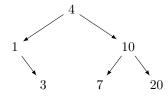
## 1 AVL tree: insert

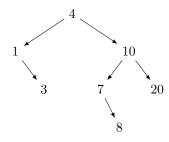
Consider the following AVL tree.



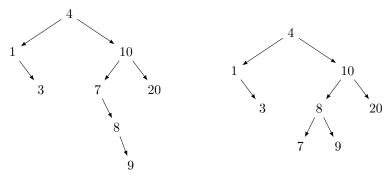
1. Give an example sequence of insert operations that, starting with an empty AVL tree, could have resulted in the above tree.

 $4,\,1,\,10,\,3,\,7,\,20$ 

2. Insert 8. Show the process and the resulting tree.

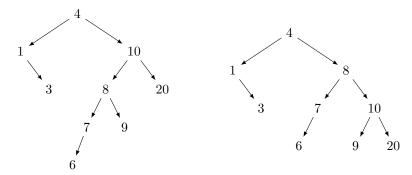


3. Insert 9 (into the tree resulting from inserting 8 above). Show the process and the resulting tree.

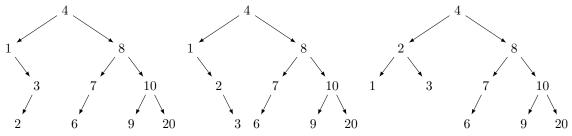


4. Insert 6 (into the tree resulting from inserting 9 above). Show the process and the resulting tree.

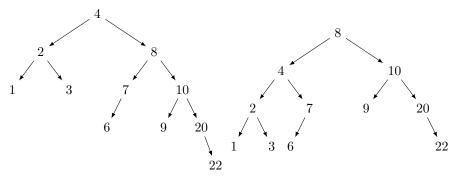
1



5. Insert 2 (into the tree resulting from inserting 6 above). Show the process and the resulting tree.

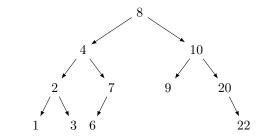


6. Finally, insert 22.

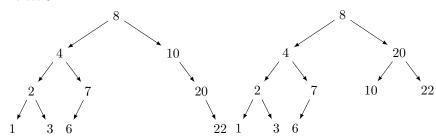


## 2 AVL tree: delete

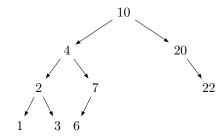
We begin with the tree we constructed in the previous question.



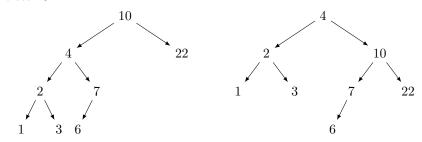
1. Delete 9.



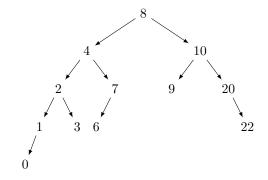
## 2. Delete 8.



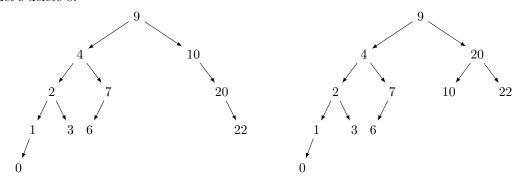
## 3. Delete 20.



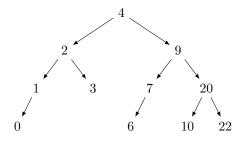
4. Now let's go back to the original tree, but with an added 0:



Let's delete 8.



But this is not enough: the tree is still unbalanced. Need to rotate again.



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