

# DISEASE MAPPING WITH ERRORS IN COVARIATES

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## SUMMARY

We describe Bayesian hierarchical-spatial models for disease mapping with imprecisely observed ecological covariates. We posit smoothing priors for both the disease submodel and the covariate submodel. We apply the models to an analysis of insulin Dependent Diabetes Mellitus incidence in Sardinia, with malaria prevalence as a covariate. © 1997 by John Wiley & Sons, Ltd.

## 1. INTRODUCTION

Maps that show relative risks of a disease in small geographical areas are important for generating aetiological hypotheses, and for identifying areas that deserve closer scrutiny.<sup>1–5</sup> Maps may show relative risks of death from the disease, or relative risks of disease incidence or prevalence.

When the disease is rare or when geographical areas are small, and when the disease is non-contagious (that is, cases may be considered to occur independently), we may assume a Poisson model for death or disease incidence within each area  $i$

$$d_i \sim \text{Poisson}(\rho_i E_i) \quad (1)$$

where  $d_i$  is the number of events, ‘ $\sim$ ’ means ‘is distributed as’,  $\rho_i$  denotes the underlying true area-specific relative risk, and  $E_i$  is the ‘expected’ number of events with control (usually) for age and sex. Thus

$$E_i = \sum_j r_j n_{ij}$$

where  $j$  indexes age-sex subgroups,  $r_j$  denotes a known reference rate for subgroup  $j$ , and  $n_{ij}$  denotes the size of subgroup  $j$  in area  $i$ . If the  $\{\rho_i\}$  are not all equal, then the data  $\{d_i\}$  display *extra-Poisson variation*.

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To investigate whether extra-Poisson variation is geographically related, we would ideally like to map the true relative risks  $\{\rho_i\}$ . Since these are unobserved, the most obvious strategy is to estimate  $\rho_i$  by the empirical relative risk:

$$\hat{\rho}_i = \frac{d_i}{E_i} \quad (2)$$

which is the maximum likelihood estimate of  $\rho_i$ . When events are deaths,  $\hat{\rho}_i$  is the *standardized mortality ratio* (SMR). Mapping the  $\{\hat{\rho}_i\}$ , however, can be misleading because sampling variability in the  $\{\hat{\rho}_i\}$  can dominate the map and obscure genuine trends. In particular, areas that have exceptionally high or low  $\hat{\rho}_i$  tend to be those that have smaller  $E_i$ , where sampling variability is most pronounced ( $\text{var } \hat{\rho}_i = \rho_i/E_i$ ).

There have been several strategies proposed for dealing with sampling variability in maps. The current state-of-the-art is to adopt a fully-Bayesian hierarchical-spatial model.<sup>6-9</sup> An important feature of this model is that the prior distribution for the  $\{\rho_i\}$  incorporates spatial correlation, allowing the estimate of  $\rho_i$  to 'borrow strength' formally from neighbouring areas. In this way one smooths the empirical map, and geographical trends and inferences become more reliable.

Mapping Bayesian estimates of relative risk may reveal geographical trends across the map, or may suggest links with area-specific covariates  $x_i$ . To incorporate these covariates into the model, a natural assumption, in conjunction with the Poisson assumption (1), is

$$\log \rho_i = \alpha_i + \beta x_i \quad (3)$$

where  $\alpha_i$  represents the covariate-adjusted area-specific log relative risk. Such a model is an *ecological regression model*. One can then effect spatial smoothing of the  $\{\rho_i\}$  via a smoothing prior on the  $\{\alpha_i\}$ .

In practice, one rarely observes ecological covariates  $x_i$  directly. Available data  $z_i$  may be either imperfect measurements of, or proxies for,  $x_i$ . The simplest approach to this problem is to estimate  $x_i$  from  $z_i$  for each area independently, using this estimate  $\hat{x}_i$  in place of  $x_i$  in the ecological regression (3). When  $z_i$  is an accurate measure of  $x_i$ , this approach is reasonable. When, however, the correspondence between  $x_i$  and  $z_i$  is not so close, this approach has several disadvantages. First, the estimate of the regression coefficient  $\beta$  is probably underestimated (see for example reference 10). Second, the precision in parameter estimates or in projections is overestimated, through failure to take account of uncertainty in the  $\{\hat{x}_i\}$ . Third, when it is reasonable *a priori* to expect spatial correlation in the  $x_i$ , one obtains improved estimates of the  $\{x_i\}$  and other unknowns through a Bayesian procedure that incorporates a spatial smoothing prior on the  $\{x_i\}$ .

