### Siddharth Mishra-Sharma (MIT/IAIFI) | IAIFI Summer School



# Variational inference

 $D_{\mathrm{KL}}\left(q_{\varphi}(z)||p(z\mid x)\right) = \log p(x) - \left\langle \log p_{\vartheta}(x,z) - \log q_{\varphi}(z) \right\rangle_{q_{\varphi}(z)}$ 



## Evidence Lower BOund (ELBO)



#### Evidence



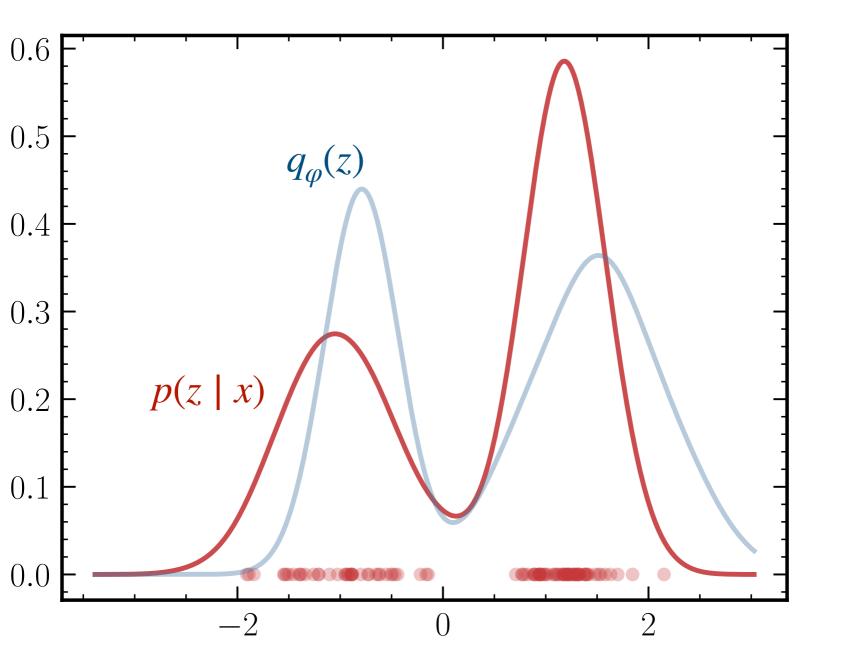
## A general-purpose technique for posterior estimation

$$= \left\langle \log p_{\vartheta}(x \mid z) + \log p(z) - \log q_{\varphi}(z \mid x) \right\rangle_{q_{\varphi}}$$
$$= \left\langle \log p_{\vartheta}(x \mid z) \right\rangle_{q_{\varphi}} - D_{\text{KL}} \left( q_{\varphi}(z \mid x) \parallel p(z) \right)$$

"Regularization"

ELBO =  $\left\langle \log p_{\vartheta}(x, z) - \log q_{\varphi}(z \mid x) \right\rangle_{q_{\varphi}}$ 

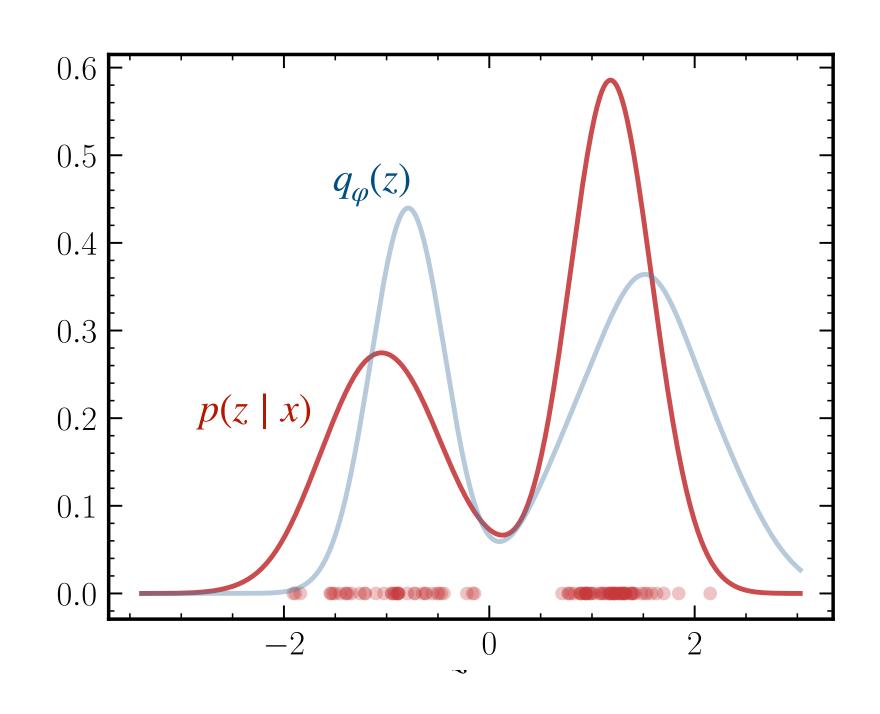
"Reconstruction"



# Variational inference

## A general-purpose technique for posterior estimation

$$\geq 0 \qquad \qquad \text{Evidence } - \text{ Evidence Lower BOund (ELBO)}$$
 
$$D_{\text{KL}} \left( q_{\varphi}(z) || p(z \mid x) \right) = \log p(x) - \left\langle \log p_{\vartheta}(x,z) - \log q_{\varphi}(z) \right\rangle_{q_{\varphi}(z)}$$



$$\begin{split} \text{ELBO} &= \left\langle \log p_{\vartheta}(x,z) - \log q_{\varphi}(z\mid x) \right\rangle_{q_{\varphi}} \\ &= \left\langle \log p_{\vartheta}(x\mid z) + \log p(z) - \log q_{\varphi}(z\mid x) \right\rangle_{q_{\varphi}} \\ &= \left\langle \log p_{\vartheta}(x\mid z) \right\rangle_{q_{\varphi}} - D_{\text{KL}} \left( q_{\varphi}(z\mid x) \parallel p(z) \right) \end{split}$$
 "Reconstruction" "Regularization"

# Variational inference

A general-purpose technique for posterior estimation: optimization instead of sampling

