

# Numerical Analysis

## Homework 11. Diode Networks

**Due: May 16, 2017**

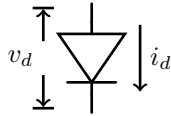


Figure 1. Diode symbol.

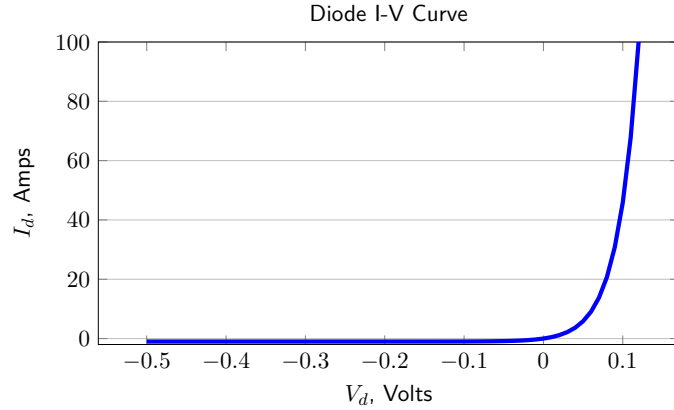


Figure 2. Diode I-V curve.

Diode is one of the most important elements in electronic circuits. It's symbol and the current-voltage (I-V) curve are shown above. The equation describing the diode current as a function of diode voltage is:

$$i_d = I_s (e^{v_d/\phi} - 1), \quad (11.1)$$

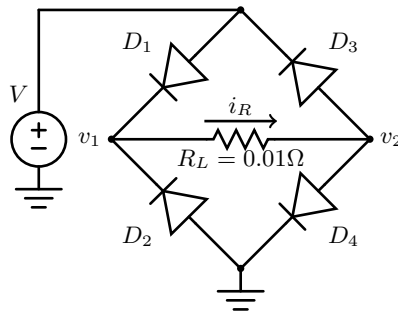
where  $I_s$  is a constant known as the saturation current and

$$\phi = \frac{\phi_0 T}{300}, \quad (11.2)$$

is the built-in potential and is a function of temperature. For this homework, we set

$$I_s = 1 \text{ Amps}, \quad (11.3)$$

$$\phi_0 = 0.026 \text{ Volts}. \quad (11.4)$$



1. Given a rectifier circuit above, assuming ambient temperature is fixed at 300 K,
  - 1.1. Let  $V=0, 0.02, \dots, 1.0$  Volt, please solve for  $v_1, v_2, i_{D1}, i_{D2}, i_{D3}, i_{D4}$ , and  $i_R$ .
  - 1.2. Let  $V=0, -0.02, \dots, -1.0$  Volt, please solve for  $v_1, v_2, i_{D1}, i_{D2}, i_{D3}, i_{D4}$ , and  $i_R$ .

2. Suppose the temperature for each diode is 300 K when  $V = 0$  Volts, and it will heat up when current flows through the diode with

$$T_d = 300 + \kappa \cdot i_d \cdot v_d, \quad (11.5)$$

where  $i_d$  is the current flows through the diode,  $v_d$  is the voltage across the diode, and  $\kappa = 2$ . (Note that when the diode temperature increases, the diode current will need to be modified since  $\phi$  is a function of temperature.)

- 2.1. Let  $V=0, 0.01, \dots, 1.0$  Volt, please solve for  $v_1, v_2, i_{D1}, i_{D2}, i_{D3}, i_{D4}, i_R, T_{D1}, T_{D2}, T_{D3}$  and  $T_{D4}$ .
  - 2.2. Let  $V=0, -0.01, \dots, -1.0$  Volt, please solve for  $v_1, v_2, i_{D1}, i_{D2}, i_{D3}, i_{D4}, i_R, T_{D1}, T_{D2}, T_{D3}$  and  $T_{D4}$ .
3. Please state your observations.

#### Notes.

1. For this homework you need to turn in a set of C++ source codes. That includes `hw11.cpp`, which solves question 2 above, `MAT.h`, `MAT.cpp`, `VEC.h` and `VEC.cpp` files.
2. A pdf file is also needed. Please name this file `hw11a.pdf`.
3. Submit your files on EE workstations. Please use the following command to submit your homework 11.

```
$ ~ee407002/bin/submit hw11 hw11a.pdf hw11.cpp MAT.h MAT.cpp VEC.h VEC.cpp
```

where `hw11` indicates homework 11.

4. Your report should be clearly written such that I can understand it. The writing, including English grammar, is part of the grading criteria.