowPosition(0, 0)

wind = glutCreateWindow(b"Combined Transformations")

glutDisplayFunc(showScreen)

glutTimerFunc(0, animate, 0)

glutMainLoop()
```

## Practice Exercises

### Exercise 1: Bouncing Ball

## **Department of Computer Science and Engineering**

### **CSE 422: Computer Graphics Lab**

**Create a circle that bounces around the screen, reversing direction when it hits the edges.**

#### **Exercise 2: Spinning Square**

**Create a square that continuously rotates around its center while also moving in a circular path around the screen center.**

#### **Exercise 3: Growing and Shrinking Star**

**Draw a star (using triangles) that grows and shrinks while rotating.**

#### **Exercise 4: Multiple Objects**

**Create 3 triangles that rotate at different speeds around different centers.**