# Handling Missing Data with Graph Representation Learning

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## The Missing Data Problem

#### **Issues with Learning**

In computational biology, clinical studies, survey research, finance, and economics.

### Two approaches

### **Feature Imputation**

Missing feature values are estimated based on observed values

#### **Label Prediction**

Downstream labels are learned directly from incomplete data

# Existing Works for Missing Data Problem

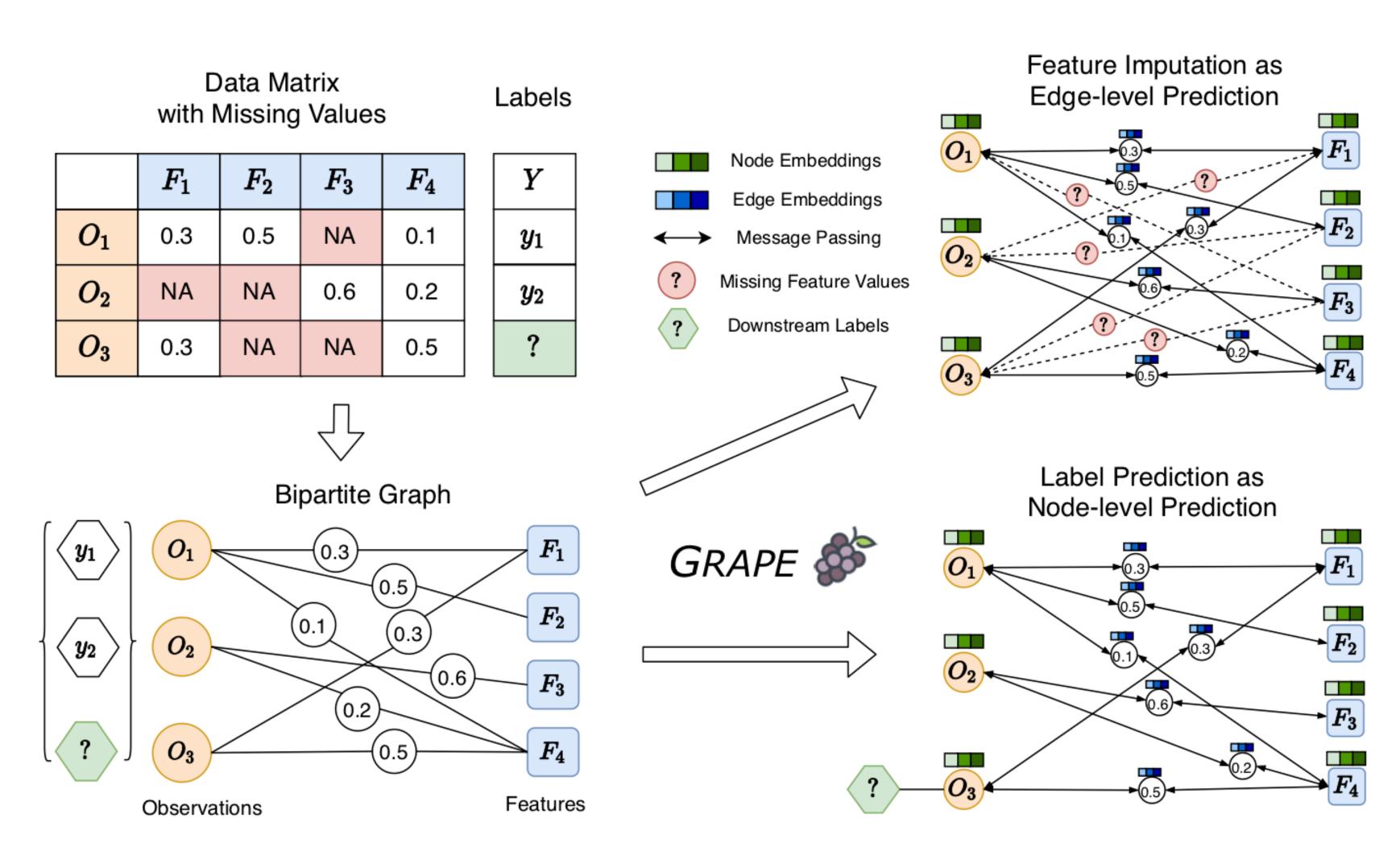
#### **Statistical Methods**

- Strong assumptions about data distributions
- Lack flexibility for handling mixed datatypes
- Fail to generalize to unseen data without retraining

#### **Deep Networks**

- Fail to make full use of feature values
- Biased assumptions about data by special value initialization