In this paper we develop Bayesian models with spatial smoothing priors for both relative risks and for imprecisely observed covariates, with estimation using Gibbs sampling.<sup>11,12</sup> We illustrate the models with an analysis of Insulin Dependent Diabetes Mellitus (IDDM) incidence in Sardinia. In this analysis the covariate of interest is malaria prevalence, which historically has varied widely across the island, and is known to have caused genetic selection in the inhabitants. Thus, we investigate the hypothesis that genetic selection has affected susceptibility to IDDM, and is responsible for geographical variation in IDDM incidence. We estimate the models using the Gibbs sampling software BUGS.<sup>13</sup>

These models have been applied in previous papers<sup>1,6</sup> and extended to allow for space-time interaction.<sup>14</sup> Bernardinelli *et al.*<sup>15</sup> discuss issues about the choice of the prior distribution for the dispersion parameter of the log relative risk. The original contribution of the present paper is the introduction of covariate measurement error.

## 2. A MARKOV RANDOM FIELD PRIOR

In this section we describe a *Markov random field* prior distribution for the  $\{\alpha_i\}$  parameters in (3). The development follows that used by Bernardinelli et al.<sup>15</sup>. This prior tends to produce similar estimates for  $\alpha_i$  and  $\alpha_j$  if areas  $i$  and  $j$  are geographically close.

The Gaussian Markov random field prior that we employ assumes, for each  $i$ , that  $\alpha_i$  is normally distributed with a mean and variance that depend on its neighbours. We consider two areas as 'neighbours' if they share a portion of boundary. The conditional prior distribution of  $\alpha_i$  given values for  $\{\alpha_j, j \neq i\}$  is

$$\alpha_i \sim N(\mu_{\alpha_i}, \sigma_{\alpha_i}^2) \quad (4)$$

where

$$\mu_{\alpha_i} = \frac{\sum_{j \neq i} w_{ij} \alpha_j}{\sum_{j \neq i} w_{ij}} \quad (5)$$

$$\sigma_{\alpha_i}^2 = \frac{1}{\gamma_{\alpha} \sum_{j \neq i} w_{ij}} \quad (6)$$

where the *adjacency weights*  $\{w_{ij}\}$  are fixed constants. In the present example, we set  $w_{ij} = 1$  if areas  $i$  and  $j$  are neighbours; otherwise  $w_{ij} = 0$ . Other values for  $w_{ij}$  are possible (for example,  $w_{ij} = \text{distance between the 'centres' of regions } i \text{ and } j$ ) but we do not consider such alternatives here.

To ensure that the Gaussian Markov random field model (4), (5) is internally consistent,  $\sigma_{\alpha_i}^2$  must depend upon the number of adjacent areas and their adjacency weights. Jointly, the  $\{\alpha_i\}$  have an intrinsic multivariate normal prior distribution with *inverse* variance-covariance matrix  $\Lambda$  given by

$$\Lambda_{ij} = \begin{cases} -\gamma_{\alpha} w_{ij} & j \neq i \\ \gamma_{\alpha} \sum_j w_{ij} & j = i \end{cases}$$

Matrix  $\Lambda$  is not full rank. Thus the prior on the  $\{\alpha_i\}$  is improper; adding an arbitrary constant to each  $\alpha_i$  does not change the probability (4). This need not concern us since the data  $d_i$  contain information on the location of the  $\{\alpha_i\}$ .

The amount of smoothing in the random effects  $\{\alpha_i\}$  is controlled by parameter  $\gamma_{\alpha}$  in (6). A small value of  $\gamma_{\alpha}$  induces little smoothing, whilst an infinite value forces all the  $\{\alpha_i\}$  to be equal. Since we do not wish to impose any fixed amount of smoothing on these parameters, but rather we wish to let the data themselves determine how much smoothing to induce, we treat  $\gamma_{\alpha}$  as a model parameter. It is computationally convenient to choose a gamma ( $a, b$ ) prior distribution for  $\gamma_{\alpha}$ , for fixed constants  $a$  and  $b$ . For the present application, we assume a just-proper prior gamma (0.001, 0.001). We also specify a vague normal prior for  $\beta$ .

With these hyperpriors, equations (1) and (3)–(6) specify a full probability model for the data  $\{d_i, E_i, x_i\}$ , assuming the  $\{x_i\}$  are accurately observed. We next consider the problem of imperfectly observed covariates.

