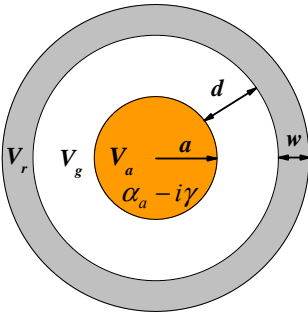


# Lasing Spectra and Thresholds of Supermodes in an Active Microdisk Assisted with a Passive Microring in View of the Mode Overlap Coefficients

## Object of research

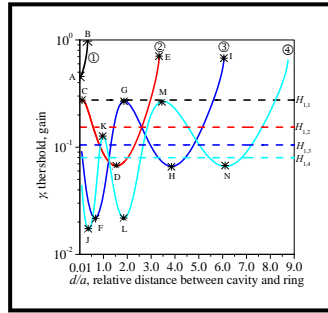
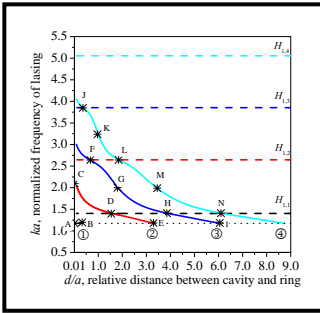


## Overlap Coefficients

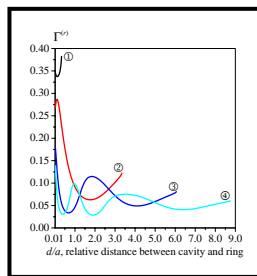
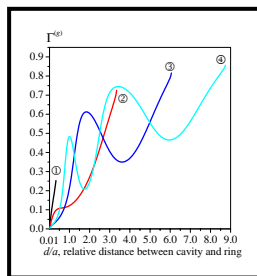
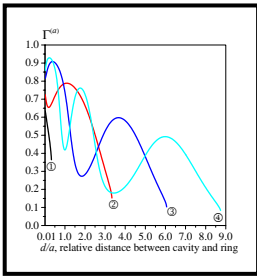
$$\Gamma_j^{(f)} = W_j^{(f)} / W_j \leq 1,$$

$$W_j^{(f)}(k_j, \gamma_j) = \int_{V_f} \alpha_f^2 |\vec{E}_j(\vec{R}, k_j, \gamma_j)|^2 dv, \quad f = a, g, r$$

$$W_j(k_j, \gamma_j) = \int_V \alpha_a^2 |\vec{E}_j|^2 dv = \int_{V_a} \alpha_a^2 |\vec{E}_j|^2 dv + \int_{V_g} \alpha_g^2 |\vec{E}_j|^2 dv + \int_{V_r} \alpha_r^2 |\vec{E}_j|^2 dv$$



$H_{1,n,q,p}$  supermodes,  $w=0.2a$ ,  $\alpha_a=\alpha_r=2.63$ ,  $\alpha_g=1$ .



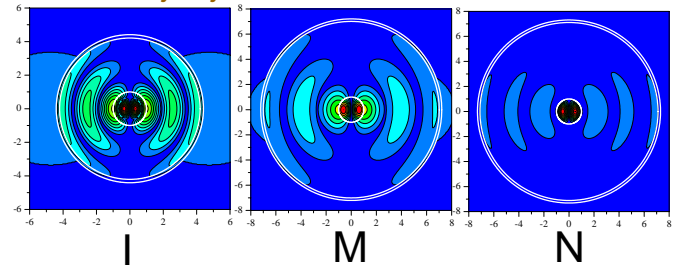
## Lasing Eigenvalue Problem (LEP)

$$U = E_z \text{ or } H_z, \quad U \neq 0$$

- ✗ Helmholtz equation off the boundary
- ✗ Transparent boundary conditions
- ✗ Sommerfeld radiation condition at infinity

The real-valued  $(\kappa_j, \gamma_j)$  are the eigenparameters

$$H_{1,1,3,0}$$



## Conclusions

- ✗ In multiple-domain microcavities all lasing modes are supermodes, i.e. optically-coupled modes of partial domains
- ✗ Thresholds are inverse proportional to the active-region overlap coefficients, which are specific for each mode of the cavity