Numerical Analysis Lab2 2020032306 송민경

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|--------|-----------|-----------|-----------|-----------|----------|----------|
| | k1 | k2 | k3 | k4 | w0 | w1 |
| h=0.05 | -0.050000 | -0.047531 | -0.047652 | -0.045348 | 1.000000 | 0.952381 |
| 0.10 | -0.045351 | -0.043218 | -0.043317 | -0.041320 | 0.952381 | 0.909091 |
| 0.15 | -0.041322 | -0.039465 | -0.039548 | -0.037805 | 0.909091 | 0.869565 |
| 0.20 | -0.037807 | -0.036181 | -0.036250 | -0.034721 | 0.869565 | 0.833333 |
| 0.25 | -0.034722 | -0.033291 | -0.033349 | -0.031999 | 0.833333 | 0.800000 |
| 0.30 | -0.032000 | -0.030733 | -0.030782 | -0.029585 | 0.800000 | 0.769231 |
| 0.35 | -0.029586 | -0.028459 | -0.028501 | -0.027434 | 0.769231 | 0.740741 |
| 0.40 | -0.027435 | -0.026428 | -0.026465 | -0.025510 | 0.740741 | 0.714286 |
| 0.45 | -0.025510 | -0.024607 | -0.024639 | -0.023781 | 0.714286 | 0.689655 |
| 0.50 | -0.023781 | -0.022968 | -0.022996 | -0.022222 | 0.689655 | 0.666667 |
| 0.55 | -0.022222 | -0.021488 | -0.021512 | -0.020811 | 0.666667 | 0.645161 |
| 0.60 | -0.020812 | -0.020146 | -0.020167 | -0.019531 | 0.645161 | 0.625000 |
| 0.65 | -0.019531 | -0.018926 | -0.018944 | -0.018365 | 0.625000 | 0.606061 |
| 0.70 | -0.018365 | -0.017813 | -0.017830 | -0.017301 | 0.606061 | 0.588235 |
| 0.75 | -0.017301 | -0.016796 | -0.016811 | -0.016326 | 0.588235 | 0.571429 |
| 0.80 | -0.016327 | -0.015863 | -0.015876 | -0.015432 | 0.571429 | 0.555556 |
| 0.85 | -0.015432 | -0.015006 | -0.015018 | -0.014609 | 0.555556 | 0.540541 |
| 0.90 | -0.014609 | -0.014217 | -0.014227 | -0.013850 | 0.540541 | 0.526316 |
| 0.95 | -0.013850 | -0.013488 | -0.013498 | -0.013149 | 0.526316 | 0.512821 |
| 1.00 | -0.013149 | -0.012814 | -0.012823 | -0.012500 | 0.512821 | 0.500000 |
| 1.05 | -0.012500 | -0.012189 | -0.012197 | -0.011898 | 0.500000 | 0.487805 |
| 1.10 | -0.011898 | -0.011609 | -0.011616 | -0.011338 | 0.487805 | 0.476190 |
| 1.15 | -0.011338 | -0.011070 | -0.011076 | -0.010817 | 0.476190 | 0.465116 |
| 1.20 | -0.010817 | -0.010567 | -0.010572 | -0.010331 | 0.465116 | 0.454545 |
| 1.25 | -0.010331 | -0.010097 | -0.010102 | -0.009876 | 0.454545 | 0.44444 |
| 1.30 | -0.009877 | -0.009658 | -0.009663 | -0.009452 | 0.44444 | 0.434783 |
| 1.35 | -0.009452 | -0.009247 | -0.009252 | -0.009054 | 0.434783 | 0.425532 |
| 1.40 | -0.009054 | -0.008862 | -0.008866 | -0.008681 | 0.425532 | 0.416667 |
| 1.45 | -0.008681 | -0.008501 | -0.008504 | -0.008330 | 0.416667 | 0.408163 |
| 1.50 | -0.008330 | -0.008161 | -0.008164 | -0.008000 | 0.408163 | 0.400000 |
| 1.55 | -0.008000 | -0.007841 | -0.007844 | -0.007689 | 0.400000 | 0.392157 |
