

$$(d) \begin{bmatrix} 1 \\ 2 \\ 0 \end{bmatrix}, \begin{bmatrix} 1 \\ 1 \\ -1 \end{bmatrix}, \begin{bmatrix} 1 \\ 4 \\ 2 \end{bmatrix}$$

$$C_1 \begin{bmatrix} 1 \\ 2 \\ 0 \end{bmatrix} + C_2 \begin{bmatrix} 1 \\ 1 \\ -1 \end{bmatrix} + C_3 \begin{bmatrix} 1 \\ 4 \\ 2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 \\ 2 & 1 & 4 \\ 0 & -1 & 2 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

$$\rightarrow \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & -1 & 2 & 0 \\ 0 & -1 & 2 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & -1 & 2 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\rightarrow C_2 = 2C_3, C_1 = -C_2 - C_3 = -3C_3$$

\rightarrow lin dep.

Thm. v_1, \dots, v_m are linearly dep.

iff $[A|b]$ has a nontrivial

solution, $A = [v_1 | v_2 | \dots | v_m]$. ⁴¹