### The GRAPE Framework



### The GRAPE Framework: GNN

#### Algorithm 1 Grape forward computation

Input: Graph  $\mathcal{G} = (\mathcal{V}; \mathcal{E})$ ; Number of layers L; Edge dropout rate  $r_{drop}$ ; Weight matrices  $\mathbf{P}^{(l)}$  for message passing,  $\mathbf{Q}^{(l)}$  for node updating, and  $\mathbf{W}^{(l)}$  for edge updating; non-linearity  $\sigma$ ; aggregation functions AGG<sub>l</sub>; neighborhood function  $\mathcal{N}: v \times \mathcal{E} \to 2^{\mathcal{V}}$ 

Output: Node embeddings  $\mathbf{h}_v$  corresponding to each  $v \in \mathcal{V}$ 

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1: \mathbf{h}_v^{(0)} \leftarrow \mathbf{I}_{NIT}(v), \forall v \in \mathcal{V} Augmented node features \rightarrow better representation power
2: \mathbf{e}_{uv}^{(0)} \leftarrow \mathbf{e}_{uv}, \forall \mathbf{e}_{uv} \in \mathcal{E}
3: \mathcal{E}_{drop} \leftarrow \text{DROPEDGE}(\mathcal{E}, r_{drop}) Edge dropout \rightarrow improved model generalization
4: for l \in \{1, \dots, L\}
5: for v \in \mathcal{V}
6: \mathbf{n}_v^{(l)} = \mathrm{AGG}_l \Big( \sigma(\mathbf{P}^{(l)} \cdot \mathrm{CONCAT}(\mathbf{h}_v^{(l-1)}, \mathbf{e}_{uv}^{(l-1)}) \mid \forall u \in \mathcal{N}(v, \mathcal{E}_{drop})) \Big)
7: \mathbf{h}_v^{(l)} = \sigma(\mathbf{Q}^{(l)} \cdot \mathbf{CONCAT}(\mathbf{h}_v^{(l-1)}, \mathbf{n}_v^{(l)}))
8: for (u, v) \in \mathcal{E}_{drop}
           \mathbf{e}_{uv}^{(l)} = \sigma(\mathbf{W}^{(l)} \cdot \text{Concat}(\mathbf{e}_{uv}^{(l-1)}, \mathbf{h}_{u}^{(l)}, \mathbf{h}_{v}^{(l)}))
                                                                                                         Edge embedding -> utilize edge features
```