## 3. ERRORS IN COVARIATES

Frequently, ecological covariates  $x_i$  are not accurately observed. Sometimes one may use epidemiological data concerning another disease as a proxy variable,  $z_i$ . For example, if  $d_i$  records deaths from heart disease in area  $i$ , an important covariate is the proportion of area residents who

smoke. Such data on smoking are generally unavailable, so the incidence of lung cancer as recorded by the cancer registry for the area might be a useful proxy. In Section 5,  $x_i$  is related to underlying malaria prevalence, and  $z_i$  is observed malaria prevalence.

When the proxy variable  $z_i$  relates to another disease, it may be natural to use a spatial smoothing prior for the unobserved covariate  $x_i$ , such as a Gaussian Markov random field prior of the form described in Section 2. In anticipation of the analysis of IDDM and malaria in Section 5, assume that

$$z_i \sim \text{binomial}(n_i, \theta_i) \quad (7)$$

where  $n_i$  is the population size of area  $i$ , and

$$\log\left(\frac{\theta_i}{1 - \theta_i}\right) = x_i. \quad (8)$$

Thus we take the covariate  $x_i$  in (3) as the logistic-transformed expectation of  $z_i$ . We assume for  $x_i$  the same form of spatial smoothing prior used in Section 2:

$$x_i \sim N(\mu_{x_i}, \sigma_{x_i}^2) \quad (9)$$

where

$$\begin{aligned} \mu_{x_i} &= \frac{\sum_{j \neq i} w_{ij} x_j}{\sum_{j \neq i} w_{ij}} \\ \sigma_{x_i}^2 &= \frac{1}{\gamma_x \sum_{j \neq i} w_{ij}}. \end{aligned} \quad (10)$$

We specify a  $\text{gamma}(0.001, 0.001)$  prior for  $\gamma_x$ .

Note that the amount of smoothing in the two Markov random field priors (4)–(6) and (9)–(10) may differ, since the smoothing is controlled by different parameter  $\gamma_z$  and  $\gamma_x$ .

#### 4. ESTIMATION

We have specified two arms to the model: the disease model (1), (3)–(6) and the covariate model (7)–(10). One approach to estimation is first to estimate the covariate model, and then to substitute resulting estimates of the  $\{x_i\}$  into the disease model. This two-stage approach, however, suffers from some of the deficiencies noted in Section 1. In particular, inferences and predictions from the disease model tend to be over-confident, through failure to acknowledge uncertainty in the  $\{x_i\}$ . A better approach is to estimate all parameters (including  $\beta$ ) simultaneously, treating equations (1), (3)–(10) as a single large model. This is quite feasible using Markov chain Monte Carlo methods such as Gibbs sampling. Indeed, it is probably simpler to do this than to attempt the two-stage procedure indicated above. This can be done using the BUGS software.<sup>13</sup>

Figure 1 shows structural relationships between the model quantities in the form of a conditional independence graph.

#### 5. IDDM AND MALARIA IN SARDINIA

##### 5.1. Background

There is scientific interest in studying the association between IDDM and malaria, since both are associated with the HLA system. Recent evidence suggests that resistance to *Plasmodium*

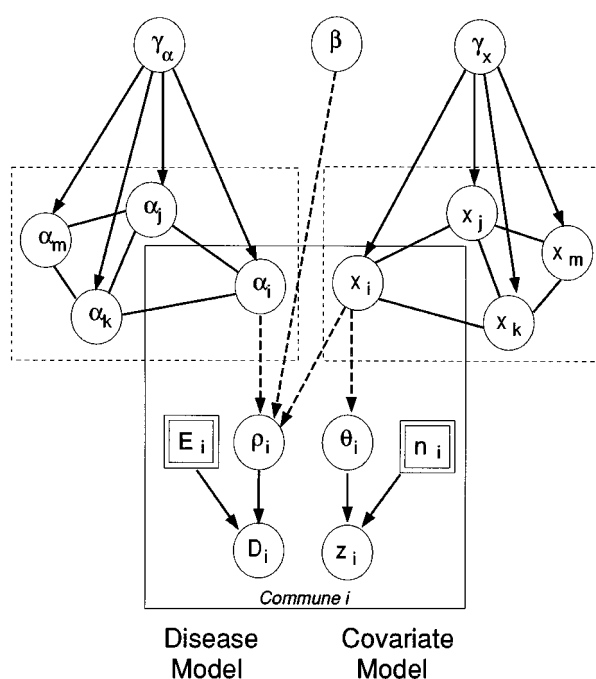


Figure 1. A conditional independence graph corresponding to equations (1), (3)–(10). Square nodes denote constants; round nodes denote model parameters and data; solid arrows denote stochastic dependence as specified in the model equations; dashed arrows denote deterministic relationship; undirected links denote bidirectional stochastic dependence between parameters of neighbouring communes

