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# Denoising score matching

# Need to compute the score $\nabla_{x_t} \log q(x_t)$

## The conditional score $\nabla_{x_t} \log q(x_t \mid x)$ can be computed using the diffusion kernel

 $(x_t - x)$ 

 $\nabla_{x_t} \log q(x_t \mid x) =$ 

### Explain why x conditioning disappears

### Noise-prediction

$$\frac{1}{2\sigma_q^2(t)} \frac{\left(1 - \alpha_t\right)^2}{\left(1 - \bar{\alpha}_t\right)\alpha_t} \left[ \left\| \epsilon - \hat{\epsilon}_\theta\left(x_t, t\right) \right\|^2 \right] \iff$$

### Score-matching

$$\frac{1}{2\sigma_q^2(t)} \frac{\left(1 - \alpha_t\right)^2}{\alpha_t} \left[ \left\| s_\theta\left(x_t, t\right) - \nabla \log p\left(x_t\right) \right\|^2 \right]$$

The noise- and score-prediction networks are equivalent up to a std-scaling

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$$\nabla_{x_t} \log q(x_t \mid x) = -\frac{(x_t - x)}{\sigma_t^2} = -\frac{\epsilon}{\sigma_t}$$

### Noise-prediction

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Score-matching

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## The noise/score-prediction model and latent diffusion

[Rombach et al 2021]