### The GRAPE Framework: GNN

Edge-level predictions at L-th layer

$$\hat{\mathbf{D}}_{uv} = \mathbf{O}_{edge} \left( \text{CONCAT}(\mathbf{h}_{u}^{(L)}, \mathbf{h}_{v}^{(L)}) \right)$$

Node-level predictions at L-th layer, using imputed dataset

$$\hat{\mathbf{Y}}_{u} = \mathbf{O}_{node} \left( \hat{\mathbf{D}}_{u} \right)$$

 $\mathbf{O}_{edge}$  and  $\mathbf{O}_{node}$  are feedforward neural networks

### The GRAPE Framework

#### Important features of this framework:

1. Connections between different features and between different observations

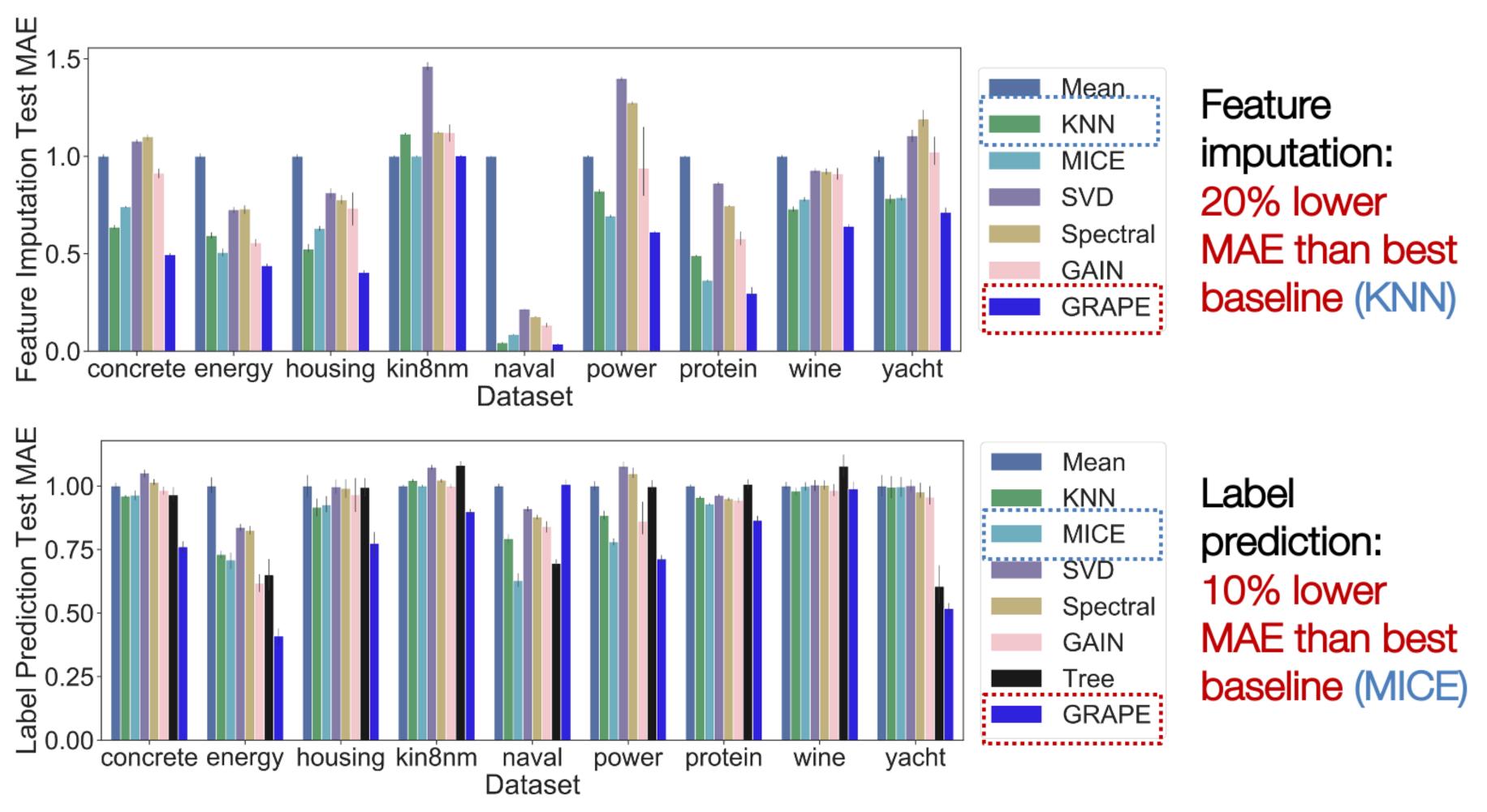
2. Propagate and borrow information from other features/observations in graph localized way

3. End-to-end feature imputation and label prediction, leads to strong performance improvement

### Datasets

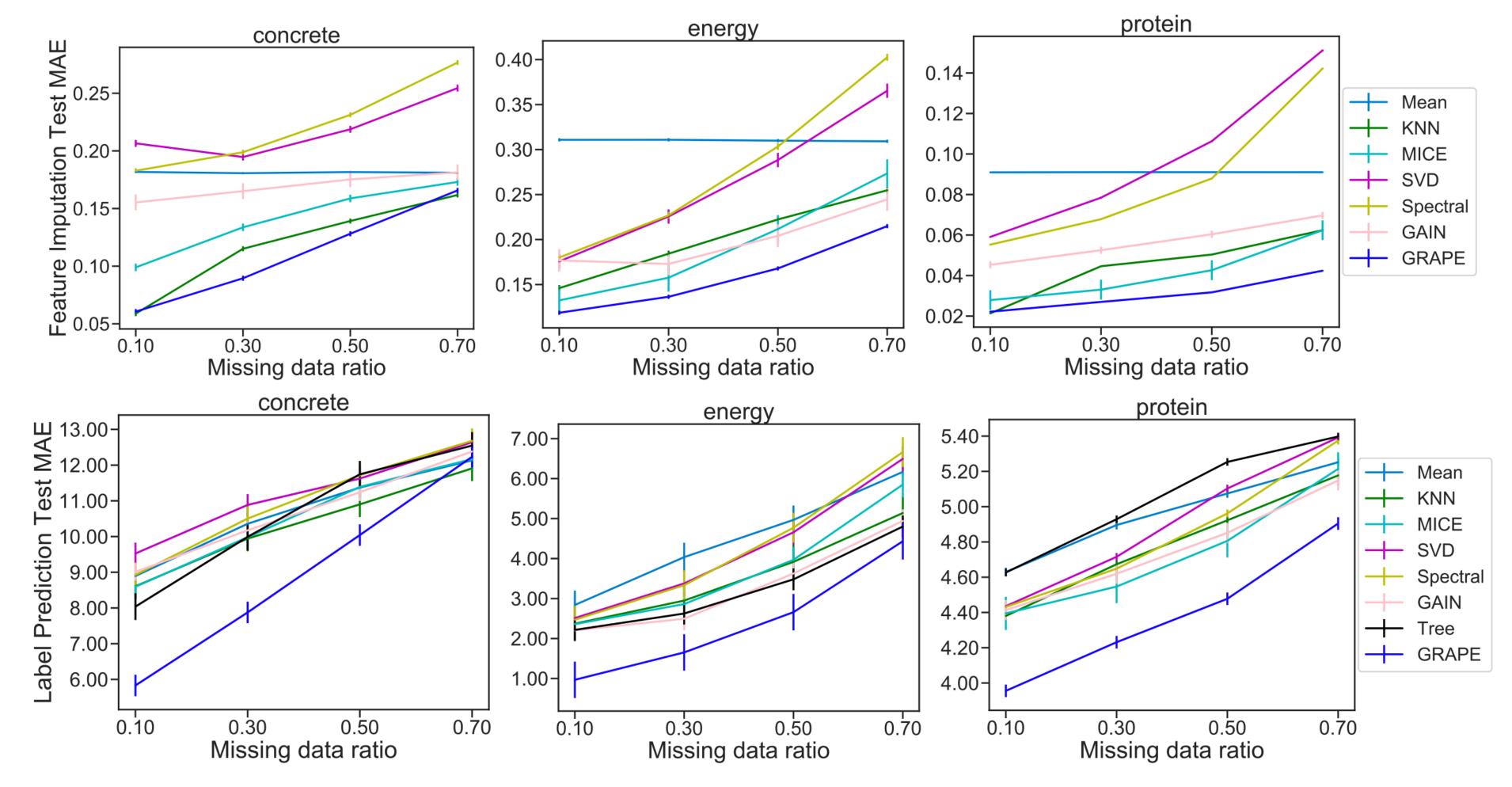
- Mean imputation (Mean): Imputes the missing Dij with the mean of all the samples with observed values in dimension j.
- K-nearest neighbors (KNN): Imputes the missing value Dij using the KNNs that have observed values in dimension j with weights based on the Euclidean distance to sample i.
- Multivariate imputation by chained equations (MICE): Runs multiple regression where each missing value is modeled conditioned on the observed non-missing values
- Iterative SVD (SVD): Imputes missing values based on matrix completion with iterative low-rank SVD decomposition
- Spectral regularization algorithm (Spectral): Matrix completion model, imputes missing values using SVD
- Generative Adversarial Imputations Nets (GAIN): state-of-the-art deep imputation model with generative adversarial training