Falciparum malaria in West Africa is associated with a human class I allele, HLA-B53, and an unusual class II haplotype.<sup>16</sup> Family studies have found genetic linkage between HLA and IDDM, suggesting that genes within or near the HLA region are involved in susceptibility to IDDM.<sup>17</sup>

Sardinia is a particularly suitable place to investigate the association between IDDM and malaria. Malaria spread gradually all over Sardinia after the Carthaginian conquest, became established after Roman occupation and remained stable until the end of the 19th century. It was completely eradicated in 1950. Malaria has for centuries been a major cause of death in the island. Population genetic studies carried out by Piazza<sup>18</sup> suggest that, in the plains of Sardinia where malaria has been endemic, some genetic traits have adapted to provide greater resistance to the haemolysing action of Plasmodium. In the hilly and mountainous areas, where malaria has been absent, such adaptation has not occurred.

IDDM incidence in Sardinia is the second highest in Europe (35 per 100,000 person years) after Finland (40 per 100,000). Sardinia is a striking exception to the north-south downward trend of IDDM in Europe, being quite atypical of other Mediterranean countries.<sup>19</sup> From studies carried out on the cumulative prevalence of IDDM in military conscripts, the risk for IDDM in Sardinia began to increase with the male birth cohort of 1950.<sup>20</sup>

## 5.2. The data

We calculated IDDM incidence from a case registry that has operated in Sardinia since 1989. The incidence data refer to the period 1989–1992 and cover the population aged 0–29 years. We let

$d_i$  denote the number of IDDM cases in commune  $i$  ( $i = 1, 2, \dots, N = 366$ ), and  $E_i$  denote the expected number of IDDM cases based on Sardinian national rates.

Fermi<sup>21,22</sup> has recorded the number of individuals affected by malaria,  $z_i$ , for each commune during the period 1938–1940. We obtained the population  $n_i$  for each commune from the 1936 census.

### 5.3. Results

We estimated the models using BUGS. In each case, we ran the Gibbs sampler for 7500 iterations. We checked convergence of the simulations with a variety of diagnostics implemented in the CODA<sup>23</sup> software, and discarded the first 2500 iterations of each run as ‘burn-in’ or ‘pre-coverage’ samples. Posterior inference was thus based on empirical summaries of the final 5000 samples in each run. Computation times ranged from 40–110 minutes per run on a SPARC-centre 2000.

The maps in Figures 2(a) and (b) show  $\rho_i$ , the estimated relative risk of IDDM, obtained by maximum likelihood (2) and by the Bayesian approach with model (1), (3)–(6). In Figure 2(b), relative risks are less variable than in Figure 2(a), and show considerable smoothing.

The map in Figure 3(a) shows the observed prevalence of malaria ( $z_i/n_i$ ) in each commune during 1938–1940. This map has been smoothed in Figure 3(b) by plotting  $\theta_i$  from the Bayesian model (7)–(10). Since the number of malaria cases is quite high in all the Sardinian communes, the two maps are almost identical. That is, there appears to be little sampling error in the malaria data. The communes for which Figures 3(a) and (b) do differ are generally quite small and have extreme values of prevalence.

Figures 2(b) and 3(b) do not exhibit a clear association between malaria prevalence and IDDM incidence. To examine this more formally, we introduced malaria prevalence as a covariate in the model. To begin with, we ignored sampling error in the observed proportions  $z_i/n_i$  and simply substituted

$$x_i = \log\left(\frac{z_i}{n_i - z_i}\right) \quad (11)$$

directly into (3). We then calculated Bayesian estimates for model (1), (3)–(6). This resulted in a posterior mean for  $\beta$  of  $-0.036$ , with 95 per cent Bayesian credible interval  $[-0.066, -0.007]$ . This indicates that communes with historically high malaria prevalence currently have relatively low incidence of IDDM and *vice versa*. Our next step was to fit model (1), (3)–(10) which allows for sampling error and spatial correlation in the covariate. This gave a posterior mean of  $-0.039$  for  $\beta$ , with 95 per cent credible interval  $[-0.071, -0.008]$ .

