



Siddhant Mishra-Sharma (MIT/AI FI) Summer School



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Continuous-time normalization flows

Parameterize the transformation by a neural ODE

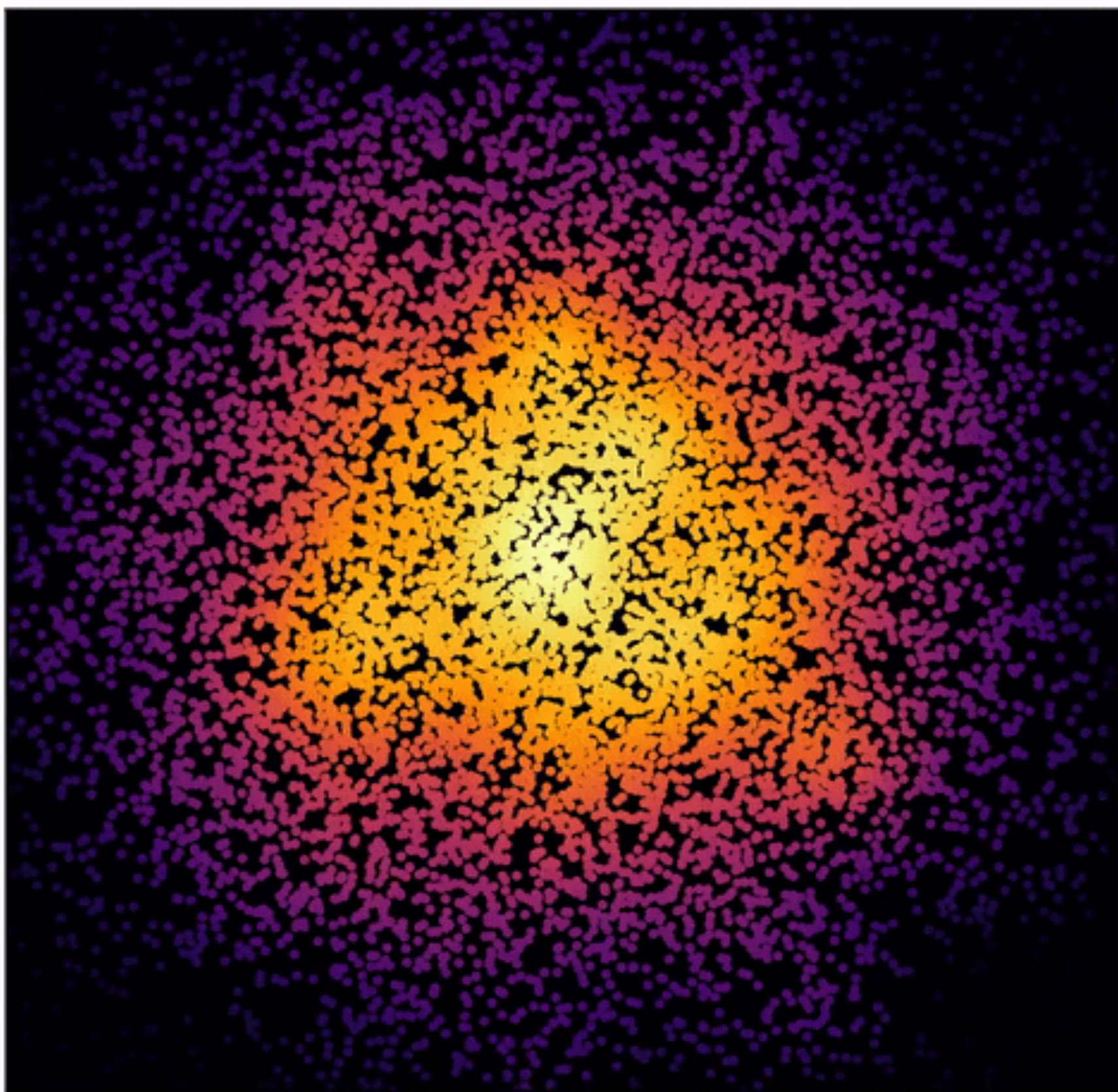
# Instantaneous change-of-variable formula

