



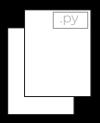
players take turns dropping pieces into a 6x7 grid. The objective is to be the first to form a horizontal, vertical, or diagonal line of one's own pieces. Players must anticipate opponent's moves to block, while simultaneously working towards their own winning line.

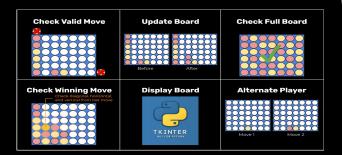
#### Contribution

Goal: Create an Al Solver using the MiniMax Algorithm and a reward function that will perform well against itself or a human player.

#### **Run Program**



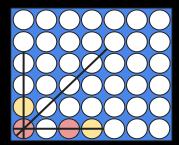


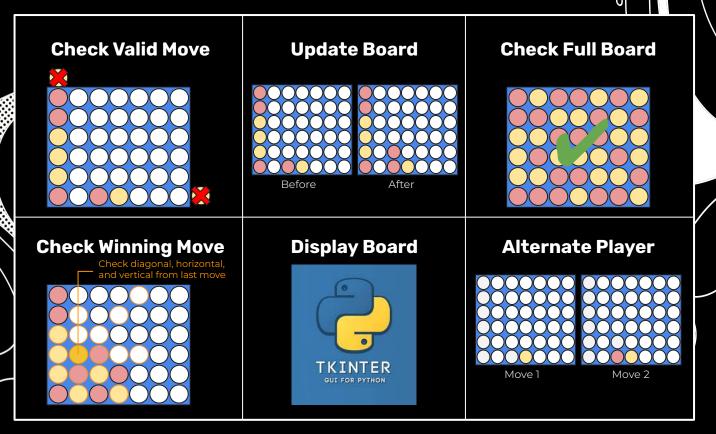












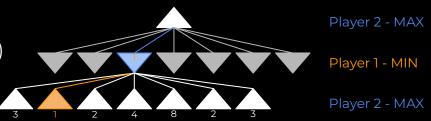
## **MiniMax** Algorithm

Each node is a board state from a subsequent move (branching factor 7)

Each node is assigned a reward

Since MiniMax assumes the opponent makes the best possible move, we can use the same reward calculation, but reverse the sign for subsequent layers

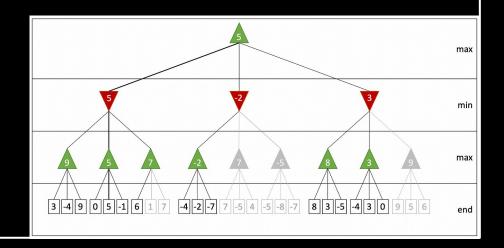
A state is terminal (does not recurse) if either player wins or the board is full



Shown with fully calculated board rewards

## **Alpha-Beta Pruning**

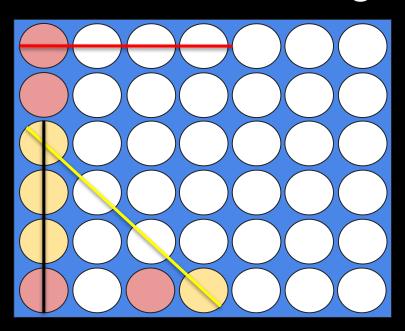
- If a maximizing node can achieve a value of x via its first branch, and the remaining minimizers beneath it would achieve values less than x, the maximizer ignores those branches and does not expand them any further than necessary.
- Similarly, if a minimizing node can achieve a value of x via its first branch, and the remaining maximizers beneath it would achieve values greater than x, the minimizer ignores those branches and does not expand them any further than necessary.



#### **Reward Calculation**

- Positive value => Player 1 is winning
- Negative value => Player 2 is winning
- Given a multiplier, for each Connect-4 possibility, if only one player is present, they get a reward of the multiplier raised to the power of the number of pieces they have
- If a player goes next, their multiplier is doubled to more heavily weight sooner outcomes
- If a Player 1 has Connect-4, we add 1,000,000; if Player 2 has Connect-4, we subtract 1,000,000
- If both players are present in a specific Connect-4 possibility, we multiply by 0 to ignore that possibility (it is no longer valid)
- Add this number to a total for each sequence of 4 on the board to assess overall position

#### Reward Walkthrough



Suppose multiplier = 7.

Horizontal from (0,0): 1 red, 3 blank =>  $(1) * (7)^1 = 7$ 

If red moves next, multiplier = 2 \*
7 = 14, so result = 14

Diagonal from (2, 0): 2 yellow, 2 blank => (-1) \* (7)<sup>2</sup> = -49

If yellow moves next, multiplier =
14, so result = -196

Vertical from (6, 0): 1 red, 3 yellow => 0

### **Challenges**

- Note: We were doing this without any foundational code; we built the entire thing from scratch
- Minimax Struggle
  - Our minimax tree depth was initially 3 (odd number) and should have been 4 (or an even number).
  - The "depth" of our tree needed to be even to allow both the minimizer and the maximizer to have an even number of moves.
- Heuristic Struggle
  - Our multiplier was too low (initially at 3).
  - As a result, the number of possible winning paths during the heuristic analysis would exceed our multiplier. For instance, if there were 4 potential winning paths, it would be better than if we had one potential winning path with 3.

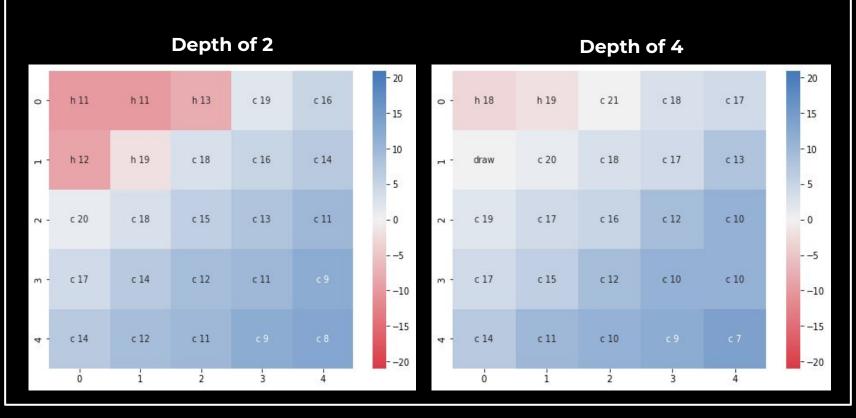


# **Accuracy Analysis**

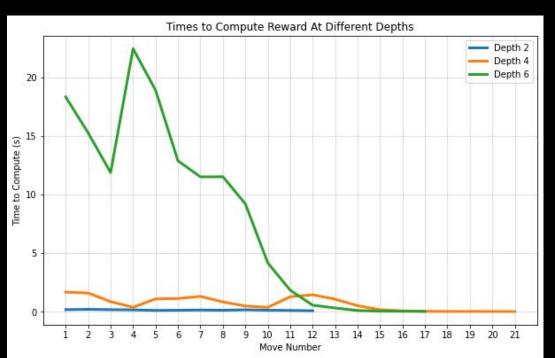
How Does Our Solver Perform?

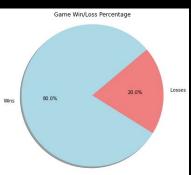


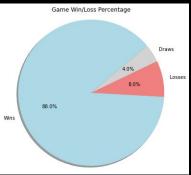
#### **Solver Performance**



# Computational Time vs. Accuracy







# Computer vs. Self (Depth 6)

# **Thank You!**