The negligible increase in the estimated magnitude of  $\beta$  after accounting for covariate sampling error supports our earlier suggestion of quite accurate measurements of malaria prevalence in 1938–1940. Recall, however, that the hypothesis of interest concerns how genetic adaptation in areas of endemic malaria affects susceptibility to IDDM. Thus, the true covariate is the long-term malaria endemicity averaged over many centuries in each commune.

Consider the following model for the observed covariate  $z_i/n_i$  (malaria prevalence between 1938–1940):

$$\begin{aligned} z_i &\sim \text{binomial}(n_i, \theta_i) \\ \log\left(\frac{\theta_i}{1 - \theta_i}\right) &\sim N(x_i, \omega). \end{aligned} \quad (12)$$

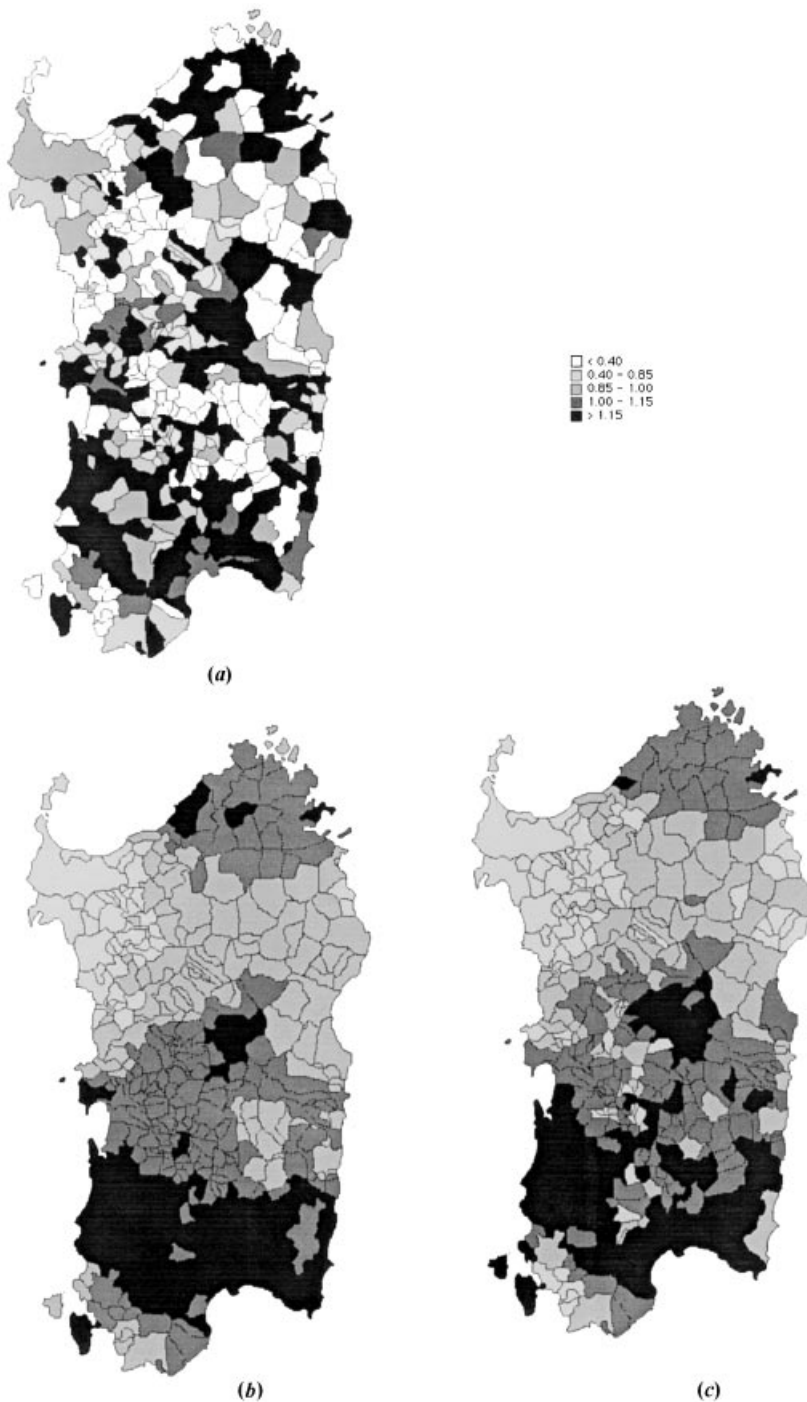


Figure 2. (a) Diabetes SMRs ( $\hat{\rho}_i$ ) calculated from Sardinian regional IDDM rates, estimated by equation (2). (b) Bayesian estimates of the relative risk of IDDM ( $\rho_i$ ) in model (1), (3)–(6), but without covariates ( $\beta = 0$ ). (c) Bayesian estimates of the relative risk of IDDM ( $\rho_i$ ) in model (1), (3)–(10), (12), allowing for spatial correlation and long-term error with fixed variance  $\omega = 2.25$  in the covariate

