

$$w - x - y + 2z = 1$$

$$y - z = 1$$

$w, y$ ; leading variables  
 $x, z$ ; free variables

$$y = z + 1$$

$$w = 1 + x + y - 2z$$

$$= 2 + x - z$$

$$\begin{bmatrix} w \\ x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 2 + x - z \\ x \\ z + 1 \\ z \end{bmatrix}$$

$$= \begin{bmatrix} 2 \\ 0 \\ 1 \\ 0 \end{bmatrix} + x \begin{bmatrix} 1 \\ 1 \\ 0 \\ 0 \end{bmatrix} + \begin{bmatrix} -1 \\ 0 \\ 1 \\ 1 \end{bmatrix}$$

Def. The rank of a matrix  
 is # of nonzero rows in