### Siddharth Mishra-Sharma (MIT/IAIFI) | IAIFI Summer School



# Rate-distortion theory: neural compression

### Autoencoding is a form of (neural) compression!

 $ELBO = \left\langle \log p_{\theta}(x \mid z) \right\rangle_{q_{\varphi}} - D_{KL} \left( q_{\varphi}(z \mid x) \parallel p(z) \right)$ 

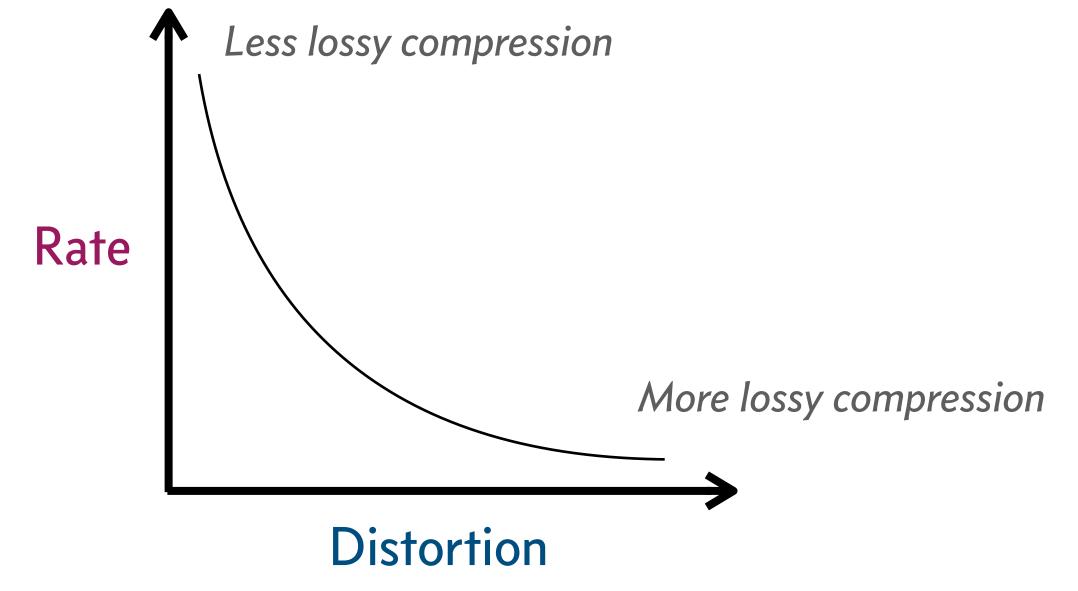
#### Rate

"Amount of compression"

### Distortion

"Information loss"

Rate-distortion curve quantified this tradeoff



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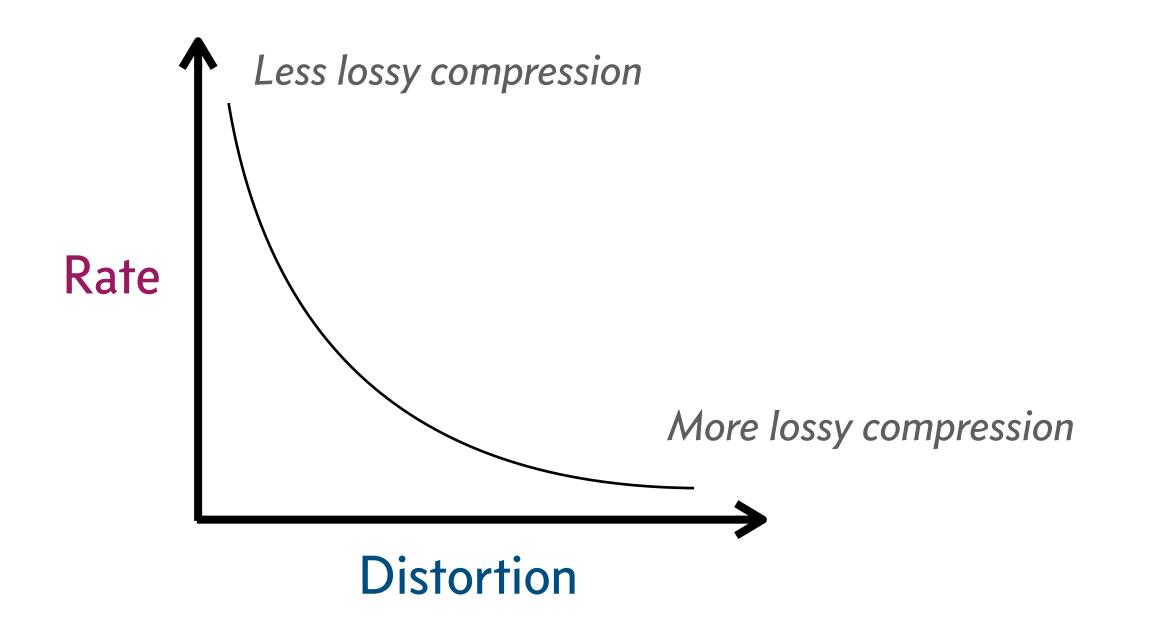
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# Controlling compression and disentanglement: $\beta$ -VAEs

$$\text{ELBO} = \left\langle \log p_{\vartheta}(x \mid z) \right\rangle_{q_{\varphi}} - \beta \cdot D_{\text{KL}} \left( q_{\varphi}(z \mid x) \parallel p(z) \right)$$

Distortion

Rate