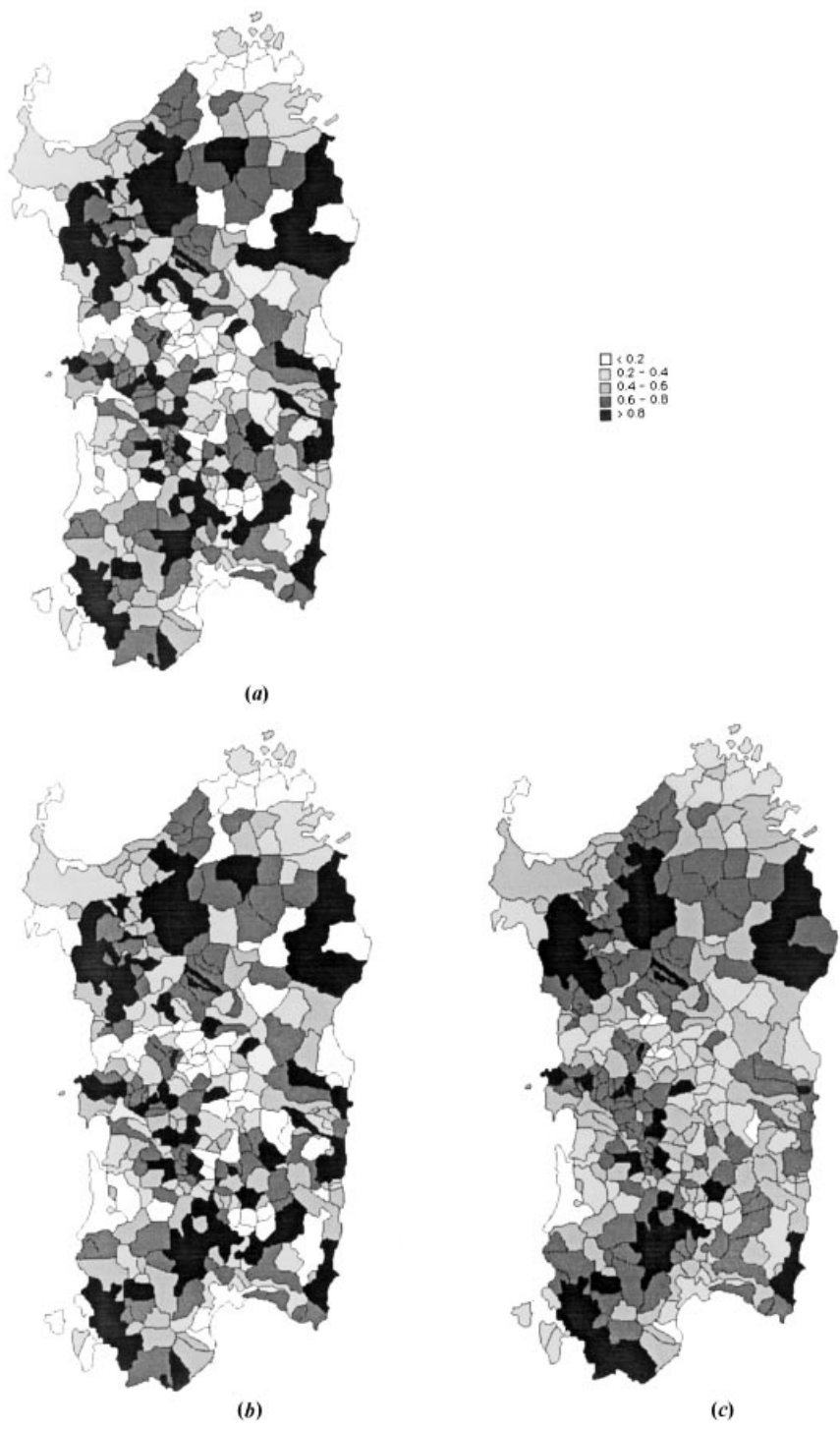


Figure 3. (a) Malaria prevalence in Sardinia in the period 1938–1940: proportion of the population affected ( $z_i/n_i$ ). (b) Bayesian estimates of malaria prevalence  $\theta_i$  in model (7)–(10). (c) Bayesian estimates of malaria prevalence  $\theta_i$  in model (9), (10), (12), obtained by setting the long-term variance  $\omega = 2.25$