$$\frac{d \log p(z(dt))}{dt} = - \text{Tr} \left( \frac{df}{dz(t)} \right)$$



# ODE with reversible dynamics

$$\frac{dz}{dt} = f(z(t))$$



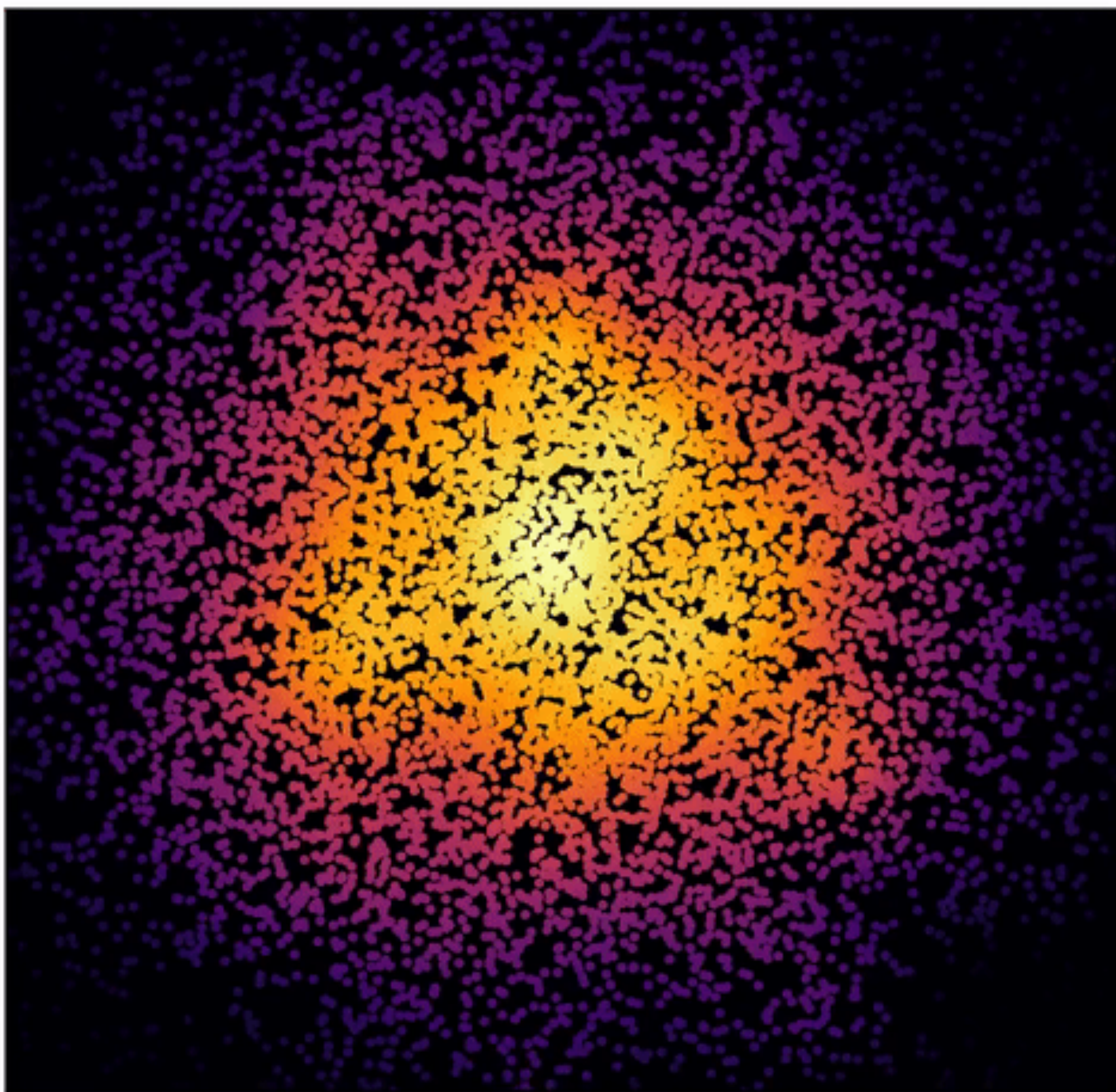
## Cons 🌀

- Need for efficient trace calculation
- Solving an ODE and backpropping through the solution can make for cumbersome training

Pro 

Unrestricted form of transformation  $f(z)$ !