| 1.60 | -0.007689 | -0.007539 | -0.007542 | -0.007396 | 0.392157 | 0.384615 |
| 1.65 | -0.007396 | -0.007255 | -0.007258 | -0.007120 | 0.384615 | 0.377359 |
| 1.70 | -0.007120 | -0.006986 | -0.006989 | -0.006859 | 0.377359 | 0.370370 |
| 1.75 | -0.006859 | -0.006732 | -0.006735 | -0.006612 | 0.370370 | 0.363636 |
| 1.80 | -0.006612 | -0.006492 | -0.006494 | -0.006378 | 0.363636 | 0.357143 |
| 1.85 | -0.006378 | -0.006264 | -0.006266 | -0.006156 | 0.357143 | 0.350877 |
| 1.90 | -0.006156 | -0.006048 | -0.006050 | -0.005945 | 0.350877 | 0.344828 |
| 1.95 | -0.005945 | -0.005843 | -0.005845 | -0.005745 | 0.344828 | 0.338983 |
| 2.00 | -0.005745 | -0.005649 | -0.005650 | -0.005556 | 0.338983 | 0.333333 |

| | k1 | k2 | k3 | k4 | w0 | w1 |
|-------|-----------|-----------|-----------|-----------|----------|----------|
| h=0.1 | -0.100000 | -0.090250 | -0.091179 | -0.082596 | 1.000000 | 0.909091 |
| 0.2 | -0.082645 | -0.075302 | -0.075941 | -0.069414 | 0.909091 | 0.833334 |
| 0.3 | -0.069445 | -0.063778 | -0.064231 | -0.059152 | 0.833334 | 0.769231 |
| 0.4 | -0.059172 | -0.054708 | -0.055038 | -0.051007 | 0.769231 | 0.714286 |
| 0.5 | -0.051020 | -0.047441 | -0.047688 | -0.044435 | 0.714286 | 0.666667 |
| 0.6 | -0.044445 | -0.041531 | -0.041719 | -0.039056 | 0.666667 | 0.625000 |
| 0.7 | -0.039063 | -0.036659 | -0.036805 | -0.034597 | 0.625000 | 0.588236 |
| 0.8 | -0.034602 | -0.032597 | -0.032711 | -0.030861 | 0.588236 | 0.55556 |
| 0.9 | -0.030864 | -0.029173 | -0.029265 | -0.027698 | 0.555556 | 0.526316 |
| 1.0 | -0.027701 | -0.026262 | -0.026336 | -0.024998 | 0.526316 | 0.500000 |
| 1.1 | -0.025000 | -0.023766 | -0.023826 | -0.022674 | 0.500000 | 0.476191 |
| 1.2 | -0.022676 | -0.021609 | -0.021658 | -0.020660 | 0.476191 | 0.454546 |
| 1.3 | -0.020661 | -0.019733 | -0.019774 | -0.018903 | 0.454546 | 0.434783 |
| 1.4 | -0.018904 | -0.018091 | -0.018125 | -0.017360 | 0.434783 | 0.416667 |
| 1.5 | -0.017361 | -0.016645 | -0.016675 | -0.015999 | 0.416667 | 0.400000 |
| 1.6 | -0.016000 | -0.015366 | -0.015391 | -0.014792 | 0.400000 | 0.384616 |
| 1.7 | -0.014793 | -0.014229 | -0.014251 | -0.013717 | 0.384616 | 0.370371 |
| 1.8 | -0.013717 | -0.013214 | -0.013232 | -0.012755 | 0.370371 | 0.357143 |
| 1.9 | -0.012755 | -0.012304 | -0.012319 | -0.011890 | 0.357143 | 0.344828 |
| 2.0 | -0.011891 | -0.011484 | -0.011498 | -0.011111 | 0.344828 | 0.333333 |

```
3. 2)
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```
implicit real*8(a-h, o-z)
dimension A(1024, 1024), p(1024), q(1024), xnew(1024), &
x(1024), r(1024), b(1024)
nx = 32
N = nx**2
tol = 1.e-8
data x/1024*0./
do i = 1, N
 if(i > 1) a(i, i-1) = -1.