Table I. Relative risk of IDDM for selected communes estimated according to various covariate models of malaria prevalence. MLE refers to the maximum likelihood estimate given by equation (2); model A refers to the disease model (1), (4)–(6) with  $\log \rho_i = \alpha_i$ ; model B refers to model (1), (3)–(6) which allows dependence of  $\rho_i$  on the *observed* malaria covariate; model C refers to model (1), (3)–(10) which allows for spatial correlation in the covariance; model D refers to model (1), (3)–(6), (9), (10), (12) which incorporates spatial correlation and long-term error in the covariate

Commune	Observed malaria prevalence	Model	RR of IDDM $\rho_i$	(95% CI)	RR associated with malaria $e^{\beta x_i}$
<i>Low-lying areas</i>					
33	77.0%	MLE	$\frac{4}{5.54} = 0.72$	—	—
		A	0.80	(0.53, 1.08)	—
		B	0.76	(0.53, 1.03)	0.96
		C	0.77	(0.57, 0.99)	0.95
		D	0.75	(0.54, 0.98)	0.89
42	96.1%	MLE	$\frac{0}{0.69} = 0.00$	—	—
		A	0.86	(0.54, 1.22)	—
		B	0.77	(0.59, 1.09)	0.89
		C	0.77	(0.55, 1.04)	0.88
		D	0.76	(0.53, 1.02)	0.84
<i>Mountainous/hilly areas</i>					
90	12.0%	MLE	$\frac{0}{0.39} = 0.00$	—	—
		A	1.13	(0.71, 1.78)	—
		B	1.19	(0.78, 1.79)	1.07
		C	1.18	(0.83, 1.66)	1.08
		D	1.21	(0.84, 1.72)	1.11
103	3.0%	MLE	$\frac{1}{0.27} = 3.70$	—	—
		A	0.97	(0.62, 1.46)	—
		B	1.09	(0.70, 1.63)	1.13
		C	1.12	(0.79, 1.56)	1.14
		D	1.15	(0.80, 1.83)	1.15

Comparison of (12) with (8) shows that we have replaced a deterministic relationship with a stochastic relationship, and have thus introduced an extra layer of uncertainty into the model. This corresponds to replacement of the dashed arrow between  $x_i$  and  $\theta_i$  in Figure 1 with a solid arrow, and inclusion of an extra node that represents  $\omega$ . We continue to assume the spatial smoothing prior (9)–(10) for  $x_i$ .

We can interpret model (12) as follows: the true log odds of malaria in commune  $i$  in 1938–1940 (that is,  $\log(\theta_i/(1 - \theta_i))$ ) represents a single realization from a latent Normal distribution with mean  $x_i$  (that is, the long-term average endemicity of malaria in commune  $i$ ) and unknown long-term variance,  $\omega$ . Since the data contain no information by which to estimate  $\omega$ , we must fix its value *a priori*. We carried out exploratory analyses to select a suitable value as follows. Using only the malaria prevalence data, we repeatedly fitted model (9)–(10), (12) using different values for  $\omega$  in the range 0.1–10. We produced maps of the estimated long-term prevalence  $\psi_i = e^{x_i}/(1 + e^{x_i})$  for each value of  $\omega$ . We compared these subjectively ‘by eye’ to identify one that showed a ‘reasonable’ amount of smoothing, that is, a map neither under-smoothed (neighbouring regions showing sharp changes in colour, giving the map a ‘speckled’ appearance) or over-smoothed (virtually all regions mapped with the same colour). Figure 3(c) shows the selected map, which corresponded to  $\omega = 2.25$ . We then substituted this value into the full model (1), (3)–(6), (9), (10),

(12), to estimate the relationship between long-term malaria endemicity and susceptibility to IDDM. Figure 2 (c) shows the estimated relative risk of IDDM obtained for the above model with allowance for spatial correlation and long-term error in the covariate. The posterior mean of  $\beta$  is now  $-0.060$  with 95 per cent Bayesian credible interval  $[-0.112, -0.012]$ . In addition, we estimated the correlation coefficient between relative risk of IDDM ( $\rho_i$ ) and long-term malaria prevalence ( $\psi_i$ ) in each region as  $-0.568$ , with 95 per cent credible interval  $[-0.812, -0.182]$ .

