#### Siddharth Mishra-Sharma (MIT/IAIFI) | IAIFI Summer School



## KL-divergence

### A measure of similarity between two probability distributions

 $\int_{-\infty}^{\infty} dx \, q(x) \, \log \left( \frac{q(x)}{p(x)} \right)$ 

 $D_{\mathrm{KL}}(Q||P) = |$ 

#### Not symmetric!

 $D_{\mathrm{KL}}(Q||P) \neq D_{\mathrm{KL}}(P||Q)$ 

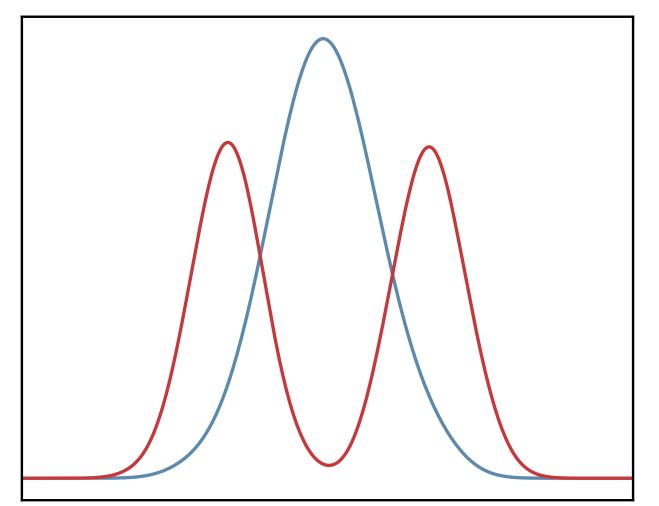
## Maximum-likelihood inference is equivalent to minimizing the forward KL

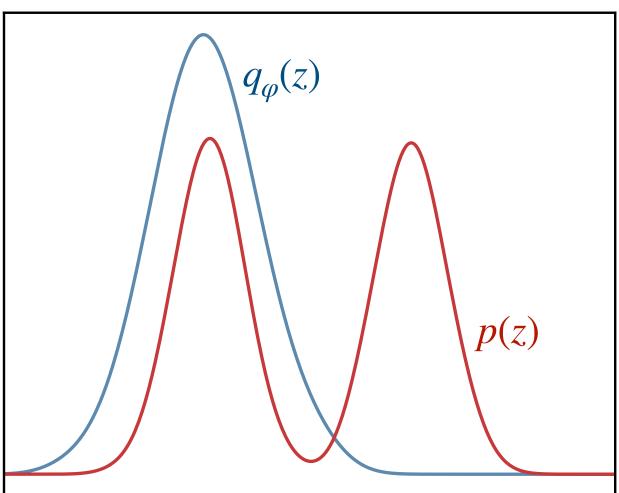
#### Forward KL

$$D_{\mathrm{KL}}(P_{\mathcal{D}}||Q_{\varphi}) = -\left\langle \log q_{\varphi}(z) \right\rangle_{z \sim p_{\mathcal{D}}(z)} + \mathrm{const}.$$

"Forward"  $KL D_{KL}(P||Q)$ 

"Reverse"  $\mathsf{KL}\,D_{\mathsf{KL}}(Q\|P)$ 







#### "True" distribution

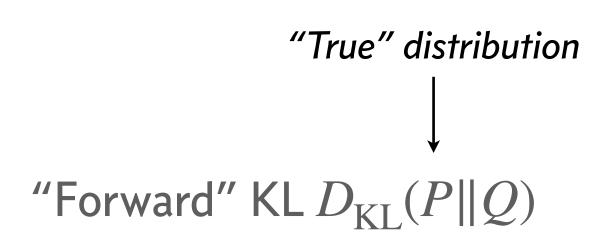
Non-negative!  $D_{\mathrm{KL}}(Q||P) \geq 0$ 

## KL-divergence

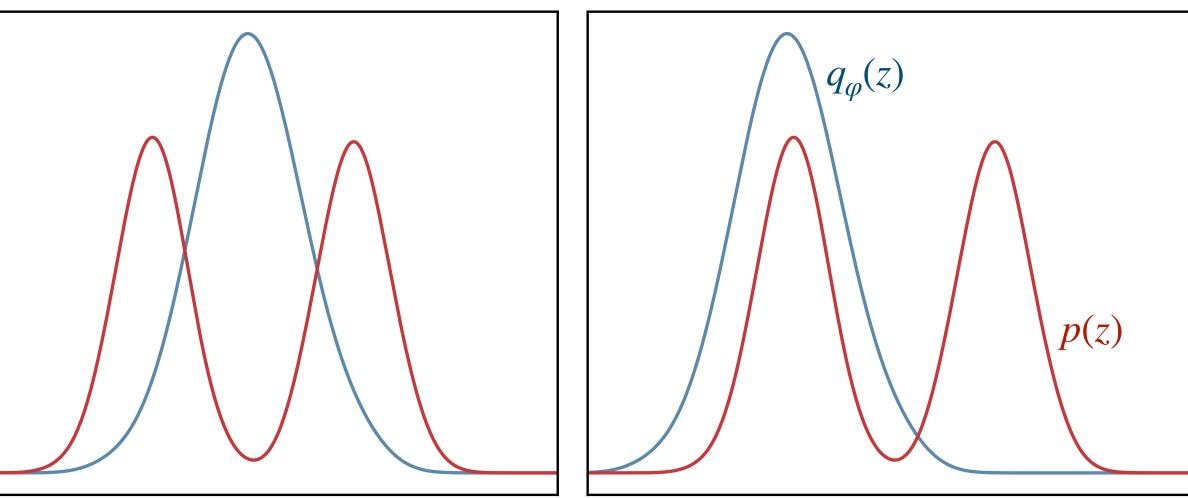
# $D_{\mathrm{KL}}(Q||P) = \int_{-\infty}^{\infty} \mathrm{d}x \, q(x) \, \log\left(\frac{q(x)}{p(x)}\right)$

A measure of similarity between two probability distributions

Not symmetric!  $D_{KL}(Q||P) \neq D_{KL}(P||Q)$ 







Forward KL

$$D_{\mathrm{KL}}(P_{\mathcal{D}}||Q_{\varphi}) = -\left\langle \log q_{\varphi}(z) \right\rangle_{z \sim p_{\mathcal{D}}(z)} + \mathrm{const}.$$

Maximum-likelihood inference is equivalent to minimizing the *forward* KL

Non-negative!  $D_{
m K}$ 

$$D_{\mathrm{KL}}(Q||P) \ge 0$$

## Variational inference

Infer the posterior over the latent parameters