  if(i < N) a(i, i+1) = -1
  if(i+nx <= N) a(i, i+nx) = -1.
  if(i-nx >= 1) a(i, i-nx) = -1
  a(i, i) = 4.5
  b(i) = cos(i+0.5)
enddo
p = b
r = b
call matvec(A, p, q, N)
rho = dot_product(r, r)
alpha = rho/dot_product(p, q)
x = x + alpha*p
r = r - alpha*q
r0 = sqrt(dot_product(b, b))
do k = 2, N/2
  rho0 = rho
  rho = dot_product(r, r)
  beta = rho/rho0
  p = r + beta*p
  call matvec(A, p, q, N)
  alpha = rho/dot_product(p, q)
  x = x + alpha*p
  r = r - alpha*q
  rn = dot_product(r, r)
  error = sqrt(rn/r0)
  write(*, *) k, rn, error
  if(error < tol) goto 300
```

```
enddo
```

```
300
       continue
               write(*, *) x(1), x(2), x(N-1), x(N)
       stop
       end
       subroutine matvec(A, x, y, N)
               implicit real*8(a-h, o-z)
       dimension A(N, *), x(*), y(*)
       do i = 1, N
         y(i) = 0.
         do j = 1, N
           y(i) = y(i) + A(i,j)*x(j)
         enddo
       enddo
       return
       end
```

2) Result

```
2
    1.1053738703419571
                             0.22102010406394906
3 0.20735558830425369
                              9.5727133434201736E-002
4
    4.0205486219384683E-002
                               4.2152160698108745E-002
5
    7.0286519478240236E-003
                               1.7624353738663112E-002
    1.6514979648255660E-003
                               8.5431140338101241E-003
6
7
    4.7989218687286548E-004
                               4.6052055733052160E-003
    2.0105159398927039E-004
                               2.9807869917960203E-003
8
9
    8.4142613174156654E-005
                               1.9283469698418154E-003
    2.9226574826844186E-005
                               1.1364913715302461E-003
10
11
    9.7040309593116191E-006
                               6.5486724520995028E-004
12
    3.2951260591238805E-006
                               3.8160424643428499E-004
    1.2565972789934757E-006
                               2.3565422982806513E-004
13
14
    4.9351597716764323E-007
                               1.4768207662557738E-004
    1.8778727473666905E-007
                               9.1098297691911474E-005
15
    6.5863369987792446E-008
16
                               5.3950957412099724E-005
17
    2.2076002328949685E-008
                               3.1234704209806312E-005
    8.4002558802844624E-009
                               1.9267414462583300E-005
18
```

```
19
            3.4305415880409289E-009
                                      1.2312848228088327E-005
        20
            1.2785822506232976E-009
                                      7.5169475091354332E-006
        21
            4.2256705716697056E-010
                                      4.3214053019595904E-006
            1.4643652258256721E-010
                                      2.5439108378385822E-006
        22
                                      1.5977413820448304E-006
        23
            5.7764178786059956E-011
            2.1806329022986759E-011
                                      9.8167665273431707E-007
        24
        25
            7.3443561717848126E-012
                                      5.6971026823776056E-007
        26
            2.6074130933283237E-012
                                      3.3945491635577335E-007
            1.1434607098317016E-012
                                      2.2479559939505651E-007
        27
        28
            4.1290627101836978E-013
                                      1.3508369182379652E-007
                                      8.1618402658318863E-008
        29
            1.5073767698714791E-013
        30
            5.4973169414503298E-014
                                      4.9289290894695457E-008
            2.0806826384968993E-014
                                      3.0323554227208665E-008
        31
                                      1.8815048591246413E-008
        32
            8.0104391290513366E-015
            2.9018311987735669E-015
                                      1.1324349249608845E-008
        33
           1.1201706858552616E-015
                                     7.0358939299116064E-009
        34
-0.16227354189609317 -0.42303156759582916
                                                   0.25294043995108778
0.37603840772234071
```

 \Rightarrow x(1) = -0.16227354189609317, x(1024) = 0.37603840772234071