Some low-lying areas near the north-west coast of Sardinia are characterized by a historically high prevalence of malaria, whilst prevalence has tended to be low in the mountainous central regions (Figure 3(a)). Table I gives the overall relative risk of IDDM in a selection of these communes, estimated according to each model described above. To illustrate the influence of malaria prevalence on the estimated risk of diabetes, we have also calculated  $e^{\beta x_i}$ , the component of the overall relative risk attributable specifically to the covariate. This appears in the final column of Table I.

## 6. CONCLUSIONS

### 6.1. Substantive conclusions

Sardinians are known for their susceptibility to autoimmune diseases. The significant negative association that emerged between long-term malaria endemicity and diabetes indicates that people who live in areas where malaria has been particularly frequent have a lesser risk of IDDM than those who live in areas with a low prevalence of malaria as observed in 1938. This is illustrated by the relative risk estimates in Table I: diabetes risk is consistently lower in the low-lying regions than in the hills and mountains. A possible interpretation of this finding is that, since malaria has been endemic in the plains of Sardinia for centuries, places with high prevalence of malaria in 1938 are those in which a stronger selection process took place, both providing resistance to malaria and preventing the onset of autoimmune conditions.<sup>24</sup>

The estimated correlation coefficient of nearly  $-0.6$  represents an alternative means to quantify the association between incidence of IDDM and possible genetic selection due to past prevalence of malaria. Although the 95 per cent credible interval of  $[-0.812, -0.182]$  is rather wide, and suggests uncertainty about the true strength of this relationship, it does tend towards scientifically significant values.

### 6.2. Methodological issues

We have shown that one can construct disease maps that take account of covariates measured with error using Bayesian hierarchical-spatial models, where one posits spatial smoothing priors for both disease relative risks and underlying covariates. We consider that such models have particular value when the covariates are themselves incidence or prevalence data for other diseases.

Our choice of prior for malaria prevalence is particularly suitable since it varies between areas in a spatially structured way. Malaria prevalence tends to be higher in low lying and damp regions and lower in the mountains and hills. The spatial prior enables us to obtain a map of this geographical variation in malaria prevalence in which we have filtered out the random variation.

Specification of a spatial smoothing prior for the disease relative risks represents a way to allow for unmeasured risk factors (other than malaria) that vary smoothly with location. If the pattern of variation in such covariates is similar to that of disease risk, location may act as a confounder. Of course, the location effect is only a surrogate for other confounding factors. Introduction of

a spatial prior to model the effect of location thus causes the estimate of the regression coefficient  $\beta$  to be controlled for these factors.

One potentially controversial aspect of our analysis concerns the subjective choice of  $\omega$ , the long-term variation parameter used in the final model. Future studies could plan to obtain repeated measurements of the covariate to estimate the value of  $\omega$  statistically. Although such data were unavailable for the present application, we did examine the sensitivity of the  $\beta$  estimate to different values of  $\omega$ . For  $\omega > 2.25$  (that is, increased long-term variation) the posterior mean of  $\beta$  became slightly more negative, with a wider credible interval. Values of  $\omega$  much less than 0.5 yielded estimates of  $\beta$  similar to those obtained using the model (1), (3)–(10), which does not account for long-term sampling error.

The results of the present analysis are typical of many studies that involve covariate measurement error: when not properly accounted for, such errors tend to disguise real associations. By fully acknowledging all potential sources of error in our final model, we could clarify considerably the relationship between malaria prevalence and incidence of IDDM – the estimate of  $\beta$  almost doubled in magnitude after accounting for both sampling and measurement error. In addition, Table I illustrates how an increase in the sophistication of the model, although producing quite small numerical changes in each relative risk estimate, does reduce the credible interval and produce greater distinction between low-lying and hilly areas. Interpretation of any model requires care, however, and ecological regression models are no exception. There is a danger of misinterpreting association as causation. With models as complex as those considered here, it is particularly important to investigate the sensitivity of any conclusions to changes in model specification. In this regard our analysis of the IDDM/malaria data is continuing. We also plan to apply our model to epidemiological data on other diseases.

#### ACKNOWLEDGEMENTS

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