# Continuous-time normalizing flows

Parameterize the transformation by a neural ODE

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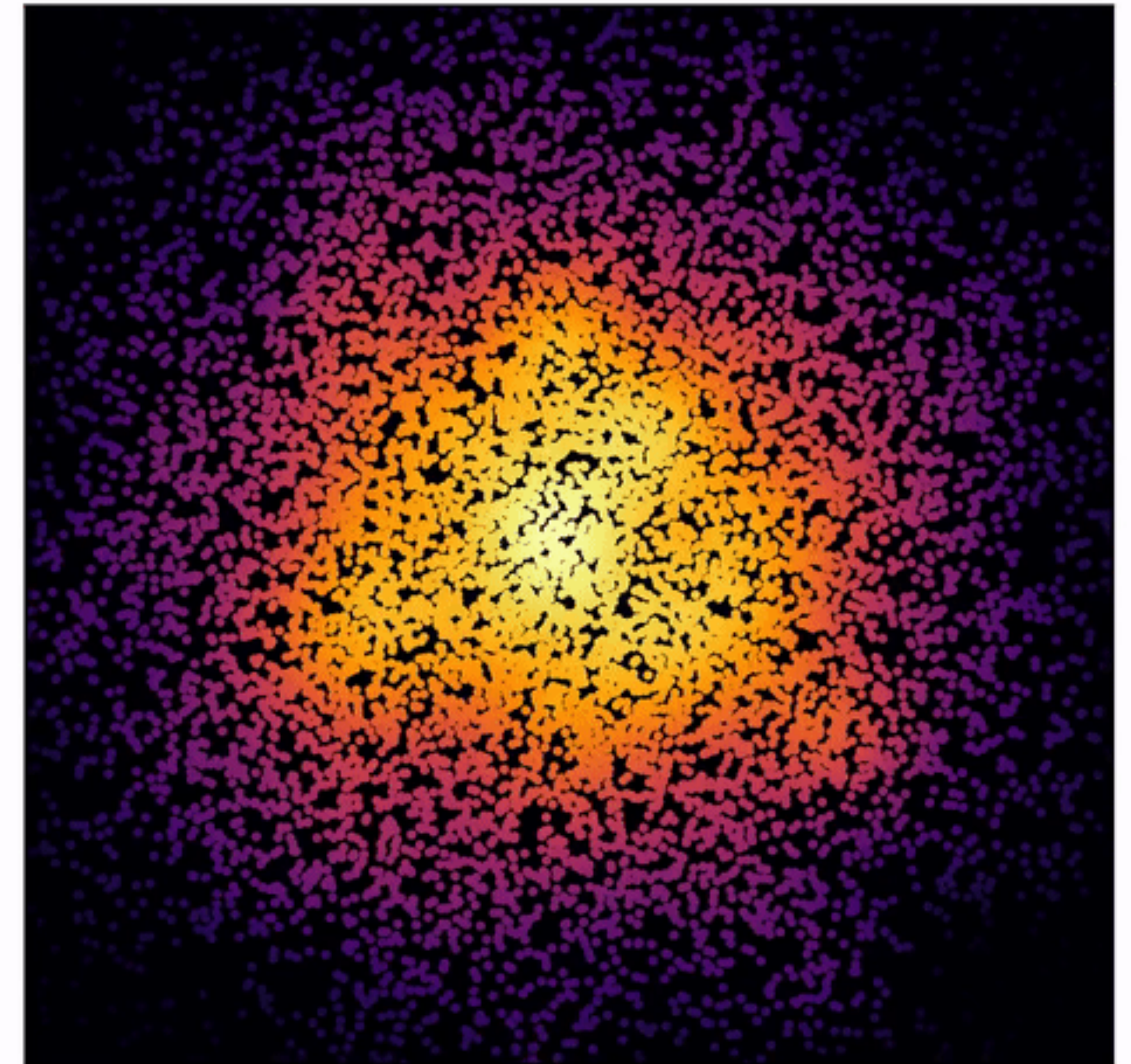
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Unrestricted form of transformation  $f(z)$ !

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# Flows in *simulation-based inference*

Flows are commonly employed as *conditional posterior density estimators* in simulation-based inference

