Siddharth Mishra-Sharma (MIT/IAIFI) | IAIFI Summer School



Simple objectives as a weighted sum of ELBOs

Kingma et al (2023) showed that common objectives can be written as a weighted sum (across different noise levels) of ELBOs

$$L_{w}(x) = \left\langle w(t) \cdot w_{\text{ML}}(t) \mid \epsilon - \hat{\epsilon}_{\theta} \left(x_{t}, t \right) \mid ^{2} \right\rangle$$
Additional weighting Weighting for ELBO/

ML objective

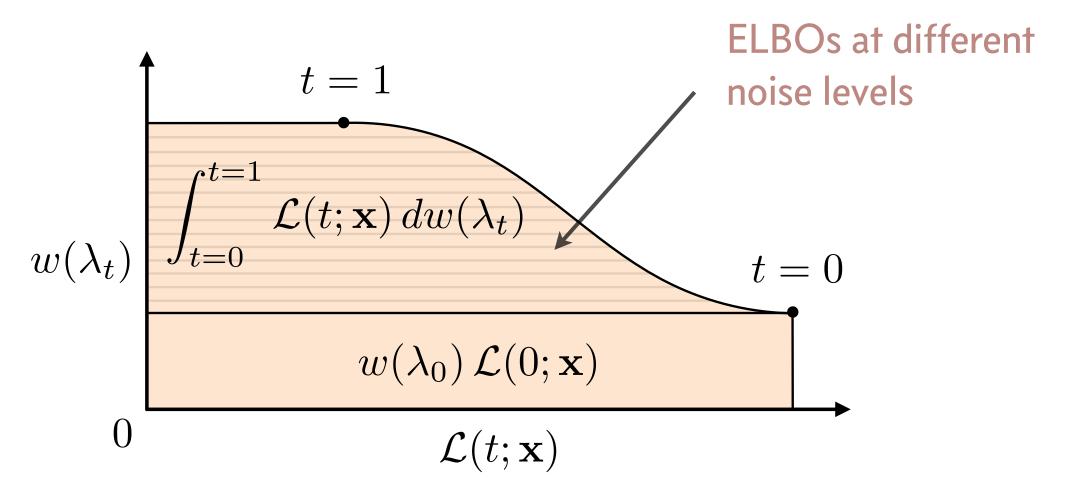
Additional weighting

($w_{\rm ML}^{-1}$ for ϵ -prediction)

$$p(w)$$

Importance weighting of different noise levels

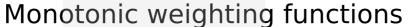
$$L_{w}(x) = \left\langle w_{\text{ML}}(t) \parallel \epsilon - \hat{\epsilon}_{\theta} \left(x_{t}, t \right) \parallel^{2} \right\rangle_{p(w)}$$
Importance weighting of different noise levels

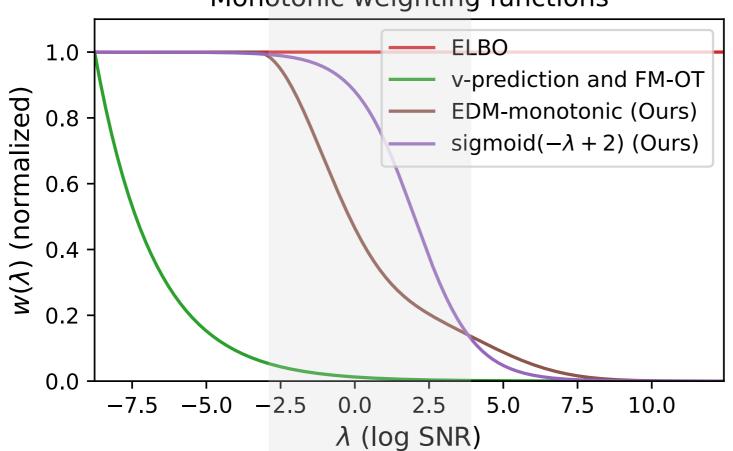


Interpretation: data augmentation with additive Gaussian noise / data-distribution smoothing

More important for perceptual quality?