- Decision tree (Tree): statistical method that can handle missing values for label prediction, baseline only for the label prediction task

# Results: Overall Comparisons



Averaged MAE of feature imputation(upper) and label prediction(lower) on UCI datasets over 5 trials at data missing level of 0.3.

# Results: Varying Missing Data Ratio



Averaged MAE of *feature imputation*(upper) and *label prediction*(lower) with different missing ratios over 5 trials. GRAPE yields 12% lower MAE on imputation and 2% lower MAE on prediction tasks across different missing data ratios

# Results: Ablation Study

	concrete	energy	housing	kin8nm	naval	power	protein	wine	yacht
Without edge dropout With edge dropout	0.171 <b>0.090</b>	0.148 <b>0.136</b>	0.104 <b>0.075</b>	0.262 <b>0.249</b>	0.021 <b>0.008</b>	0.192 <b>0.102</b>	0.047 <b>0.027</b>	0.094 <b>0.063</b>	0.20.
$Sum(\cdot)$	0.094	0.143	0.078	0.277	0.024	0.134	0.040	0.069	0.154
$\mathbf{M}\mathbf{A}\mathbf{X}(\cdot)$	0.088	0.142	0.074	0.252	0.006	0.102	0.024	0.063	0.153
$Mean(\cdot)$	0.090	0.136	0.075	0.249	0.008	0.102	0.027	0.063	0.151
Impute then predict	9.36	2.59	3.80	0.181	0.004	4.80	4.48	0.524	9.02
End-to-End	<b>7.88</b>	1.65	3.39	0.163	0.007	<b>4.61</b>	4.23	0.535	4.72

Averaged MAE of Grape on UCI datasets over 5 trials

Edge dropout (upper) reduces the average MAE by 33% on feature imputation tasks.

MEAN( $\cdot$ ) is adopted in implementation given by authors.

End-to-End training (lower) reduces the average MAE by 19% on prediction tasks (excluding two outliers).

### Conclusion

Feature Imputation - edge level task

Label Prediction - node level task

Learning in end-to-end fashion

Extension of GNNs to include edge values

Significant improvement over state-of-the-art approaches