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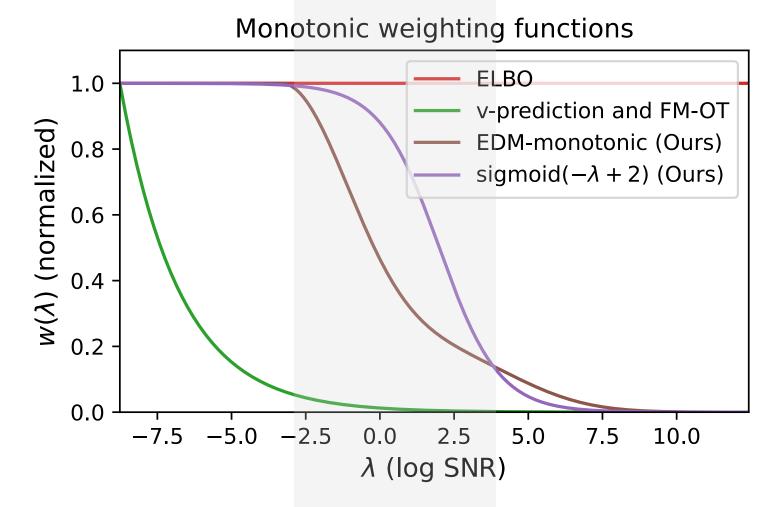
Weighting for ELBO/ ML objective

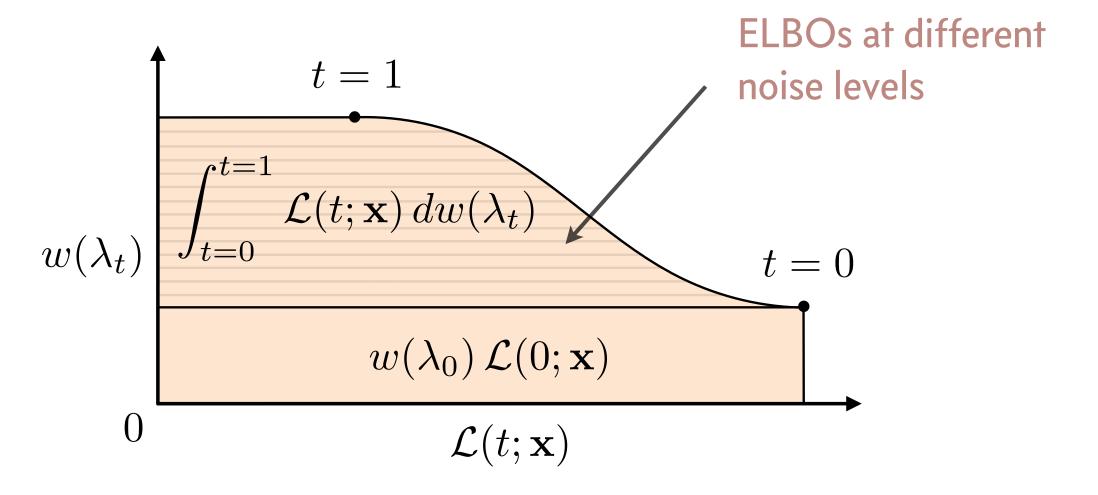
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Continuous-time/SDE formulation

In the limit of infinite time steps, $\Delta_t \to 0$ and the forward diffusion process can be written as

$$x_{t} = \sqrt{1 - \beta(t)\Delta_{t}}x_{t-1} + \sqrt{\beta(t)\Delta_{t}}\mathcal{N}(0,\mathbb{I})$$

$$\approx x_{t-1} - \frac{\beta(t)\Delta_{t}}{2}x_{t-1} + \sqrt{\beta(t)\Delta_{t}}\mathcal{N}(0,\mathbb{I})$$